

Disc 8 - CFGs and Parsing

Tuesday, October 26, 2021 9:43 PM

- 1) Identify the terminals, non-terminals, production rules, and the start state of the following CFG:

$S \rightarrow aSa \mid B$

$B \rightarrow bC \mid C$

$C \rightarrow \epsilon$

- 2) Show that the following CFG is ambiguous:

$S \rightarrow S + S \mid 1$

- 3) Convert the following into a non-ambiguous CFG:

$S \rightarrow S + S \mid 1$

- 4) Convert the following CFG into one that can be used with recursive descent parsing:

$S \rightarrow S + S \mid M$

- 5) Convert the following CFG into one that can be used with recursive descent parsing:

$S \rightarrow S + S \mid 1 \mid 2 \mid 3$

6) Write a CFG for the following:

$$a^x b^x$$

7) Write a CFG for the following:

$$a^x b^y, \text{ where } x=2y$$

8) Write a CFG for the following:

$$a^x b^y, \text{ where } x > y$$

9) Write a CFG for the following:

$$a^x b^y c^z, \text{ where } z = x + y$$

10) Write a grammar for all palindromes consisting of a's and b's

11) Write a CFG equivalent to $(wp)^+g^*$

12) Write a CFG for the following:

$$a^x b^y c^z, \text{ where } y = x + z$$

13) Define a lexer for the following token definitions

```
type token =  
  | Tok_Int of int  
  | Tok_Add  
  | Tok_EOF
```

Useful functions:

Str.string_match (Str.regexp "some string") string index -> boolean

Str.matched_string input -> string

let rec lexer (input: string) : token list =

14) Define a parser for the above tokens and following CFG and expr type

$S \rightarrow M + S \mid M$

$M \rightarrow n$

Where n is any integer

Type expr =

```
| Int of int  
| Plus of expr * expr
```

Useful functions:

match_token (toks : token list) (tok : token) : token list

lookahead (toks : token list) : token

let rec parser (toks : token list) : expr =

and parse_S (toks : token list) : (token list * expr) =

and parse_M (toks : token list) : (token list * expr) =