General:

- newtype Parser a = P (String -> [(a,String)])
- Predicate: a function that takes one argument and returns a boolean
- * if pred x == True then x satisfies predicate pred
- function composition:

```
-- the . operator composes functions:

(f \cdot g) x == f (g x)
```

useful functions:

Parsing.hs:

• sat :: (Char -> Bool) -> Parser Char

concatMap f xs = foldr ((++) . f) [] xs

- * returns a character if that character satisfies the predicate
- digit, letter, alphanum :: Parser Char
- * parses a digit, letter, or alpha-numeric letter respectively
- char :: Char -> Parser Char
- * char 'a' parses exactly the character 'a'
- item :: Parser Char
- * parses any character
- similar to above: digit letter alphanum lower upper string
- many :: Parser a -> Parser [a]
- * parses 0 or more instances of a and collects them into a list
- many1 :: Parser a -> Parser [a]
- * same as many, but
- (+++) choice:
- * parse first argument if possible, else parse second argument
- * first successfully parsed argument is returned

- ((>>=)) sequential composition
- *a >>= b unboxes monad a into an output a0 and then unboxes monad b with input a0

- digit >>= \a -> digit >>= \b -> return [a,b]
- -- is equivalent to
 doubleDigit' :: Parser [Char]
 doubleDigit' = do
 - a <- digit b <- digit return [a,b]
- * (>>) is the same except that it discards the result of the first monad (thus it has signature (>>) :: Parser a -> Parser b -> Parser b)

Parsing Examples:

- \bullet bind and lambda method of parsing:
 - * parse a number:
- parse arithmetic expressions using do syntax:

Trees

- represent either a leaf node or some kind of internal node
- arithmetic tree declaration:

• how to fold over a tree:

```
-- exprFold valF negF addF

exprFold :: (Int->b) -> (b->b) -> (b->b->b) ->

-- mulF input output

(b->b->b) -> Expr -> b

exprFold valF negF addF mulF (Neg e)

= negF (exprFold valF negF addF mulF e)

exprFold valF negF addF mulF (Add s1 s2)

= addF (exprFold valF negF addF mulF s1)

(exprFold valF negF addF mulF s2)

exprFold valF negF addF mulF (Mul s1 s2)

= mulF (exprFold valF negF addF mulF s2)

exprFold valF negF addF mulF s2)
```

* basically, just collect values into some type b and use supplied functions at each node to fold into single value

* useful for evaluating simple things like:

```
-- evaluate an expression

evalExpr' = exprFold id (\x -> 0 - x) (+) (*)

id -- integers map to integers
(\x -> 0 - x) -- negation

-- everything else is just simple numeric operators

-- count leaves in a tree
countLeaves' = exprFold (\_ -> 1) id (+) (+)
(\_ -> 1) -- leaf integer node is one node
id -- negation node has only one child, pass on count
(+) (+) -- nodes with two children: add number

-- of leaf grandchildren
```

HW2: Water Gates:

```
waterGate :: Int -> Int
waterGate n =
length -- number of True's
$ filter id -- filter just True's
$ waterGate'n initial -- initial call to helper
where
-- start with all gates closed
initial = replicate n False
--
-- flip states
waterGate' 1 state = map not state
-- base case: flip every state
waterGate'n state = flip n $ waterGate' (n-1) state
-- otherwise, first get the state for (n-1) and then flip ex
--
-- flip every nth gate
flip:: Int -> [Bool] -> [Bool]
flip 1 xs = map not xs -- flip every gate
-- flip only gates which index are multiples of n
flip nth xs = [ if (i 'mod' nth == 0) then not x else x
-- zip each state with it's index
| (x,i) <- (zip xs [1..]) ]</pre>
```

| HW2: Goldbach's Other Conjecture:

```
-- check if a number is prime primeTest :: Integer -> Bool
primeTest 1 = False
primeTest t = and [(gcd t i) == 1 | i <- [2..t-1]]
 -- all numbers less than n that are double a square
twiceSquares :: Integer -> [Integer]
twiceSquares n = takeWhile (< n) [ 2 *x^2 | x <- [1..]]
-- list of odd numbers
oddList = map (\x -> 2*x + 1) [0..]
-- all odd numbers that are composite (not prime)
allOddComp = [ o | o <- (drop 1 oddList)</pre>
                   , not (primeTest o)
-- if a number satisfies conditions for conjecture
-- method: for enough square nubmers, check if n-(that number)
-- is prime
satsConds n = or [ primeTest k |
                     k \leftarrow map (\x->(n-x)) (twiceSquares n)
-- find the first number
goldbachNum = head [ x | x <- allOddComp, not (satsConds x) ]</pre>
HW4: Sets:
type Set a = [a]
a = mkSet [1,2,3,4,5]
b = mkSet [1,2,3]
addToSet :: Eq a \Rightarrow Set a \Rightarrow a \Rightarrow Set a
addToSet s a | a 'elem' s = s
                | otherwise = a : s
mkSet :: Eq a \Rightarrow [a] \rightarrow Set a
mkSet lst = foldl addToSet [] lst
isInSet :: Eq a => Set a -> a -> Bool
isInSet : Eq a -> book a sisInSet [] _ = False
isInSet [a] b = a == b
isInSet (x:xs) b | x == b = True
| otherwise = isInSet xs b
subset :: Eq a => Set a -> Set a -> Bool
subset sub super = and [ isInSet super x | x <- sub ]</pre>
setEqual :: Eq a => Set a -> Set a -> Bool
setEqual a b = subset a b && subset b a
-- instance (Eq a) => Eq (Set a) where
-- a == b = subset a b & subset b a setProd :: Set a -> Set a -> [(a,a)]
setProd a b = [ (ai,bj) | ai <- a</pre>
                            , bj <- b
Prev Exam: Run Length Encoding:
import Parsing
import Data.Char
q4 = do
  d <- sat isUpper
```

```
import Parsing
import Data.Char
q4 = do
    d <- sat isUpper
    e <- char (toLower d)
    f <- many item
    return [d,e]
ones = (map (\_ -> 1) [1..])
myRLE [] = []
myRLE ls = myhelper (zip ones ls)
myhelper [(n,c)] = [(n,c)]
myhelper ((n,c):(m,d):rest)
    | (d == c) = myhelper (((n+m),c):rest)
    | otherwise = (n,c):myhelper ((m,d):rest)
```