

CSCE 222: Discrete Structures for Computing
Section 503
Fall 2016

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Problem Set 9

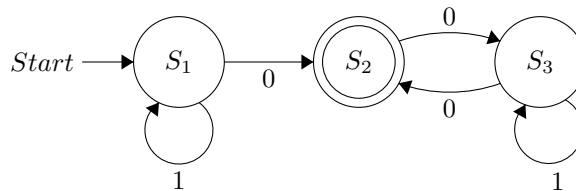
Due: 30 October 2016 (Sunday) before 11:59 p.m. on eCampus (ecampus.tamu.edu).
You must show your work in order to receive credit.

Problem 1. (25 points)

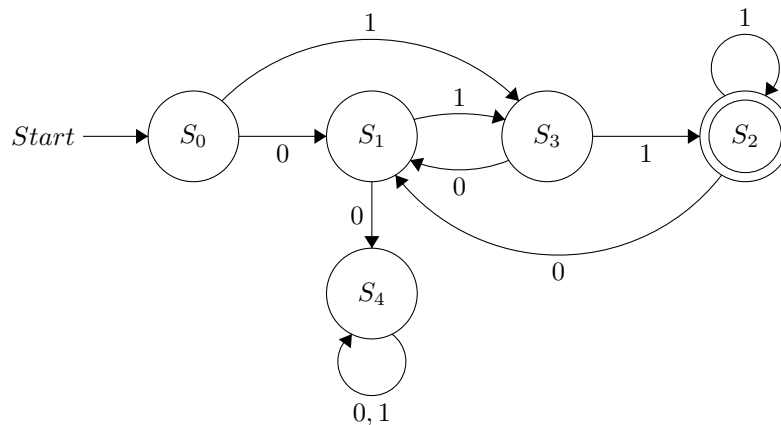
1. Build a finite-state automaton that accepts the language $1^*0(1 \cup 01^*0)^*$. Give an English description of the language (your description should be about 10 words long, of which the first 5 are *the set of strings containing*).
2. Build a finite state automaton that recognizes the set of strings that end in 11 and do not contain 00. Convert this finite-state automaton into an equivalent regular expression.

Solution.

1. The set of strings containing bitstrings 10, 0010, or 0



- 2.



Regular Expression: $(1 + (01)^*)(01)^*(1 + \lambda)^*$

Problem 2. (25 points)

Construct a Turing machine that recognizes the set $\{0^{2^n}1^n \mid n \geq 0\}$. The Turing machine starts with the input on the tape and the head over the leftmost symbol of the input. The symbols to the left of the input are blanks out to infinity, as are the symbols to the right of the input. If the string is accepted, the machine should halt with 1 on the tape (the rest of the tape should be blank). If the string is rejected, the machine should halt with 0 on the tape.

Note: this is not an easy task, it will take you several revisions to get it right, do not get discouraged.

Solution.

Problem 3. (25 points)

For each relation on the set of all people, determine whether it is an equivalence relation. For each relation that is not an equivalence relation, determine which properties of an equivalence relation it lacks. Your answers are not complete unless you include the definition of each property.

1. $\{(a, b) \mid a \text{ and } b \text{ are the same age}\}$
2. $\{(a, b) \mid a \text{ and } b \text{ have the same parents}\}$
3. $\{(a, b) \mid a \text{ and } b \text{ share a common parent}\}$
4. $\{(a, b) \mid a \text{ and } b \text{ have met}\}$
5. $\{(a, b) \mid a \text{ and } b \text{ speak a common language}\}$

Solution.

Problem 4. (25 points)

Which of these are partially ordered sets? For each relation which is not a partial ordering, determine which properties of a partial ordering the relation lacks. Your answers are not complete unless you include the definition of each property.

1. $(\mathbb{R}, =)$
2. (\mathbb{R}, \leq)
3. $(\mathbb{R}, >)$
4. (\mathbb{R}, \neq)
5. $(\mathcal{P}(\mathbb{Z}), \subseteq)$, where $\mathcal{P}(\cdot)$ is the powerset.

Solution.

Aggie Honor Statement: On my honor as an Aggie, I have neither given nor received any unauthorized aid on any portion of the academic work included in this assignment.

Checklist: Did you...

1. abide by the Aggie Honor Code?
2. solve all problems?
3. start a new page for each problem?
4. show your work clearly?
5. type your solution?
6. submit a PDF to eCampus?