

## Part 1

Let

A=Timestamp  
B=State  
C=locality  
D=precinct  
E=geo  
F=totalvotes  
G=Biden  
H=Trump

Let  $R=ABCDEFGH$  be a relation. Since the precinct determines the location, which contains the state, locality, and geo, we have  $D$  (precinct) determine  $B$  (state),  $C$  (locality), and  $E$  (geo). In addition to location, the precinct determines the voting as well, so we have  $D$  (precinct) determine  $A$  (timestamp),  $F$  (totalvotes),  $G$  (Biden), and  $H$  (Trump).

a) In total, we have two functional dependencies,  $D \rightarrow BCE$  and  $AD \rightarrow FGH$  and have  $F=\{D \rightarrow BCE, AD \rightarrow FGH\}$ .

b)

- i) Penna, as  $R(ABCDEFGH)$ , is decomposed to form  $R_1(DBCE)$  and  $R_2(ADFGH)$  since it is candidate key and does not satisfy BCNF due to conflicts with all functional dependencies. (By  $R - R_1$ )
- ii)  $R_1(DBCE)$  satisfies BCNF because it determines all attributes of  $D \rightarrow BCE$ , and is trivial with  $AD \rightarrow FGH$  via projection ( $D \rightarrow 0$ ).
- iii)  $R_2(ADFGH)$  satisfies BCNF because it determines all attributes of  $AD \rightarrow FGH$ , and is trivial with  $D \rightarrow BCE$  via projection ( $D \rightarrow 0$ ).

Final two relations in BCNF:  $R_1(DBCE)$ ,  $R_2(ADFGH)$