#### Question 1 - Bash

 Using "echo", print your student number to the terminal. Additionally, print out your username from the operating system. Take a screenshot and include it in your submission

```
joshlegrice@Joshs-MacBook-Pro-2 ~ % echo "Student Number: 720017170" [echo "Username: $(whoami)" Student Number: 720017170 Username: joshlegrice
```

b) Move inside the directory DATE\_FILES, which was provided along with unit 2 of the course, which you should store somewhere on your computer.

```
joshlegrice@Joshs-MacBook-Pro-2 ~ % cd /Users/joshlegrice/Desktop/University/3rd\ Year/Data\ Science\ in\ Economics/DATE_FILES
joshlegrice@Joshs-MacBook-Pro-2 DATE_FILES % |
```

# cd = changes the current working directory to the file path given

c) Count the number of files in this directory.

```
# ls -1 = Lists all files in the directory, one per line
```

# | allows the output of the command before to be used as the input to the next command # wc -l = Counts the number of lines in the output of ls -1

#\$ = allow the code inside the brackets to be executed and not just echoed, like Python f string

```
joshlegrice@Joshs-MacBook-Pro-2 DATE_FILES % echo "Number of files: $(ls -1 | wc -1)"

Number of files: 3289
```

d) Print the names of the first 8 files in this directory, along with information about their ownership, date, and size.

```
joshlegrice@Joshs-MacBook-Pro-2 DATE_FILES % ls -lh | head -n 8
total 26312
           1 joshlearice
                          staff
                                   110B 25 Jan
                                                2024 2015 01 01.txt
                                   110B 25 Jan
           1 joshlegrice
                                                2024 2015_01_02.txt
                           staff
   -rw-r--@ 1 joshlegrice
                                   110B 25 Jan
                                                2024 2015_01_03.txt
                           staff
     w-r--@ 1 joshlegrice
                                   110B 25 Jan
                                                2024 2015_01_04.txt
    rw-r--@ 1 joshlegrice
                           staff
                                   110B 25 Jan
                                                2024 2015_01_05.txt
  cw-rw-r--@ 1 joshlegrice
                           staff
                                   110B 25 Jan
                                                2024 2015 01 06.txt
-rw-rw-r--@ 1 joshlegrice
                           staff
                                   110B 25 Jan
                                                2024 2015_01_07.txt
```

# ls -lh = lists the contents of the directory in long (l) format and human-readable (h).

 $\#\ |\ allows\ the\ output\ of\ the\ command\ before\ to\ be\ used\ as\ the\ input\ to\ the\ next\ command\$ 

# head -n 8 = only displays the first 8 lines of the output

e) Move to the parent directory of this folder

```
[joshlegrice@Joshs-MacBook-Pro-2 DATE_FILES % cd ..
```

# cd = change directory to the file path given

# .. = indicates the parent directory of the current file

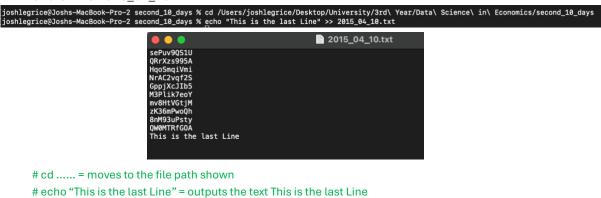
f) Create a new directory there, named second\_10\_days

```
joshlegrice@Joshs-MacBook-Pro-2 Data Science in Economics % mkdir -p second_10_days
```

# mkdir = command to make a new directory
# -p = ensures parent directories exist
# second\_10\_days = the name of the new directory

g) Copy from the DATE\_FILES directory the files that are related to the days 10-19 of every month to the newly created directory.

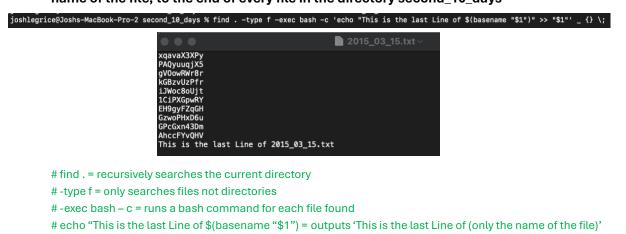
h) Move inside second\_10\_days directory, and append the line "This is the last Line" to the end of file 2015\_04\_10



i) Write a one-line command to append the line "This is the last Line of X", where X is the name of the file, to the end of every file in the directory second\_10\_days

# >> 2015\_04\_10.txt = appends the echoed text into the file 2015\_04\_10.txt

#>> "\$1"'\_{} \; = appends the output of the echo into the file.



j) Using Bash: create a bash file Q1.sh. Write your code from (i) to it. Run the file Q1.sh including a screenshot showing how this runs on your system. Please explain any steps needed to run this file.

Had to place the .sh file into another directory as if placed in the second\_10\_days directory, it would write into the Q1.sh file with 'this is the last Line of Q1.sh'

Second step = Write code in .sh file



Final Step = Run .sh file

```
Last login: Thu Feb 20 11:29:33 on console [joshlegrice@Joshs-MacBook-Pro-2 ~ % ./Q1.sh joshlegrice@Joshs-MacBook-Pro-2 ~ %
```

Output in an example file – I ran it a lot to make sure it worked

```
TcyEMjZYKt
PArpAcEa9e
48QDGRKLMF
VZ5nV4MpOk
3mmblBfsSc
5Gkva3CkuS
9Am8wWncYK
AAVg6AHyCe
ijGMJJdgY9
cF3KQJQ11g
This is the last Line of 2023_12_27.txt
```

#### Question 2 - SQL

a) Create a new database in SQLite named Q2.db

```
[joshlegrice@Joshs-MacBook-Pro-2 Assignment % sqlite3 Q2.db
SQLite version 3.43.2 2023-10-10 13:08:14
Enter ".help" for usage hints.
sqlite> ■
```

b) Create two tables named US\_Code and US\_Pop with column headings that match these two data frames

```
CREATE TABLE US_Code (
    CountryCode VARCHAR(5),
    ZipCode VARCHAR(10) PRIMARY KEY,
    City VARCHAR(100),
    StateFull VARCHAR(50),
    State2 VARCHAR(5),
    CountyFull VARCHAR(100),
    FIPSCountyCode VARCHAR(10),
    MunicipalityFull VARCHAR(10),
    MunicipalityCode VARCHAR(10),
    Latitude REAL,
    Longitude REAL,
    Accuracy INTEGER
);
```

```
CREATE TABLE US_Pop (
ID INTEGER PRIMARY KEY AUTOINCREMENT,
Geo_ID VARCHAR(20),
Zip VARCHAR(10),
Gender VARCHAR(10),
AgeRange VARCHAR(20),
Population INTEGER,
FOREIGN KEY (Zip) REFERENCES US_Code(ZipCode)
);
```

c) Insert the data from the two files into the two tables. Make sure you don't insert the column heading from the file US\_population.csv. Explain how you did this.

```
[sqlite> .mode tabs
[sqlite> .import US_codes.txt US_Code
US_codes.txt:41098: INSERT failed: UNIQUE constraint failed: US_Code.ZipCode
US_codes.txt:41439: INSERT failed: UNIQUE constraint failed: US_Code.ZipCode
US_codes_txt:41440: INSERT failed: UNIQUE constraint failed: US_Code.ZipCode
```

# Had to remove duplicates before loading in the US\_Code data due to the above error

```
joshlegrice@Joshs-MacBook-Pro-2 Assignment % awk -F'\t' '{print $2}' US_codes.txt | sort | uniq -d

09464

96860

96863
joshlegrice@Joshs-MacBook-Pro-2 Assignment % awk -F'\t' '!seen[$2]++' US_codes.txt > US_codes_cleaned.txt
```

# awk -F'\t' '{print \$2}' US\_codes.txt = Extracts the second column from the .txt file which is ZipCode # sort = sorts the values within the column

# uniq -d = identifies and prints only the duplicate values = Used to visualise all duplicate values

# awk -F'\t' '!seen[\$2]++' US\_codes.txt = collects all the non-duplicates in the column into an array # > US\_codes\_cleaned.txt = saves the contents of the previous output into a new file

```
|sqlite> .mode tabs
|sqlite> .import US_codes_cleaned.txt US_Code
|sqlite> select * from US_Code Limit 5;
```

CountryCode	ZipCode	City	StateFull	State2	CountyFull	FIPSCountyCode	MunicipalityFull	MunicipalityCode	Latitude	Longitude	Accurac
US US US US US	99553	Akutan	Alaska	AK	Aleutians East	013			54.143	-165.7854	1
US	99571	Cold Bay	Alaska	AK	Aleutians East	013			55.1858	-162.7211	1
US	99583	False Pass	Alaska	AK	Aleutians East	013			54.841	-163.4368	1
US	99612	King Cove	Alaska	AK	Aleutians East	013			55.0628	-162.3056	1
US	99661	Sand Point	Alaska	AK	Aleutians East	013	l i		55.3192	-160.4914	1

# .mode tabs to set the delimiter to tabs to distinguish columns

joshlegrice@Joshs-MacBook-Pro-2 Assignment % tail -n +2 US\_population.csv > US\_population\_cleaned.csv joshlegrice@Joshs-MacBook-Pro-2 Assignment % ■

# tail -n +2 = starts at line 2 and collects all rows
# > US\_population\_cleaned.csv = moves the new data into the new file

#I had trouble with importing the data straight into the US\_Pop table due to this error

```
Isqlite> .mode csv
sqlite> .import US_Pop_Clean.csv US_Pop

US_Pop_Clean.csv:125718: expected 6 columns but found 5 - filling the rest with NULL
US_Pop_Clean.csv:125718: INSERT failed: datatype mismatch
US_Pop_Clean.csv:125719: expected 6 columns but found 5 - filling the rest with NULL
US_Pop_Clean.csv:125719: INSERT failed: datatype mismatch
```

# So, I imported the data into a temporary table and then copied the data into US\_Pop

```
sqlite> .mode csv
sqlite> .import US_population_cleaned.csv temp_US_Pop
CREATE TABLE temp_US_Pop (
                                                     sqlite> .mode box
sqlite> Select * from temp_US_Pop limit 5;
       Geo_ID VARCHAR(20),
       Zip VARCHAR(10),
                                                           Geo_ID
                                                                         Zip
                                                                                 Gender
                                                                                           AgeRange
                                                                                                      Population
       Gender VARCHAR(10),
                                                       8600000US61747
8600000US64120
       AgeRange VARCHAR(20),
                                                                        64120
95117
74074
                                                                                 male
male
female
                                                                                                      5
1389
231
                                                                                           85-
                                                       8600000US95117
8600000US74074
                                                                                          30--34
60--61
       Population INTEGER
                                                       8600000US58042
                                                                         58042
```

# Inserting data from temp table to US\_Pop

```
    sqlite> INSERT INTO US_Pop (Geo_ID, Zip, Gender, AgeRange, Population)

    ...> SELECT Geo_ID, Zip, Gender, AgeRange, Population FROM temp_US_Pop;

    sqlite> Select * from US_Pop Limit 5;

    ID
    Geo_ID
    Zip
    Gender
    AgeRange
    Population

    1
    8600000US61747
    61747
    female
    30--34
    50

    2
    8600000US61747
    64120
    male
    85---
    5

    3
    8600000US95117
    95117
    male
    30--34
    1389

    4
    8600000US58042
    74074
    female
    60--61
    231

    5
    860000US58042
    58042
    female
    0--4
    56
```

d) Write an SQL query to print the total population per gender (using the US\_Pop table only)

```
[sqlite> SELECT Gender, SUM(Population) as Total_Population
[ ...> FROM US_Pop
[ ...> GROUP BY Gender;

Gender Total_Population
female 378160746
male 365004493
```

e) Write an SQL query to print the total population per gender but join the two tables. If you see any difference in your results between this question and part (d), explain why this occurs.

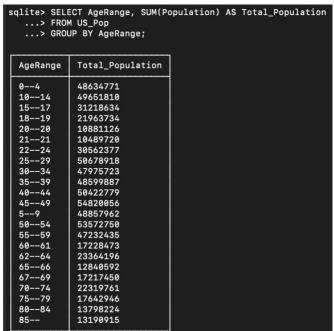
```
sqlite> SELECT Gender, SUM(Population) AS Total_Population
...> FROM US_Pop
...> INNER JOIN US_Code ON US_Code.ZipCode = US_Pop.Zip
...> GROUP BY Gender;

Gender Total_Population

female 345258967
male 333951977
```

The difference is because INNER JOIN only includes records where zip codes exist in both US\_Pop and US\_Code, excluding unmatched zip codes from US\_Pop. This results in a lower total population in part (e) compared to part (d).

f) Write an SQL query to print the total population per age group (use the US\_Pop table only).



g) Write an SQL query to print the Top 10 largest states (full name) in terms of population size

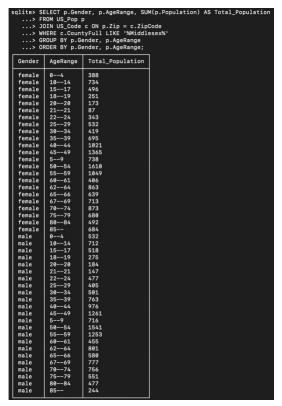
```
sqlite> SELECT c.StateFull, SUM(p.Population) AS Total_Population
   ...> FROM US_Pop p
   ...> JOIN US_Code c ON p.Zip = c.ZipCode ...> GROUP BY c.StateFull
   ...> ORDER BY Total_Population DESC
   ...> LIMIT 10;
    StateFull
                    Total_Population
  California
                    88526840
                    59743982
  Texas
                    46247865
 New York
                    44945558
  Florida
  Illinois
                    30596527
  Pennsylvania
                    30255696
                    27462317
  Ohio
  Michigan
                    23490804
  Georgia
                    23123141
  North Carolina
                    22670061
```

h) Write an SQL query to print the number of existing counties (not countries) in the database

```
sqlite> SELECT COUNT(DISTINCT CountyFull) AS Total_Counties
...> FROM US_Code;

Total_Counties
1853
```

i) Write an SQL query to print the total population per gender and age group for any counties containing "Middlesex" in their name.



# Question 3 + 4

# 720017170

# Question 3 - See QMD for Code

(a) Import each dataset into memory as a separate data frame, keeping all countries as your sample.

```
plt.rcParams.update({'font.size': 14})

# Loading in the Data
Health_Data = pd.read_csv('Health.csv', index_col=None)
Infant_Data = pd.read_csv("Infant.csv",index_col=None)

# Replace .. with NA
Health_Data.replace("..", pd.NA, inplace=True)
Infant_Data.replace("..", pd.NA, inplace=True)

# Removing unnecessary columns
Health_Data = Health_Data.drop(columns=['Series Name', 'Series Code'])
Infant_Data = Infant_Data.drop(columns=['Series Name', 'Series Code'])

# Remove names in []
Health_Data.columns = Health_Data.columns.str.replace(r'\[.*\]', '', regex=True)
Infant_Data.columns = Infant_Data.columns.str.replace(r'\[.*\]', '', regex=True)
print(Infant_Data.head())
print(Health_Data.head())
```

```
Country Name Country Code 2000 2001 2002 2003 2004 2005
                                                            2006
0
                        AFG
                              92 89.3 86.6 83.7 80.9
     Afghanistan
                                                         78
                                                             75.1
                              24 22.9 21.6 20.4
1
         Albania
                        ALB
                                                  19.1 17.8
                                                             16.5
2
         Algeria
                        DZA 35.6 34.3
                                         33 31.6 30.3
                                                          29
                                                             27.8
                        ASM <NA> <NA> <NA> <NA> <NA>
3 American Samoa
                                                             <NA>
```

```
4
          Andorra
                             AND
                                    6.5
                                          6.3
                                                       5.8
                                                              5.6
                                                                    5.3
                                                                           5.1
                                              2019 2020
  2007
              2014
                    2015 2016
                                 2017
                                        2018
                                                            2021
                                                                  2022
                                                                         2023
  72.3
               56.2
                     54.6
                              53
                                  51.5
                                         50.1 48.8
                                                      47.4
                                                            46.1
                                                                   44.8
                                                                          <NA>
   15.3
                8.8
                      8.5
                             8.4
                                    8.3
                                          8.3
                                                 8.3
                                                       8.4
                                                              8.4
                                                                    8.4
                                                                          <NA>
1
2
   26.6
                 22
                     21.7
                            21.4
                                     21
                                         20.6
                                               20.1
                                                      19.7
                                                             19.2
                                                                   18.7
                                                                          <NA>
3
   <NA>
               <NA>
                      <NA>
                            <NA>
                                  <NA>
                                         <NA>
                                                <NA>
                                                      <NA>
                                                             <NA>
                                                                   <NA>
                                                                          <NA>
                                    3.1
                                                 2.9
4
    4.9
                3.5
                      3.4
                             3.2
                                            3
                                                       2.8
                                                              2.7
                                                                    2.6
                                                                          <NA>
[5 rows x 26 columns]
     Country Name Country Code
                                           2000
                                                            2001
                                                                          2002
                                                                                 \
0
      Afghanistan
                             AFG
                                                             <NA>
                                                                   17.00758553
                                            <NA>
1
                                                                   78.99478149
           Albania
                             ALB
                                      65.1501236
                                                     73.78884125
2
                                     62.11769485
                                                     67.33850098
                                                                   66.94760132
           Algeria
                             DZA
3
   American Samoa
                             ASM
                                            <NA>
                                                             <NA>
                                                                           <NA>
           Andorra
                             AND
                                  1287.00280762
                                                   1336.21142578
                                                                   1486.171875
            2003
                           2004
                                           2005
                                                            2006
                                                                            2007
                                                                                    \
0
     17.81492424
                    21.42946434
                                     25.10707283
                                                     28.91982269
                                                                     32.71720505
1
    106.29218292
                  138.11340332
                                    152.12762451
                                                    166.81382751
                                                                    212.61096191
     76.23547363
                                    101.30373383
                                                                    151.77920532
2
                    93.02433014
                                                    117.43313599
3
             <NA>
                            <NA>
                                            <NA>
                                                             <NA>
                                                                             <NA>
   1772.71337891
                   1990.0748291
                                  2214.64697266
                                                   2139.27539063
                                                                   2489.43115234
                 2014
                                 2015
                                                  2016
                                                                  2017
                                                                          \
   . . .
0
          60.18957901
                           60.05854034
                                           61.48645782
                                                            66.90921783
   . . .
         295.12359619
                          255.35635376
                                          277.04321289
                                                            297.4619751
1
2
                                          261.40023804
                                                           265.83843994
   . . .
         361.15942383
                            292.275177
3
                                                   <NA>
                  <NA>
                                   <NA>
                                                                   <NA>
4
        3089.84301758
                         2688.20629883
                                         2755.44848633
                                                         2873.29614258
                                                             2021
            2018
                            2019
                                            2020
                                                                   2022
                                                                          2023
0
     71.33430481
                                      80.28805542
                     74.23410797
                                                      81.31976318
                                                                    <NA>
                                                                           <NA>
1
     351.3012085
                    367.75839233
                                     396.88024902
                                                     464.74285889
                                                                    <NA>
                                                                           <NA>
2
    266.46469116
                    235.99041748
                                     206.03512573
                                                     204.56661987
                                                                           <NA>
                                                                    <NA>
3
             <NA>
                             <NA>
                                              <NA>
                                                              <NA>
                                                                    <NA>
                                                                           <NA>
   3164.38842773 3026.59741211 3269.29736328
                                                    3505.99145508
                                                                           <NA>
                                                                    <NA>
```

[5 rows x 26 columns]

(b) If data are not already stored in this way, please reshape data so that they consist of a single line of data for each country and year.

	Country Name	Country Code	Year	Heathcare Expenditure (USD)
0	Afghanistan	AFG	2000	<na></na>
1	Albania	ALB	2000	65.1501236
2	Algeria	DZA	2000	62.11769485
3	American Samoa	ASM	2000	<na></na>
4	Andorra	AND	2000	1287.00280762

	Country Name	Country Code	Year	Infant Mortality Rates (per 1,000 live births)
0	Afghanistan	AFG	2000	92
1	Albania	ALB	2000	24
2	Algeria	DZA	2000	35.6
3	American Samoa	ASM	2000	<NA $>$
4	Andorra	AND	2000	6.5

(c) Calculate the total number of countries observed in each data frame Calculate the total number of years observed in each data frame.

```
# Counts the number of unique contries
num_countries_FDI = Health_Data_long["Country Name"].nunique()

# Outputs the number of unique countries using an f string
print(f"Total number of unique countries in Health_Data: {num_countries_FDI}")
num_years_FDI = Health_Data_long["Year"].nunique() # Counts the number of unique years
print(f"Total number of unique years observed in Health_Data: {num_years_FDI}")
```

```
num_countries_GDP = Infant_Data_long["Country Name"].nunique()
print(f"Total number of unique countries in Infant_Data: {num_countries_GDP}")
num_years_GDP = Infant_Data_long["Year"].nunique()
print(f"Total number of unique years observed in Infant_Data: {num_years_GDP}")
Total number of unique countries in Health_Data: 217
Total number of unique years observed in Health_Data: 24
Total number of unique countries in Infant_Data: 217
Total number of unique years observed in Infant_Data: 24
```

(d) Calculate the number of observations for which data is missing

```
# Sums the number of missing values in each dataset
missing_values_Health = Health_Data_long.isna().sum().sum()
print(f"Total missing observations in Health_Data: {missing_values_Health}")
missing_values_Infant = Infant_Data_long.isna().sum().sum()
print(f"Total missing observations in Infant_Data: {missing_values_Infant}")
# Create a dataframe showing the number of missing values for each dataset
missing_values_table = pd.DataFrame({
    'Dataset': ['Health_Data', 'Infant_Data'],
    'Total Missing Observations': [missing_values_Health, missing_values_Infant]
})
```

Total missing observations in Health\_Data: 1099 Total missing observations in Infant\_Data: 700

(e) Join the two files by country and year so that you have single dataframe containing both variables. Explain clearly what type of join this is, and carefully check that the number of observations resulting from the join makes sense.

```
# Merge the data on Country Name, Country code and Year
merged_data = pd.merge(Health_Data_long, Infant_Data_long, on=['Country Name',
'Country Code', 'Year'])
print(merged_data.head())

# Print the number of rows in the DataFrame
num_rows = merged_data.shape[0]
print(f"Number of rows in the DataFrame: {num_rows}")
```

```
Year Heathcare Expenditure (USD)
     Country Name Country Code
0
      Afghanistan
                            AFG
                                 2000
                                                               <NA>
1
          Albania
                            ALB
                                 2000
                                                         65.1501236
2
          Algeria
                            DZA
                                 2000
                                                        62.11769485
   American Samoa
3
                            ASM 2000
                                                               <NA>
                                                      1287.00280762
          Andorra
                            AND
                                 2000
  Infant Mortality Rates (per 1,000 live births)
0
                                                92
1
                                                24
2
                                             35.6
3
                                             <NA>
                                              6.5
4
```

Number of rows in the DataFrame: 5208

The join completed in the above code chunk is an inner join and only keeps rows that exist in both Health\_Data\_long and Infant\_Data\_long. If a country-year exists in one dataset but not the other, it will be dropped.

# Question 4 - Investigating the Relationship Between Current Healthcare Expenditure per capita and Infant Mortality Rates from 2000 - 2022

#### Missing Data - Table 1

Total Missing Observations					

Both datasets contained a considerable amount of missing data, illustrated in Table 1. Potentially due to countries not collecting the data or collecting the data at different year intervals. Missing data can have a large impact on data analysis if not handled properly and can lead to skewed or incorrect conclusions. The year 2023 contained no data; therefore, this column was dropped. To deal with the other missing data, I decided to drop all rows containing missing data, sometimes, this could result in a significant reduction of sample size; however, in this case, 1099 observations were removed (21.1% of the dataset) and only 27 countries were dropped, indicating this was an effective method to handling missing data as there were still 4109 observations. An alternative approach would've been mean, multiple or regression imputation if dropping rows with missing data caused a significant decrease in sample size.

#### Summary Statistics - Table 2

Variable	N	Mean	Median	SD	Min	Max
Heathcare Expenditure (USD) Infant Mortality Rates (per 1,000 live births)	4109.0	956.0	256.7	1685.7	4.0	12473.8
	4109.0	26.9	17.7	25.0	1.4	138.3

Table 2 displays the summary statistics for healthcare expenditure (USD) and infant mortality rates (per 1,000 live births) across 4109 observations, revealing significant differences between countries.

Healthcare expenditure per capita showed a mean of \$956.0 but a far lower median of \$256.7, indicating a negatively skewed distribution where few countries spend significantly more. The large standard deviation (\$1,685.7) and range (\$4.0–\$12,473.8) highlight large global and temporal differences in healthcare investment.

Infant mortality rates show similar variation, with a mean of 26.9 deaths per 1,000 live births and a median of 17.7. The high standard deviation (25.0) and range (1.4–138.3) suggest major differences in healthcare quality and access.

Overall, the data underscores global disparities in healthcare funding and outcomes, suggesting that higher healthcare expenditure may be linked to lower infant mortality.

#### Distribution Analysis

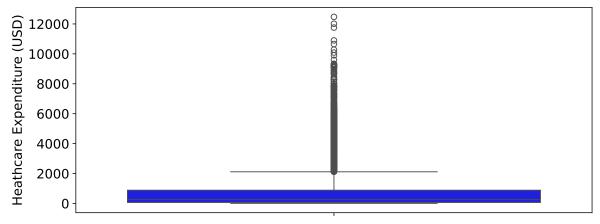


Figure 1: Box Plot of Healthcare Spend Per Capita (USD)

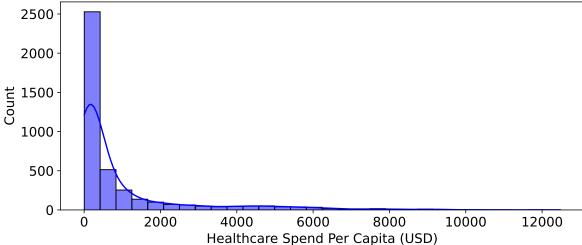


Figure 2: Histogram with Density of Healthcare Spend Per Capita (USD)

Figures 1 and 2 show the distribution of healthcare spending per capita (USD). Figure 1 shows that healthcare expenditure is highly negatively skewed, with many outliers at the upper end, supporting the analysis from the summary statistics. The median expenditure is positioned toward the lower end of the distribution, indicating that most countries spend relatively little, while a few spend significantly more. The whiskers of the box plot are short, suggesting that a large proportion of the data is concentrated within a lower range, while the numerous outliers highlight extreme spending levels in some countries.

Figure 2 reiterates the negative skew of the data. Most countries have low healthcare spending, grouped toward the left of the axis, with just a handful having exceptionally high expenditures. The density curve (smooth blue line) depicts the exponential drop in frequency as expenditure increases, emphasising that high-spending countries are exceptions rather than the rule

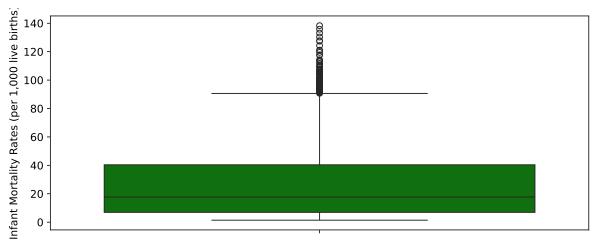


Figure 3: Box Plot of Infant Mortality Rate (per 1,000 live births)

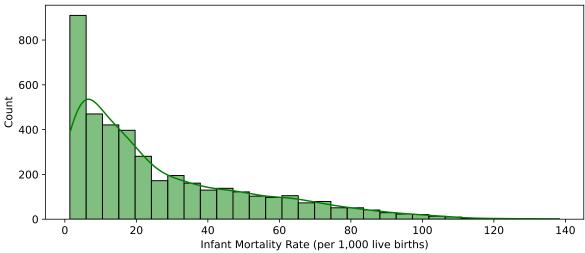


Figure 4: Histogram with Density of Infant Mortality Rate (per 1,000 live births)

The distribution of the infant mortality rate (per 1,000 live births) seen in Figures 3 and 4 is comparable to that of healthcare spend per capita (USD).

There are several outliers in Figure 3, with specific countries having abnormally high infant death rates. The data is still negatively skewed, as seen by the median being significantly lower than the upper quartile.

This is supported by Figure 4, which displays a dramatic fall as rates rise, with most values clustering below 40 deaths per 1,000 live births. While infant mortality is low in many nations, it is much higher in others, most likely because of infrastructural constraints, economic considerations, and healthcare discrepancies.

# Correlation Analysis

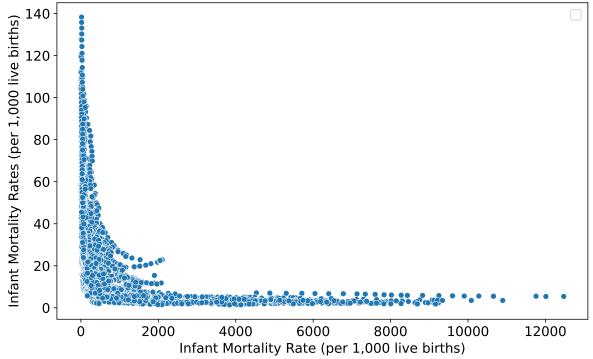


Figure 5: Scatter Plot: Healthcare Spend Per Capita vs Infant Mortality Rate

A scatter plot showing the correlation between infant mortality rate (per 1,000 live births) and healthcare spending per capita (USD) is shown in Figure 5. Higher healthcare spending is linked to decreased infant death rates, according to the trend, which shows a significant negative association.

However, the relationship is non-linear, with infant mortality declining sharply at lower health-care spending levels and plateauing as spending rises. This points to diminishing returns, where early increases in healthcare spending have a major positive influence on infant mortality, with the effect decreasing as spending levels rise

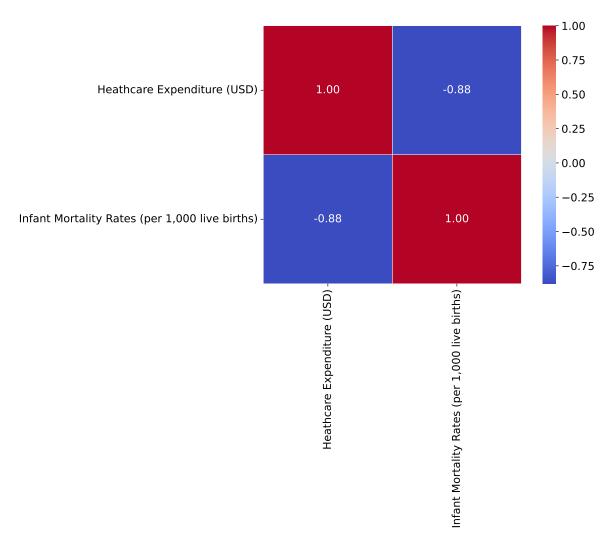


Figure 6: Correlation Matrix of Infant Mortality and Healthcare Spend per Capita

Due to this non-linearity, a correlation plot was created using Spearman's rank correlation illustrated in Figure 6. The correlation matrix confirms a strong negative correlation (-0.88) between healthcare spend per capita and infant mortality rates, indicating that as healthcare spending increases, infant mortality rates decrease, supporting the conclusions from Figure 5. The magnitude of this correlation suggests a substantial association, reinforcing the importance of healthcare investment in improving child survival outcomes. However, the correlation does not imply causation, and other socio-economic factors, such as healthcare infrastructure, accessibility, and policy effectiveness, likely influence this relationship.

#### Regression Analysis

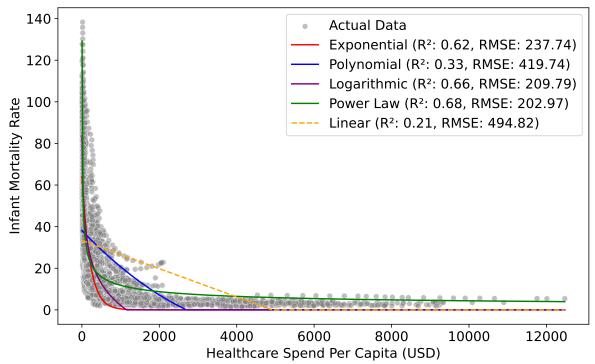


Figure 7: Comparison of Regression Models: Healthcare Spend vs Infant Mortality Rate

Figure 7 compares five regression models, exponential, polynomial, logarithmic, power law, and linear, in quantifying the relationship between healthcare spend per capita and infant mortality rates. The power law model achieves the best fit with an  $R^2$  of 0.68, revealing that 68% of the variance in infant mortality rates is explained by healthcare spending per capita, and the lowest RMSE (14.25), supporting the strong inverse relationship shown in Figure 5. Exponential and logarithmic regression perform well ( $R^2 = 0.62$  and 0.66, respectively), capturing the steep initial decline before stabilizing at lower mortality levels.

Polynomial regression initially follows the trend but ultimately performs poorly, indicated by its lower R<sup>2</sup> of 0.33. The linear model performs worst, failing to capture the non-linearity of the data. All models are constrained to prevent infant mortality predictions below 0, ensuring a realistic representation. This analysis highlights that non-linear models, particularly power law and exponential regression, provide the most accurate representation of the data, reiterating the non-linearity of the relationship between healthcare spend per capita and infant mortality rates.

#### Time Series Analysis

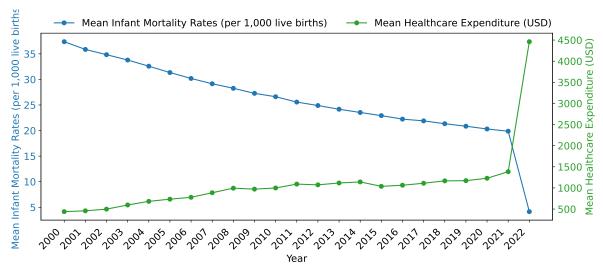


Figure 8: Time Series Analysis of Mean Infant Mortality Rates and Healthcare Expenditure

Figure 8 illustrates the negative association between mean infant mortality rates (IMR) and mean healthcare spending (USD) from 2000 to 2022. The trend indicates a continual drop in IMR, reflecting improvements in healthcare, economic development, and medical advances. Meanwhile, healthcare spending has steadily climbed, indicating greater investment in health infrastructure and services.

A noteworthy anomaly arises in 2022 when healthcare expenditures significantly increase and infant death rates significantly decrease. This large shift may be due to pandemic-related spending, emergency health interventions, or data errors. The high rise in expenditure may signal a significant policy shift, but further research is needed to assess the long-term consequences.

Overall, Figure 8 reinforces the strong negative correlation between healthcare investment and infant mortality reduction illustrated by Figures 6 and 7. However, the presence of diminishing returns suggests that beyond a certain threshold, additional spending alone may not yield proportional improvements, emphasizing the need for efficient resource allocation and targeted healthcare policies to maximize impact.

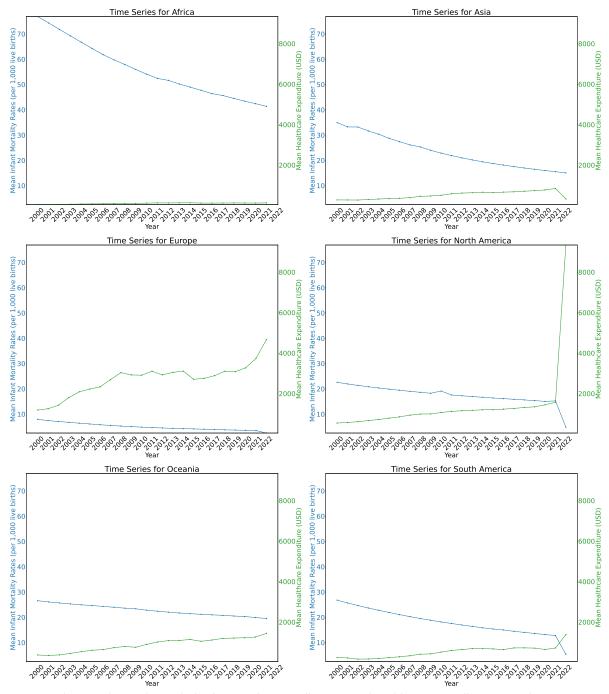


Figure 9: Time Series Analysis of Mean Infant Mortality Rates and Healthcare Expenditure By Continent

Figure 9 shows continent-specific trends in IMR and mean healthcare spending (USD) from 2000 to 2022. The constant negative relationship across each location suggests an association between increasing healthcare investment and reduced infant mortality.

Africa and Asia have had considerable drops in IMR, indicating significant improvements in healthcare despite relatively little investment. Europe and North America, with larger beginning expenditures, experienced lower IMR decreases, indicating declining returns on investment. South America and Oceania follow similar trends but have different purchasing preferences.

Healthcare expenditure rose significantly in 2022 in North and South America, most likely because of pandemic-related measures. This substantial rise in spending corresponds to a transient acceleration in IMR decreases, implying short-term healthcare gains.

Overall, Figure 9 highlights regional differences in healthcare availability and efficiency. While investment is critical to lowering infant mortality, the impact of expenditure varies by location.

#### Conclusion

This analysis confirms a strong negative relationship between healthcare expenditure and infant mortality rates across global regions. Countries with higher healthcare investment generally experience lower infant mortality, though the impact varies based on economic and healthcare infrastructure factors.

The non-linear nature of this relationship indicates diminishing returns, where initial increases in spending lead to substantial improvements, but further investments yield smaller reductions in infant mortality. Logarithmic and time-series analyses further reinforce this pattern, high-lighting long-term declines in infant mortality alongside growing healthcare expenditure.

Regional disparities remain significant, with high-income regions investing more per capita while achieving lower mortality rates, whereas lower-income regions show greater relative improvements despite lower absolute spending. The 2022 anomaly suggests short-term shifts in healthcare spending and outcomes, likely due to pandemic-driven policies.

While healthcare expenditure is a crucial driver of infant survival, efficient allocation, accessibility, and policy effectiveness remain key determinants of long-term health improvements worldwide.