## ECEN315 - Open Loop Response of a Motorised, Propellor Driven Pendulum

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Abstract—We propose

## 1 Introduction

## APPENDIX A MATLAB CODE

1

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<sup>1</sup> %Script for ECEN315 Lab 2
The aim of this report is to derive a model<sup>2</sup> clear
for the open loop response of a motorised,3 clf
                                          _{4} R_a = 6.3; %Ohms
propellor driven pendulum arm.
                                          _{5} L_a = 0.797; %H
                                          _{6} K b = 0.0043; %Vs/rad
                                          _{7} K_t = K_b; \%Mm/A
                                          _{8} D_m = 0.00000553; %Nms/rad
                                          _{9} J_{m} = 0.00000241; %Kgm^{2}
                                         numerator = K_t/(L_a*J_m);
2
   BACKGROUND
                                         _{12} sSqCoef = 1;
                                         _{13} sCoef = (L_a * D_m + R_a * J_m)/(
                                               L_a * J_m);
                                         _{14} \text{ coef3} = (R_a * D_m + K_t * K_b)/(
                                               L_a * J_m);
3
   METHODS
                                         _{16} sys = tf(numerator, [sSqCoef
                                               sCoef coef3])
                                         _{17} \text{ stepCoefs} = [1 \ 2 \ 3 \ 4 \ 5 \ 6];
   RESULTS
                                         steps = 6;
                                         20 Legend = cell(steps, 1);
5
   DISCUSSION
                                           for i = 1: steps
                                               step(i * sys, 10)
                                               hold on
                                               Legend{i} = strcat(num2str(i),
                                                   'V Step');
   CONCLUSION
                                         26 end
                                         27 hold off
                                         vlabel("\omega_m (rad/s)");
```

```
29 xlabel("Time (s)");
  title ("Step Response of the Motor
                                       15 figure (1)
                                       plot(data.Var1, data.Var2); % plot
31 legend (Legend)
                                             csv data
                                       17 xlabel("Time (s)")
stepResponseInfo = stepinfo(
                                       18 ylabel("y(t)")
     stepCoefs.*sys)%,
     SettlingTimeThreshold',
                                       20 positiveValues = abs(data.Var2); %
     0.000005); %Include this setting
                                             make all peaks positive
      to know approx when oscillation 21
      ends
                                       22 [peaks, locs] = findpeaks(
                                            positiveValues); % find all
35 %units of steady state gains rad/
                                            peaks
                                       23 peaksTable = table(data.Var1(locs)
 Gain = numerator/coef3
                                            , peaks); % convert to table
  steadyStateValue = Gain *
                                       25 hold on
     stepCoefs
                                       plot(peaksTable.Var1, peaksTable.
38
39 SettlingTime = [stepResponseInfo
                                            peaks); % plot line connecting
     (1:6). SettlingTime | %The
                                            all peaks
     inductance of the motor is
                                       27 hold off
     likely too high which is causing 28
      the critical damping/
                                       29 %Fitting coefficients to the
     overdamping and thus quick
                                            function
                                       30 modelfun = @(b,x) b(1)*exp(-b(2).*
     settling time.
                                            x(:, 1)); % function to model
40 %steadyStateValue = [
     stepResponseInfo(1:6).Peak]
                                       _{31} beta0 = [200, 1]; % initial
41 %steadyStateGain = [
                                            Guesses
     stepResponseInfo(1:6).Peak] ./
                                       32 model = fitnlm (peaksTable,
     stepCoefs %Not sure about this
                                            modelfun, beta0); % the non-
                                            linear model we get out
     method
                                       33 coefs = model. Coefficients {:,
                                            Estimate'}; % Coefficients we
1 % Finding Coefficients from un-
     driven Damped pendulum
                                            are looking for
2 clear
                                       34
 clf
                                       _{36} A = coefs(1); % Our A coefficient
                                       _{37} B = coefs(2); % Our B coefficient
_{5} m = 0.168; %kg
_{6} g = 9.81; \%m/s^2
7 d = 0.14; %m distance from pivot
                                       _{39} j_p = (m*d*g) / (power(w,2)+power(
                                            B,2)) % moment of inertia we are
     to cog
                                             looking for
s r = 0.165; %m length of pendulum
                                       40 c = 2 * B * j_p % damping coeff we
     arm
<sub>9</sub> T = 0.97; %Period in seconds
                                             are looking for
_{10} f = 1/T; %freq
w = 2*pi*f; %angular frequency
                                       42 % Transfer Function
 data = readtable("Data.csv"); %
                                       44 numerator = 1/j_p;
     load csv data
                                       45 coefB = c/j_p;
```

```
46 coefC = (d*m*g)/j_p;
  sys = tf(numerator, [1, coefB],
     coefC])
  figure (2)
  step(sys)
51
 % Combined Transfer function
54 % Lab 2 Transfer Function
_{55} R_a = 6.3; %Ohms
 L_a = 0.797; \%H
 K_b = 0.0043; %Vs/rad
 K_t = K_b; \%m/A
_{59} D_m = 0.00000553; %Nms/rad
 J_m = 0.00000241; %Kgm<sup>2</sup>
 numeratorLab2 = K_t/(L_a*J_m);
  coefALab2 = 1;
  coefBLab2 = (L_a * D_m + R_a * J_m)
     )/(L_a * J_m);
 coefCLab2 = (R_a * D_m + K_t * K_b)
     )/(L_a * J_m);
 sysLab2 = tf(numeratorLab2 , [
     coefALab2 coefBLab2 coefCLab2]);
  ylabel("\theta (rads)")
 k_p = 0.0053;
 sys3 = sysLab2 * sys * k_p * r
 Leg = cell(3, 1);
  figure (3)
  hold on
  for i = 3:5
      step(i * sys3);
      Leg{i-2} = strcat(num2str(i)),
         'V Step');
79 end
 hold off
81 ylabel("\theta (rads)")
82 legend (Leg)
```

## APPENDIX B RISK ASSESSMENT