

# FA4

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## FA6 Questions

1. A geospatial analysis system has four sensors supplying images. The percentage of images supplied by each sensor and the percentage of images relevant to a query are shown in the following table.

Sensor	Percentage_of_Images_Supplied	Percentage_of_Relevant_Images
1	15	50
2	20	60
3	25	80
4	40	85

What is the overall Percentage of the Relevant Images?

```
percentSupplied <- c(15, 20, 25, 40)
percentRelevant <- c(50, 60, 80, 85)

overallPercentage <- sum(percentSupplied * percentRelevant) / sum(percentSupplied)

cat("Overall percentage of the Relevant images:", overallPercentage, "%\n")
```

```
## Overall percentage of the Relevant images: 73.5 %
```

2. **A fair coin is tossed twice.** Let  $E$  be the event that both tosses have the same outcome, that is,  $E1 = (HH, TT)$ . Let  $E2$  be the event that the first toss is a head, that is,  $E2 = (HH, HT)$ . Let  $E3$  be the event that the second toss is a head, that is,  $E3 = (TH, HH)$ . Show that  $E1$ ,  $E2$ , and  $E3$  are pairwise independent but not mutually independent.

	Heads	Tails
Heads	HH	HT
Tails	TH	TT

```
## E1 is the Event both results are the Same
## E2 is the Event first results are the Heads
## E1 is the Event second results are the Heads
## From the table we can see each event has 1/2 of the chance
## 0.5 0.5 0.5
## The two events E1 UNION E2 happening are the the products of its probabilities
```

```

## 0.25 Which is just the probability of HH on the table which is 1/4 and the UNION of the two events is
## We can derive that E1 UNION E3 and E2 UNION E3 will also have 1/4 probabilities
## and respectively have HH as the UNION too
## 0.25 0.25

## These prove their Pairwise Independent but now to show they are not Mutually Independent.
## We can just apply the same principle of multiplying the Probabilities and their UNION's and we will see
## E1 UNION E2 UNION E3 have HH as the probability which is 1/4 but is not equal to the probability of HH
## 0.125 Hence they are not Mutually Independent because E2 and E3 itself doesn't carry information or
## data to help form the probability of E1 it is still 1/2 but having the UNION of E2 and E3 will
## change the probability of E1 to happen becoming 1 means it's guaranteed

```