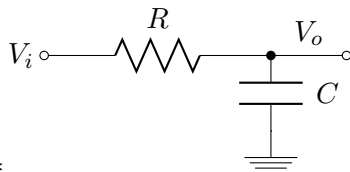


Metric Prefixes

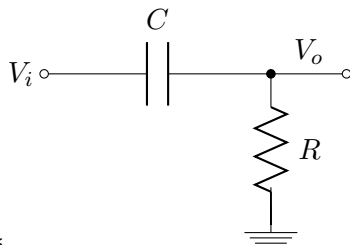
peta	P	10^{15}	1 000 000 000 000 000
tera	T	10^{12}	1 000 000 000 000
giga	G	10^9	1 000 000 000
mega	M	10^6	1 000 000
kilo	k	10^3	1 000
hecto	h	10^2	100
deca	da	10^1	10
one		10^0	1
deci	d	10^{-1}	0.1
centi	c	10^{-2}	0.01
milli	m	10^{-3}	0.001
micro	μ	10^{-6}	0.000 001
nano	n	10^{-9}	0.000 000 001
pico	p	10^{-12}	0.000 000 000 001
femto	f	10^{-15}	0.000 000 000 000 001

RC Filter

- Transmission Function: $T(s) = \frac{V_o(s)}{V_i(s)}$
- Corner frequency: frequency s at which $T(s) = \frac{1}{\sqrt{2}}$
- for simple circuit: ground \rightarrow source $\rightarrow R \rightarrow C \rightarrow$ ground
 - * $T(s) = \frac{1}{1+RCs}$
 - * $|T(j\omega)| = \frac{1}{\sqrt{1+R^2C^2\omega^2}}$
 - * $|\angle T(j\omega)| = \frac{1}{\sqrt{1+R^2C^2\omega^2}}$
- low pass



- * $T(s) = \frac{V_o}{V_i} = \frac{1}{1+RCs}$
- * corner frequency: $s = \frac{1}{RC}$ (also pole)
- high pass



- * $T(s) = \frac{V_o}{V_i} = \frac{RCs}{1+RCs}$
- * zero: $s = 0$, pole: $s = \frac{1}{RC}$

Bode Plots

- magnitude is plotted in dB: $|T(j\omega)|_{dB} = 20 \log_{10} |T(j\omega)|$
- starts on y-axis at DC offset with slope 0
- just add together the bode plots of each individual pole, zero, and the DC offset
- poles always slope down, zeros slope up (applies for both magnitude and phase)
- dec=decade, e.g. from 10^0 to 10^1
- magnitude:
 - * Pole/Zero at origin: constant slope $\pm 20\text{dB/dec}$ for all ω ; 0dB at $\omega = 10^0 = 1$
 - * Pole/Zero at ω_0 : 0 for $\omega < \omega_0$, slope $\pm 20 \frac{dB}{dec}$ after

- * Constant C : constant line at $20 \log_{10}(|C|)$
- phase:
 - * Pole at origin: constant $-\frac{\pi}{2}$ or -90°
 - * Zero at origin: constant $+\frac{\pi}{2}$ or $+90^\circ$
 - * Pole/Zero at ω_0 : 0 for $\omega < \frac{\omega_0}{10}$, slope linearly ($\pm 45^\circ/dec$) until $10\omega_0$, 0 slope for $\omega > 10\omega_0$
 - * Constant C : no effect (0 for all ω)

Solving systems with Op Amps

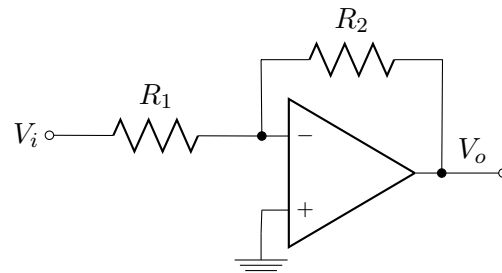
- step 0: if the op amp is ideal, write out ideal properties:
 - * $V_+ = V_-$
 - * $I_- = 0, I_+ = 0$
 - * $A \approx \infty$
- avoid doing KCL/KVL directly on the output node of the op amp
- ignore resistors from a point at $0V$ to ground

Non-Ideal Op Amps

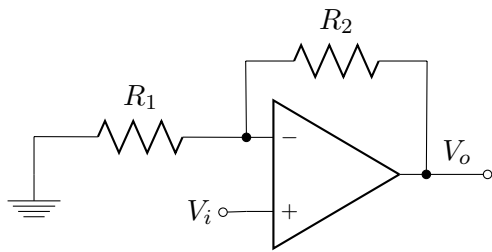
- $V_o = A(V_+ - V_-)$
 - * A : open-loop gain. Typically very large, 100,000 or more
- open-loop gain dependent on frequency: $A(s) = \frac{A_0}{1 - \frac{s}{\omega_b}}$
 - * open-loop response drops off after ω_b (usually $2\pi \leq \omega_b \leq 2\pi 100$)
 - * A_0 : DC gain
 - * ω_t : unity gain frequency: $dB(T(\omega_t)) = 1$
 - * $\omega_t \approx A_0 \omega_b$
 - * AKA gain bandwidth product
 - * in this case, we still assume $I_- = I_+ = 0$ and $V_- = V_+$?
- slew rate
 - * max rate at which the output can change
 - * for a sinusoidal signal: (V_{pk} : peak voltage) $SR > 2\pi f V_{pk}$ or $SR > \omega V_{pk}$
 - * $\frac{dV_o}{dt}|_{MAX} < SR$

Op Amp Equations

- general form: $T(s) = \frac{K_0}{1 + \frac{s}{\omega_0}}$
 - * $T(0) = K_0$: DC offset. For these simple ones, it's equal to ideal response
 - * $\omega_0 = \frac{\omega_t}{1+R_2/R_1}$
- inverting op amp:
 - * ideal: $T(s) = \frac{V_o}{V_i} = -\frac{R_2}{R_1}$
 - * non-ideal: $T(s) = \frac{V_o}{V_i} = \frac{-R_2/R_1}{1 + \frac{1+R_2/R_1}{A(s)}} = \frac{-R_2/R_1}{1 + \frac{s}{\frac{\omega_t}{1+R_2/R_1}}}$



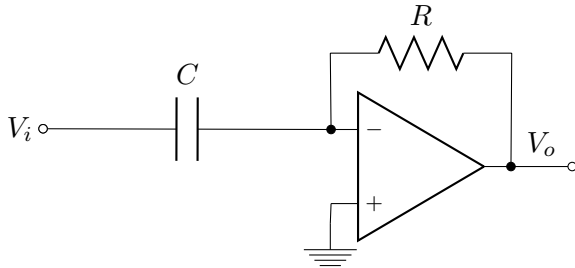
- non-inverting op-amp:
 - * ideal: $T(s) = \frac{V_o}{V_i} = 1 + \frac{R_2}{R_1}$
 - * non-ideal: $T(s) = \frac{V_o}{V_i} = \frac{1+R_2/R_1}{1 + \frac{1+R_2/R_1}{A(s)}} = \frac{1+R_2/R_1}{1 + \frac{s}{\frac{\omega_t}{1+R_2/R_1}}}$



• integrating

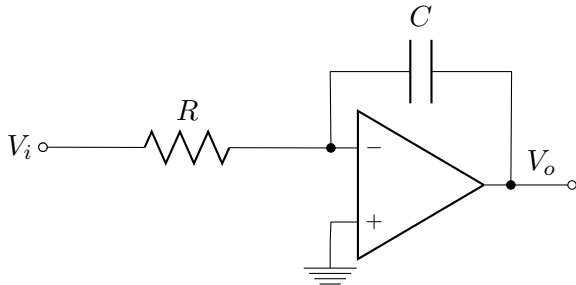
* ideal: $V_o = -\int_0^t \frac{V_i}{RC} dt + C$

% $C = V_o(t)$ at $t = 0$



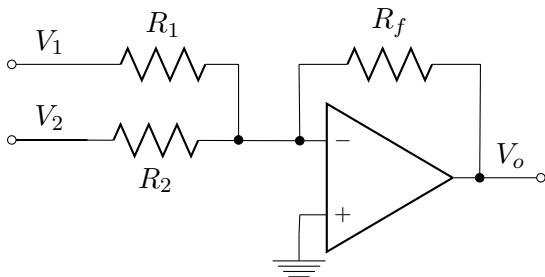
• differentiating

* ideal: $V_o = -RC \frac{dV_i}{dt}$



• summing

* ideal: $V_o = -R_f \left(\frac{V_1}{R_1} + \frac{V_2}{R_2} \right)$



• differential (subtracting)

* ideal: $V_o = \frac{(R_f + R_1)R_g}{(R_g + R_2)R_1} V_2 - \frac{R_f}{R_1} V_1$

