

1a Not acceptable if $\bar{X} < 50$
lower CL of 98% is 50.1

$$H_0: \mu < 50 \text{ vs } H_1: \mu > 50$$

a We are given the 98% ($P < 0.02$) confidence bounds so unable to find $P < 0.01$ we don't know where $P < 0.01$ begins.

b We can because we know $P < 0.042 < 0.05$.
We are able to reject the null hypothesis.

2 $x = 12$ $n = 300$ want $P < 0.05$ $\therefore H_0: P \geq 0.05$
 $H_1: P < 0.05$

$$\hat{p} = \frac{x}{n}$$

$$= \frac{12}{300}$$

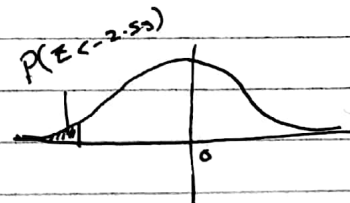
$$= 0.04$$

$$Z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$$

$$= \frac{0.04 - 0.05}{\sqrt{\frac{0.05 \times 0.95}{300}}}$$

$$= -2.55$$

$$P(Z < -2.55) = 0.0054$$



Pick a significance level of 0.05 5% level

$0.0054 < 0.05 \therefore$ Reject H_0

We can quantify the machine as confident at the 5% level

3 $\bar{X} = 23.2$ $S = 0.2$

a $H_0: \mu = 23$
 $H_1: \mu \neq 23$

b $t = \frac{23.2 - 23}{0.2 / \sqrt{10}}$
 $= \sqrt{10}$
 ≈ 3.16

should use student's t dist as small sample size

$\star v = 10 - 1$
 $= 9$

for 9 degrees of freedom (using the t table) the calculated t value falls between $0.005 < p < 0.01$ (one tail or P value)
 as it's a two tail P value we are looking for we ~~can double~~ double this to be $0.01 < p < 0.02$ (somewhere between here)

c Yes. if we wanted something like 95% or 98% confidence that the mean was exactly 23 then our current P value ~~is~~ says we should reject H_0 . if we wanted 99% confidence then we could say it's plausible that the mean is 23. however this range is likely too lenient so yes this process should be recalibrated.