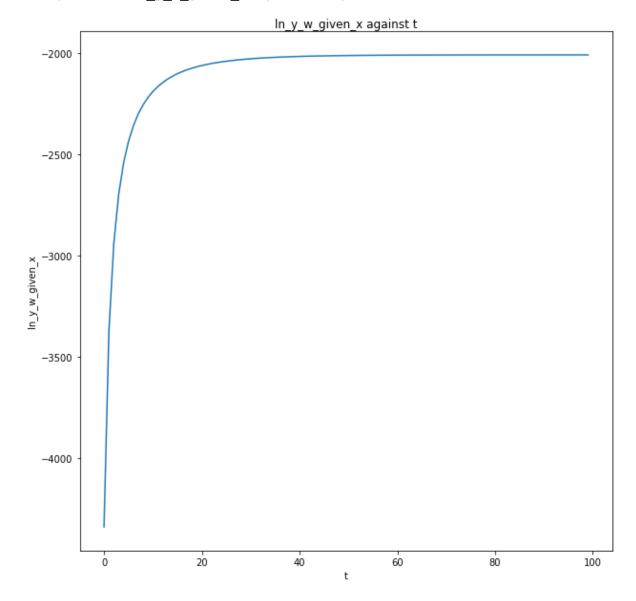
```
In [1]: %matplotlib inline
        import matplotlib.pyplot as plt
        import numpy as np
        from scipy.io import loadmat
        from scipy.stats import norm
In [2]: | data = loadmat('hw2_data_mat/mnist_mat.mat')
In [3]: sigma = 1.5
        lamda = 1
        T = 100
In [4]: | dim = data['Xtrain'].shape[0]
        n = data['Xtrain'].shape[1]
        print dim, n
        15 11791
In [5]: Xtrain_P = []
        Xtrain_N = []
In [6]: for i in xrange(n):
            if data['ytrain'][:, i][0] == 1:
                Xtrain_P.append(data['Xtrain'][:, i])
            else:
                Xtrain_N.append(data['Xtrain'][:, i])
In [7]: Xtrain P = np.transpose(np.array(Xtrain P))
        Xtrain_N = np.transpose(np.array(Xtrain_N))
In [8]: | n_P = Xtrain_P.shape
        n_N = Xtrain_N.shape
```

```
In [9]: w = np.zeros((15, 1))
        w_t = []
        ln = []
        for i in range(T):
            # E-Step
            X_t_w_P = np.dot(Xtrain_P.T, w)
            X_t_w = np.dot(Xtrain_N.T, w)
            E phi P = X t w P + sigma * norm.pdf(-X t w P / sigma) / (1 - norm.c
        df(-X_t w P / sigma))
            E_phi_N = X_t_w_N + sigma * - norm.pdf(-X_t_w_N / sigma) /
        norm.cdf(-X_t_w_N / sigma)
            # M-Step
            x x T = np.divide((np.dot(Xtrain P, Xtrain P.T) + np.dot(Xtrain N, X
        train N.T)), sigma**2)
            inverted = np.linalg.inv(np.dot(np.identity(15), lamda) + x x T)
            x_E_phi = np.divide((np.dot(Xtrain_P, E_phi_P) + np.dot(Xtrain_N, E_
        phi_N)), sigma **2)
            w = np.dot(inverted, x_E_phi)
            # Calculate ln
            ln y w given x = (\dim / 2.0 * np.log(lamda/(2 * np.pi)) - lamda / 2.
        0 * np.dot(w.T, w) +
                             np.sum(np.log(norm.cdf(np.dot(Xtrain_P.T,
        w)/sigma))) +
                             np.sum(np.log(1 - norm.cdf(np.dot(Xtrain N.T, w)/si
        gma))))
            if i in [0, 4, 9, 24, 49, 99]:
                w t.append(w)
            ln.append(ln y w given x[0][0])
```

```
In [10]: x = range(100)
   plt.figure(figsize=(10, 10))
   plt.plot(x, ln)
   plt.ylabel('ln_y_w_given_x')
   plt.xlabel('t')
   plt.title('ln_y_w_given_x against t')
```

Out[10]: Text(0.5,1,u'ln_y_w_given_x against t')



```
In [11]: pred_Y = []
    true_P = 0
    true_N = 0
    false_P = 0
    false_N = 0
    print data['ytest'].shape
```

(1, 1991)

```
40 [[ 0.75483351]]
46 [[ 0.78198279]]
64 [[ 0.9757452]]
74 [[ 0.93095418]]
80 [[ 0.99911947]]
81 [[ 0.5119825]]
84 [[ 0.76368115]]
94 [[ 0.57854307]]
138 [[ 0.95722124]]
142 [[ 0.8313627]]
156 [[ 0.93107843]]
162 [[ 0.7001229]]
163 [[ 0.80849723]]
183 [[ 0.55764663]]
195 [[ 0.56546922]]
210 [[ 0.50613315]]
221 [[ 0.99995144]]
223 [[ 0.92184408]]
231 [[ 0.97702347]]
239 [[ 0.6933672611
259 [[ 0.80182825]]
263 [[ 0.98936797]]
269 [[ 0.57763019]]
271 [[ 0.79579723]]
293 [[ 0.65842084]]
301 [[ 0.8632953211
312 [[ 0.88172473]]
340 [[ 0.50463717]]
348 [[ 0.84173697]]
357 [[ 0.6722796]]
360 [[ 0.78870087]]
396 [[ 0.83967772]]
420 [[ 0.84403436]]
440 [[ 0.68536092]]
441 [[ 0.7419132]]
465 [[ 0.99140899]]
476 [[ 0.63800794]]
489 [[ 0.92204447]]
529 [[ 0.55398608]]
559 [[ 0.55595442]]
564 [[ 0.62612537]]
586 [[ 0.5002525]]
587 [[ 0.84138435]]
592 [[ 0.72139615]]
603 [[ 0.71099252]]
676 [[ 0.53796456]]
715 [[ 0.55112567]]
730 [[ 0.57909342]]
744 [[ 0.56129254]]
832 [[ 0.77852964]]
842 [[ 0.99887344]]
909 [[ 0.64406079]]
988 0.474083033582
1002 0.269198185046
1010 0.453734536313
1038 0.303886863706
```

1094 0.0757977206357

- 1097 0.432676699926
- 1117 0.200664111189
- 1140 0.144547024545
- 1149 0.242954813462
- 1168 0.00737809598847
- 1181 0.386164722497
- 1184 0.0181905757155
- 1201 0.329625700235
- 1253 0.47781449629
- 1293 0.43736224498
- 1327 0.0444890217592
- 1342 0.0325323547972
- 1346 0.371389733048
- 1351 0.0513670697336
- 1370 0.0474757622353
- 1373 0.400084382476
- 1382 3.52883864409e-05
- 1390 0.085294317303
- 1392 0.0271206625297
- 1407 0.181200072876
- 1424 0.337774248592
- 1427 0.379945440526
- 1429 0.220657060203
- 1435 0.259888936895
- 1445 0.477676387607
- 1446 0.475532410749
- 1459 0.483528548889
- 1463 0.400709456576
- 1467 0.30159094869
- 1475 0.0544963824207
- 1477 0.174858993188
- 1482 0.00422627610849
- 1484 0.412956839443
- 1491 0.0644173987111
- 1496 0.245623856429
- 1502 0.131667521065 1504 0.0444568111736
- 1516 0 045001171600
- 1516 0.045001171609
- 1519 0.0141013720126
- 1567 0.462978305496
- 1618 0.289568538565
- 1619 0.457926185862
- 1653 0.0309947503052
- 1655 0.297382340981
- 1658 0.467922433693
- 1660 0.343703062665
- 1662 0.0265922674236
- 1674 0.219925031864
- 1678 0.391164092904
- 1681 0.295885693414
- 1688 0.344571402597
- 1707 0.34317243534
- 1708 0.342637632353
- 1757 0.160389173707
- 1758 0.0531235773196
- 1837 0.384270370656
- 1842 0.441564104377

```
1901 0.397782616551

1902 0.0109345042581

1919 0.0962604432108

1924 0.445970034101

1958 0.00868376514755

1971 0.293557212774

1972 0.0741919661533

1973 0.474485374353

1977 0.00011529151587

1980 0.37273573069

1981 0.016122208355

1982 0.0109516727919

1983 0.221224009317

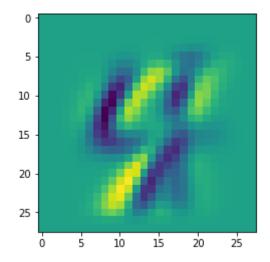
1986 0.437457475958

1988 0.410013424395
```

In [13]: print true_P, true_N, false_P, false_N

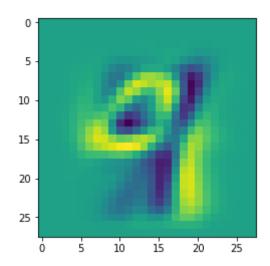
932 930 52 77

0.999951444623



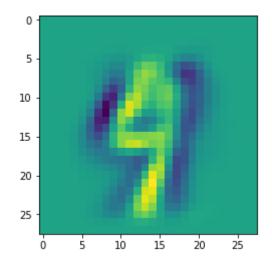
```
In [16]: misclass_1 = np.dot(Q, data['Xtest'][:, 263]).reshape(28, 28)
plt.imshow(misclass_1)
print pred_Y[263]
```

0.989367967151



In [17]: misclass_1 = np.dot(Q, data['Xtest'][:, 269]).reshape(28, 28)
 plt.imshow(misclass_1)
 print pred_Y[269]

0.577630188348



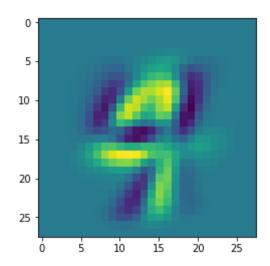
```
In [18]: abs_diff = np.abs(np.array(pred_Y) - 0.5)
```

```
In [19]: ambi_index = np.argsort(abs_diff)[:3]
    ambi_index
```

Out[19]: array([586, 340, 210])

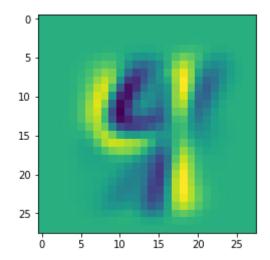
```
In [20]: ambi_1 = np.dot(Q, data['Xtest'][:, ambi_index[0]]).reshape(28, 28)
    plt.imshow(ambi_1)
    print pred_Y[ambi_index[0]]
```

0.500252498451



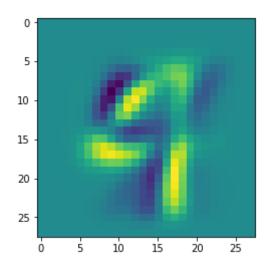
In [21]: ambi_2 = np.dot(Q, data['Xtest'][:, ambi_index[1]]).reshape(28, 28)
 plt.imshow(ambi_2)
 print pred_Y[ambi_index[1]]

0.504637167196



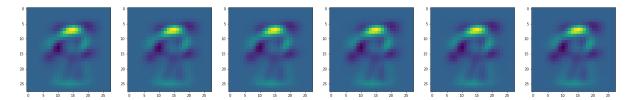
```
In [22]: ambi_3 = np.dot(Q, data['Xtest'][:, ambi_index[2]]).reshape(28, 28)
    plt.imshow(ambi_3)
    print pred_Y[ambi_index[2]]
```

0.506133148466



```
In [23]: plt.figure(figsize=(30, 180))
    ax1 = plt.subplot(161)
    plt.imshow(np.dot(Q, w_t[0]).reshape(28, 28))
    ax2 = plt.subplot(162)
    plt.imshow(np.dot(Q, w_t[1]).reshape(28, 28))
    ax3 = plt.subplot(163)
    plt.imshow(np.dot(Q, w_t[2]).reshape(28, 28))
    ax4 = plt.subplot(164)
    plt.imshow(np.dot(Q, w_t[3]).reshape(28, 28))
    ax5 = plt.subplot(165)
    plt.imshow(np.dot(Q, w_t[4]).reshape(28, 28))
    ax6 = plt.subplot(166)
    plt.imshow(np.dot(Q, w_t[5]).reshape(28, 28))
```

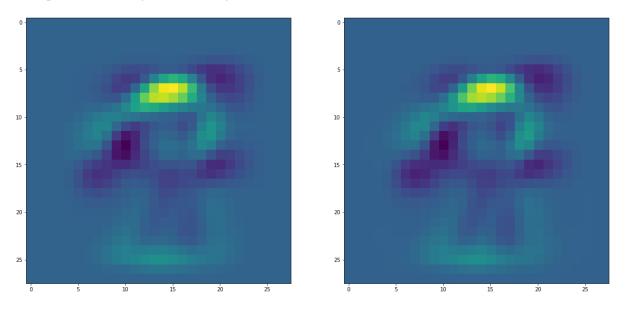
Out[23]: <matplotlib.image.AxesImage at 0x10d421c10>



The images all look quite similar, but if we compare the first and last Ws closely, we can observe slightly more structure in the form of more defined patches of yellow and blue highlighting characteristics of 9 and 4 respectively.

```
In [24]: plt.figure(figsize=(20, 40))
    ax1 = plt.subplot(121)
    plt.imshow(np.dot(Q, w_t[0]).reshape(28, 28))
    ax2 = plt.subplot(122)
    plt.imshow(np.dot(Q, w_t[5]).reshape(28, 28))
```

Out[24]: <matplotlib.image.AxesImage at 0x114329750>



In []: