

TEMA 2 - CORRIENTE CONTINUA

Problema 2 - Libro

- a) Calcular la resistencia equivalente entre A y B.
 b) Si $V_A - V_B = 12V$, determinar la corriente en cada resistencia.

Datos

$$R_1 = 6\Omega$$

$$R_2 = R_4 = R_5 = 4\Omega$$

$$R_3 = 2\Omega$$

$$R_6 = R_7 = 8\Omega$$

En serie
 $R_A = R_3 + R_4 = 6\Omega$

$$\frac{1}{R_B} = \frac{1}{R_2} + \frac{1}{R_A} \Rightarrow R_B = \frac{12}{5}\Omega$$

$$R_C = R_1 + R_B = 6 + \frac{12}{5} = \frac{42}{5}\Omega$$

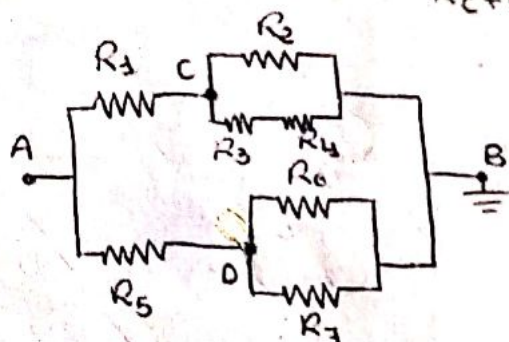
Rama superior

$$\frac{1}{R_D} = \frac{1}{R_6} + \frac{1}{R_7} \Rightarrow R_D = 4\Omega$$

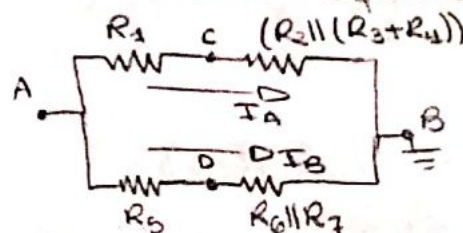
$$R_E = R_5 + R_D = 4 + 4 = 8\Omega$$

Rama inferior

$$R_{final} = \frac{R_C R_E}{R_C + R_E} = \frac{168}{41}\Omega$$



Necesitamos conocer las tensiones en los nudos esenciales (B, C, D). Ponemos el nudo B como el nudo de referencia, por lo que $V_B = 0$ y como $V_A - V_B = 12V$, $V_A = 12V$. Dibujamos un sistema equivalente:



Por la ley de Ohm:

$$I_A = \frac{V_A - V_B}{R_1 + (R_2 \parallel (R_3 + R_4))} = \frac{12}{6 + \frac{12}{5}} = 1.428A$$

$$I_B = \frac{V_A - V_B}{R_5 + R_6 \parallel R_7} = \frac{12}{4 + 4} = 1.5A$$

$$V_C - V_A = -I_A R_1 \Rightarrow V_C = -1.428 \cdot 6 + 12 = 3.432V$$

$$V_D - V_A = -I_B R_5 \Rightarrow V_D = -1.5 \cdot 4 + 12 = 6V$$

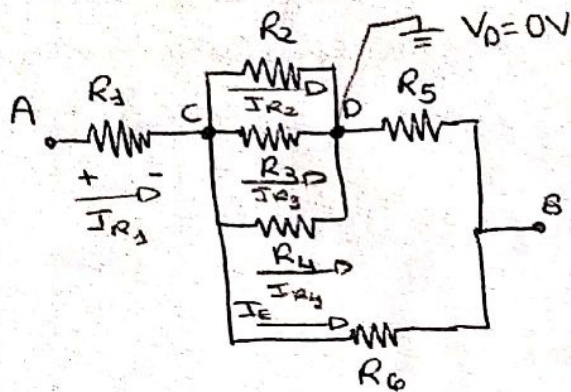
$$I_{R_1} = I_A \quad I_{R_2} = \frac{V_C - V_B}{R_2} \quad I_{R_3} = I_{R_4} = \frac{V_C - V_B}{R_3 + R_4}$$

$$I_{R_5} = I_B \quad I_{R_6} = \frac{V_D - V_B}{R_6} \quad I_{R_7} = \frac{V_D - V_B}{R_7}$$

Problema 3.- Libro

Considere el siguiente circuito donde la caída de tensión a través de la resistencia R_1 es 100V.

- a) $\mathcal{C} I_{R_2}, I_{R_3}, I_{R_4}$? b) $\mathcal{C} \Delta V$ en R_2 ? c) $\mathcal{C} P$ consumida por R_6 ?



Datos

$$\begin{aligned} R_1 &= 10\Omega & R_4 &= 6\Omega \\ \Delta V_{R_1} &= 100V & R_5 &= 2\Omega \\ R_2 &= 5\Omega & R_6 &= 20\Omega \\ R_3 &= 3\Omega \end{aligned}$$

Ley de Ohm

$$I_{R_1} = \frac{\Delta V_{R_1}}{R_1} = \frac{100}{10} = 10A$$

Aplico ley de nudos:

$$\boxed{C} \quad I_{R_1} = I_{R_2} + I_{R_3} + I_{R_4} + I_E$$

$$I_{R_2} = \frac{V_C - V_0}{R_2} = \frac{V_C}{R_2} \quad I_{R_3} = \frac{V_C}{R_3} \quad I_{R_4} = \frac{V_C}{R_4} \quad I_E = \frac{V_C}{\underbrace{R_5 + R_6}_{\text{En serie}}}$$

$$\Rightarrow 10 = \frac{V_C}{R_2} + \frac{V_C}{R_3} + \frac{V_C}{R_4} + \frac{V_C}{R_5 + R_6} \Rightarrow 10 = V_C \left(\frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4} + \frac{1}{R_5 + R_6} \right)$$

$$V_C = \frac{10}{\frac{1}{5} + \frac{1}{3} + \frac{1}{6} + \frac{1}{22}} = 13.41V \Rightarrow I_{R_2} = 2.683A \quad a)$$

$$I_{R_3} = 4.4715A$$

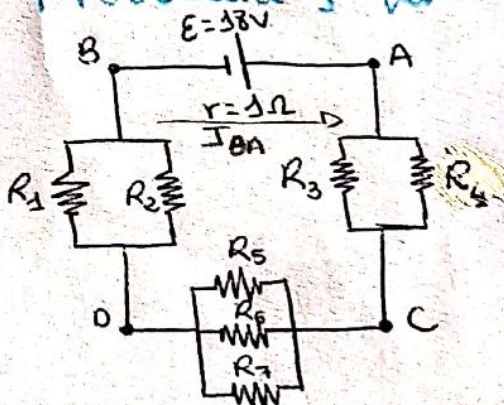
$$I_{R_4} = 2.24A$$

$$I_E = 0.60975A$$

$$b) \Delta V_{R_2} = V_C - V_0 = 13.41V$$

$$c) P_{R_6} = I_E^2 \cdot R_6 = 0.60975^2 \cdot 20 = 7.4359W$$

Problema 4.- Libro (6 Relación)



- a) Calcular la resistencia equivalente entre A y B.

$$\frac{1}{R_1 \parallel R_2} = \frac{1}{R_1} + \frac{1}{R_2} \Rightarrow R_1 \parallel R_2 = 2\Omega$$

$$\frac{1}{R_3 \parallel R_4} = \frac{1}{R_3} + \frac{1}{R_4} \Rightarrow R_3 \parallel R_4 = 1\Omega$$

$$\frac{1}{R_5 \parallel R_6 \parallel R_7} = \frac{1}{R_5} + \frac{1}{R_6} + \frac{1}{R_7} = \frac{1}{2}\Omega$$

$$R_T = R_1 \parallel R_2 + R_3 \parallel R_4 + R_5 \parallel R_6 \parallel R_7 = \frac{7}{2}\Omega$$

Datos

$$R_1 = R_4 = R_5 = 3\Omega$$

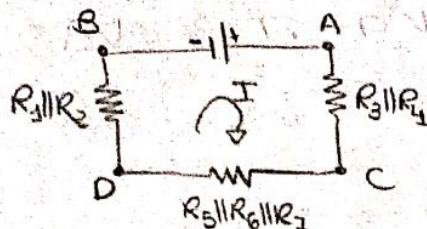
$$R_2 = 6\Omega$$

$$R_3 = R_6 = 1.5\Omega$$

$$R_7 = 1\Omega$$

b) La corriente que circula por el punto A.

Aplico ley de mallas:



$$\sum E = \sum IR$$

$$18 = Ir + IR_1 \parallel R_2 + IR_3 \parallel R_4 + IR_5 \parallel R_6 \parallel R_7$$

$$18 = I + 2I + I + \frac{1}{2}I = 4I = 4A$$

c) La intensidad en todos los hilos.

Conecto a tierra el nudo B, por lo que $V_B = 0$

$$\Delta V_{AB} = E - Ir = 18 - 4 \cdot 1 = 14V$$

$$V_A - V_B^0 = 14 = \Delta V_A = 14V$$

$$I_{R_3} = \frac{V_A - V_C}{R_3} \quad I = \frac{V_A - V_C}{R_3 \parallel R_4} \Rightarrow 4 = \frac{14 - V_C}{1} \Rightarrow V_C = 10V$$

$$I_{R_3} = \frac{14 - 10}{1.5} = 2.6A$$

$$I_{R_4} = \frac{V_A - V_C}{R_4} = \frac{14 - 10}{3} = 1.3A$$

$$I = \frac{V_C - V_D}{R_5 \parallel R_6 \parallel R_7} \Rightarrow 4 = \frac{10 - V_D}{1/2} \Rightarrow V_D = 8V$$

$$I_{R_5} = \frac{V_C - V_D}{R_5} = \frac{10 - 8}{3} = 0.6A \quad I_{R_6} = \frac{V_C - V_D}{R_6} = \frac{10 - 8}{1.5} = 1.3A$$

$$I_{R_7} = \frac{V_C - V_D}{R_7} = \frac{10 - 8}{1} = 2A \quad I_{R_1} = \frac{V_D - V_B^0}{R_1} = \frac{8}{3} = 2.6A$$

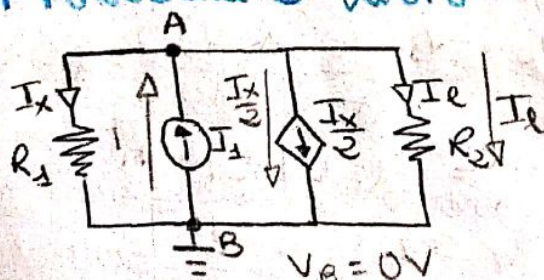
$$I_{R_2} = \frac{V_D - V_B^0}{R_2} = \frac{8}{6} = 1.3A$$

d) $\Delta V_{AB}, V_{AC}, V_{CD}, V_{DB}?$

$$V_{DB} = V_D - V_B^0 = 8V \quad V_{AB} = V_A - V_B^0 = 14V$$

$$V_{CD} = V_C - V_D = (10 - 8)V = 2V \quad V_{AC} = V_A - V_C = (14 - 10)V = 4V$$

Problema 5 Libro



Determinar I_e

Datos

$$I_1 = 6mA \quad R_1 = 2k\Omega \quad R_2 = 4k\Omega$$

Aplico ley de nudos:

$$[A] \quad I_1 = I_x + \frac{I_x}{2} + I_e = 6 \cdot 10^{-3} = \frac{V_A}{2000\Omega} + \frac{V_A}{4000\Omega} + \frac{V_A}{4000\Omega}$$

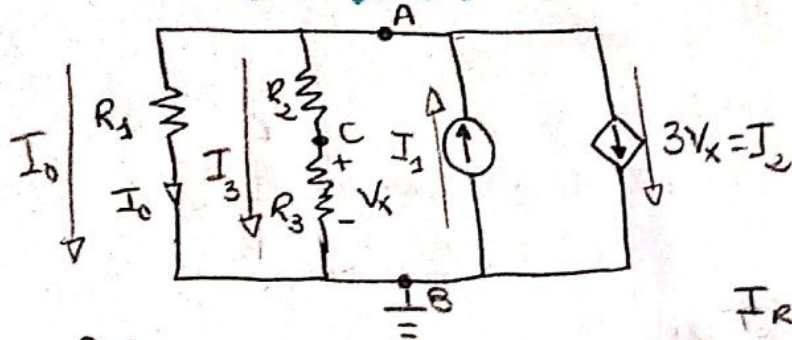
$$V_A = \frac{6 \cdot 10^{-3}}{\frac{1}{2000} + \frac{1}{4000} + \frac{1}{4000}} = 6V$$

$$I_x = \frac{V_A - V_B^0}{R_1}$$

$$I_e = \frac{V_A - V_B^0}{R_2}$$

$$I_e = \frac{V_A}{R_2} = 0.0015A = 1.5mA$$

Problema 7 Libro



Aplico ley de nudos:

$$\boxed{A} \quad I_1 = I_0 + I_3 + 3V_x$$

$$I_0 = \frac{V_A - V_B}{R_1} = \frac{V_A}{R_1}$$

$I_{R_2} = I_{R_3}$ porque están en serie.

$$\frac{V_A - V_C}{R_2} = \frac{V_C - V_B}{R_3}$$

$$V_A = \frac{V_C}{R_3} \cdot R_2 + V_C$$

$$5 = \frac{V_A}{R_1} + \frac{V_A - V_B}{R_2 + R_3} + 3V_x \Rightarrow 5 = \frac{\frac{V_C}{R_3} \cdot R_2 + V_C}{R_1} + \frac{\frac{V_C}{R_3} \cdot R_2 + V_C}{R_2 + R_3} + 3V_C$$

$$V_x = V_C - V_B = V_C$$

$$5 = \frac{3V_C}{6} + \frac{3V_C}{12} + 3V_C$$

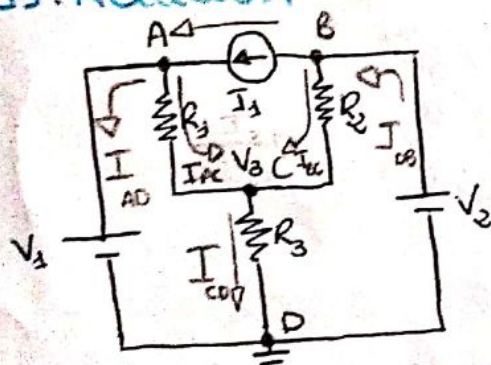
$$60 = 6V_C + 3V_C + 36V_C$$

$$V_C = \frac{4}{3} V = V_x$$

$$-3V_x + 5 = V_A \left(\frac{1}{R_1} + \frac{1}{R_2 + R_3} \right)$$

$$\Rightarrow V_A = \frac{-4 + 5}{\frac{1}{6} + \frac{1}{12}} = 4V \Rightarrow I_0 = \frac{V_A}{R_1} = \frac{4}{6} = 0.6 A$$

11. Relación



Ley de nudos $\sum I_{entran} = \sum I_{salen}$

$$\boxed{A} \quad I_1 = I_{AD} + I_{AC} \quad I_1 = 0.002A$$

$$\boxed{B} \quad I_{DB} = I_1 + I_{BC}$$

$$\boxed{C} \quad I_{AC} + I_{AB} = I_{CD} = I_{AC} + I_1 = I_{CD}$$

$$I_{AC} = \frac{V_A - V_C}{R_1} = \frac{V_1 - V_C}{R_1} = \frac{1 - V_C}{1000} = -0.0005A$$

$$I_{CD} = \frac{V_C - V_D}{R_3} = \frac{V_C}{1000} = 0.0015A$$

$$I_{BC} = \frac{V_B - V_C}{R_2} = \frac{V_2 - V_C}{R_2} = \frac{2 - V_C}{1000} = 0.0005A$$

$$\boxed{C} \quad \frac{1 - V_C}{1000} + 0.002A = \frac{V_C}{1000}$$

$$1 - V_C + 2 = V_C \Rightarrow 3 = 2V_C \Rightarrow V_C = 1.5V$$

Datos

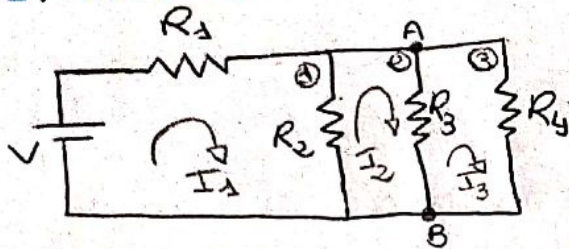
$$R_1 = R_2 = R_3 = 1000 \Omega$$

$$I_1 = 0.002A$$

$$V_1 = 1V$$

$$V_2 = 2V$$

9. Relación



Datos

$$V = 12V$$

$$R_1 = 2000\Omega$$

$$R_2 = R_3 = R_4 = 6000\Omega$$

d) Corrientes rama?

c) Potencia por resistencia?

$$\begin{cases} 12 = I_1 \cdot 8000 - I_2 \cdot 6000 \\ 0 = I_2 \cdot 12000 - I_1 \cdot 6000 - I_3 \cdot 6000 \\ 0 = I_3 \cdot 12000 - I_2 \cdot 6000 \end{cases}$$

$$\begin{cases} 6000a - 12000b + 6000c = 0 \\ 6000b - 12000c = 0 \\ 8000a - 6000b = 12 \end{cases} \Rightarrow \begin{cases} 12000a - 18000b = 0 \\ 8000a - 6000b = 12 \end{cases}$$

$$12 = 0.003 \cdot 8000 - I_2 \cdot 6000$$

$$\boxed{I_2 = 0.002A}$$

$$0 = 0.002 \cdot 12000 - 0.003 \cdot 6000 - I_3 \cdot 6000$$

$$\boxed{I_3 = 0.001A}$$

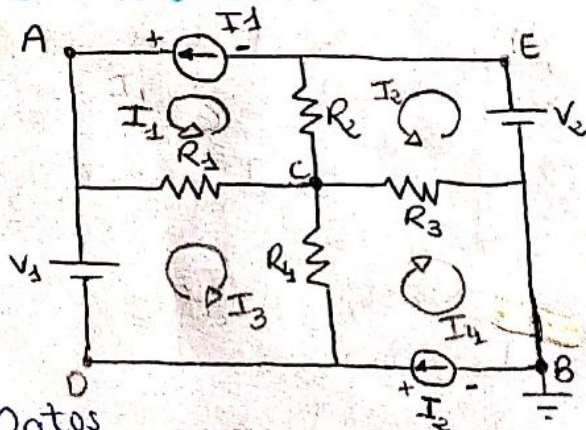
$$\text{Corriente rama } R_1 = I_1 = 0.003A \Rightarrow P_{R_1} = I \cdot \Delta V = 0.003 \cdot 12 = 0.036W$$

$$* \text{ Corriente rama } R_2: I_{R_2} = I_1 - I_2 = 0.001A \Rightarrow P_{R_2} = I \cdot \Delta V = 0.001 \cdot 12 = 0.012W$$

$$\text{Corriente rama } R_3: I_{R_3} = I_2 - I_3 = 0.001A \Rightarrow P_{R_3} = I \cdot \Delta V = 0.001 \cdot 12 = 0.012W$$

$$\text{Corriente rama } R_4: I_{R_4} = I_3 = 0.001A \Rightarrow P_{R_4} = I \cdot \Delta V = 0.001 \cdot 12 = 0.012W$$

13. Relación



Datos

$$V_1 = V_2 = 6V \quad I_1 = I_2 = 1mA$$

$$R_2 = R_3 = 10k\Omega \quad R_1 = R_4 = 6k\Omega$$

Método de mallas

$$1^\circ) n = 2$$

$$2^\circ) r = 4 \quad n^\circ \text{ mallas} = r - (n - 1) = 3$$

3º) Aplicar ley de mallas:

$$\sum \mathcal{E} = \sum I \cdot R$$

Malla 1

$$V = I_1(R_1 + R_2) - I_2 R_2$$

Malla 2

$$0 = I_2(R_2 + R_3) - I_1 R_2 - I_3 R_3$$

Malla 3

$$0 = I_3(R_3 + R_4) - I_2 R_3$$

Método de mallas

Hay 4 mallas independientes.

Usar ley de mallas: $\sum \mathcal{E} = \sum I R$

Malla 1

$$\mathcal{E}_{I_1} = I_1(R_1 + R_2) + I_3 R_1 - I_2 R_2$$

Malla 2

$$V_2 = I_2(R_2 + R_3) - I_1 R_2 + I_4 R_3$$

Malla 3

$$V_1 = I_3(R_1 + R_4) + I_1 R_1 - I_4 R_4$$

Malla 4

$$E_{I_2} = I_4(R_3 + R_4) + I_2 R_3 - I_3 R_4$$

$$\begin{cases} E_{I_3} = 16 + 6000I_3 - 10000I_2 \Rightarrow E_{I_3} = 16V \\ 6 = 20000I_2 - 10 + 10 \Rightarrow I_2 = 0.0003A \\ 6 = 12000I_3 \Rightarrow I_3 = 0.0005A \\ E_{I_2} = 16 + I_2 10000 - I_3 6000 \Rightarrow E_{I_2} = 16V \end{cases}$$

a) ¿Potencia aportada por las fuentes al circuito?

$$P_{I_1} = I \cdot \Delta V = 0.001 \cdot 16 = 0.016W$$

$$P_{I_2} = I \cdot \Delta V = 0.001 \cdot 16 = 0.016W$$

$$P_{V_1} = I \cdot \Delta V = I_3 \cdot V_1 = 0.0005 \cdot 6 = 0.003W$$

$$P_{V_2} = I \cdot \Delta V = I_2 \cdot V_2 = 0.0003 \cdot 6 = 0.0018W$$

b) ¿Potencia disipada por las resistencias?

c) ¿Tensión en c? ¿ΔV entre A y B?

$$V_A - V_E = 16$$

$$V_E - V_B = 6$$

$$V_A - V_B = 22 \Rightarrow V_A = 22V$$



$$V_A = 22V \quad R_1 = 6000\Omega$$

$$I = I_1 + I_3 = 0.0015A$$

$$V_A - V_C = I \cdot R_1$$

$$V_C = V_A - I \cdot R_1 = 22 - 0.0015 \cdot 6000 = 13V$$

$$P_{R_1} = I \cdot \Delta V = 0.0015 \cdot (22 - 13) = 0.0135W$$

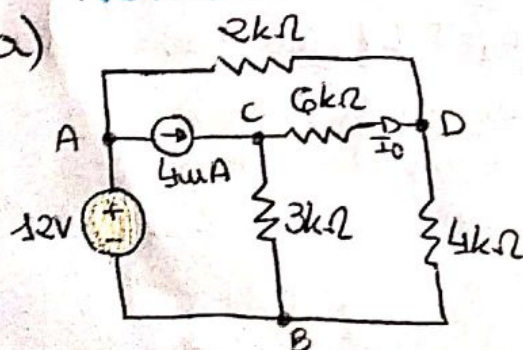
$$P_{R_2} = I \cdot \Delta V = (0.001 - 0.0003) \cdot (13 - 6) = 0.0049W$$

$$P_{R_3} = I \cdot \Delta V = (0.001 + 0.0003) \cdot (13 - 0) = 0.0169W$$

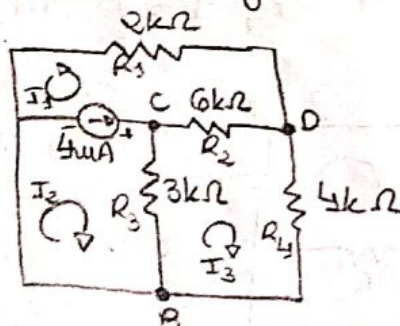
$$P_{R_4} = I \cdot \Delta V = (0.001 - 0.0005) \cdot (16 - 13) = 0.0015W$$

20. Relación

a)



Anulo la fuente de tensión:



Malla 1

$$E_I = I_1(R_1 + R_2) + I_3 R_2$$

Malla 2

$$E_I = I_2(R_3) - I_3 R_3$$

Malla 3

$$0 = I_3(R_2 + R_3 + R_4) - I_2 R_3 + I_1 R_2$$

$$E_I = 8.52V$$

$$I_1 = 0.00077A$$

$$I_2 = 0.003225A$$

$$I_3 = 0.000387A$$

$$E_I = I_1 8000 + I_3 6000$$

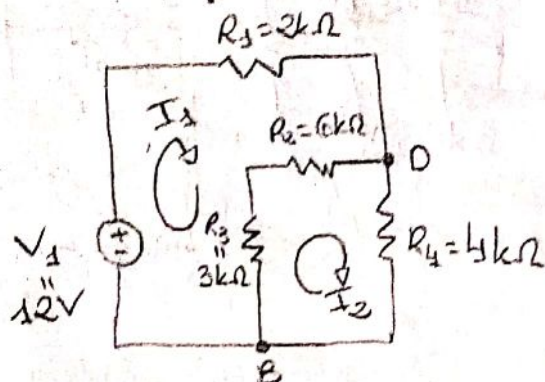
$$E_I = I_2 3000 - I_3 3000$$

$$0 = I_3 13000 - I_2 3000 + I_1 6000$$

$$I_1 + I_2 = 0.004$$

$$I_0^1 = I_1 + I_3 = 0.001157 \text{ A}$$

Anulo la fuente de corriente



Uso ley de mallas:

Malla 1

$$V_1 = I_1(R_1 + R_3) - I_2 R_2 - I_3 R_3$$

Malla 2

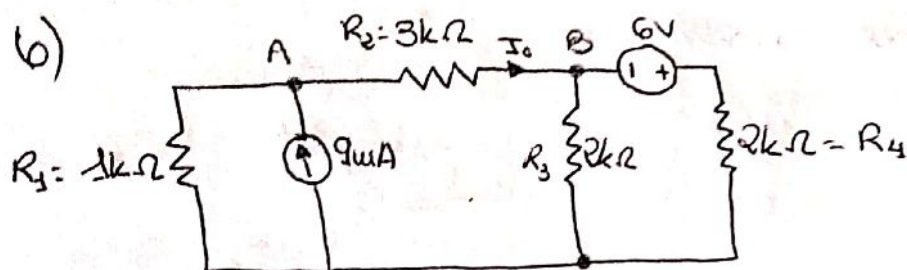
$$0 = I_2(R_2 + R_3 + R_4) - I_1 R_2 - I_3 R_3$$

$$\begin{cases} 12 = 11000I_1 - 9000I_2 \\ 0 = 13000I_2 - 9000I_1 \end{cases} \Rightarrow \begin{aligned} I_1 &= 0.00252 \text{ A} \\ I_2 &= 0.00174 \text{ A} \end{aligned}$$

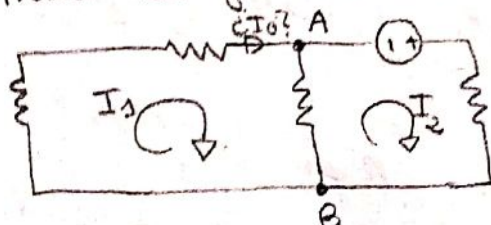
$$I_0^2 = I_1 - I_2 = 0.00078 \text{ A}$$

$$I_0 = I_0^1 - I_0^2 = 0.000377 \text{ A} \quad (\rightarrow \text{En este sentido})$$

b)

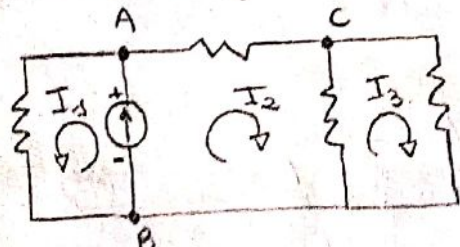


Anulo la fuente de corriente:



$$I_0^1 = I_1 = 0.0006 \text{ A}$$

Anulo la fuente de tensión:



$$\begin{cases} E_T = 1000I_1 \\ E_T = 5000I_2 - 2000I_3 \\ 0 = 4000I_3 - 2000I_2 \\ I_1 + I_2 = 0.009 \end{cases}$$

Uso ley de mallas:

Malla 1

$$E_T = I_1 R_1$$

Malla 2

$$E_T = I_2(R_2 + R_3) - I_3 R_3$$

Malla 3

$$0 = I_3(R_3 + R_4) - I_2 R_3$$

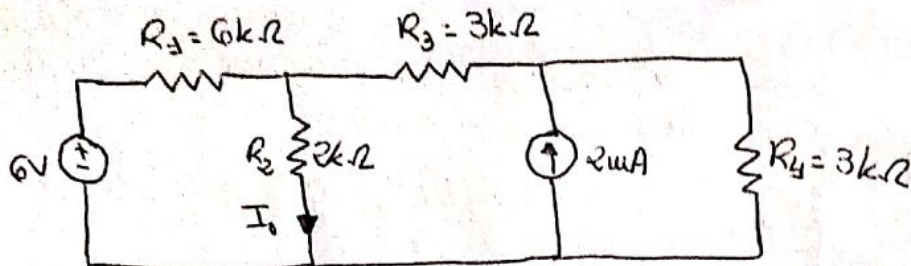
cuarta ecuación

$$I_1 + I_2 = 0.009$$

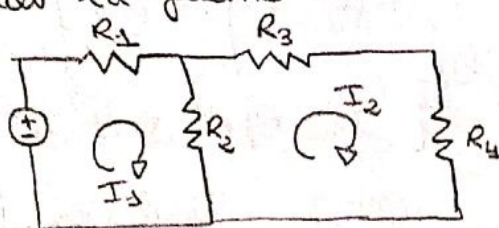
$$\Rightarrow I_2 = 0.0018 \text{ A} \quad (\rightarrow) \Rightarrow I_0^2 = 0.0018 \text{ A}$$

$$I_0 = I_0^1 + I_0^2 = 0.0024 \text{ A}$$

c)



Anulo la fuente de corriente:



Malla 1

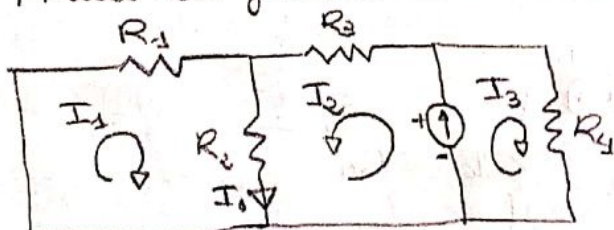
$$V_1 = I_1(R_1 + R_2) - I_2 R_2$$

Malla 2

$$0 = I_2(R_2 + R_3 + R_4) - I_1 R_2$$

$$I_0^1 = I_1 - I_2 = 0.0006A (\downarrow) \quad \begin{cases} 6 = 8000I_1 - 2000I_2 \\ 0 = 8000I_2 - 2000I_1 \end{cases}$$

Anulo la fuente de tensión:



$$I_1 = 0.0008A$$

$$I_2 = 0.0002A$$

Malla 1

$$0 = I_1(R_1 + R_2) + I_2 R_2$$

Malla 2

$$E_I = I_2(R_2 + R_3) + I_1 R_2$$

Malla 3

$$E_I = I_3 R_4$$

Cuarta ecuación

$$I_2 + I_3 = 0.002A$$

$$\begin{cases} 0 = 8000I_1 + 2000I_2 \\ E_I = 5000I_2 + 2000I_1 \\ E_I = 3000I_3 \\ I_2 + I_3 = 0.002 \end{cases}$$

$$I_1 = -0.0002A$$

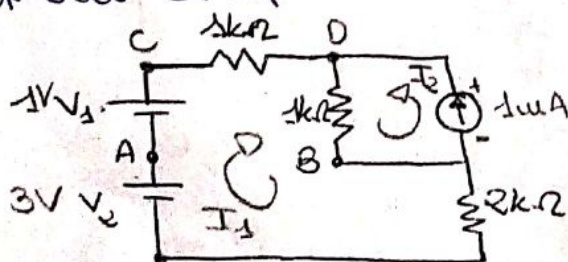
$$I_2 = 0.0008A$$

$$I_0^2 = 0.0008 - 0.0002 = 0.0006 (\downarrow)$$

$$I_0 = I_0^1 + I_0^2 = 0.0012A$$

14. Relación

* Solo el equivalente Thevenin y Norton.



Malla 1

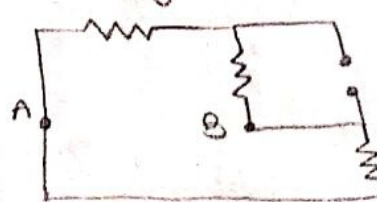
$$V_1 + V_2 = I_1(1 + 1 + 2) + I_2 \cdot 1000$$

Malla 2

$$E_I = 1000I_2 + 1000 \cdot I_1$$

Cálculo R_{th}

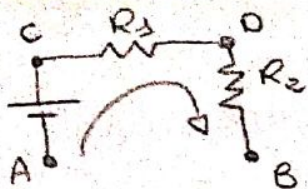
Anulo fuentes:



$$R_{th} = R_1 + R_2 + R_3 = 4000\Omega$$

$$\begin{cases} 4 = 4000I_1 + 1000I_2 \\ E_I = 1000I_2 + 1000I_1 \\ I_2 = 0.001A \end{cases}$$

$$\begin{cases} I_1 = 0.00075A \\ I_2 = 0.001A \\ E_I = 1.75V \end{cases}$$



$V_A - V_B = ?$

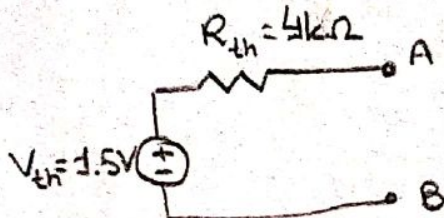
$$V_C - V_A = 1V$$

$$V_C - V_D = I_1 R_1 \Rightarrow V_D - V_C = 0.00075 \cdot 1000 = 0.75V$$

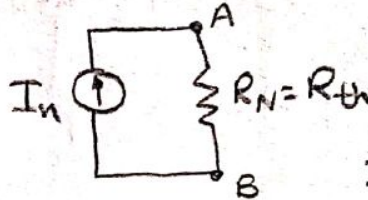
$$V_D - V_B = (I_1 + I_2) R_2 = 1.75V$$

$$V_C - V_A - (V_C - V_D) = -V_A + V_D = 0.25V$$

$$V_D - V_B - (-V_A + V_D) = V_A - V_B = 1.5V = V_{th} = 1.5V$$



Equivalente
Thevenin



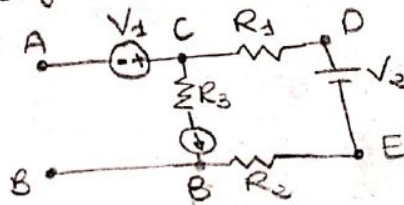
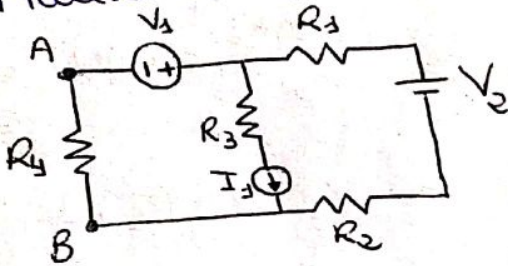
Equivalente
Norton

$$I_n = \frac{V_{th}}{R_{th}} = \frac{1.5V}{4000\Omega} = 0.000375A$$

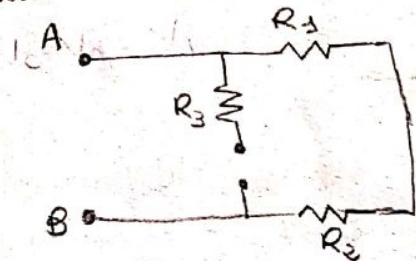
* Ejemplo Pág. 31

Hallar el equivalente Thevenin y Norton.

Dejamos abierto el camino entre A y B.

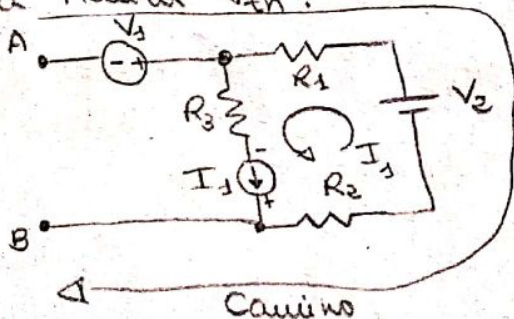


Para hallar R_{th} , se anulan las fuentes:



$$R_{th} = R_1 + R_2$$

Para hallar V_{th} :



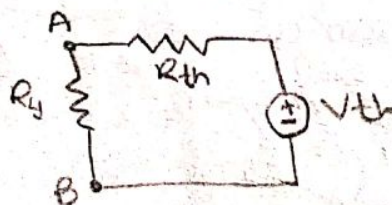
Malla 1

$$V_1 + E_1 = I_1 (R_1 + R_2 + R_3) \Rightarrow DE_1 = I_1 (R_1 + R_2 + R_3) - V_2$$

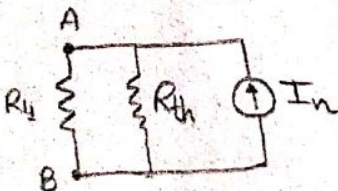
$$I_1 = I$$

$$V_A + V_1 + I_1 R_1 - V_2 + I_1 R_2 = V_B$$

$$\Rightarrow V_A - V_B = V_2 - V_1 - I_1 R_1 - I_1 R_2 = V_{th}$$

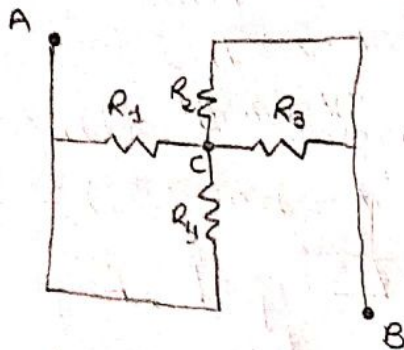
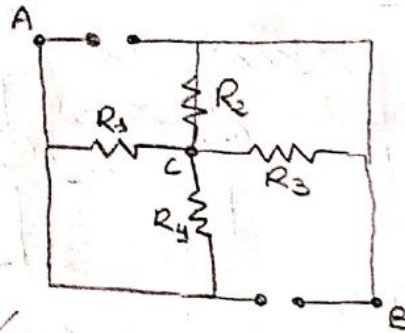
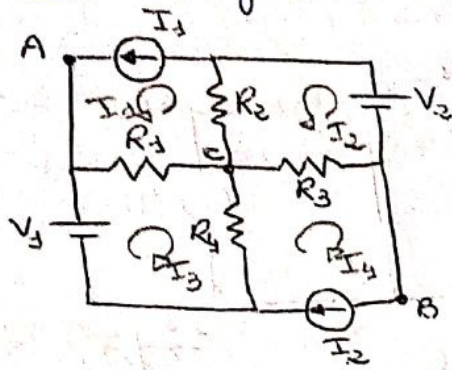


Equivalente
Thevenin



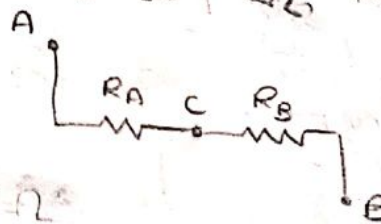
13. Relación

d) Calcular los equivalentes Thevenin y Norton del circuito entre A y B. Para calcular R_{th} , anulamos las fuentes:



R_1 y R_4 están en paralelo.
 R_2 y R_3 también lo están

$$R_A = \frac{R_1 R_4}{R_1 + R_4} = 3000 \Omega, \quad R_B = \frac{R_2 R_3}{R_2 + R_3} = 5000 \Omega$$



R_A y R_B están en serie

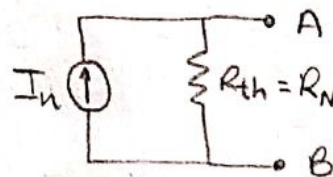
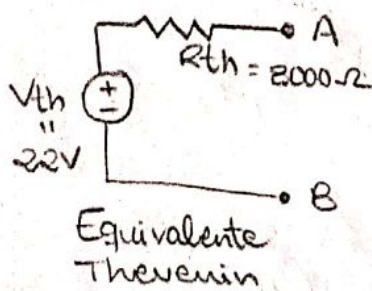
$$R_{th} = R_A + R_B = 8000 \Omega$$

Para calcular V_{th} :

Ya tengo el circuito resuelto de antes:

$$V_A - E_{I_1} - V_2 = V_B \Rightarrow V_A - V_B = E_{I_1} + V_2 = V_{th} \quad (\text{He tomado el camino } \square)$$

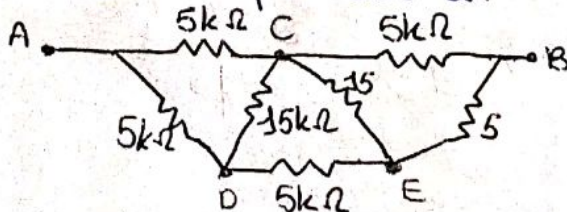
$$16 + 6 = 22V$$



$$I_n = \frac{V_{th}}{R_{th}} = \frac{22V}{8000 \Omega} = 0.00275A$$

Problema 1 - Libro

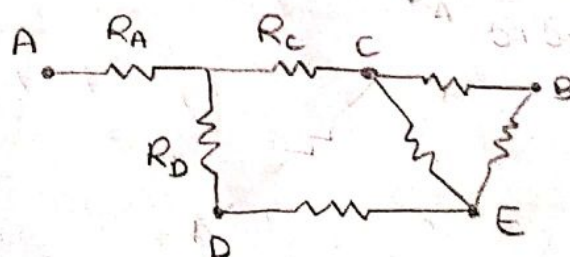
Solo el apartado a.



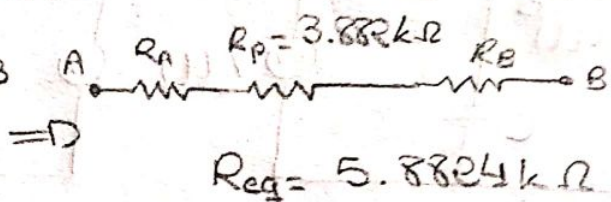
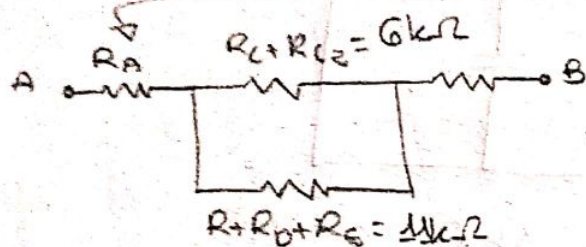
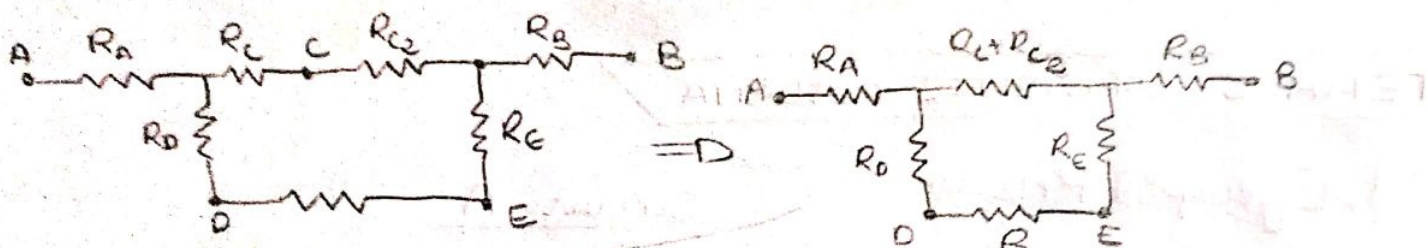
$$R_A = \frac{5 \cdot 5}{5 + 5 + 15} = 1k \Omega$$

$$R_C = \frac{5 \cdot 15}{25} = 3k \Omega$$

$$R_D = 3k \Omega$$

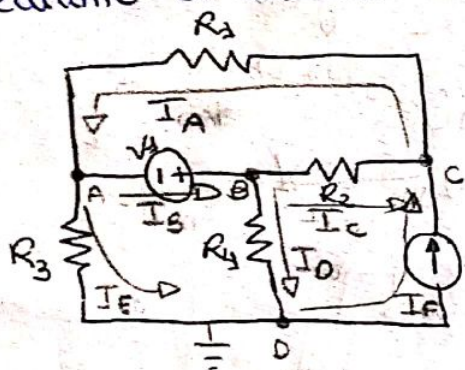


$$R_C = 3k \Omega, \quad R_E = 3k \Omega, \quad R_B = 1k \Omega$$



21. Libro

Mediante el método de nudos, obtener la E_I .



Datos

$$R_1 = R_2 = R_3 = R_4 = 6k\Omega$$

$$V_1 = 12V$$

$$I_1 = 2mA$$

Ley de nudos

[A] $I_A = I_B + I_E$

[B] $I_B = I_C + I_D$

[C] $I_C + I_F = I_A$

Cuarta ecuación: $V_B - V_A = 12V$

$$\begin{cases} \frac{c-a}{6} = x + \frac{a}{6} \Rightarrow 6x = c - 2a & I_A = \frac{V_C - V_A}{R_1} & I_E = \frac{V_B - V_C}{R_2} \\ x = \frac{b-c}{6} + \frac{b}{6} \Rightarrow 6x = 2b - c & I_D = \frac{V_B}{R_4} & I_F = 2mA \\ \frac{b-c}{6} + 2 = \frac{c-a}{6} \Rightarrow b - 2c + a = -12 \end{cases}$$

$$b - a = 12$$

$$a = 0V \quad b = 12V \quad c = 12V \quad x = I_B = 0.002A$$

$$E_I = V_C - V_D = V_C = 12V$$