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CSCE 314 Reference Sheet Last Updated: March 7, 2017
                                                                              * same as many, but
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                                                                             • (+++) choice:
                                                                               * parse first argument if possible, else parse second argument
General:
                                                                              * first successfully parsed argument is returned
• newtype Parser a = P (String -> [(a,String)])
                                                                                (+++) :: Parser a -> Parser a -> Parser a
• Predicate: a function that takes one argument and returns a
                                                                               p +++ q = P (\inp -> case parse p inp of -> parse q in
                                                                                                                  -> parse q inp
                                                                                                       [(v,out)] -> [(v,out)])
 * if pred x == True then x satisfies predicate pred
• function composition:
                                                                             • ((>>=)) sequential composition
                                                                              * a >>= b unboxes monad a into an output a0 and then un-
    the . operator composes functions:
                                                                               boxes monad b with input a0
 (f \cdot g) x == f (g x)
                                                                               type Parser a = String -> [(a, String)]
-- implementation for in-class mostly-complete
-- parser 'monads'
useful library functions:
-- Data.List
nubBy :: (a -> a -> Bool) -> [a] -> [a]
                                                                                (>>=) :: Parser a -> (a -> Parser b) -> Parser b
                                                                                (>>=) p1 p2 = \inp -> case parse p1 inp of
nubBy pred xs = -- unique elements only from xs as
                    -- determined by pred
                                                                                        [(v, out)] -> parse (p2 v) out
nub :: Eq a => [a] -> [a]
nub xs = nubBy (==) a -- unique elements from xs
                                                                              * usage:
                                                                                doubleDigit :: Parser [Char]
doubleDigit =
                                                                                  digit >>= \a ->
                                                                                  digit >>= \b ->
-- concatenate container of lists
                                                                                  return [a,b]
concat :: Foldable t => t [a] -> [a]
-- or for list-of-lists specifically:
concat :: [[a]] -> [a]
                                                                                -- is equivalent to
                                                                                doubleDigit' :: Parser [Char]
doubleDigit' = do
concat xs = foldl (++) [] xs
                                                                                  a <- digit
b <- digit
-- like concat, but use a function to get the inner lists
concatMap :: (a -> [b]) -> [a] -> [b]
concatMap f xs = foldr ((++) . f) [] xs
                                                                                  return [a,b]
                                                                              * (>>) is the same except that it discards the result of the
                                                                                first monad (thus it has signature (>>) :: Parser a ->
-- get the longest prefix of xs for which pred is true
-- and also return the rest of the list

span :: (a -> Bool) -> [a] -> ([a], [a])
                                                                                Parser b -> Parser b)
                                                                             Parsing Examples:
span pred xs = (takeWhile pred xs, dropWhile pred xs)
                                                                             • bind and lambda method of parsing:
-- repeat a = infinite \ list \ of \ a
                                                                              * parse a number:
repeat :: a -> [a]
                                                                             • parse arithmetic expressions using do syntax:
expr :: Parser Int
repeat x = [x \mid -(1..]]
-- replicate n a = list of length n repeating a
                                                                              expr = do t <- term</pre>
                                                                                            do {char '+' ;e <- expr
replicate :: Int -> a -> [a]
                                                                                                ;return (t + e)
replicate n x = map (\  \  ) [1..n]
replicate n x = [ x | _ <- [1..n] ]
                                                                              term :: Parser Int
term = do f <- factor
do char '*'
t <- term
return (f * t)
+++ return f
factor :: Parser Int
factor = do d <- digit
-- folds (works on any foldable, not just lists)
foldr :: (a -> b -> b) -> b -> [a] -> b
foldr f z [a,b,c] = a 'f' (b 'f' (c 'f' z))
foldr f z [a,b,c] = f a $ f b $ f c z
-- combines into z from right to left
-- can potentially work on an empty list if one of the
-- folds does not evaluate it's second argument
foldl :: (b \rightarrow a \rightarrow b) \rightarrow b \rightarrow [a] \rightarrow b

foldl f z [a,b,c] = ((z 'f' a) 'f' b) 'f' c

foldl f z [a,b,c] = f (f (f z a) b) c

-- evaluates from right to left

-- will not work on infinite list because it must start at
                                                                                             return (digitToInt d)
                                                                                            +++ do char '('
                                                                                                     e <- expr
                                                                                                     char ')
                                                                                     return e
:: String -> Int
-- the end of the list
                                                                              eval xs = fst (head (parse expr xs))
-- these are the same as above, except they take the first
-- two elements for the first application of f foldr1 :: (a -> a -> a) -> [a] -> a foldl1 :: (a -> a -> a) -> [a] -> a
                                                                             • represent either a leaf node or some kind of internal node
                                                                             • arithmetic tree declaration:
                                                                              data Expr = Val Int
                                                                                            Neg Expr
Parsing.hs:
                                                                                           Add Expr Expr
• sat :: (Char -> Bool) -> Parser Char
                                                                                           | Mul Expr Expr
 * returns a character if that character satisfies the predicate
                                                                             • how to fold over a tree:
• digit, letter, alphanum :: Parser Char
                                                                                                             negF
                                                                               -- exprFold valF
                                                                                                                          addF
 * parses a digit, letter, or alpha-numeric letter respectively
                                                                              exprFold :: (Int->b) -> (b->b) -> (b->b->b) ->
```

- char :: Char -> Parser Char \* char 'a' parses exactly the character 'a'
- item :: Parser Char
- \* parses any character
- similar to above: digit letter alphanum lower upper string
- many :: Parser a -> Parser [a]
- \* parses 0 or more instances of a and collects them into a list
- many1 :: Parser a -> Parser [a]

= negF

= addF

input output

(exprFold valF negF addF mulF e)

(exprFold valF negF addF mulF s1)

(exprFold valF negF addF mulF s2)

(exprFold valF negF addF mulF s2)

(b->b->b) -> Expr -> b exprFold valF \_ \_ (Val i) = valF i exprFold valF negF addF mulF (Neg e)

exprFold valF negF addF mulF (Add s1 s2)

exprFold valF negF addF mulF (Mul s1 s2)

= mulF (exprFold valF negF addF mulF s1)

```
setProd a b = [ (ai,bj) | ai <- a</pre>
   plied functions at each node to fold into single value
                                                                                                    , bj <- b
  * useful for evaluating simple things like:
   -- evaluate an expression
   evalExpr'
               = exprFold id (\x \rightarrow 0 - x) (+) (*)
                                                                       Prev Exam: Run Length Encoding:
   id -- integers map to integers
   (\x -> 0 - x) - negation
                                                                       import Parsing
   -- everything else is just simple numeric operators
                                                                       import Data.Char
                                                                       q4 = do
   -- count leaves in a tree countLeaves' = exprFold (\_ -> 1) id (+) (+) (\_ -> 1) -- leaf integer node is one node id -- negation node has only one child, pass on count
                                                                          d <- sat isUpper
                                                                          e <- char (toLower d) f <- many item
                                                                          return [d,e]
   (+) (+) -- nodes with two children: add number -- of leaf grandchildren
                                                                       ones = (map (\ -> 1) [1..])
                                                                       myRLE [] = []
HW2: Water Gates:
                                                                       myRLE ls = myhelper (zip ones ls)
waterGate :: Int -> Int
waterGate n =
length -- number of True's
                                                                       myhelper [(n,c)] = [(n,c)]
                                                                       myhelper ((n,c):(m,d):rest)
                                                                          | (d == c) = myhelper (((n+m),c):rest)
 $ filter id -- filter just True's
                                                                          | otherwise = (n,c):myhelper ((m,d):rest)
 $ waterGate' n initial -- initial call to helper
 where -- start with all gates closed
                                                                       Rock Paper Scissors:
  initial = replicate n False
                                                                       data RPS = Rock | Paper | Scissors
   -- flip states
                                                                          deriving (Eq, Show)
  waterGate' 1 state = map not state
                                                                       rps :: RPS -> RPS -> Int
     -- base case: flip every state
                                                                       rps a b | a == b = 0
  waterGate' n state = flip n $ waterGate' (n-1) state
                                                                                      Scissors = 1
                                                                       rps Rock
                                                                                   Rock
   -- otherwise, first get the state for (n-1) and then
                                                                       rps Paper
   -- flip every nth state
                                                                       rps Scissors Paper
  -- flip every nth gate
                                                                       rps _ = 2
rps2 :: RPS -> RPS -> Int
                                                                                                 = 2
  flip :: Int -> [Bool] -> [Bool]
flip 1 xs = map not xs -- flip every gate
-- flip only gates which index are multiples of n
                                                                       rps2 a b =
                                                                          if a == b then 0 else case (a,b) of
  flip nth xs = [ if (i 'mod' nth == 0) then not x else x
                                                                            (Rock,
                                                                                      Scissors) -> 1
                                                                            (Paper,
                                                                                        Rock)
                    - zip each state with it's index
                                                                            (Scissors, Paper)
                   | (x,i) \leftarrow (zip xs [1..])
                                                                            _ -> 2
HW2: Goldbach's Other Conjecture:
                                                                       99 problems:
-- check if a number is prime
                                                                        -- 9. pack consecutive duplicates into sublists
primeTest :: Integer -> Bool
                                                                       pack (x:xs) = let (first,rest) = span (==x) xs
primeTest 1 = False
                                                                                         in (x:first) : pack rest
primeTest t = and [ (gcd t i) == 1 | i < - [2..t-1]]
                                                                       pack [] = []
-- all numbers less than n that are double a square
                                                                         - example:
twiceSquares :: Integer -> [Integer]
                                                                       pack [1,2,3,2,2,3] == [[1,1],[2],[3],[2,2],[3]]
twiceSquares n = takeWhile (<n) [ 2 *x^2 | x < [1..]]
-- list of odd numbers
oddList = map (x -> 2*x + 1) [0..]
-- all odd numbers that are composite (not prime)
allOddComp = [ o | o <- (drop 1 oddList)</pre>
                   , not (primeTest o)
-- if a number satisfies conditions for conjecture -- method: for enough square nubmers, check if
-- n-(that number) is prime
satsConds n = or [ primeTest k |
                     k \leftarrow map (\x->(n-x)) (twiceSquares n)
-- find the first number
{\tt goldbachNum} \ = \ {\tt head} \ [\ {\tt x} \ | \ {\tt x} \ {\tt <-} \ {\tt allOddComp}
                           , not (satsConds x) ]
HW4: Sets:
type Set a = [a]
a = mkSet [1,2,3,4,5]
b = mkSet [1,2,3]
addToSet :: Eq a => Set a -> a -> Set a
addToSet s a | a 'elem' s = s
               | otherwise = a : s
mkSet :: Eq a => [a] -> Set a
mkSet lst = foldl addToSet [] lst
isInSet :: Eq a => Set a -> a -> Bool
isInSet [] = False
isInSet [a] b = a == b
isInSet (x:xs) b | x == b = True
| otherwise = isInSet xs b
subset :: Eq a => Set a -> Set a -> Bool
subset sub super = and [ isInSet super x | x <- sub ]</pre>
setEqual :: Eq a \Rightarrow Set a \rightarrow Set a \rightarrow Bool
setEqual a b = subset a b && subset b a
-- instance (Eq a) => Eq (Set a) where
```

setProd :: Set a -> Set a -> [(a,a)]

\* basically, just collect values into some type b and use sup-

-- a == b = subset a b & subset b a