

Model Solutions and Marking Notes

Note: The model solutions for each question are not intended to be exhaustive – there may be other correct solutions. Any Examiner unsure of the validity of the approach adopted by a particular candidate to a particular question should contact his / her Advising Examiner.

Q1	Model Solution – 30 Marks	Marking Notes
(a)(i)&(ii)	(i) 999 999 (ii) 100 000	Scale 10C (0, 4, 8, 10) Accept correct answers without work <i>Low Partial Credit</i> <ul style="list-style-type: none"> Any 6-digit number <i>High Partial Credit</i> <ul style="list-style-type: none"> One part correct 6-digit numbers with correct first digit in (i) and (ii)
(b)(i)-(iv)	(i) 11 (ii) 25 (iii) 32 (iv) 7	Scale 20D (0, 6, 11, 16, 20) Accept correct answers without work <i>Low Partial Credit</i> <ul style="list-style-type: none"> One part correct Work of merit, e.g. finds 1st difference <i>Mid Partial Credit</i> <ul style="list-style-type: none"> Two parts correct <i>High Partial Credit</i> <ul style="list-style-type: none"> Three parts correct

Q2	Model Solution – 30 Marks	Marking Notes																		
(a)	<p>A Venn diagram with a universal set U represented by a rectangle. Inside U are two overlapping circles, S and T. Circle S contains the elements Evan, Fiona, and Dee. Circle T contains the elements Máire, Ray, and Dee. The intersection of S and T contains the elements Dee, Máire, and Ray. The element Zach is located outside both circles S and T within the universal set U.</p>	<p>Scale 10C (0, 4, 8, 10)</p> <p>Accept correct answer without work</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> One or two correct entries <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> Three correct entries 																		
(b)(i)&(ii)	<p>(i) Dee, Máire, Ray</p> <p>(ii) Zach</p>	<p>Scale 10C (0, 4, 8, 10)</p> <p>Accept correct answers without work</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> One correct element <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> One part correct 																		
(c)	<table border="1"> <thead> <tr> <th>Statement</th><th>True</th><th>False</th></tr> </thead> <tbody> <tr> <td>$\# S = 3$</td><td></td><td>✓</td></tr> <tr> <td>$Dee \in T$</td><td>✓</td><td></td></tr> <tr> <td>$S \cup T = T \cup S$</td><td>✓</td><td></td></tr> <tr> <td>$T \subset S$</td><td>✓</td><td></td></tr> <tr> <td>$S \setminus T = \{ \}$</td><td></td><td>✓</td></tr> </tbody> </table>	Statement	True	False	$\# S = 3$		✓	$Dee \in T$	✓		$S \cup T = T \cup S$	✓		$T \subset S$	✓		$S \setminus T = \{ \}$		✓	<p>Scale 10D (0, 4, 6, 8, 10)</p> <p>Accept correct answer without work</p> <p>If a candidate ticks both True and False for a statement without clearly indicating which is the final answer, consider it to be incorrect</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> 1 part correct <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> 3 parts correct <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> 4 parts correct
Statement	True	False																		
$\# S = 3$		✓																		
$Dee \in T$	✓																			
$S \cup T = T \cup S$	✓																			
$T \subset S$	✓																			
$S \setminus T = \{ \}$		✓																		

Q3	Model Solution – 20 Marks	Marking Notes
(a)&(b)	(a)(i) 3 (a)(ii) 2 (b) right-hand box: 4 (b) left-hand box: 8	Scale 20D (0, 6, 11, 16, 20) Accept correct answers without work <i>Low Partial Credit</i> <ul style="list-style-type: none"> • Work of merit in (a) or (b) E.g. finds a value with x and y swapped (i.e. (a)(i) = 6, (a)(ii) = 0, (b) right-hand box = 10, or (b) left-hand box = 3·5); or indicates relevant point on graph (i.e. (4,3), (2,1), (6,4), or (8,5)) <i>Mid Partial Credit</i> <ul style="list-style-type: none"> • 1 value correct (out of the 4) • Work of merit in (a) and (b) <i>High Partial Credit</i> <ul style="list-style-type: none"> • 2 values correct (out of the 4)

Q4	Model Solution – 20 Marks	Marking Notes
(a)&(b)	(a) $0.2 \times 2450 = \text{€}490$ (b) $2450 - (490 - 275)$ $= 2450 - 215$ $= \text{€}2235$	Scale 20D (0, 6, 11, 16, 20) Accept correct answers without work <i>Low Partial Credit</i> <ul style="list-style-type: none"> • Work of merit in one part E.g. in (a) mentions 100, 0·2, or similar E.g. in (b) subtracts tax credit, or subtracts some figure from gross income <i>Mid Partial Credit</i> <ul style="list-style-type: none"> • Work of merit in both parts • One part correct <i>High Partial Credit</i> <ul style="list-style-type: none"> • One part correct and work of merit in other part

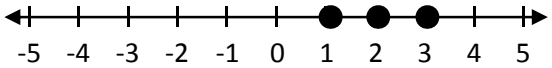
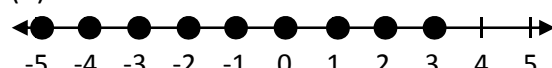
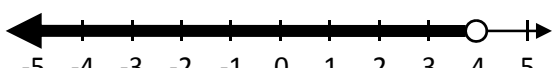
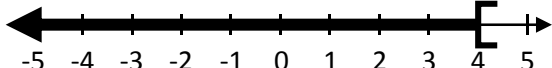
Q5	Model Solution – 30 Marks	Marking Notes
(a)	$40 + (3 \times 30)$ $= \text{€}130$	Scale 10C (0, 4, 8, 10) Accept correct answer without work Accept correct answer without € sign <i>Low Partial Credit</i> <ul style="list-style-type: none"> • Mentions 3 hours • Adds €40 to something • Multiplies €30 by something <i>High Partial Credit</i> <ul style="list-style-type: none"> • Mostly correct but uses incorrect time (eg. 2:45) or swops 30 and 40
(b)	$24.83 \div 0.71$ $= 34.9718\dots$ $= \text{€}34.97 \text{ (2 DP)}$	Scale 10B (0, 5, 10) Accept correct answer without work Accept correct answer without € sign <i>Partial Credit</i> <ul style="list-style-type: none"> • Multiplies by 0.71 or divides by 24.83 <i>Full Credit –1</i> <ul style="list-style-type: none"> • Correct answer with incorrect or no rounding
(c)	$\frac{75.90}{330} \times 100 = 23\%$	Scale 10C (0, 4, 8, 10) Accept correct answer without work <i>Low Partial Credit</i> <ul style="list-style-type: none"> • Some relevant work, e.g. uses 100, inverted fraction, adds VAT to €330, etc. <i>High Partial Credit</i> <ul style="list-style-type: none"> • $\frac{75.90}{330}$ or 0.23 or equivalent • 77%

Q6	Model Solution – 20 Marks	Marking Notes
(a)&(b)	<p>(a) $3 \cdot 60 \div 2 = \text{€}1 \cdot 80$</p> <p>(b) Brand A is cheaper per litre</p> <p><i>Calculation:</i></p> <p>B: $1 \cdot 50 \div 0 \cdot 75 = \text{€}2$</p> <p style="text-align: center;">OR</p> <p>A: $1 \cdot 80 \times 0 \cdot 75 = \text{€}1 \cdot 35$</p> <p><i>or any other valid calculation(s) that allow a price per litre comparison</i></p>	<p>Scale 15D (0, 5, 9, 12, 15)</p> <p>In (a), accept correct answer without work</p> <p>In (b), correct answer without supporting work is considered work of merit (not correct).</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • Work of merit in one part <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> • Work of merit in both parts • One part correct <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • One part correct and work of merit in the other part <p><i>Full Credit – 1</i></p> <ul style="list-style-type: none"> • Calculations fully correct but cheaper brand not clearly indicated
(c)	<p>Lowest price = $\text{€}9 \cdot 60$</p> <p>Combination 1:</p> $3 \times 2\text{L} = 3 \times 3 \cdot 60 = \text{€}10 \cdot 80$ <p>Combination 2:</p> $(2 \times 2\text{L}) + (2 \times 0 \cdot 75\text{L})$ $= (2 \times 3 \cdot 60) + (2 \times 1 \cdot 50) = \text{€}10 \cdot 20$ <p>Combination 3:</p> $(1 \times 2\text{L}) + (4 \times 0 \cdot 75\text{L})$ $= (1 \times 3 \cdot 60) + (4 \times 1 \cdot 50) = \text{€}9 \cdot 60$ <p>Combination 4:</p> $7 \times 0 \cdot 75\text{L} = 7 \times 1 \cdot 50 = \text{€}10 \cdot 50$	<p>Scale 5C (0, 2, 4, 5)</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • Some attempt at combining quantities to make up at least 5 litres • Uses price per litre from (a) or (b) <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • Correct total for any combination making up at least 5 litres • Correct answer with no work <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> • $\text{€}9 \cdot 60$ as answer, with price of 1 other relevant combination calculated • All 4 possible totals calculated, cheapest not selected

Q7	Model Solution – 10 Marks	Marking Notes
(a)-(c)	(a) 89 270 (b) 89 000 (c) 8.93×10^4	<p>Scale 10D (0, 4, 6, 8, 10)</p> <p>Accept correct answer without work</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> Work of merit in 1 part: In (a): answers 89 260, 89 300, or 89 000 In (b): answers 90 000 or 89 300 In (c): incorrect relevant answer in the correct format <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> 1 part correct Work of merit in 2 parts <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> 2 parts correct 1 part correct and work of merit in other 2 parts

Q8	Model Solution – 15 Marks	Marking Notes
(a)&(b)	(a) $x(2x - 1) + 9(2x - 1)$ $= 2x^2 - x + 18x - 9$ $= 2x^2 + 17x - 9$ (b) $a(3x + y) + c(3x + y)$ $= (3x + y)(a + c)$ <p style="text-align: center;">OR</p> $3x(a + c) + y(a + c)$ $= (a + c)(3x + y)$	<p>Scale 15D (0, 5, 9, 12, 15)</p> <p>In (a), accept correct answer without work</p> <p>In (b), correct answer without supporting work is considered substantial work (not correct)</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> Work of merit in one part, e.g. in (a) sets up multiplication (including 2 arrows), or any correct relevant multiplication (including sign); in (b) indication of grouping of relevant terms <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> Work of merit in both parts Substantial work in (a) or (b), e.g. in (a) 3 terms correctly multiplied with correct signs, or all 4 terms correct in absolute value; in (b) one common factor correctly taken out of each pair, or correct answer with no supporting work <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> One part correct Substantial work in one part and work of merit in the other

Q9	Model Solution – 25 Marks	Marking Notes
(a)&(b)	(a) 30 m (b) 25 m	Scale 10B (0, 5, 10) Accept correct answer without work <i>Partial Credit</i> <ul style="list-style-type: none"> • (a) or (b) correct <i>Full Credit –1</i> <ul style="list-style-type: none"> • Correct answers for (a) & (b) swapped
(c)&(d)	(c) 10 seconds (d) $\frac{\text{Distance}}{\text{Time}} = \frac{25}{10} = 2.5 \text{ m/s}$ or $\frac{5}{2} \text{ m/s}$	Scale 10C (0, 4, 8, 10) Accept correct answer without work Accept correct answer without unit in (d) <i>Low Partial Credit</i> <ul style="list-style-type: none"> • Part (c) correct • Work of merit in part (d) <i>High Partial Credit</i> <ul style="list-style-type: none"> • Part (d) correct • Part (c) correct and work of merit in (d) <i>Full Credit –1</i> <ul style="list-style-type: none"> • $\frac{25}{10}$
(e)	Answer: No Reason: The graph does not go in a straight line or any other valid reason	Scale 5B (0, 2, 5) <i>Partial Credit</i> <ul style="list-style-type: none"> • Correct answer, incorrect or no reason • Incorrect or no answer, correct reason

Q10	Model Solution – 5 Marks	Marking Notes
(a)-(c)	(a)  (b)  (c)  OR 	Scale 5D (0, 2, 3, 4, 5) Accept 0 as an element in (a) Accept correct answer without work <i>Low Partial Credit</i> <ul style="list-style-type: none"> • Any correct element in any part <i>Mid Partial Credit</i> <ul style="list-style-type: none"> • One part correct <i>High Partial Credit</i> <ul style="list-style-type: none"> • Two parts correct <i>Full Credit – 1</i> <ul style="list-style-type: none"> • 4 included in one or more solutions, otherwise fully correct

Q11	Model Solution – 15 Marks	Marking Notes
	<p>Row 2: 2^5</p> <p>Row 3: 2^6</p> <p>Row 4: $2^{7+10} = 2^{17}$</p> <p>Row 5: $2^{4 \times 6} = 2^{24}$</p>	<p>Scale 15D (0, 5, 9, 12, 15)</p> <p>Accept correct answer without work</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • Work of merit in one part e.g. expansion such as $32 = 2 \times 2 \times 2 \times 2 \times 2$, or one relevant formula <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> • Two parts correct • Work of merit in three parts <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • Three parts correct <p><i>Full Credit –1</i></p> <ul style="list-style-type: none"> • Misreading: Correct powers given instead of numbers in form 2^p, i.e. 5, 6, 17, 24

Q12	Model Solution – 30 Marks	Marking Notes
(a)	<p>Row 3: $J + 5$</p> <p>Row 4: $J - 4$</p> <p>Row 5: $2 \times J$ OR $2J$</p> <p>Row 6: $\frac{1}{3} \times J$ OR $J \div 3$ OR $\frac{J}{3}$</p>	<p>Scale 15D (0, 5, 9, 12, 15)</p> <p>Accept correct answer without work</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • One part correct • Work of merit in one part, e.g. shows operation described (+5, -4, etc.) <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> • Two parts correct • Work of merit in 3 parts <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • Three parts correct • Work of merit in all 4 parts
(b)	$5M - 2M = 35 - 2$ $\Rightarrow 3M = 33$ $\Rightarrow M = 11$	<p>Scale 15C (0, 5, 10, 15)</p> <p>Note: 5 operations are needed to complete the question algebraically: 2 transpositions, 2 subtractions, and 1 division.</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • 1 correct relevant operation • Substitutes a value in for M <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • 3 correct relevant operations • Correct answer with no supporting work • Substitutes a number of values in for M, including 11, but answer not indicated, or both sides not fully worked out in case of $M = 11$

Q13	Model Solution – 20 Marks	Marking Notes
(a)&(b)	<p>(a) $f(x)$ is the straight line. $h(x)$ is the curve.</p> <p>(b) <i>Function: $f(x)$</i> <i>Reason: There's no x^2 term</i> or any other valid reason</p> <p style="text-align: center;">OR</p> <p><i>Function: $h(x)$</i> <i>Reason: It has an x^2 term</i> or any other valid reason</p>	<p>Scale 10C (0, 4, 8, 10)</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • Work of merit in (a) or (b), e.g. in (a): 1 answer correct in (b): mentions linear, straight, curved and/or quadratic, or similar <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • (a) or (b) correct. In (b), accept answer of $f(x)$ and reference to e.g. it being straight / linear, or to point on line; or answer of $h(x)$ and reference to e.g. it being quadratic / curved, or to point on curve
(c)&(d)	<p>(c) -0.45</p> <p>(d) $8^2 - 24 - 1$ $= 64 - 24 - 1 = 39$</p>	<p>Scale 10C (0, 4, 8, 10)</p> <p>Accept correct answer without work</p> <p>In (c), accept answer from -0.3 to -0.5, inclusive</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • Work of merit in (c) or (d), e.g. in (c): indicates correct point on graph, or indicates answer from y-axis; in (d): any correct substitution <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • (c) correct and work of merit in (d) • (d) correct

Q14	Model Solution – 30 Marks	Marking Notes
(a) (i)&(ii)	(i) $(x + 7)(x - 1)$ (ii) $x + 7 = 0$ $\Rightarrow x = -7$ AND $x - 1 = 0$ $\Rightarrow x = 1$	Scale 15D (0, 5, 9, 12, 15) Accept correct answers without additional supporting work <i>Low Partial Credit</i> <ul style="list-style-type: none"> Work of merit in (i) or (ii), e.g. In (i): Correct factorising of x^2 or 7, ignoring signs In (ii): Puts answer(s) from (i) = 0, or substitutes in a value for x, or quadratic formula. <i>Mid Partial Credit</i> <ul style="list-style-type: none"> (i) or (ii) correct Work of merit in both parts <i>High Partial Credit</i> <ul style="list-style-type: none"> One part correct and work of merit in the other part
(b)	Equation 1 – Equation 2: $2x = 14$ $\Rightarrow x = 7$ Equation 2: $7 + 2y = 25$ $\Rightarrow 2y = 25 - 7 = 18$ $\Rightarrow y = 9$	Scale 15C (0, 5, 10, 15) Accept solution by inspection, or by trial and improvement, if it is verified for both equations <i>Low Partial Credit</i> <ul style="list-style-type: none"> One correct operation Substitution of incorrect solution into both equations <i>High Partial Credit</i> <ul style="list-style-type: none"> One correct solution for x or y, by algebra x and y correct, with no supporting work Finds x incorrectly by algebra, finishes correctly to find y