Regularization

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Contents

```
Examples
                                                                                  1
  library(gamlr)
## Loading required package: Matrix
sessionInfo()
## R version 4.2.1 (2022-06-23 ucrt)
## Platform: x86_64-w64-mingw32/x64 (64-bit)
## Running under: Windows 10 x64 (build 19044)
## Matrix products: default
##
## locale:
## [1] LC_COLLATE=English_United States.utf8
## [2] LC_CTYPE=English_United States.utf8
## [3] LC_MONETARY=English_United States.utf8
## [4] LC NUMERIC=C
## [5] LC_TIME=English_United States.utf8
## attached base packages:
## [1] stats
               graphics grDevices utils
                                           datasets methods
                                                              base
##
## other attached packages:
## [1] gamlr_1.13-7 Matrix_1.4-1
## loaded via a namespace (and not attached):
   [1] lattice_0.20-45 digest_0.6.29
                                    grid_4.2.1
                                                   magrittr_2.0.3
   [5] evaluate_0.15
                                     stringi_1.7.8
                                                    cli_3.3.0
                      rlang_1.0.3
   [9] rmarkdown_2.14 tools_4.2.1
                                     stringr_1.4.0
                                                    xfun_0.31
## [13] yaml_2.3.5
                      fastmap_1.1.0
                                     compiler_4.2.1
                                                   htmltools_0.5.2
## [17] knitr_1.39
```

Regularization is essentially another way to say desensitization. What we will do is trade off bias (deviations from minimizing SSR) and variance (variation in predicted values).

Examples

We are going to go through multiple examples.

NHL

The data comprise of information about play configuration and the players on ice (including goalies) for every goal from 2002-03 to 2012-14 NHL seasons. Collected using A. C. Thomas's nlhscrapr package. See the Chicago hockey analytics project at github.com/mataddy/hockey

- goal -> Info about each goal scored, including homegoal an indicator for the home team scoring.
- player -> Sparse Matrix with entries for who was on the ice for each goal: +1 for a home team player, -1 for an away team player, zero otherwise.
- team -> Sparse Matrix with indicators for each team*season interaction: +1 for home team, -1 for away team.
- config -> Special teams info. For example, S5v4 is a 5 on 4 powerplay, +1 if it is for the home-team and -1 for the away team

Data Cleaning

Bringing in data

```
data(hockey)
```

```
x <- cbind(config,team,player) # cbind binds together two sparse matrices
```

Generate Independent Variables

```
y <- goal$homegoal
```

Generating dependent variable, Binary response

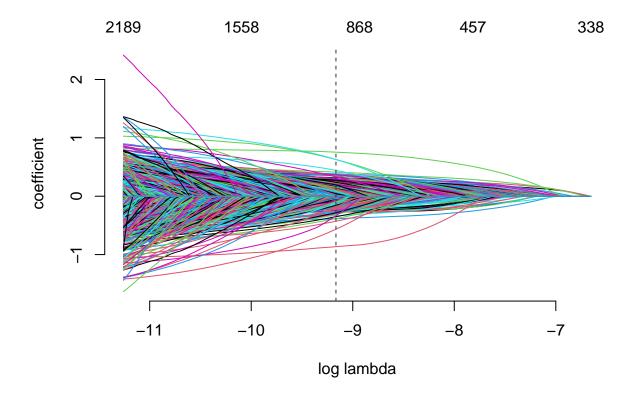
Generate Model

```
nhlreg <- gamlr(x, y, verb=TRUE,
    free=1:(ncol(config)+ncol(team)), ## free denotes unpenalized columns
    family="binomial", standardize=FALSE)</pre>
```

```
## *** n=69449 observations and p=2776 covariates ***
## segment 1: lambda = 0.001289, dev = 8.096e+04, npass = 292
## segment 2: lambda = 0.001231, dev = 8.095e+04, npass = 3
## segment 3: lambda = 0.001175, dev = 8.094e+04, npass = 3
## segment 4: lambda = 0.001121, dev = 8.094e+04, npass = 3
## segment 5: lambda = 0.00107, dev = 8.093e+04, npass = 4
## segment 6: lambda = 0.001022, dev = 8.092e+04, npass = 4
## segment 7: lambda = 0.0009753, dev = 8.091e+04, npass = 3
## segment 8: lambda = 0.000931, dev = 8.089e+04, npass = 3
## segment 9: lambda = 0.0008887, dev = 8.087e+04, npass = 4
## segment 10: lambda = 0.0008483, dev = 8.084e+04, npass = 4
## segment 11: lambda = 0.0008097, dev = 8.081e+04, npass = 4
## segment 12: lambda = 0.0007729, dev = 8.079e+04, npass = 4
## segment 13: lambda = 0.0007378, dev = 8.076e+04, npass = 4
## segment 14: lambda = 0.0007043, dev = 8.073e+04, npass = 4
## segment 15: lambda = 0.0006723, dev = 8.07e+04, npass = 4
## segment 16: lambda = 0.0006417, dev = 8.066e+04, npass = 4
## segment 17: lambda = 0.0006125, dev = 8.063e+04, npass = 4
## segment 18: lambda = 0.0005847, dev = 8.059e+04, npass = 4
## segment 19: lambda = 0.0005581, dev = 8.055e+04, npass = 4
```

```
## segment 20: lambda = 0.0005327, dev = 8.051e+04, npass = 4
## segment 21: lambda = 0.0005085, dev = 8.046e+04, npass = 4
## segment 22: lambda = 0.0004854, dev = 8.041e+04, npass = 4
## segment 23: lambda = 0.0004634, dev = 8.036e+04, npass = 4
## segment 24: lambda = 0.0004423, dev = 8.031e+04, npass = 4
## segment 25: lambda = 0.0004222, dev = 8.025e+04, npass = 4
## segment 26: lambda = 0.000403, dev = 8.019e+04, npass = 4
## segment 27: lambda = 0.0003847, dev = 8.013e+04, npass = 4
## segment 28: lambda = 0.0003672, dev = 8.007e+04, npass = 4
## segment 29: lambda = 0.0003505, dev = 8.001e+04, npass = 4
## segment 30: lambda = 0.0003346, dev = 7.995e+04, npass = 4
## segment 31: lambda = 0.0003194, dev = 7.99e+04, npass = 4
## segment 32: lambda = 0.0003049, dev = 7.984e+04, npass = 4
## segment 33: lambda = 0.000291, dev = 7.978e+04, npass = 4
## segment 34: lambda = 0.0002778, dev = 7.972e+04, npass = 4
## segment 35: lambda = 0.0002651, dev = 7.967e+04, npass = 4
## segment 36: lambda = 0.0002531, dev = 7.961e+04, npass = 4
## segment 37: lambda = 0.0002416, dev = 7.955e+04, npass = 4
## segment 38: lambda = 0.0002306, dev = 7.949e+04, npass = 4
## segment 39: lambda = 0.0002201, dev = 7.943e+04, npass = 4
## segment 40: lambda = 0.0002101, dev = 7.937e+04, npass = 4
## segment 41: lambda = 0.0002006, dev = 7.931e+04, npass = 4
## segment 42: lambda = 0.0001915, dev = 7.925e+04, npass = 4
## segment 43: lambda = 0.0001828, dev = 7.919e+04, npass = 4
## segment 44: lambda = 0.0001745, dev = 7.913e+04, npass = 4
## segment 45: lambda = 0.0001665, dev = 7.907e+04, npass = 4
## segment 46: lambda = 0.000159, dev = 7.901e+04, npass = 4
## segment 47: lambda = 0.0001517, dev = 7.895e+04, npass = 4
## segment 48: lambda = 0.0001448, dev = 7.889e+04, npass = 4
## segment 49: lambda = 0.0001382, dev = 7.883e+04, npass = 4
## segment 50: lambda = 0.000132, dev = 7.877e+04, npass = 4
## segment 51: lambda = 0.000126, dev = 7.871e+04, npass = 4
## segment 52: lambda = 0.0001202, dev = 7.865e+04, npass = 4
## segment 53: lambda = 0.0001148, dev = 7.86e+04, npass = 4
## segment 54: lambda = 0.0001096, dev = 7.854e+04, npass = 4
## segment 55: lambda = 0.0001046, dev = 7.848e+04, npass = 4
## segment 56: lambda = 9.983e-05, dev = 7.843e+04, npass = 4
## segment 57: lambda = 9.529e-05, dev = 7.838e+04, npass = 4
## segment 58: lambda = 9.096e-05, dev = 7.832e+04, npass = 4
## segment 59: lambda = 8.682e-05, dev = 7.827e+04, npass = 4
## segment 60: lambda = 8.288e-05, dev = 7.821e+04, npass = 4
## segment 61: lambda = 7.911e-05, dev = 7.816e+04, npass = 4
## segment 62: lambda = 7.552e-05, dev = 7.811e+04, npass = 4
## segment 63: lambda = 7.208e-05, dev = 7.806e+04, npass = 4
## segment 64: lambda = 6.881e-05, dev = 7.801e+04, npass = 4
## segment 65: lambda = 6.568e-05, dev = 7.795e+04, npass = 4
## segment 66: lambda = 6.269e-05, dev = 7.79e+04, npass = 4
## segment 67: lambda = 5.984e-05, dev = 7.786e+04, npass = 4
## segment 68: lambda = 5.712e-05, dev = 7.781e+04, npass = 4
## segment 69: lambda = 5.453e-05, dev = 7.776e+04, npass = 4
## segment 70: lambda = 5.205e-05, dev = 7.772e+04, npass = 3
## segment 71: lambda = 4.968e-05, dev = 7.767e+04, npass = 4
## segment 72: lambda = 4.743e-05, dev = 7.763e+04, npass = 3
## segment 73: lambda = 4.527e-05, dev = 7.758e+04, npass = 3
```

```
## segment 74: lambda = 4.321e-05, dev = 7.754e+04, npass = 3
## segment 75: lambda = 4.125e-05, dev = 7.75e+04, npass = 3
## segment 76: lambda = 3.937e-05, dev = 7.745e+04, npass = 3
## segment 77: lambda = 3.758e-05, dev = 7.741e+04, npass = 3
## segment 78: lambda = 3.588e-05, dev = 7.737e+04, npass = 3
## segment 79: lambda = 3.425e-05, dev = 7.733e+04, npass = 3
## segment 80: lambda = 3.269e-05, dev = 7.729e+04, npass = 3
## segment 81: lambda = 3.12e-05, dev = 7.725e+04, npass = 3
## segment 82: lambda = 2.978e-05, dev = 7.721e+04, npass = 3
## segment 83: lambda = 2.843e-05, dev = 7.717e+04, npass = 3
## segment 84: lambda = 2.714e-05, dev = 7.714e+04, npass = 3
## segment 85: lambda = 2.591e-05, dev = 7.71e+04, npass = 3
## segment 86: lambda = 2.473e-05, dev = 7.707e+04, npass = 3
## segment 87: lambda = 2.36e-05, dev = 7.703e+04, npass = 3
## segment 88: lambda = 2.253e-05, dev = 7.7e+04, npass = 3
## segment 89: lambda = 2.151e-05, dev = 7.697e+04, npass = 1
## segment 90: lambda = 2.053e-05, dev = 7.695e+04, npass = 1
## segment 91: lambda = 1.96e-05, dev = 7.691e+04, npass = 3
## segment 92: lambda = 1.871e-05, dev = 7.688e+04, npass = 3
## segment 93: lambda = 1.786e-05, dev = 7.685e+04, npass = 3
## segment 94: lambda = 1.704e-05, dev = 7.683e+04, npass = 1
## segment 95: lambda = 1.627e-05, dev = 7.68e+04, npass = 1
## segment 96: lambda = 1.553e-05, dev = 7.678e+04, npass = 1
## segment 97: lambda = 1.482e-05, dev = 7.676e+04, npass = 1
## segment 98: lambda = 1.415e-05, dev = 7.672e+04, npass = 3
## segment 99: lambda = 1.351e-05, dev = 7.67e+04, npass = 3
## segment 100: lambda = 1.289e-05, dev = 7.667e+04, npass = 3
plot(nhlreg)
```



Extracting Coefficients Let's grab the coefficients of each player

```
# AICc selection
Baicc <- coef(nhlreg)[colnames(player),]</pre>
```

First, a simple gut-check point: the intercept. This is the effect on odds that a goal is home rather than away, regardless of any info about what teams are playing or who is on ice. It's the home ice advantage!

We find that home-ice increases odds you've scored by 8%

```
100*(exp(coef(nhlreg)[1])-1)
```

```
## [1] 8.235434
```

Now, lets look at the player effects. The regression finds 646 significant player effects sum(Baicc!=0)

[1] 646

Here are the top 10 players

Baicc[order(Baicc, decreasing=TRUE)[1:10]]

```
SIDNEY_CROSBY
## PETER_FORSBERG
                   TYLER_TOFFOLI
                                    ONDREJ_PALAT ZIGMUND_PALFFY
##
        0.7548254
                        0.6292577
                                       0.6284040
                                                       0.4426997
                                                                       0.4131174
##
     JOE_THORNTON
                   PAVEL_DATSYUK
                                   LOGAN_COUTURE
                                                       ERIC_FEHR MARTIN_GELINAS
        0.3837632
                        0.3761981
                                       0.3682103
                                                       0.3677283
                                                                       0.3577613
```

Here are the bottom 10

Baicc[order(Baicc)[1:10]]

```
##
       TIM_TAYLOR
                    JOHN_MCCARTHY P. J._AXELSSON NICLAS_HAVELID
                                                                     THOMAS_POCK
##
                       -0.5651886
       -0.8643214
                                       -0.4283811
                                                      -0.3854583
                                                                      -0.3844128
##
    MATHIEU_BIRON
                    CHRIS_DINGMAN
                                    DARROLL_POWE RAITIS_IVANANS
                                                                    RYAN_HOLLWEG
##
       -0.3512101
                       -0.3342243
                                      -0.3339906
                                                      -0.3129481
                                                                      -0.2988769
```

Specifically, the model says, e.g., that whenever a goal is scored, Pittsburgh's odds of having scored (rather than scored on) increase by a 51% if Sidney Crosby is on the ice.

```
exp(Baicc["SIDNEY_CROSBY"])
## SIDNEY_CROSBY
## 1.511523
```

And the Blue Jackets (or Kings, pre 2011-12) odds of having scored drop by around 22% if Jack Johnson is on the ice

```
exp(Baicc["JACK_JOHNSON"])
## JACK_JOHNSON
## 0.7813488
```

hockey fans among you may feel free to comment in much more detail.

Standardizing vs Not Standardizing Data

Without standardize=FALSE, you'd be multiplying the penalty for each coefficient (player effect) by that player's standard deviation in onice. The players with big SD in onice are guys who play a lot. Players with small SD are those who play little (almost all zeros). So weighting penalty by SD in this case is exactly what you don't want: a bigger penalty for people with many minutes on ice, a smaller penalty for those who seldom play. Indeed, running the regression without standardize=FALSE leads to a bunch of farm teamers coming up tops.

```
JEFF_TOMS
                           RYAN_KRAFT
                                           COLE_JARRETT
                                                           TOMAS_POPPERLE
##
          1.7380706
                            1.4826419
                                              1.2119318
                                                                 1.1107806
                                           ERIC_SELLECK
##
     DAVID_LIFFITON ALEXEY_MARCHENKO
                                                              MIKE_MURPHY
##
          1.0974872
                            1.0297324
                                              1.0060015
                                                                 0.9600939
##
         DAVID GOVE
                           TOMAS KANA
          0.9264895
                            0.8792802
##
```

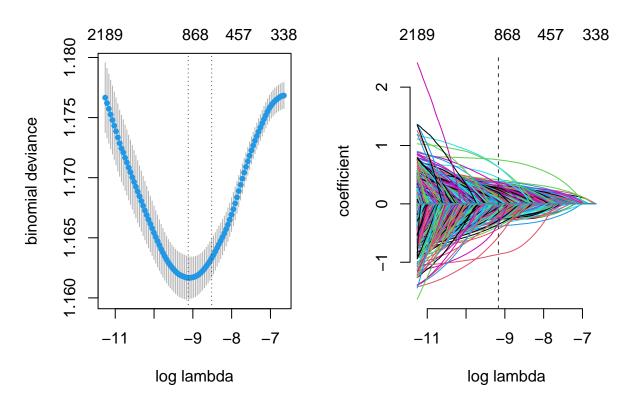
NOTE: this is an exceptional case! You almost always want standardize=TRUE.

Cross-Validation

```
cv.nhlreg <- cv.gamlr(x, y,
    free=1:(ncol(config)+ncol(team)),
    family="binomial", verb=TRUE, standardize=FALSE)

## fold 1,2,3,4,5,done.</pre>
```

```
par(mfrow=c(1,2))
plot(cv.nhlreg)
plot(cv.nhlreg$gamlr) ## cv.gamlr has included a gamlr object into cv.nhlreg
```



Plotting Results

Lambda Selection

```
log(nhlreg$lambda[which.min(AICc(nhlreg))])

## seg55
## -9.165555

log(nhlreg$lambda[which.min(AIC(nhlreg))])

## seg55
## -9.165555

log(nhlreg$lambda[which.min(BIC(nhlreg))])

## seg1
## -6.653644

log(cv.nhlreg$lambda.min)

## [1] -9.119038

log(cv.nhlreg$lambda.1se)

## [1] -8.514319
```

AIC and AICc give exactly the same answer here (n»df) and both are close to the cv.min answer.

```
Bcvmin <- coef(cv.nhlreg, select="min")[colnames(player),]
sum(Bcvmin!=0) # around 600</pre>
```

[1] 622

```
exp(sort(Bcvmin, decreasing=TRUE)[1:10]) # similar top 10
```

```
PETER_FORSBERG
                     ONDREJ_PALAT
                                   TYLER_TOFFOLI ZIGMUND_PALFFY
                                                                   SIDNEY_CROSBY
##
         2.119080
                         1.834845
                                         1.830916
                                                         1.531845
                                                                        1.506432
##
     JOE_THORNTON
                    PAVEL_DATSYUK
                                   LOGAN_COUTURE
                                                        ERIC_FEHR MARTIN_GELINAS
                         1.449265
##
         1.464191
                                         1.437288
                                                         1.435486
                                                                        1.421528
```

Both AIC and AICc are trying to approximate the OOS deviance (MSE here). Thus the lambdas at minimum AIC and AICc values are estimates of the lambda which minimizes OOS error – the same thing targeted with the cv.min rule. Also, in this case, the degrees of freedom are low enough relative to 'n' that AIC works fine, and gives an answer close to AICc.

The 1se rule accounts for uncertainty about OOS error, and thus chooses a simpler model.

```
Bcv1se <- coef(cv.nhlreg)[colnames(player),]</pre>
```

Even though log lambdas are close, df drops by 1/2

```
sum(Bcv1se!=0) # only around 300
```

[1] 341

Top 10 changes a bit as well

```
exp(sort(Bcv1se,decreasing=TRUE)[1:10]) # top 10 changes a bit
```

```
PETER_FORSBERG
##
                          SIDNEY_CROSBY
                                                                PAVEL_DATSYUK
                                              JOE_THORNTON
##
            1.973963
                               1.422968
                                                   1.403477
                                                                      1.354780
##
     ALEXANDER_SEMIN
                          LADISLAV_NAGY LUBOMIR_VISNOVSKY
                                                                  MATT_MOULSON
##
            1.351025
                               1.334468
                                                   1.334158
                                                                      1.323587
       LOGAN_COUTURE
##
                          ALEX_OVECHKIN
##
            1.315394
                               1.311600
```

BIC is way more (overly I think) conservative than all these options.

```
Bbic <- coef(nhlreg, select=which.min(BIC(nhlreg)))[colnames(player),]
sum(Bbic!=0) # zero! Nobody is different from average according to BIC
```

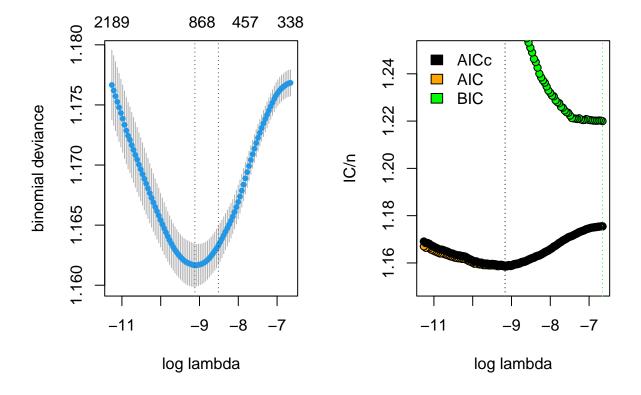
```
## [1] 0
```

The BIC is trying to find lambda with highest probability of having the minimum OOS error, which is subtly different than finding the lambda corresponding to lowest expected OOS error. For example, if there is more uncertainty about OOS error at the lambda with min expectation, then it could be that another value with higher expected error but lower uncertainty around this value will have a higher probability of being best. In this case, the BIC says there is much uncertainty at everything other than the null model, so that the null model ends up highest probability of being best.

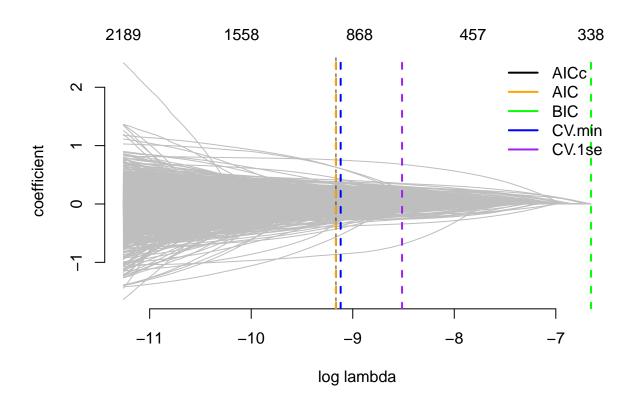
As an aside: note that the null model here is not just an intercept, but rather includes onice configuration info along with information about the team and season. So the BIC is not saying that no players matter, but rather that it cannot confidently tell them apart from their team's average level of play in a given season.

Comparing Model Selections

Finally, some plots to compare model selections



Plot all the answers along the path



Browsing History

The table has three columns: [machine] id, site [id], [# of] visits

Data Mangement

```
web <- read.csv("browser-domains.csv")</pre>
```

Read in the actual website names and relabel site factor

```
sitenames <- scan("browser-sites.txt", what="character")
web$site <- factor(web$site, levels=1:length(sitenames), labels=sitenames)</pre>
```

also factor machine id

```
web$id <- factor(web$id, levels=1:length(unique(web$id)))</pre>
```

Let's get total visits per-machine and % of time on each site tapply(a,b,c) does c(a) for every level of factor b.

```
machinetotals <- as.vector(tapply(web$visits,web$id,sum))
visitpercent <- 100*web$visits/machinetotals[web$id]</pre>
```

Since there are many sites that some people do not visit, our dataframe could blow out of proportion. We will first need to generate a sparse matrix.

```
xweb <- sparseMatrix(
   i=as.numeric(web$id), j=as.numeric(web$site), x=visitpercent,
   dims=c(nlevels(web$id),nlevels(web$site)),
   dimnames=list(id=levels(web$id), site=levels(web$site)))</pre>
```

We can extract values from the sparse matrix. Ex: What sites did household 1 visit?

xweb[1, xweb[1,]!=0]

##	atdmt.com	yahoo.com
##	4.05202601	11.85592796
##	msn.com	google.com
##	0.25012506	6.52826413
##	aol.com	questionmarket.com
##	0.15007504	1.35067534
##	googlesyndication.com-o02	casalemedia.com
##	3.40170085	0.82541271
##	mywebsearch.com	myspace.com
##	0.10005003	0.05002501
##	pointroll.com	yieldmanager.com
##	0.72536268	0.65032516
##	live.com	mediaplex.com
##	0.02501251	0.32516258
##	precisionclick.com	tribalfusion.com
##	0.15007504	0.52526263
##	insightexpressai.com	trafficmp.com
##	0.65032516	0.30015008
##	ebay.com	realmedia.com 0.52526263
##	1.97598799	
## ##	zedo.com 0.62531266	advertising.com 0.40020010
##	microsoft.com	hotbar.com
##	0.57528764	0.02501251
##	adrevolver.com	ru4.com
##	0.35017509	0.27513757
##	nextag.com	overture.com
##	1.67583792	0.07503752
##	starware.com	relevantknowledge.com
##	0.10005003	2.37618809
##	myway.com	partner2profit.com
##	1.12556278	2.92646323
##	ditto.com	kanoodle.com
##	0.07503752	0.20010005
##	ebayobjects.com	comcast.net
##	1.35067534	0.07503752
##	fastclick.net	adbrite.com
##	0.57528764	0.50025013
##	vpptechnologies.com	specificclick.net
##	0.05002501	0.32516258
##	serving-sys.com	weather.com
##	0.40020010	0.15007504
##	adserver.com	go.com
##	0.15007504	0.42521261
##	intellisrv.net	dell.com

##	0.20010005	4.77738869
##	cnn.com	burstnet.com
##	0.05002501	0.45022511
##	adknowledge.com	funwebproducts.com
##	0.27513757	0.15007504
##	belnk.com	netscape.com
##	0.02501251	0.05002501
##	real.com	liveperson.net
##	0.02501251	0.05002501
##	adsonar.com	euroclick.com
##	0.15007504	0.07503752
##	m7z.net	mywebface.com
##	0.20010005	0.02501251
##	tacoda.net	unicast.com
##	0.85042521	0.10005003
##	personalweb.com	earthlink.net
##	0.20010005	0.07503752
##	falkag.net	amazon.com
##	0.07503752	1.05052526
##	dellfix.com	ysbweb.com
##	3.90195098	0.02501251
##	googleadservices.com	
##	0.25012506	qnsr.com 2.17608804
##		
##	revenue.net	addynamix.com 0.12506253
	0.07503752	
## ##	cox.net	akamai.net
##	13.38169085	0.02501251
##	admarketplace.net	amazon.com-001
	0.37518759	0.40020010
##	opinionsquare.com 0.05002501	interclick.com
##		0.07503752
##	go.com-004	ask.com
##	0.02501251	0.60030015
##	contextweb.com	intellitxt.com
##	0.25012506	0.22511256
##	yceml.net	about.com
##	0.12506253	0.40020010
##	youtube.com	wikipedia.org
##	0.07503752	1.32566283
##	windowsmedia.com	foxsports.com
##	0.07503752	0.02501251
##	walmart.com	partypoker.com
##	0.07503752	0.05002501
##	${ t mymailstamp.com}$	windows.com
##	0.02501251	0.02501251
##	musicmatch.com	specificmedia.com
##	1.60080040	0.05002501
##	paypal.com	monster.com-o01
##	0.52526263	0.17508754
##	information.com	207.net
##	0.12506253	0.42521261
##	ebayrtm.com	match.com
##	0.15007504	0.02501251
##	screensavers.com	smileycentral.com
		-

##	0.05002501	1.30065033
##	careerbuilder.com	
		mlb.com
##	0.10005003	0.05002501
##	searchignite.com	thinktarget.com
##	0.30015008	0.12506253
##	dotomi.com	blogspot.com
##	0.02501251	0.25012506
##	chase.com	vonage.com
##	0.02501251	0.02501251
##	compuserve.com	lycos.com
##	0.07503752	0.15007504
##	azjmp.com	tmcs.net-o01
##	0.07503752	0.05002501
##	exitexchange.com	imdb.com
##	0.05002501	0.07503752
##	adecn.com	go.com-o03
##	0.10005003	0.07503752
##	excite.com	imiclk.com
##	0.02501251	0.02501251
##	bloglines.com	foxnews.com
##	0.55027514	0.02501251
##	marketwatch.com	monster.com
##	0.25012506	0.02501251
##	adobe.com	chitika.net
##	0.05002501	0.02501251
##	geocities.com	sharewareonline.com
##	0.10005003	0.07503752
##	llnwd.net	oingo.com
##	0.17508754	0.07503752
##	lightningcast.net	xolox.nl
##	0.02501251	0.12506253
##	aavalue.com	bluestreak.com
##	0.02501251	0.02501251
##	usps.com	bbc.co.uk
##	0.10005003	0.05002501
##	att.net	alumnigroup.org
##	0.02501251	0.10005003
##	verizonwireless.com	webshots.com
##	0.17508754	0.12506253
##	bestbuy.com	paypopup.com
##	0.05002501	0.02501251
##	cheaptickets.com	nytimes.com
##	0.02501251	0.02501251
##	cpmstar.com	ticketmaster.com
##	0.02501251	0.05002501
##		
##	tripod.com 0.10005003	buy.com 0.05002501
##		
	contextuads.com	hbmediapro.com
##	0.02501251	0.02501251
##	usatoday.com	adoutput.com
##	0.05002501	0.02501251
##	sbc.com	lowermybills.com
##	0.02501251	0.02501251
##	clicksor.com	legacy.com

##	0.02501251	0.02501251
##	hgtv.com	sprintpcs.com
##	0.25012506	0.02501251
##	webmd.com	clearchannel.com
##	0.02501251	0.05002501
##	tmcs.net	tx.us
##	0.05002501	0.05002501
##	sony.com	citysearch.com
##	0.02501251	0.02501251
##	connextra.com	adlegend.com
##	0.02501251	0.02501251
##	sears.com	fl.us
##	0.02501251	0.02501251
##	coolsavings.com	liquidmedianetworks.com
##	0.02501251	0.02501251
##	perfectmatch.com	stockgroup.com
##	0.25012506	0.02501251
##		kontera.com
##	consumerpromotioncenter.com 0.02501251	0.02501251
##	circuitcity.com	yimg.com
##	0.02501251	0.05002501
##	wunderground.com	ca.us
##	0.02501251	0.02501251
##	washingtonpost.com	adjuggler.com
##	0.07503752	0.12506253
##	scripps.com-o01	irs.gov
##	0.12506253	0.05002501
##	nih.gov	ign.com
##	0.15007504	0.02501251
##	proficient.com	checkm8.com
##	0.02501251	0.02501251
##	oasei.com	passion.com
##	0.02501251	0.02501251
##	trafficmarketplace.com	flickr.com
##	0.02501251	0.07503752
##	andale.com	entrepreneur.com
##	0.20010005	0.02501251
##	webmd.com-o01	bbeplayer.com
##	0.02501251	0.02501251
##	204.95.60.12	napster.com
##	0.02501251	0.42521261
##	msnbc.com	
##	0.02501251	linkexchange.com 0.02501251
##		angelfire.com
##	searchmarketing.com 0.05002501	0.05002501
##	spynet.com	macromedia.com
##	1.50075038	0.05002501
##		frontiernet.net
	ed.gov	
##	0.17508754	0.02501251
##	nc.us	ticketmaster.com-o01
##	0.05002501	0.02501251
##	flowgo.com	oddcast.com
##	0.12506253	0.05002501
##	answers.com	lowes.com

##	0.10005003	0.05002501
##	shop.com	orchardbank.com
##	0.02501251	0.02501251
##	google.com-o03	cbs.com
##	0.12506253	0.05002501
##	bannerspace.com	technorati.com
##	0.05002501	0.05002501
##	ebaumsworld.com	
		gamespot.com
##	0.05002501	0.07503752
##	bebo.com	subsag.com
##	0.07503752	0.05002501
##	local.com	gms1.net
##	0.02501251	0.02501251
##	gannettonline.com	superbrewards.com
##	0.07503752	0.02501251
##	ugo.com-o02	comcast.com
##	0.02501251	0.02501251
##	sun.com	gamespot.com-o01
##	0.05002501	0.05002501
##	youravon.com	yahoo.net
##	0.05002501	0.02501251
##	go.com-002	deepnetexplorer.co.uk
##	0.05002501	0.10005003
##	break.com	hallmark.com
##	0.20010005	0.02501251
##	pro-market.net	mate1.com
##	0.05002501	0.02501251
##	tickle.com	bluemountain.com
##	0.05002501	0.07503752
##	blogger.com	xmradio.com
##	0.05002501	0.02501251
##	ancestry.com	imixserver.com
##	0.02501251	0.10005003
##	pricegrabber.com	limewire.com
##	0.02501251	0.05002501
##	freelaptop4you.com	typepad.com
##	0.05002501	0.02501251
##	allrecipes.com	eversave.com
##	0.02501251	0.02501251
##	boston.com	ibanking-services.com
##	0.02501251	0.02501251
##	custhelp.com	mn.us
##	0.02501251	0.02501251
##	gamefaqs.com	premiumproductsonline.com
##	0.02501251	0.02501251
##	tv.com	65.115.67.11
##	0.02501251	0.02501251
##	snapfish.com	artistdirect.com
##	0.02501251	0.02501251
##	scottrade.com	rootv.com
##	0.02501251	0.02501251
		inklineglobal.com
##	webstat.com	INKIINEELODAI.COM
		_
## ## ##	webstat.com 0.02501251 seeq.com	0.02501251 sonypictures.com

```
##
                     0.07503752
                                                   0.02501251
##
                                            123greetings.com
                      slate.com
                     0.02501251
##
                                                   0.10005003
##
                     blinko.com
                                                     turn.com
##
                     0.02501251
                                                   0.02501251
             householdbank.com
##
                                                   active.com
                     0.02501251
                                                   0.02501251
##
##
                   michigan.gov
                                              dada-mobile.net
##
                     0.02501251
                                                   0.02501251
##
                   pennyweb.com
                                                      tmz.com
##
                     0.02501251
                                                   0.02501251
##
               blogrolling.com
                                                 samsclub.com
                     0.15007504
##
                                                   0.02501251
##
                                                  gamespy.com
                    toseeka.com
##
                     0.02501251
                                                   0.02501251
##
                  cafepress.com
                                                        ea.com
##
                                                   0.07503752
                     0.22511256
##
                  petfinder.com
                                       websourcedtraffic.com
##
                     0.02501251
                                                   0.05002501
##
           trafficexplorer.com
                                           freegiftworld.com
                     0.02501251
##
                                                   0.02501251
##
                     zap2it.com
                                               gadgetcity.com
##
                     0.02501251
                                                   0.02501251
##
                       army.mil
                                           yourgiftcards.com
                     0.02501251
##
                                                   0.02501251
##
                statcounter.com
                                                      ajc.com
##
                     0.02501251
                                                   0.02501251
##
             jacquielawson.com
                                                    atomz.com
##
                     0.05002501
                                                   0.05002501
##
                      topix.net
                                                mybloglog.com
##
                     0.07503752
                                                   0.02501251
##
                       away.com
                                                     grab.com
##
                     0.02501251
                                                   0.02501251
##
                                                 business.com
                        pbs.org
##
                     0.12506253
                                                   0.02501251
##
            myinsiderdeals.com
                                                 homegain.com
##
                     0.02501251
                                                   0.02501251
##
              findarticles.com
                                              cursormania.com
##
                     0.10005003
                                                   0.02501251
##
       thebreastcancersite.com
                                                      cox.com
##
                     0.05002501
                                                   0.02501251
```

Read in the spending data

```
yspend <- read.csv("browser-totalspend.csv", row.names=1) # use 1st column as row names
yspend <- as.matrix(yspend) ## good practice to move from dataframe to matrix</pre>
```

LASSO

```
spender <- gamlr(xweb, log(yspend), verb=TRUE)

## *** n=10000 observations and p=1000 covariates ***
## segment 1: lambda = 0.2325, dev = 2.783e+04, npass = 0
## segment 2: lambda = 0.2219, dev = 2.778e+04, npass = 3
## segment 3: lambda = 0.2118, dev = 2.774e+04, npass = 3</pre>
```

```
## segment 4: lambda = 0.2022, dev = 2.77e+04, npass = 3
## segment 5: lambda = 0.193, dev = 2.766e+04, npass = 3
## segment 6: lambda = 0.1842, dev = 2.76e+04, npass = 3
## segment 7: lambda = 0.1759, dev = 2.753e+04, npass = 4
## segment 8: lambda = 0.1679, dev = 2.744e+04, npass = 5
## segment 9: lambda = 0.1602, dev = 2.733e+04, npass = 5
## segment 10: lambda = 0.153, dev = 2.72e+04, npass = 5
## segment 11: lambda = 0.146, dev = 2.708e+04, npass = 5
## segment 12: lambda = 0.1394, dev = 2.697e+04, npass = 5
## segment 13: lambda = 0.133, dev = 2.687e+04, npass = 5
## segment 14: lambda = 0.127, dev = 2.676e+04, npass = 5
## segment 15: lambda = 0.1212, dev = 2.663e+04, npass = 5
## segment 16: lambda = 0.1157, dev = 2.65e+04, npass = 5
## segment 17: lambda = 0.1104, dev = 2.639e+04, npass = 5
## segment 18: lambda = 0.1054, dev = 2.628e+04, npass = 5
## segment 19: lambda = 0.1006, dev = 2.616e+04, npass = 5
## segment 20: lambda = 0.09606, dev = 2.605e+04, npass = 5
## segment 21: lambda = 0.09169, dev = 2.595e+04, npass = 5
## segment 22: lambda = 0.08753, dev = 2.584e+04, npass = 5
## segment 23: lambda = 0.08355, dev = 2.574e+04, npass = 4
## segment 24: lambda = 0.07975, dev = 2.564e+04, npass = 4
## segment 25: lambda = 0.07613, dev = 2.553e+04, npass = 4
## segment 26: lambda = 0.07267, dev = 2.543e+04, npass = 4
## segment 27: lambda = 0.06936, dev = 2.532e+04, npass = 4
## segment 28: lambda = 0.06621, dev = 2.522e+04, npass = 4
## segment 29: lambda = 0.0632, dev = 2.511e+04, npass = 4
## segment 30: lambda = 0.06033, dev = 2.501e+04, npass = 4
## segment 31: lambda = 0.05759, dev = 2.491e+04, npass = 4
## segment 32: lambda = 0.05497, dev = 2.481e+04, npass = 4
## segment 33: lambda = 0.05247, dev = 2.47e+04, npass = 4
## segment 34: lambda = 0.05009, dev = 2.46e+04, npass = 4
## segment 35: lambda = 0.04781, dev = 2.449e+04, npass = 5
## segment 36: lambda = 0.04564, dev = 2.438e+04, npass = 5
## segment 37: lambda = 0.04356, dev = 2.427e+04, npass = 6
## segment 38: lambda = 0.04158, dev = 2.416e+04, npass = 6
## segment 39: lambda = 0.03969, dev = 2.405e+04, npass = 6
## segment 40: lambda = 0.03789, dev = 2.395e+04, npass = 6
## segment 41: lambda = 0.03617, dev = 2.384e+04, npass = 6
## segment 42: lambda = 0.03452, dev = 2.374e+04, npass = 6
## segment 43: lambda = 0.03295, dev = 2.365e+04, npass = 6
## segment 44: lambda = 0.03146, dev = 2.355e+04, npass = 5
## segment 45: lambda = 0.03003, dev = 2.346e+04, npass = 5
## segment 46: lambda = 0.02866, dev = 2.337e+04, npass = 5
## segment 47: lambda = 0.02736, dev = 2.328e+04, npass = 5
## segment 48: lambda = 0.02611, dev = 2.319e+04, npass = 5
## segment 49: lambda = 0.02493, dev = 2.311e+04, npass = 5
## segment 50: lambda = 0.02379, dev = 2.302e+04, npass = 5
## segment 51: lambda = 0.02271, dev = 2.293e+04, npass = 5
## segment 52: lambda = 0.02168, dev = 2.285e+04, npass = 5
## segment 53: lambda = 0.0207, dev = 2.277e+04, npass = 5
## segment 54: lambda = 0.01975, dev = 2.269e+04, npass = 5
## segment 55: lambda = 0.01886, dev = 2.261e+04, npass = 4
## segment 56: lambda = 0.018, dev = 2.253e+04, npass = 4
## segment 57: lambda = 0.01718, dev = 2.245e+04, npass = 4
```

```
## segment 58: lambda = 0.0164, dev = 2.238e+04, npass = 4
## segment 59: lambda = 0.01566, dev = 2.23e+04, npass = 4
## segment 60: lambda = 0.01494, dev = 2.223e+04, npass = 4
## segment 61: lambda = 0.01426, dev = 2.216e+04, npass = 5
## segment 62: lambda = 0.01362, dev = 2.209e+04, npass = 4
## segment 63: lambda = 0.013, dev = 2.203e+04, npass = 4
## segment 64: lambda = 0.01241, dev = 2.197e+04, npass = 4
## segment 65: lambda = 0.01184, dev = 2.191e+04, npass = 4
## segment 66: lambda = 0.0113, dev = 2.186e+04, npass = 4
## segment 67: lambda = 0.01079, dev = 2.18e+04, npass = 4
## segment 68: lambda = 0.0103, dev = 2.175e+04, npass = 6
## segment 69: lambda = 0.009832, dev = 2.17e+04, npass = 4
## segment 70: lambda = 0.009385, dev = 2.165e+04, npass = 6
## segment 71: lambda = 0.008959, dev = 2.16e+04, npass = 7
## segment 72: lambda = 0.008551, dev = 2.155e+04, npass = 7
## segment 73: lambda = 0.008163, dev = 2.151e+04, npass = 6
## segment 74: lambda = 0.007792, dev = 2.147e+04, npass = 6
## segment 75: lambda = 0.007438, dev = 2.143e+04, npass = 6
## segment 76: lambda = 0.007099, dev = 2.139e+04, npass = 6
## segment 77: lambda = 0.006777, dev = 2.136e+04, npass = 6
## segment 78: lambda = 0.006469, dev = 2.132e+04, npass = 6
## segment 79: lambda = 0.006175, dev = 2.129e+04, npass = 7
## segment 80: lambda = 0.005894, dev = 2.126e+04, npass = 7
## segment 81: lambda = 0.005626, dev = 2.122e+04, npass = 10
## segment 82: lambda = 0.00537, dev = 2.119e+04, npass = 10
## segment 83: lambda = 0.005126, dev = 2.117e+04, npass = 9
## segment 84: lambda = 0.004893, dev = 2.114e+04, npass = 9
## segment 85: lambda = 0.004671, dev = 2.112e+04, npass = 9
## segment 86: lambda = 0.004459, dev = 2.109e+04, npass = 8
## segment 87: lambda = 0.004256, dev = 2.107e+04, npass = 8
## segment 88: lambda = 0.004063, dev = 2.105e+04, npass = 8
## segment 89: lambda = 0.003878, dev = 2.103e+04, npass = 7
## segment 90: lambda = 0.003702, dev = 2.102e+04, npass = 7
## segment 91: lambda = 0.003533, dev = 2.1e+04, npass = 7
## segment 92: lambda = 0.003373, dev = 2.098e+04, npass = 7
## segment 93: lambda = 0.00322, dev = 2.097e+04, npass = 6
## segment 94: lambda = 0.003073, dev = 2.095e+04, npass = 6
## segment 95: lambda = 0.002934, dev = 2.094e+04, npass = 6
## segment 96: lambda = 0.0028, dev = 2.093e+04, npass = 6
## segment 97: lambda = 0.002673, dev = 2.091e+04, npass = 6
## segment 98: lambda = 0.002551, dev = 2.09e+04, npass = 5
## segment 99: lambda = 0.002435, dev = 2.089e+04, npass = 5
## segment 100: lambda = 0.002325, dev = 2.088e+04, npass = 5
summary(spender)
##
## gaussian gamlr with 1000 inputs and 100 segments.
               lambda par df
                                       r2
                                               aicc
          0.232476092
                            1 0.000000000 10236.678
## seg1
                       1
## seg2
          0.221909695
                        2
                            2 0.001725303 10221.411
## seg3
          0.211823557
                        2
                            2 0.003297334 10205.651
                        2
## seg4
          0.202195849
                            2 0.004729710 10191.270
```

2 0.006034838 10178.148

seg5

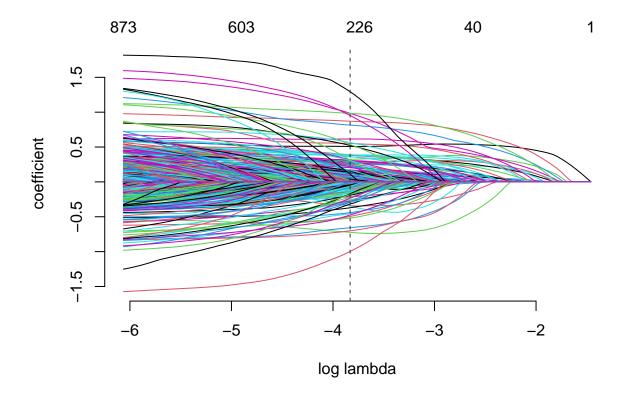
0.193005736

2

```
## seg6
          0.184233327
                         3
                             3 0.008059419 10159.760
## seg7
          0.175859638
                         5
                             5 0.010759747 10136.503
## seg8
          0.167866546
                             7 0.013978241 10107.920
                            10 0.018051482 10072.536
## seg9
          0.160236753
                        10
## seg10
          0.152953745
                        11
                            11 0.022568088 10028.438
## seg11
          0.146001761
                        12
                            12 0.026834473
                                            9986.698
## seg12
          0.139365756
                        12
                            12 0.030824198
                                             9945.617
## seg13
          0.133031367
                        13
                            13 0.034577333
                                            9908.822
## seg14
          0.126984886
                        16
                            16 0.038557614
                                            9873.526
## seg15
          0.121213227
                        18
                            18 0.043190423
                                            9829.238
## seg16
          0.115703899
                        18
                            18 0.047623601
                                             9782.797
## seg17
          0.110444978
                        18
                            18 0.051662879
                                            9740.294
## seg18
          0.105425083
                        21
                            21 0.055664541
                                            9704.032
          0.100633351
## seg19
                            22 0.059819719
                                             9661.943
                        24
                                             9624.181
## seg20
          0.096059410
                            24 0.063739653
## seg21
          0.091693361
                        25
                            25 0.067595723
                                             9584.920
                        28
## seg22
          0.087525756
                            28 0.071296509
                                             9551.183
## seg23
          0.083547576
                            31 0.074986542
                                             9517.407
                                            9477.520
## seg24
          0.079750209
                        31
                            31 0.078668776
## seg25
          0.076125439
                        37
                            37 0.082487125
                                             9448.073
## seg26
          0.072665421
                        40
                            40 0.086306440
                                            9412.407
                                             9375.524
## seg27
          0.069362665
                            42 0.090037319
## seg28
          0.066210025
                        49
                            49 0.093679230
                                             9349.550
## seg29
          0.063200677
                        54
                            54 0.097580298
                                            9316.519
## seg30
          0.060328109
                        54
                            54 0.101267227
                                            9275.580
## seg31
          0.057586103
                       58
                            58 0.104923128
                                             9242.910
                                            9212.700
## seg32
          0.054968726
                       63
                            63 0.108525962
## seg33
          0.052470312
                        68
                            68 0.112302698
                                            9180.378
                       79
## seg34
          0.050085456
                            79 0.116044277
                                             9160.469
## seg35
          0.047808994
                        87
                            87 0.119877269
                                             9133.283
## seg36
          0.045636002
                       92
                            92 0.123789610
                                             9098.915
## seg37
          0.043561775 101 101 0.127898571
                                             9070.264
## seg38
          0.041581825 108 108 0.131909537
                                             9038.465
## seg39
          0.039691867 115 115 0.135762390
                                             9008.302
          0.037887811 122 122 0.139472471
                                             8979.620
## seg40
## seg41
          0.036165751 130 130 0.143148598
                                            8953.221
## seg42
          0.034521962 143 143 0.146752614
                                             8937.799
          0.032952885 150 150 0.150323859
                                             8910.277
## seg43
          0.031455126 155 155 0.153730158
                                             8880.420
## seg44
## seg45
          0.030025442 165 165 0.157075185
                                             8861.473
## seg46
          0.028660739 176 176 0.160363792
                                             8845.155
          0.027358064 186 186 0.163519645
                                            8828.244
## seg47
## seg48
          0.026114598 196 196 0.166631375
                                             8811.763
## seg49
          0.024927649 208 208 0.169708540
                                            8799.773
## seg50
          0.023794649 226 226 0.172763466
                                             8800.530
          0.022713146 238 238 0.175884937
                                             8787.882
## seg51
## seg52
          0.021680798 249 249 0.178885990
                                             8774.514
## seg53
          0.020695372 270 270 0.181813234
                                             8783.073
## seg54
          0.019754736 286 286 0.184724207
                                             8781.291
## seg55
          0.018856853 303 303 0.187588758
                                            8782.192
## seg56
          0.017999780 319 319 0.190425860
                                            8781.300
## seg57
          0.017181662 336 336 0.193222530
                                            8783.040
## seg58
         0.016400729 353 353 0.195936722
                                            8785.814
## seg59 0.015655290 367 367 0.198593764
                                            8782.848
```

```
## seg60
         0.014943733 387 387 0.201160348
                                           8793.971
         0.014264517 402 402 0.203659807
## seg61
                                           8795.152
         0.013616173 412 412 0.206047391
                                           8786.860
         0.012997297 431 431 0.208312775
## seg63
                                           8799.709
         0.012406550 444 444 0.210482821
## seg64
                                           8800.697
## seg65
         0.011842653 463 463 0.212587024
                                           8815.711
## seg66
         0.011304386 478 478 0.214637570
                                           8822.674
## seg67
         0.010790584 492 492 0.216619355
                                           8828.339
## seg68
         0.010300136 505 505 0.218518166
                                           8832.874
## seg69
         0.009831979 513 513 0.220339652
                                           8827.303
## seg70
         0.009385100 531 531 0.222145966
                                           8844.187
## seg71
         0.008958533 545 545 0.223896744
                                           8852.932
## seg72
         0.008551354 559 559 0.225538511
                                           8863.126
## seg73
         0.008162681 571 571 0.227089202
                                           8870.047
         0.007791675 586 586 0.228546255
## seg74
                                           8884.979
## seg75
          0.007437531 603 603 0.229936408
                                           8905.381
## seg76
         0.007099484 618 618 0.231283973
                                           8921.898
## seg77
          0.006776801 638 638 0.232580144
                                           8950.568
## seg78
         0.006468785 646 646 0.233810612
                                           8952.794
## seg79
         0.006174769 662 662 0.235015469
                                           8973.696
## seg80
         0.005894116 675 675 0.236187355
                                           8988.227
         0.005626220 689 689 0.237333116
                                           9005.467
## seg81
## seg82
         0.005370499 703 703 0.238393719
                                           9023.901
## seg83
         0.005126402 714 714 0.239395276
                                           9036.228
## seg84
         0.004893399 721 721 0.240338414
                                           9040.070
## seg85
         0.004670986 730 730 0.241208491
                                           9049.538
## seg86
         0.004458683 738 738 0.242015972
                                           9057.529
## seg87
         0.004256029 747 747 0.242766854
                                           9068.623
## seg88
         0.004062586 760 760 0.243477983
                                           9089.641
## seg89
         0.003877935 773 773 0.244149588
                                           9111.259
## seg90
         0.003701677 786 786 0.244792248
                                           9133.338
## seg91
         0.003533430 800 800 0.245411685
                                           9158.168
## seg92
         0.003372830 809 809 0.245997670
                                           9171.689
## seg93
         0.003219530 820 820 0.246538742
                                           9190.588
## seg94
         0.003073197 827 827 0.247066267
                                           9200.212
## seg95
         0.002933516 830 830 0.247559945
                                           9200.787
## seg96 0.002800183 841 841 0.248026092
                                           9220.787
## seg97
         0.002672910 849 849 0.248465108
                                           9234.039
## seg98 0.002551422 855 855 0.248856592
                                           9243.170
## seg99 0.002435456 867 867 0.249232707
                                           9266.900
## seg100 0.002324761 873 873 0.249589392
                                           9276.545
```

plot(spender) ## path plot



Extracting and observing coefficients

DO NOT GO TO THESE LINKS

```
B <- coef(spender) ## the coefficients selected under AICc

B <- B[-1,] # drop intercept and remove STM formatting
B[which.min(B)] ## low spenders spend a lot of time here

## cursormania.com
## -0.998143

B[which.max(B)] ## big spenders hang out here

## shopyourbargain.com
## 1.294246

coef(spender, select=which.min(BIC(spender))) ## and BIC instead
```

Extracting Coefficients Using Other Rules

```
## weatherbug.com
## msn.com
## google.com
## aol.com
## questionmarket.com 0.013756425
## googlesyndication.com-o02 .
## casalemedia.com
## mywebsearch.com
## myspace.com
## pointroll.com
## atwola.com
## yieldmanager.com
## live.com
## aim.com
## mediaplex.com
## precisionclick.com
## tribalfusion.com
## insightexpressai.com
## trafficmp.com
                             .
-0.003495242
## ebay.com
## realmedia.com
## zedo.com
## advertising.com
## microsoft.com
## hotbar.com
## adrevolver.com
## ru4.com
## 180solutions.com
## nextag.com
## accuweather.com
## overture.com
## hotmail.com
## passport.com
## my-etrust.com
## starware.com
## relevantknowledge.com -0.034187615
## myway.com
## partner2profit.com
## ditto.com
## kanoodle.com
## ebayobjects.com
## mcafee.com
                            0.007369149
## comcast.net
## fastclick.net
## adbrite.com
## vpptechnologies.com
## specificclick.net
## serving-sys.com
## weather.com
## adserver.com
## licenseacquisition.org
## pogo.com
## go.com
## btgrab.com
```

```
## bellsouth.net
## intellisrv.net
## dell.com
## waol.exe
## cnn.com
## facebook.com
## incredibarvuz1.com
## burstnet.com
## adknowledge.com
## funwebproducts.com
## belnk.com
## netscape.com
## mysearch.com
## real.com
## liveperson.net
                            0.077066698
## adsonar.com
## passport.net
## euroclick.com
## m7z.net
## mywebface.com
## kazaa.com
## bestoffersnetworks.com
## vitalstream.com
## tacoda.net
## unicast.com
## offeroptimizer.com
## bankofamerica.com
## acsd.exe
## gator.com
## quickbrowsersearch.com
## revsci.net
## personalweb.com
## rr.com
## msnusers.com
## zango.com
## earthlink.net
## mapquest.com
## falkag.net
## freeze.com
                             0.054639845
## amazon.com
## net-offers.net
## shopperreports.com
## dellfix.com
## plaxo.com
## ysbweb.com
## googleadservices.com
## qnsr.com
## revenue.net
## adultfriendfinder.com
## addynamix.com
## seekmo.com
## verizon.net
## cox.net
## metricsdirect.com
```

```
## akamai.net
## admarketplace.net
## amazon.com-o01
## aolacsd.exe
## opinionsquare.com
## interclick.com
## peoplepc.com
## go.com-o04
## realtechnetwork.net
## freezecoldcash.com
## ask.com
## contextweb.com
## intellitxt.com
## yceml.net
## about.com
## youtube.com
## wikipedia.org
## surfaccuracy.com
                             .
-0.015026396
## windowsmedia.com
## craigslist.org
## hackerwatch.org
## foxsports.com
## spamblockerutility.com
## walmart.com
## navexcel.com
## partypoker.com
## wellsfargo.com
## travelzoo.com
## photobucket.com
## viewpoint.com
## nielsennetpanel.com
## mymailstamp.com
## windows.com
## optonline.net
## eguard.com
## aolcdn.com
## musicmatch.com
## qksz.net
## cometsystems.com
## netzero.net
## specificmedia.com
## paypal.com
## iwon.com
## monster.com-o01
## vmn.net
## juno.com
## information.com
## sysupdates.com
## 2o7.net
## adwave.com
## need2find.com
## target.com
                                   0.092833283
## ebayrtm.com
## match.com
```

```
## bridgetrack.com
## comcastsupport.com
## rs6.net
## screensavers.com
## footprint.net
## sportsline.com
## adelphia.net
## smileycentral.com
## dlqm.net
## careerbuilder.com
## mlb.com
## searchignite.com
## wachovia.com
## expedia.com
## thinktarget.com
## authnow.com
## dotomi.com
## blogspot.com
## hpdjjs.com
## chase.com
## outerinfo.com
## nscpcdn.com
## vonage.com
## searchscout.com
                             -0.004372746
## compuserve.com
## lycos.com
## xanga.com
## websearch.com
## azjmp.com
## tmcs.net-o01
## exitexchange.com
## toshibapc.com
## runescape.com
## weatherstudio.com
## imdb.com
## adecn.com
## bargain-buddy.net
## carsdirect.com
## mspaceads.com
## apple.com
## ups.com
                                 0.094620100
## 88.80.5.21
## exct.net
## cingular.com
## foodnetwork.com
## go.com-o03
## excite.com
## capitalone.com
                                   0.542497908
## imiclk.com
## overstock.com
## bloglines.com
## compfused.com
## morpheus.com
## foxnews.com
```

```
## marketwatch.com
## wamu.com
## monster.com
## adobe.com
## 888.com
## untd.com
## abetterinternet.com
## centralmedia.ws
## valuead.com
## targetsaver.com
## lynxtrack.com
## cartoonnetwork.com
## netflix.com
## chitika.net
## geocities.com
## qsrch.com
## drsnsrch.com
## autobytel.com
## web-nexus.net
## webservicehosts.com
## sharewareonline.com
## llnwd.net
## instantnavigation.com
## nick.com
## nfl.com
## oingo.com
## lightningcast.net
## altbill.com
## xolox.nl
## superpages.com
## classmates.com
## aavalue.com
## bluestreak.com
                                 0.019405476
## southwest.com
## whitepages.com
## usps.com
## webhancer.com
## bbc.co.uk
## true.com
## bearshare.com
## citibank.com
## blackplanet.com
## pch.com
## att.net
## autoweb.com
## insightexpress.com
## charter.net
## alumnigroup.org
## verizonwireless.com
## fedex.com
## mobilesidewalk.com
## netteller.com
## webshots.com
## sprint.com
```

```
## orbitz.com
                                   0.033293451
## bestbuy.com
## grandstreetinteractive.com
## paypopup.com
## cheaptickets.com
## dell4me.com
## new.net
                                  -0.050232563
## nytimes.com
## nyadmcncserve-05y06a.com
## aoltpspd.exe
## toprebates.com
## jcpenney.com
                                 0.289035701
## geotrust.com
                                0.241033879
## travelocity.com
## qvc.com
                                  0.116683951
## 4at1.com
## cpmstar.com
## bizrate.com
## ticketmaster.com
## usbank.com
## tripod.com
## buy.com
## nascar.com
## aebn.net
## infospace.com
## wxbug.com
## contextuads.com
## bns1.net
## download.com
## gocyberlink.com
## 192.168.1.1
## dvlabs.com
## defamer.com
                             -0.217028216
## tracking101.com
## accountonline.com
## hbmediapro.com
## usatoday.com
## bigfishgames.com
## neopets.com
## adoutput.com
## sbc.com
## noaa.gov
## lowermybills.com
## kmpads.com
## directtrack.com
## clicksor.com
## legacy.com
## eajmp.com
## nastydollars.com
## worldofwarcraft.com
## mirarsearch.com
## verizon.com
## miniclip.com
## iwin.com
```

```
## peel.com
## hgtv.com
## amaena.com
## sprintpcs.com
## shopping.com
## webmd.com
## clearchannel.com
## winamp.com
## reference.com
## interpolls.com
## americangreetings.com
                              0.427568831
## tmcs.net
## midtenmedia.com
## domainsponsor.com
## thunderdownloads.com
## akamaistream.net
## livejournal.com
## tx.us
## onlinerewardcenter.com
## msn.com-o18
## sony.com
## dogpile.com
## nba.com
                       0.148218793
## citysearch.com
## connextra.com
## nickjr.com
## t-mobile.com
## winfixer.com
## adlegend.com
## adsrevenue.net
## sears.com
## ap.org
                                  0.015598852
## luna.net
## shockwave.com
## hsn.com
## fl.us
## mypoints.com
## mozilla.org
## aresgalaxy.org
                                  0.026481191
## realtor.com
## addictinggames.com
## clickbooth.com
## amateurmatch.com
## worldnow.com
## surveys.com
## pa.us
## arcaderockstar.com
## coolsavings.com
                                 -0.591097345
## yournewsletters.net
## liquidmedianetworks.com
## everythinggirl.com
## perfectmatch.com
## stockgroup.com
## netster.com
```

```
## bidclix.com
## dropspam.com
## hp.com
## drivecleaner.com
## consumerpromotioncenter.com
## aolwbspd.exe
## americanexpress.com 0.019242435
## totaltalk.com
## wwe.com
## kontera.com
## gamehouse.com
## circuitcity.com
## yimg.com
## lightningcast.com
## edgefcs.net
## wunderground.com
## realarcade.com
## singlesnet.com
## azcentral.com
## yellowpages.com
## eharmony.com
## paviliondownload.com
## insightbb.com
## imageshack.us
## shopzilla.com
## ca.gov
## donotchangeme.com
## ca.us
## sourceforge.net
## washingtonpost.com
## adjuggler.com
## careercast.com
## bangbros1.com
## scripps.com-o01
## migente.com
## homedepot.com
## winantivirus.com
## irs.gov
## blockbuster.com
## kodakgallery.com
## nih.gov
## aol.com-o07
## icq.com
## wordcents.com
## drudgereport.com
## quizilla.com
## srch-results.com
## inqwire.com
## ign.com
## oinadserver.com
## azoogleads.com
## incredimail.com
## shopathome.com
## mtv.com
```

```
## fidelity.com
## bullseye-network.com
## flash-gear.com
## proficient.com
## autotrader.com
## charter.com
## healthology.com
## evite.com
                             -0.024862981
## checkm8.com
## rsc01.net
                                 0.018608014
## oasei.com
## heavy.com
## slotch.com
## passion.com
## nbc.com
## trafficmarketplace.com
## univision.com
## priceline.com
## flickr.com
## andale.com
## dealtime.com
## yfdirect.com
## entrepreneur.com
## go.com-o01
## webmd.com-o01
## sexsearch.com
## pornaccess.com
## gcion.com
## shoplocal.com
## kliptracker.com
## nationalcity.com
## bbeplayer.com
## videodome.com
## 204.95.60.12
## napster.com
## myweather.net
## msnbc.com
## linkexchange.com
## searchmarketing.com
## angelfire.com
## callwave.com
## sonnerie.net
## scout.com
## rivals.com
## altnet.com
## spynet.com
                                  -0.021666664
## macromedia.com
## ed.gov
## wannawatch.com
## frontiernet.net
## flycell.com
                                 0.103259214
## edgesuite.net
## 89.com
## nc.us
```

```
## ticketmaster.com-o01
## flowgo.com
## cnet.com
## oddcast.com
## answers.com
## timeinc.net
## m5-systems.com
## guideforyou.com
## rn11.com
## lowes.com
## lifescript.com
## shop.com
## errorsafe.com
## cams.com
## macys.com
                                  0.305866313
## aa.com
## addictingclips.com
                            0.760703451
## victoriassecret.com
## orchardbank.com
## bravenet.com
## imesh.com
## nextel.com
## screensandthemes.com
## suntrust.com
## discovercard.com
## nbads.com
## consumerincentiverewards.com
## valueclick.com
## google.com-o03
## cbs.com
## bannerspace.com
## technorati.com
## cjt1.net
## exactsearch.net
## munky.com
                                 -0.011421111
## cs.com
## kohls.com
## tagged.com
## babycenter.com
## ebaumsworld.com
## userplane.com
## mediaplazza.com
## netzerovoice.com
## gamespot.com
## keen.com
## bebo.com
## rsc02.net
                                  0.171100930
## sysupdates2.com
## imlive.com
## oldnavy.com
## regalinteractive.com
## weightwatchers.com
## subsag.com
## aol.com-o08
```

```
## azlyrics.com
## freeringtonesnow.com
## freewebs.com
## toysrus.com
## hollywood.com
## findwhat.com
## local.com
## webroot.com
## tvguide.com
## ny.us
## resultsmaster.com
## jamster.com
## gms1.net
## switchboard.com
## nicheseek.com
## intelius.com
## hi5.com
## glispa.com
## gannettonline.com
## cstv.com
## adengage.com
## superbrewards.com
## videocodezone.com
## symantecliveupdate.com
## pbskids.org
## revresda.com
## americansingles.com
## ugo.com-o02
## job.com
## installshield.com
## eprize.net
## metacafe.com
## focalex.com
## cciads.us
## perfectgonzo.com
## kbb.com
## reunion.com
## eproof.com
## tripadvisor.com
## bellsouth.com
## search.com
## comcast.com
## ivillage.com
## sun.com
## regionsnet.com
## mininova.org
## beliefnet.com
## intellicast.com
## fastonlineusers.com
## gamespot.com-o01
                              0.379543304
## expedia.com-o01
## military.com
## musicnet.com
## 53.com
```

```
## oh.us
## itrack.it
                                  0.274625984
## officedepot.com
## adultadworld.com
## univision.com-o01
## youravon.com
## blackboard.com
                                  0.228710425
## yahoo.net
## casinolasvegas.com
## warnerbros.com
## delta.com
                                  0.036077437
## go.com-o02
## deepnetexplorer.co.uk
## mozilla.com
## opentracker.net
## break.com
## catcha10.com
## hotels.com
## hallmark.com
## sportsbook.com
## mycheckfree.com
## ezboard.com
## pro-market.net
## mate1.com
## awempire.com
## jigzone.com
## bangbrosnetwork.com
## marketlinx.com
                                 -0.319689884
## tickle.com
## bbandt.com
## mercuras.com
## adtology2.com
## bluemountain.com
## freepornofreeporn.com
## internet-optimizer.com
## autotrader.com-o01
## blogger.com
## kraftfoods.com
## loveaccess.com
                            0.035946832
## shutterfly.com
## stopzilla.com
## xmradio.com
## ga.us
## ancestry.com
## honda.com
## fulltiltpoker.com
## il.us
## ibsys.com
## imixserver.com
## barnesandnoble.com
## pricegrabber.com
## constantcontact.com
## zonelabs.com
## pimpyourpro.com
```

```
## netflame.cc
## slide.com
## xnxx.com
## upromise.com
## livesexbar.com
## videosz.com
## freeweblayouts.net
                                 -0.321858177
## limewire.com
## ameritrade.com
## freelaptop4you.com
## nickarcade.com
## utkn.com
## nj.us
## 360i.com
## finestresults.com
## asseenontvnetwork.com
## typepad.com
                           0.154058729
## efax.com
## regions.com
## emachines.com
## playaudiomessage.com
## bofunk.com
## millsberry.com
## cpvfeed.com
## allrecipes.com
## clubpenguin.com
## eversave.com
## ppmdating.com
## lexico.com
## usaa.com
## directv.com
## postini.com
## secure-banking.com
## eyewonder.com
## boston.com
## ibanking-services.com
## astrology.com
## datinggold.com
## mlxchange.com
                        .
0.611641785
## travelhook.net
## custhelp.com
## mn.us
## zwire.com
## emarketmakers.com
## gamefaqs.com
## premiumproductsonline.com
## chrysler.com
## prodigy.net
## tv.com
## windowsmedia.com-o04
## smashits.com
## 65.115.67.11
## snapfish.com
## commerceonlinebanking.com
```

```
## bbt.com
## linksynergy.com
## yahoo.com-o08
## freecodesource.com
## streamate.com
## freecreditreport.com -0.026140494
## intuit.com
## rapid-pass.net
## artistdirect.com
## servedbyadbutler.com
## sidestep.com
## adult.com
## alltel.net
## bcentral.com
## openbank.com
## nichedsites.com
## cars.com
## gm.com
## adshuffle.com
## freeslots.com
## blink.com
## candystand.com
## pncbank.com
## discovery.com
## hsbcbillpay.com
## movietickets.com
## page-not-found.net
## fandango.com
## providianservices.com
## carad.com
## homestead.com
## realcastmedia.com
## webratsmusic.com
## scottrade.com
## cs102175.com
## fnismls.com
## shopperssavingcenter.com -0.153796903
## hit-now.com
## whatismyip.com
## costco.com
## bolt.com
## bmgmusic.com
## myhealthwealthandhappiness.com .
## symantec.com
## forbes.com
## digitalcity.com
## live365.com
## firstadsolution.com
## linkconnector.com
## freepagegraphics.com
## imgfarm.com
## insightexpresserdd.com
```

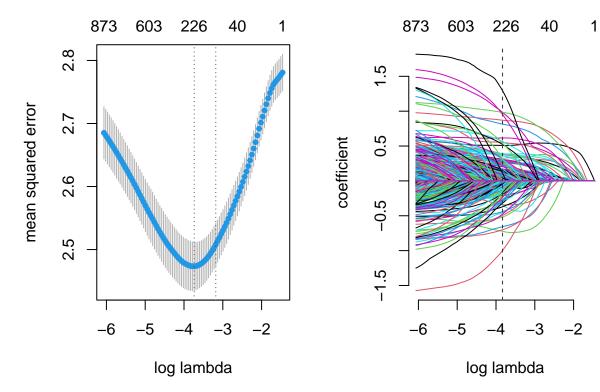
```
## pcsecurityshield.com
## allposters.com-o01
## msnvideo.com
## miva.com
## jackpotmadness.com
## mbnanetaccess.com
## newcarinsider.com
## edmunds.com
## net-nucleus.com
## popcap.com
## alt.com
                              0.769446720
## staples.com
## ussearch.com
## bankone.com
## rootv.com
## citizensbankonline.com
## juggcrew.com
## navyfcu.org
                                0.330762740
## nordstrom.com
## webstat.com
## inklineglobal.com
## seeq.com
## onetruemedia.com
## paltalk.com
## sonypictures.com
## 204.181.57.155
## commerceonline.com
## friendster.com
## slate.com
## hermoment.com
## lovehappens.com
## mi.us
## kmart.com
## paidsurveys.com
## 123greetings.com
## blinko.com
## citizensbank.com
## sirius.com
## qrs1.net
## adbureau.net
## turn.com
## abcdistributing.com
## fundsxpress.com
## pichunter.com
## cbsnews.com
## 216.139.222.230
## anywho.com
## sedoparking.com
## householdbank.com
## treborwear.com
## evault.ws
## vh1.com
## financialcontent.com
                                  0.053801713
## gap.com
```

```
## active.com
## exclusivegiftcards.com
## michigan.gov
## dada-mobile.net
## textplussolutions.com
## myriadmarket.com
## ifriends.net
## aptimus.com
## valueclick.net
## pennyweb.com
## blackpeoplemeet.com
## eltpath.com
## yahoo.com-o46
## sysprotect.com
## dadamobile.com
## cpxinteractive.com
## clickspring.net
## staples-deals.com
## myyearbook.com
## bravenetmedianetwork.com
## etrade.com
## marykayintouch.com
## 64.39.16.166
## moregamers.com
## redorbit.com
## tmz.com
## blogrolling.com
## checkfree.com
## samsclub.com
## va.us
                                   0.514951014
## united.com
## certified-safe-downloads.com
## aimtoday.com
## toseeka.com
## bidz.com
## gamespy.com
## nylottery.org
## godaddy.com
## rsc03.net
## altavista.com
## ltdcommodities.com
## bhg.com
## opm.gov
## onlinemediaoutlet.com
## beboframe.com
## cafepress.com
## tarot.com
## webgavel.com
## rapmls.com
## ztod.com
                            0.256454941
## marriott.com
## walgreens.com
## rovion.com
## ultimatebet.com
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## ea.com
## petfinder.com
## winsoftware.com
## literotica.com
## websourcedtraffic.com
## 032439.com
## marketbanker.com
## clearchannelmusic.com
## colonize.com
## searchfeed.com
## eimg.net
## shermanstravel.com
## key.com
## multi-pops.com
## yandex.ru
## us.com
## kinghost.com
## sublimedirectory.com
## gogotools.com
## camcrush.com
## trafficexplorer.com
## myfamily.com
## gay.com
## freegiftworld.com
## dexonline.com
## trade-in-value.com
## shopyourbargain.com
## dyndns.org
                           0.453258899
## bizrate.com-o01
## xctrk.com
## webtoolcafe.com
                             0.187201727
## zappos.com
## wi.us
## toptvbytes.com
## 157.22.32.111
## hotfreelayouts.com
## registrydefender.com
## zap2it.com
                        -0.038111674
## 64.136.28.49
## afy11.net
## 207.97.212.250
## invisionfree.com
## bravenet.com-o01
## gadgetcity.com
## army.mil
## yourgiftcards.com
## craigslist.com
                             0.362587840
## usairways.com
## drivelinemedia.com
## edline.net
## dayport.com
## axill.com
## smartbargains.com
## newgrounds.com
```

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## 216.155.193.91
## providian.com
## statcounter.com
## ajc.com
## oprah.com
## slingo.com
                            0.234217772
## continental.com
## relevantchoice.com
## toontown.com
## thumbplay.com
## jacquielawson.com
## hotwire.com
## nwa.com
## atomz.com
## nsgalleries.com
## uclick.com
## mercurial.ca
## schwab.com
## nvero.net
## ediets.com
## ichotelsgroup.com
                           0.162595661
## 216.133.243.28
## aggregateknowledge.com
## topix.net
## flalottery.com
## dlv4.com
## mybloglog.com
## lanxtra.com
## away.com
## grab.com
## tipany.com
## quickbooks.com
## instream.com
## pbs.org
## findology.com
## business.com
## cmt.com
## myinsiderdeals.com
## imagine-msn.com
## nhl.com
## modern-singles.net
## addfreestats.com
## rent.com
## homegain.com
## freeones.com
                           0.117016468
## jetblue.com
## loanweb.com
## findarticles.com
## iwon.com-o04
## incredigames.com
## webkinz.com
## dealerconnection.com
## streamaudio.com
## grantmedia.com
```

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## home123info.com
## exittracking.com
## worldsex.com
## yfdmedia.com
## automotive.com
## cursormania.com
## tradedoubler.com
## equifax.com
## hotornot.com
## falkag.de
## chicagotribune.com
## airtran.com
## thebreastcancersite.com
## charmingshoppes.com
## ugo.com
## cox.com
## spicymint.com
## real.com-o01
## targetnet.com
## effectivebrand.com
## dallascowboys.com
## leadgenetwork.com
## in.us
## vistaprint.com
Cross-Validation
cv.spender <- cv.gamlr(xweb, log(yspend), verb=TRUE,nfold =10)</pre>
## fold 1,2,3,4,5,6,7,8,9,10,done.
beta1se <- coef(cv.spender) ## 1se rule; see ?cv.gamlr</pre>
betamin <- coef(cv.spender, select="min") ## min cv selection</pre>
cbind(beta1se,betamin)[c("tvguide.com", "americanexpress.com"),]
## 2 x 2 sparse Matrix of class "dgCMatrix"
##
                          seg38
                                -0.01207381
## tvguide.com
## americanexpress.com 0.04801744 0.04869937
par(mfrow=c(1,2))
plot(cv.spender)
plot(cv.spender$gamlr) ## cv.gamlr includes a gamlr object
```



Ploting CV Results

```
log(spender$lambda[which.min(AICc(spender))])
Log lambdas selected under various criteria
##
       seg52
## -3.831328
log(spender$lambda[which.min(AIC(spender))])
##
       seg62
## -4.296497
log(spender$lambda[which.min(BIC(spender))])
##
       seg31
## -2.854474
log(cv.spender$lambda.min)
## [1] -3.738295
log(cv.spender$lambda.1se)
## [1] -3.180092
```

All Metrics, together in a path plot.

