

# HW1 Problem 4

September 28, 2016

```
In [1]: import matplotlib.pyplot as plt
        %matplotlib inline

In [2]: import numpy as np

In [3]: from scipy.io import loadmat
        from scipy.special import gammaln

In [4]: data = loadmat('hw1_data_mat/mnist_mat.mat')

In [5]: a = b = c = e = f = 1.0

In [6]: dim = data['Xtrain'].shape[0]
        n = data['Xtrain'].shape[1]

In [7]: Xtrain_P = []
        Xtrain_N = []

In [8]: for i in xrange(n):
        if data['ytrain'][:, i][0] == 1:
            Xtrain_P.append(data['Xtrain'][:, i])
        else:
            Xtrain_N.append(data['Xtrain'][:, i])

In [9]: Xtrain_P = np.transpose(np.array(Xtrain_P))
        Xtrain_N = np.transpose(np.array(Xtrain_N))

In [10]: n_P = Xtrain_P.shape[1]
        n_N = Xtrain_N.shape[1]

In [11]: x_bar_P = []
        x_bar_N = []
        for i in xrange(15):
            x_bar_P.append(np.mean(Xtrain_P[i]))
            x_bar_N.append(np.mean(Xtrain_N[i]))

In [12]: x_bar_P, x_bar_N
```

```

Out[12]: ([-0.47061730664131385,
           0.58286614230845868,
           0.20587045510959476,
           -0.40882726075281095,
           0.56292712801894862,
           0.46453685788723231,
           0.083284904986044864,
           -0.16829601501539504,
           0.3337881746038015,
           -0.050308009077472522,
           -0.1021845627499352,
           0.11035410083574052,
           -0.046616043393231263,
           -0.049521882310979128,
           0.030770746331257301],
          [0.44559820987050736,
           -0.63681884607506056,
           -0.2750122492444384,
           0.40989926135792615,
           -0.57246165678908867,
           -0.45722997130591531,
           -0.080959618408045581,
           0.17310278209683494,
           -0.33627257361027529,
           0.052285728424823333,
           0.12688412801189222,
           -0.10852735709995273,
           0.053593082195101144,
           0.052877011940705786,
           -0.030761838621929601])

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In [13]: print Xtrain_P.shape

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x_2_P = []
x_2_N = []
for i in xrange(15):
    x_2_P.append(sum(map(lambda x:x * x, Xtrain_P[i, :])))
    x_2_N.append(sum(map(lambda x:x * x, Xtrain_N[i, :])))

```

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(15, 5949)

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In [14]: x_2_P, x_2_N

```

```

Out[14]: ([35736.495824099024,
           21940.399070690841,
           17726.881231744133,
           11416.856006645525,
           9080.5320089872457,

```

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8339.6941494976909,
7658.3117853378553,
7164.0182013244539,
6906.9606531207564,
5776.0189943804389,
4561.9198564108001,
4789.244744705602,
4379.0394427675983,
5323.9431311741964,
3699.2630534896903],
[27725.4275292926,
22413.030576790454,
15366.956765373496,
12264.395076509658,
11593.133112525949,
11048.704541648358,
9373.2972086597674,
8773.5387732982854,
6407.3255050389062,
7003.2779376883327,
6650.3368683887084,
4668.7243042215305,
4665.0021636265847,
3261.32490157961,
3750.1433414824633])

```

```

In [15]: mu_n_P = map(lambda x: (a * n_P * x) / (n_P + 1), x_bar_P)
mu_n_N = map(lambda x: (a * n_N * x) / (n_N + 1), x_bar_N)

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In [16]: kappa_n_P = (a * n_P + 1) / a
kappa_n_N = (a * n_N + 1) / a

```

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In [17]: alpha_n_P = b + n_P * 0.5
alpha_n_N = b + n_N * 0.5

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In [18]: beta_n_P = []
beta_n_N = []
for i in xrange(15):
    beta_n_P.append(c + 0.5 * x_2_P[i] - 0.5 * ((a * n_P * x_bar_P[i]) **
    beta_n_N.append(c + 0.5 * x_2_N[i] - 0.5 * ((a * n_N * x_bar_N[i]) **

```

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In [19]: beta_n_P, beta_n_N

```

```

Out[19]: ([17210.564442388786,
9960.8337436838883,
8738.3946282008674,
5212.354434830967,
3598.8441842234333,
3529.0742364083558,

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3809.5271116507975,
3498.7748645373322,
3123.1334588649365,
2881.482612935733,
2250.9063565412357,
2359.4049173324956,
2184.0570541393131,
2655.6780777356635,
1847.8156279855054],
[13283.825796024681,
10023.14081583915,
7463.595887621439,
5642.5026941465539,
4840.4826144439412,
4914.7947230627387,
4668.5063038857888,
4300.2578481429955,
2874.4148114346649,
3494.65491331254,
3279.1496037569946,
2300.9639552710833,
2325.1127675575008,
1623.4967956573598,
1873.3080286259246])

```

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In [20]: p_y_1_y_star = (e + n_P) / (n + e + f)
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```
In [21]: p_y_0_y_star = (f + n_N) / (n + e + f)
```

```
In [22]: p_y_1_y_star, p_y_0_y_star
```

```
Out[22]: (0.5045365895022471, 0.4954634104977529)
```

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In [23]: alpha_n_P_1 = alpha_n_P + 0.5
         alpha_n_N_1 = alpha_n_N + 0.5
```

```
In [24]: log_kappa_t_P = np.log((kappa_n_P / (kappa_n_P + 1)) ** 0.5)
         log_kappa_t_N = np.log((kappa_n_N / (kappa_n_N + 1)) ** 0.5)
```

```
In [25]: log_pi_t = np.log((2 * np.pi) ** -0.5)
```

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In [26]: log_gamma_t_P = gammaln(alpha_n_P + 0.5) - gammaln(alpha_n_P)
         log_gamma_t_N = gammaln(alpha_n_N + 0.5) - gammaln(alpha_n_N)
```

```
In [27]: log_beta_alpha_n_P = map(lambda x: alpha_n_P * np.log(x), beta_n_P)
         log_beta_alpha_n_N = map(lambda x: alpha_n_N * np.log(x), beta_n_N)
```

```
In [28]: pred_Y = []
         true_P = 0
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true_N = 0
false_P = 0
false_N = 0
print data['ytest'].shape

```

(1, 1991)

```

In [29]: for i in xrange(data['Xtest'].shape[1]):
    log_beta_alpha_n_P_1 = alpha_n_P_1 * np.log(beta_n_P + kappa_n_P / (2
    log_beta_alpha_n_N_1 = alpha_n_N_1 * np.log(beta_n_N + kappa_n_N / (2
    log_x_star_y_star_P = 0
    log_x_star_y_star_N = 0
    for j in xrange(dim):
        log_x_star_y_star_P += log_kappa_t_P + log_pi_t + log_gamma_t_P +
        log_x_star_y_star_N += log_kappa_t_N + log_pi_t + log_gamma_t_N +
    prob_P = (np.exp(log_x_star_y_star_P) * p_y_1_y_star) / (np.exp(log_x_st
    if prob_P >= 0.5 and data['ytest'][:, i][0] == 1:
        true_P += 1
    elif prob_P >= 0.5 and data['ytest'][:, i][0] == 0:
        false_P += 1
        print i, prob_P
    elif prob_P < 0.5 and data['ytest'][:, i][0] == 1:
        false_N += 1
        print i, prob_P
    else:
        true_N += 1
    pred_Y.append(prob_P)

```

```

40 0.735341099219
42 0.519414358248
55 0.726598587938
64 0.701842013806
74 0.700507707503
80 0.881922974112
84 0.697147381991
138 0.687353528054
140 0.51157890678
142 0.595579185123
162 0.633583349415
163 0.544612037314
165 0.599412617182
183 0.730262330533
195 0.680087852783
221 0.869011319805
223 0.609825384577
231 0.924084301304
259 0.720940241961

```

263 0.743521958157  
269 0.532529824223  
301 0.732475379438  
312 0.691490895793  
340 0.538750403504  
359 0.53902758375  
360 0.642289312963  
361 0.655817783764  
363 0.623808389513  
396 0.561092410497  
420 0.659919216283  
440 0.574170617614  
452 0.662089382196  
464 0.686901195342  
465 0.610660497954  
483 0.552351348601  
486 0.726901976947  
489 0.606340817531  
529 0.628567971756  
564 0.558361268951  
592 0.547354973312  
603 0.643990976414  
676 0.519077919589  
696 0.587439192542  
698 0.594264341275  
730 0.549834245897  
740 0.506914849834  
744 0.584898620774  
809 0.770441364925  
842 0.733327738141  
909 0.585400537411  
948 0.509748290726  
974 0.538432740883  
982 0.488061012185  
1002 0.459395611182  
1033 0.421506542228  
1047 0.426510207758  
1053 0.333858208763  
1074 0.442557085153  
1094 0.124032156167  
1108 0.480684404771  
1117 0.281203967899  
1149 0.388839878998  
1154 0.474475500766  
1168 0.135448164486  
1181 0.378561400278  
1193 0.355863768104  
1201 0.245238453639

1215 0.44888313304  
1227 0.474213366977  
1253 0.486818617865  
1316 0.475110658808  
1327 0.208879475306  
1342 0.202839107736  
1364 0.461907434992  
1370 0.27444694741  
1373 0.372606665472  
1382 0.0208425006864  
1390 0.269151613696  
1392 0.190727601643  
1407 0.331766530256  
1410 0.418554731716  
1412 0.435891432469  
1423 0.374732923964  
1429 0.384208231477  
1435 0.469404897468  
1445 0.234467198756  
1446 0.49141707841  
1450 0.384277032681  
1463 0.202181633727  
1475 0.314760058107  
1482 0.101806915334  
1502 0.451700429112  
1504 0.471298143308  
1505 0.426618896825  
1516 0.301102341479  
1519 0.374748307052  
1567 0.3772504598  
1571 0.454909656883  
1647 0.280671011541  
1653 0.376796621611  
1658 0.481346241638  
1661 0.435284314152  
1662 0.466148252439  
1663 0.424153435047  
1669 0.302281955375  
1671 0.344266742345  
1672 0.443586006186  
1673 0.470097616182  
1674 0.371686677093  
1678 0.279276429663  
1680 0.367559782431  
1681 0.484068088818  
1707 0.355900376749  
1708 0.309552073111  
1743 0.37938380269

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1757 0.374560779564
1758 0.301756165547
1818 0.250939409432
1837 0.465601466584
1842 0.357526498319
1901 0.251646581501
1902 0.215273072548
1919 0.233849180984
1922 0.415256045997
1924 0.31944791191
1926 0.397682146311
1958 0.207130240425
1971 0.330333149237
1972 0.299037054181
1977 0.0810884879762
1981 0.371858471927
1982 0.262648381326
1983 0.396717687222
1986 0.304740256968
```

```
In [30]: print true_P, true_N, false_P, false_N
```

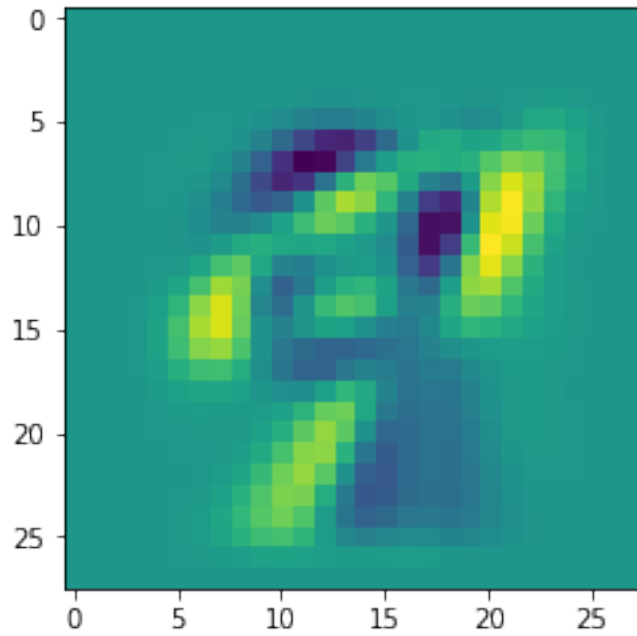
```
927 930 52 82
```

```
In [31]: Q = data['Q']
```

```
In [32]: misclass_1 = np.dot(Q, data['Xtest'][:, 1986]).reshape(28, 28)
          plt.imshow(misclass_1)
          print pred_Y[1986]
```

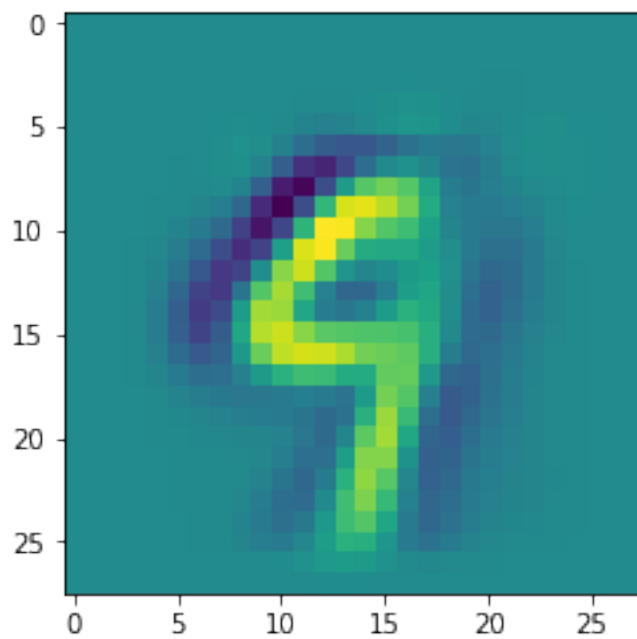
```
0.304740256968
```





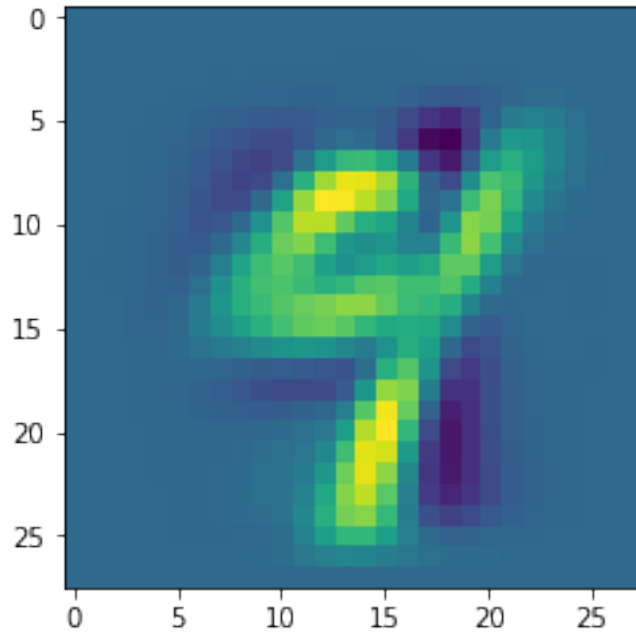
```
In [33]: misclass_2 = np.dot(Q, data['Xtest'][:, 1958]).reshape(28, 28)
plt.imshow(misclass_2)
print pred_Y[1958]
```

0.207130240425



```
In [34]: misclass_3 = np.dot(Q, data['Xtest'][:, 231]).reshape(28, 28)
plt.imshow(misclass_3)
print pred_Y[231]
```

0.924084301304

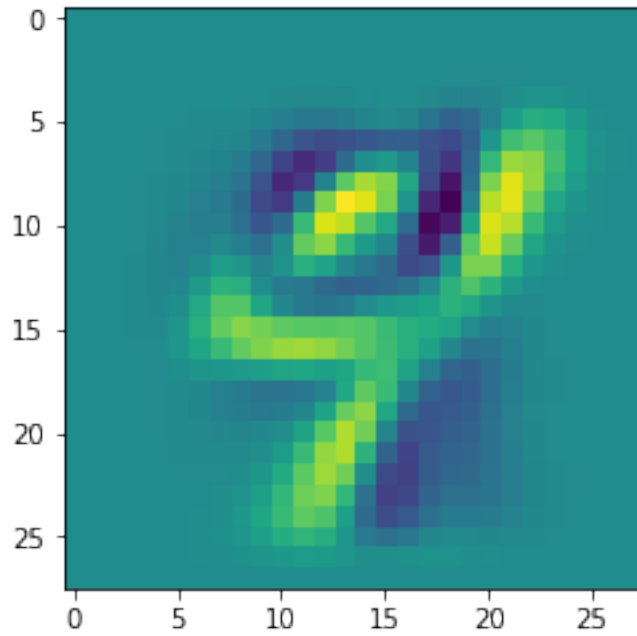


```
In [35]: abs_diff = np.abs(np.array(pred_Y) - 0.5)
```

```
In [36]: ambi_index = np.argsort(abs_diff)[:3]
```

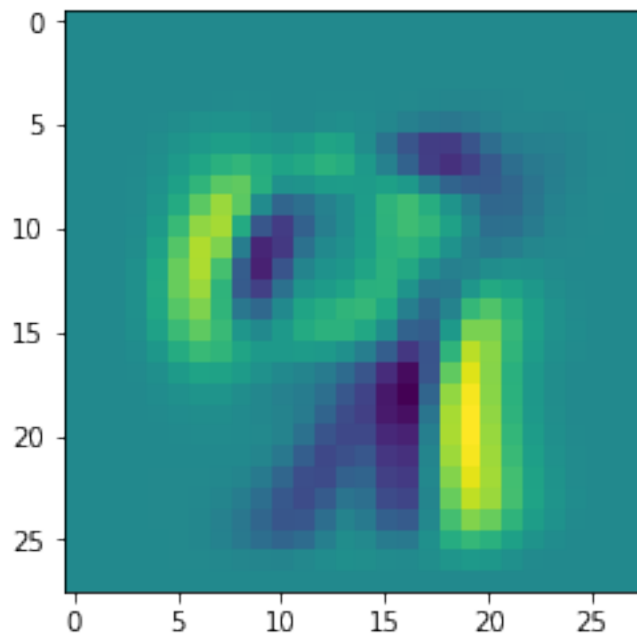
```
In [37]: ambi_1 = np.dot(Q, data['Xtest'][:, ambi_index[0]]).reshape(28, 28)
plt.imshow(ambi_1)
print pred_Y[ambi_index[0]]
```

0.499616378259



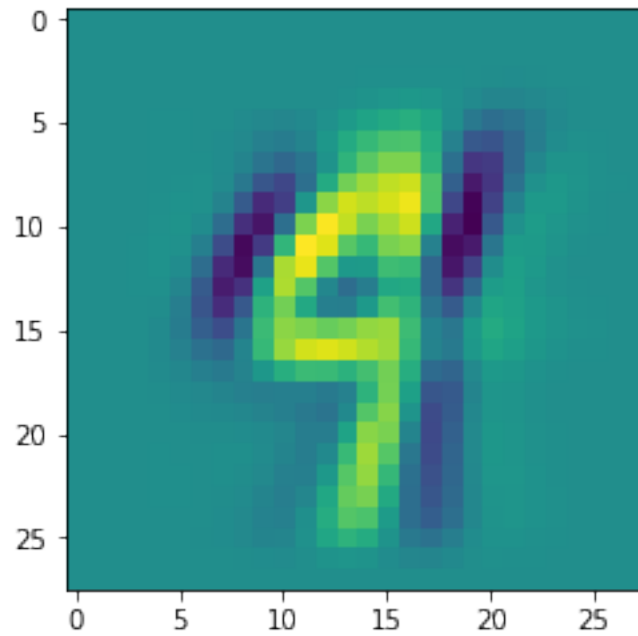
```
In [38]: ambi_2 = np.dot(Q, data['Xtest'][:, ambi_index[1]]).reshape(28, 28)
plt.imshow(ambi_2)
print pred_Y[ambi_index[1]]
```

0.502011187547



```
In [39]: ambi_3 = np.dot(Q, data['Xtest'][:, ambi_index[2]]).reshape(28, 28)
plt.imshow(ambi_3)
print pred_Y[ambi_index[2]]
```

0.496365983337



```
In [ ]:
```