

Metric Prefixes

peta	P	10^{15}	1 000 000 000 000 000
tera	T	10^{12}	1 000 000 000 000
giga	G	10^9	1 000 000 000
mega	M	10^6	1 000 000
kilo	k	10^3	1 000
hecto	h	10^2	100
deca	da	10^1	10
one		10^0	1
deci	d	10^{-1}	0.1
centi	c	10^{-2}	0.01
milli	m	10^{-3}	0.001
micro	μ	10^{-6}	0.000 001
nano	n	10^{-9}	0.000 000 001
pico	p	10^{-12}	0.000 000 000 001
femto	f	10^{-15}	0.000 000 000 000 001

Ohm's Law $V = IR$, $I = \frac{V}{R}$, $R = \frac{V}{I}$

Battery Symbol

The side with the longer line is the positive side

Complex Numbers

- $z = x + iy = re^{i\theta} = r[\cos(\theta) + i\sin(\theta)]$
- $[r(\cos(\theta) + i\sin(\theta))]^n = r^n[\cos(n\theta) + i\sin(n\theta)]$
- $z^n = (re^{i\theta}) = r^n e^{in\theta}$
- $\frac{1}{i} = -i$
- $\sqrt[n]{z} = \sqrt[n]{r} e^{\frac{\theta}{n} + \frac{2k\pi}{n}}$ for $n \in \mathbb{N}^*$ (ints ≥ 0)
- $e^{j\theta} = \cos(\theta) + j\sin(\theta)$
- $e^{-j\theta} = \cos(\theta) - j\sin(\theta)$
- $\cos(\theta) = \frac{1}{2}(e^{j\theta} + e^{-j\theta})$
- $\sin(\theta) = \frac{1}{2j}(e^{j\theta} - e^{-j\theta})$
- normalized: $\text{sinc}(t) = \frac{\sin(\pi t)}{\pi t}$
- $|\frac{a}{b}| = \frac{|a|}{|b|}$
- $\angle \frac{a}{b} = \angle a - \angle b$

Trig

- $\cos^2(a) + \sin^2(a) = 1$
- $\cos(2a) = \cos^2(a) - \sin^2(a) = 2\cos^2(a) - 1 = 1 - 2\sin^2(a)$
- $\sin(2a) = 2\sin(a)\cos(a)$
- $\cos^2(a) = \frac{1}{2}(1 + \cos(2a))$
- $\sin^2(a) = \frac{1}{2}(1 - \cos(2a))$

Bode Plots

- magnitude is plotted in dB: $|T(j\omega)|_{dB} = 20 \log_{10} |T(j\omega)|$
- starts on y-axis at DC offset with slope 0
- just add together the bode plots of each individual pole, zero, and the DC offset
- poles always slope down, zeros slope up (applies for both magnitude and phase)
- *dec*=decade, e.g. from 10^0 to 10^1
- magnitude:
 - * Pole/Zero at origin: constant slope $\pm 20\text{dB/dec}$ for all ω ; 0dB at $\omega = 10^0 = 1$
 - * Pole/Zero at ω_0 : 0 for $\omega < \omega_0$ slope $\pm 20 \frac{\text{dB}}{\text{dec}}$ after
 - * Constant C : constant line at $20 \log_{10}(|C|)$
- phase:
 - * Pole at origin: constant $-\frac{\pi}{2}$ or -90°
 - * Zero at origin: constant $+\frac{\pi}{2}$ or $+90^\circ$

* Pole/Zero at ω_0 :

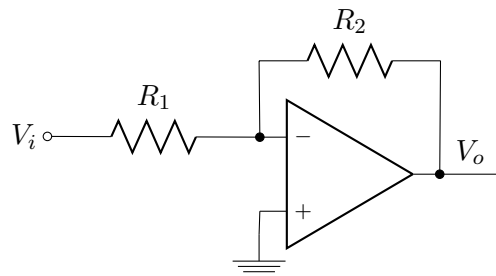
- 0 for $\omega < \frac{\omega_0}{10}$
- slope linearly ($\pm 45^\circ/\text{dec}$) until $10\omega_0$
- 0 slope for $\omega > 10\omega_0$

* Constant C : no effect (0 for all ω)

- Prof wants us to actually show the -3dB drop curve, not just a straight intersection

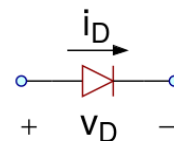
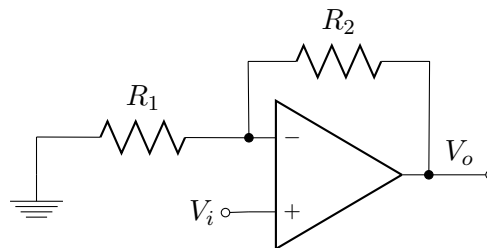
Op Amp Equations

- general form: $T(s) = \frac{K_0}{1 + \frac{s}{\omega_0}}$
 - * $T(0) = K_0$: DC offset. For these simple ones, it's equal to ideal response
 - * $\omega_0 = \frac{\omega_t}{1 + R_2/R_1}$
- inverting op amp:
 - * ideal: $T(s) = \frac{V_o}{V_i} = -\frac{R_2}{R_1}$
 - * non-ideal: $T(s) = \frac{V_o}{V_i} = \frac{-R_2/R_1}{1 + \frac{1 + R_2/R_1}{A(s)}} = \frac{-R_2/R_1}{1 + \frac{\frac{\omega_t}{1 + R_2/R_1}}{s}} = \frac{-R_2/R_1}{1 + \frac{s}{\omega_0}}$



- non-inverting op-amp:

- * ideal: $T(s) = \frac{V_o}{V_i} = 1 + \frac{R_2}{R_1}$
- * non-ideal: $T(s) = \frac{V_o}{V_i} = \frac{1 + R_2/R_1}{1 + \frac{1 + R_2/R_1}{A(s)}} = \frac{1 + R_2/R_1}{1 + \frac{\frac{\omega_t}{1 + R_2/R_1}}{s}} = \frac{1 + R_2/R_1}{1 + \frac{s}{\omega_0}}$

**Diodes**

- ideal:
 - * $I_D(V_D < 0) = 0$
 - * $I_D(V_D \geq 0) = \infty$
- constant drop model: (just the ideal model shifted right by 0.7V)
 - * $I_D(V_D < 0.7) = 0$
 - * $I_D(V_D \geq 0.7) = \infty$
- exponential model: $I_D = I_S(e^{\frac{V_D}{nV_T}} - 1)$
 - * $I_S = 10^{-12}\text{A}$ (saturation current)
 - * $V_T = 25\text{mV}$
- current goes \rightarrow from cathode (-) to anode (+)
- small signal resistance: $R_d = \frac{nV_T}{I_D}$
 - * I_D : average (DC) current through diode (due to forward bias)
- bridge rectifier shape: square/diamond with all the diodes point toward the + end of the output (away from ground)
- To solve a circuit with an op-amp and diodes, try individually solving with each possible combination of diodes off/on, and throw out the ones that cause

contradictions

Diode DC biasing for approximating AC linearity

- assumes $v(t) \ll nV_T$ (AC signal is much smaller than V_T)

$$r_D = \frac{nV_T}{I_D}$$

- first find DC solution to find I_D

- find r_D , then find AC solution

Design an (unregulated) AC adapter

- V_S : AC voltage input

*standard AC voltage is $110\sqrt{2}V \approx 155.563V$

- V_{S2} : output of transformer (still AC)

- V_p : peak DC output

- V_r : peak-to-peak ripple voltage (maximum variation)

*often given as a small percentage of V_p

- $V_p = V_{S2} -$ (diode voltage)

*diode voltage = 0.7V for single wave rectifier or center-tapped transformer

*diode voltage = 1.4V for full-wave rectifier

*(corresponds to how many diodes you need)

- turns ratio = $n = \frac{V_S}{V_{S2}}$

*if the transformer is center-tapped, each sub-coil only gets half of V_{S2} ; so use $n = \frac{1}{2} \frac{V_S}{V_{S2}}$

- apparent load resistance: $R_L = \frac{V_o}{I_L}$

- ripple voltage: $V_r = V_p \frac{T}{R_L C}$

* T : period of ripple (half of frequency of AC input)

$$T = \frac{1}{f}$$

* f : actual ripple frequency (double for full-wave rectifier)

* C : filter cap size

- Peak Inverse Voltage: minimum reverse bias breakdown voltage of the diodes

*center-tapped transformer, two diodes:

$$PIV = 2V_{S2} - 0.7$$

*bridge rectifier topology (two-terminal transformer):

$$PIV = V_{S2} - 0.7V$$

- avg diode current: $I_{Davg} = I_L \left(1 + \pi \sqrt{\frac{2}{V_r}}\right)$

- max diode current: $I_{Dmax} = I_L \left(1 + 2\pi \sqrt{\frac{2}{V_r}}\right)$

*only difference is $\pi \rightarrow 2\pi$

Transistors

- $V_T = 25mV$ at room temperature (according to textbook and prof),

$V_T = 26mV$ at room temperature (according to lab)

- β : a physical constant of the transistor. Usually about 100 or 200

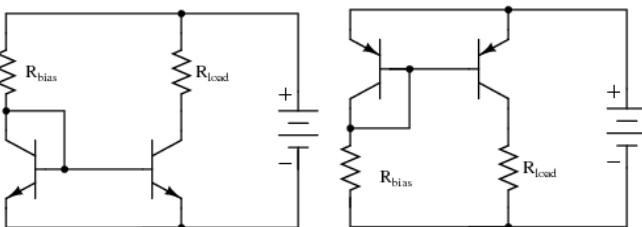
- $I_B + I_C = I_E$, $I_C = \beta I_B$, $I_E = (1 + \beta)I_B$

- $\alpha = \frac{\beta}{1 + \beta}$, $I_C = \alpha I_E$

- $I_C = I_S(e^{\frac{V_{BE}}{nV_T}})$,

- AC (assumes correct DC bias): $g_m = \frac{1}{r_e} = \frac{I_C}{V_T}$

Current Mirror



(a) current sinking

(b) current-sourcing

- Q1 has the base shorted to collector, Q2 does not

- $R_{bias} = R_{ref}$: the current that is mirrored

- $I_{ref} = (V_{CC} - 0.7)/R_{ref}$

- R_{load} has the same current through it as R_{ref} does

*that is, $I_{ref} = I_{load}$

- you can chain together multiple transistors (Q3, Q4...) all off of the same Q1 and they will all get the same current

*In this case, each Q2, Q3... output is considered separate from each other in both DC and AC analysis

- only applies when transistors are matched! (we assume they are)

Transistor circuits by inspection

- this all assumes that the transistor is properly DC biased

- three types of amplifier circuits: common emitter, common base, common collector

*CE, CB, CC

*the "common" pin is the one that is neither AC input nor output

- intrinsic gain: gain directly from the input pin of the transistor to the output, ignoring any source resistance or such things whatever

*when you chain multiple amplifiers together, this is the one you use

- when you're driving a finite-impedance load (a load other than open circuit), you have to consider R_o as $R_o || R_L$

*this will change the gain, which is why it's often

helpful to put a CC buffer at the end of an amplifier

- R_i : input impedance: impedance as seen from the input

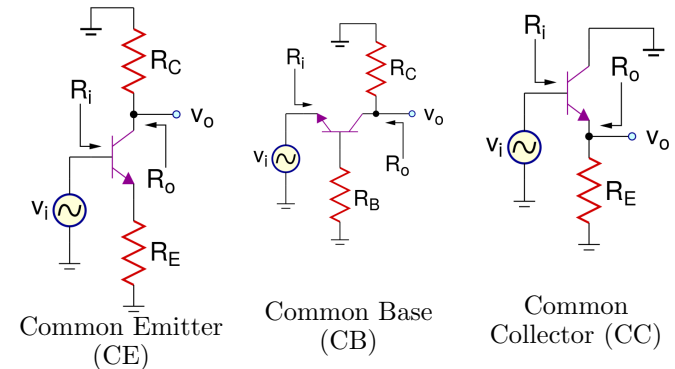
*includes the transistor, does not include R_s

- $g_m = \frac{I_C}{V_T}$

$$r_\pi = \frac{\beta}{g_m}$$

$$r_e = \frac{V_T}{I_E} = \frac{\alpha}{g_m} \approx \frac{1}{g_m}$$

$$r_o = \frac{V_A}{I_C} \approx \infty$$



- CE: Common Emitter

*input: base; output: collector

*intrinsic gain: $\frac{V_o}{V_b} = -\alpha \frac{R_C}{r_e + R_E} \approx -\frac{R_C}{r_e + R_E}$

* $R_i = (\beta + 1)(r_e + R_E)$

* $R_o = R_C$

*if you have a R_L then you have to put that in parallel with R_C when calculating $\frac{V_o}{V_b}$

- CB: Common Base

* $\frac{V_o}{V_b} = \alpha \frac{R_C}{R_i} \approx \frac{R_C}{R_i}$

* $R_i = r_e + \frac{R_B}{\beta + 1}$

* $R_o = R_C$

- CC: Common Collector

*gain ≈ 1 because it's a buffer

* $\frac{V_o}{V_b} = \frac{R_E}{r_e + R_E}$

* $R_i = (\beta + 1)(r_e + R_E)$

* $R_o = R_E || r_e = \frac{R_E * r_e}{R_E + r_e}$