



$$\bullet I_1 = \frac{V_1 - V_{int-1}}{R} ; I_2 = \frac{V_2 - V_{int-1}}{R} ; I_3 = \frac{V_3 - V_{int-1}}{R}$$

$$\hookrightarrow I_n = \frac{V_n - V_{int-1}}{R}$$

$$\bullet I_{tot} = (I_1 + I_2 + I_3 + \dots + I_n) - I_{exit}$$

$$\Rightarrow 0 = (I_1 + I_2 + I_3 + \dots + I_n) - I_{exit}$$

$$\Rightarrow 0 = \left(\frac{V_1 - V_{int-1}}{R} + \frac{V_2 - V_{int-1}}{R} + \dots + \frac{V_n - V_{int-1}}{R} \right) - \frac{V_{int-1}}{R}$$

$$\Leftrightarrow V_{int-1} + n V_{int-1} = V_1 + V_2 + \dots + V_n$$

$$\Leftrightarrow V_{int-1} = \frac{(V_1 + V_2 + \dots + V_n)}{(n+1)} \quad (*)$$

$$\bullet I_{tot} = \frac{V_{out} - V_{int-2}}{nR} \quad \& \quad I_{tot} = \frac{V_{int-2}}{R}$$

$$\Rightarrow \frac{V_{out} - V_{int-2}}{n} = V_{int-2}$$

$$\Rightarrow V_{out} = V_{int-2} (n+1)$$

$$V_{int-2} = V_{int-1}, \text{ SO: } V_{out} = V_{int-1} (n+1) \quad (**)$$

$$(*) \text{ into } (**): V_{out} = V_{int-1} (n+1)$$

$$\Rightarrow V_{out} = \frac{(V_1 + V_2 + \dots + V_n)}{(n+1)} (n+1)$$

$$\Rightarrow \boxed{V_{out} = V_1 + V_2 + \dots + V_n}$$