Figure 1: Frequency response of the circuit in LTSpice
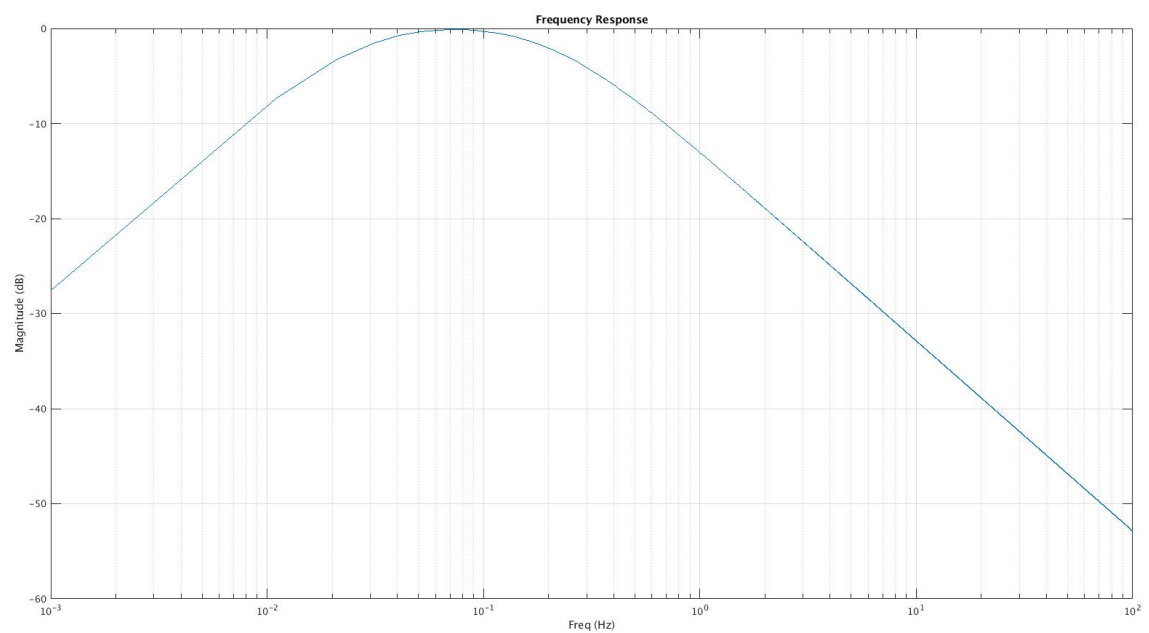


Figure 2: Frequency response of the transfer function in Matlab
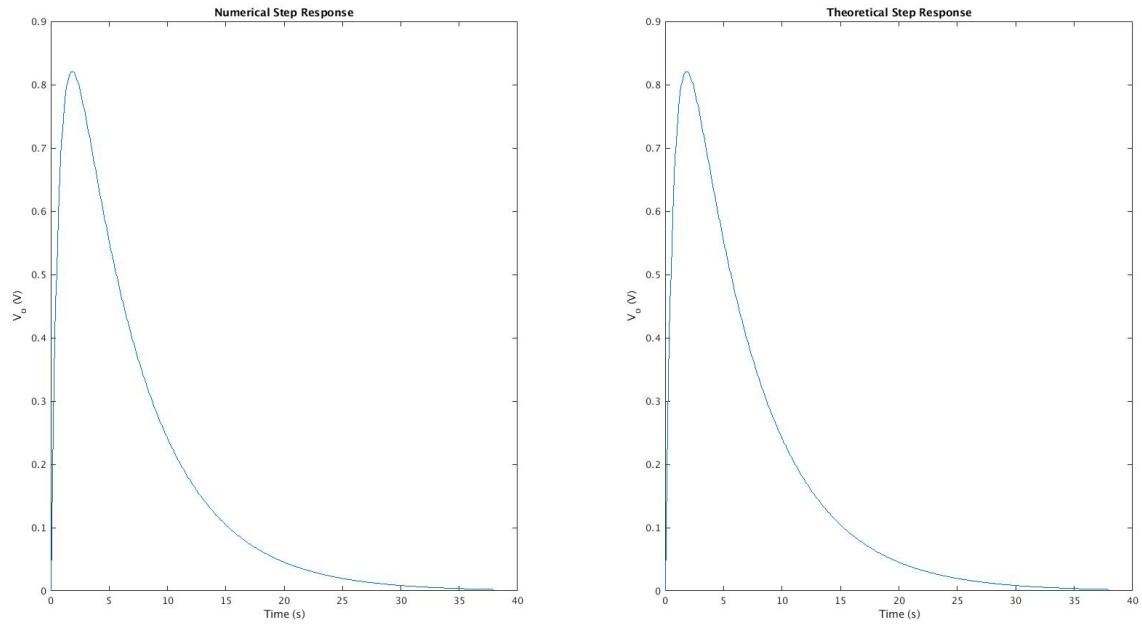
1

Figure 3: Time response to a step input in Matlab

Figures 1 and 2 show the frequency response of the circuit that was made in spice and the transfer function that was derived above. These plots are the same with gain in dB vs frequency in Hz and have the same intercepts and shape. This indicates a correct derivation.

Figure 3 contains both the numerical (left plot) and theoretical (right plot) time responses to a step input. The numerical one was found using the step function in matlab and the theoretical one was found by inverse laplace transform of the equation with a step response (shown above). As we can see though these are both pretty much identical indicating that the numerical methods are fairly accurate.

# Appendices

## A    Matlab Code

```
1  clear
2  W = linspace(0.001*2*pi, 100*2*pi, 10000);
3  H = freqs([200 0], [140 203 30], W);
4  figure(1)
5  semilogx(W./(2*pi), 20*log10(abs(H)))
6  grid on
7  xlabel("Freq (Hz)")
8  ylabel("Magnitude (dB)")
9  title("Frequency Response")
10
11 sys = tf([200 0], [140 203 30]);
12 [Y,T] = step(sys);
13 figure(2)
14 subplot(1,2,1)
15 plot(T,Y)
16 title("Numerical Step Response")
17 xlabel("Time (s)")
18 ylabel("V_{o} (V)")
```

```matlab
19
20  subplot(1,2,2)
21  y = (400./sqrt(24409)).*exp(T.*(-29/40)).*sinh((sqrt(3487).*T)./(40*sqrt(7)));
22  plot(T,y)
23  title("Theoretical Step Response")
24  xlabel("Time (s)")
25  ylabel("V_{o} (V)")
26  %stepFunction = (1: T >= 0);
```