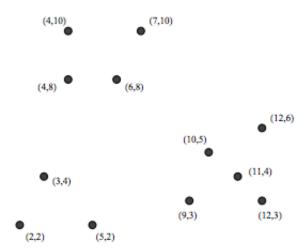


Assignment 5, due: 31 May 2016

You must return your assignment sheet and have a correct solution in order to present in the exercise groups. Please write legibily! Do no forget to put your name and matriculation number on your solution!

Problem 1.

- 1. Perform a hierarchical clustering of the one-dimensional set of points 1, 4, 9, 16, 25, 36, 49, 64, 81, assuming clusters are represented by their centroid (average), and at each step the clusters with the closest centroids are merged.
- 2. How would the clustering of the figure below (you can also see Example 7.2, page 246 of the MMDS book) change if we used for the distance between two clusters:
 - (a) The minimum of the distances between any two points, one from each cluster.
 - (b) The average of the distances between pairs of points, one from each of the two clusters.



Problem 2. In k-means algorithm we compute the cluster centroid (prototype) as the mean of the points in the cluster, as this minimizes the sum of squared errors. Consider a variation of k-means for one-dimensional data where we want to minimize the sum of *absolute* errors, that is, our goal is to find clusters C_1, C_2, \ldots, C_k that minimize

$$\sum_{j=1}^k \sum_{x_i \in C_j} |\nu_j - x_i|,$$

where ν_j is the prototype of cluster C_j . Prove that we should use the median of points in C_j as ν_j . Hint: compute the derivative of sum of absolute errors w.r.t. cluster prototypes.

Problem 3.

1. Consider the K-Means algorithm. For the points of the figure in Problem 1, if we select three starting points using the methods described in the lecture, and the first point we choose is (3,4), which other points are selected.

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2. For the three clusters in the figure

- (a) Compute the representation of the cluster as in the BFR Algorithm. That is, compute N, SUM, and SUMSQ.
- (b) Compute the variance and standard deviation of each cluster in each of the two dimensions.

Problem 4. Give an example of a dataset and a selection of k initial centroids such that when the points are reassigned to their nearest centroid at the end, at least one of the initial k points is reassigned to a different cluster.