

# Corrección parcial

1.  $\ddot{x} + \ddot{x} + 2\dot{x} + x = 2f(t)$

$\xrightarrow{s} s^3 + s^2 + 2s + 1 = 2f(s) \rightarrow X(s) [s^3 + s^2 + 2s + 1] = 2f(s)$

$\therefore G(s) = \frac{2}{s^3 + s^2 + 2s + 1}$

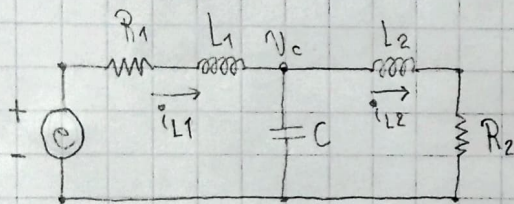
• Variables de estado:

$q_1 = x ; q_2 = \dot{q}_1 ; q_3 = \dot{q}_2 ; f(t) = u$

$\therefore 2u = \ddot{q}_3 + \dot{q}_3 + 2\dot{q}_2 + q_1 \rightarrow \dot{q}_3 = -q_1 - 2q_2 - q_3 + 2u$

$$\begin{bmatrix} \dot{q}_1 \\ \dot{q}_2 \\ \dot{q}_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -2 & -1 \end{bmatrix} \begin{bmatrix} q_1 \\ q_2 \\ q_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 2 \end{bmatrix} u$$

2.



$$\left. \begin{array}{l} x_1 = i_{L1} \\ x_2 = i_{L2} \\ x_3 = v_C \end{array} \right\} \begin{array}{l} u = c \\ v_o = R_2 x_2 \end{array} \quad U = R_1 x_1 + L_1 \dot{x}_1 + x_3$$

$\rightarrow \dot{x}_1 = -\frac{R_1}{L_1} x_1 + 0x_2 - \frac{x_3}{L_1} + \frac{u}{L_1}$

$x_3 = L_2 \dot{x}_2 + R_2 x_2 \rightarrow \dot{x}_2 = 0R_1 - \frac{R_2}{L_2} x_2 + \frac{x_3}{L_2}$

$x_1 = C \dot{x}_3 + x_2 \rightarrow \dot{x}_3 = \frac{x_1}{C} - \frac{x_2}{C}$

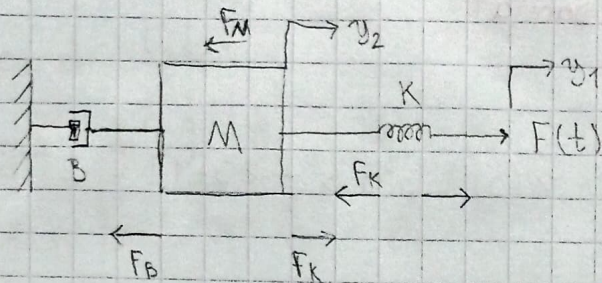
• Variables de estado:

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} -R_1/L_1 & 0 & -1/L_1 \\ 0 & -R_2/L_2 & 1/L_2 \\ 1/C & -1/C & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 1/L_1 \\ 0 \\ 0 \end{bmatrix} u$$

$y = \begin{bmatrix} 0 & R_2 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + 0u$



3.



$$\dot{y}_1 > \dot{y}_2 \quad \nabla$$

•  $F = F_K$  y  $F_K = F_N + F_B$

•  $x_1 = y_2$  ;  $x_2 = \dot{x}_1 = \dot{y}_1$  ;  $u = f_K = k(y_1 - x_1)$

•  $y_1 = x_1 + u/k \rightarrow u = M\dot{x}_2 + Bx_2 \rightarrow \dot{x}_2 = -\frac{B}{M}x_2 + \frac{u}{M}$

• Variables de estado:

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 0 & -\frac{B}{M} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ \frac{1}{M} \end{bmatrix} u \quad \text{y} \quad \begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} \frac{1}{K} \\ 0 \end{bmatrix} u$$