

Mobilkommunikation - Mobile Communications

Exercise: Cellular Frequency Planning

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Cellular network planning

- ▶ Maximum cell size \Rightarrow minimal number of access points
- ▶ Minimum co-channel distance \Rightarrow minimal number of channels



The access points have a transmit power of 63 mW. Transmit antennas with a gain of 2 dB are used. The required received signal power to ensure a data rate of 24 Mb/s is -74 dBm. Assume a path loss coefficient of $\gamma = 2.5$

What is the maximum cell size?



The received power for free space propagation is

$$P_r = P_t \frac{G_t G_r}{L_p}$$

- ▶ P_r = received power
- ▶ P_t = transmitted power
- ▶ G_r = gain of the receiving antenna
- ▶ G_t = gain of the transmitting antenna
- ▶ L_p = free space path loss in distance d
- ▶ γ = path loss coefficient ($\gamma = 2$ for free space)

$$L_p = \left(\frac{4\pi d}{\lambda} \right)^\gamma \quad \text{or} \quad L_p = 10\gamma \log \left(\frac{4\pi d}{\lambda} \right) \text{ [dB]}$$

- ▶ λ = wave length = c/f
- ▶ c = speed of light, in free space $c = 3 \cdot 10^8$ m/s
- ▶ f = carrier frequency



Decibel and decibel milliwatt (log is \log_{10})

- ▶ $10 \log(X/Y)$ [dB]
- ▶ $10 \log(X/1\text{mW})$ [dBm]

$$P_r = P_t \frac{G_t G_r}{L_p}$$

$$\Rightarrow 10 \log \left(\frac{P_r}{1\text{mW}} \right) = 10 \log \left(\frac{P_t}{1\text{mW}} \right) + 10 \log G_t + 10 \log G_r - 10 \log L_p$$

- ▶ Transmit power: $10 \log(63\text{mW}/1\text{mW}) = 18$ dBm
- ▶ Transmit antenna gain: 2 dB
- ▶ Minimum receive power: -74 dBm
- ▶ Allowed path loss: 94 dB



$$L_p = 10\gamma \log \left(\frac{4\pi d}{\lambda} \right) \text{ dB} \leq 94 \text{ dB}$$

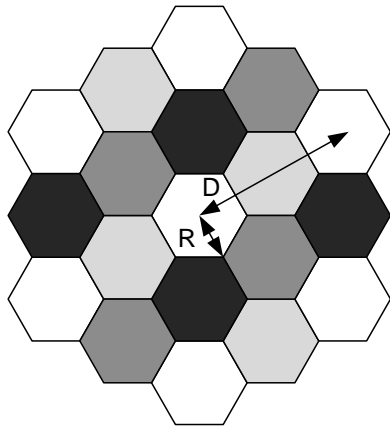
$$\Rightarrow \frac{4\pi d}{\lambda} \leq 10^{9.4/\gamma}$$

$$\Rightarrow d \leq \frac{\lambda}{4\pi} 10^{9.4/\gamma}$$

- ▶ $\lambda = c/f = (3 \cdot 10^8 \text{ m/s}) / (5 \cdot 10^9 \text{ Hz}) = 0.06 \text{ m}$
- ▶ $\gamma = 2.5$
- ▶ cell radius $R \leq 27,5 \text{ m}$
- ▶ larger path loss $\gamma \Rightarrow$ smaller radius $R \Rightarrow$ more access points

Some typical cluster sizes N and reuse ratios $D/R = \sqrt{3N}$

N	D/R	(u,v)
1	1.7	(1,0)
3	3.0	(1,1)
4	3.5	(2,0)
7	4.6	(2,1)
9	5.2	(3,0)
12	6.0	(2,2)
13	6.2	(3,1)
16	6.9	(4,0)
19	7.5	(3,2)



How many different channels N are required for $S/I \geq 13$ dB?



Considering the tier-1 interferers, the signal to interference ratio can be written as

$$\frac{S}{I} = \frac{S}{\sum_{k=1}^6 I_k}$$

where

- ▶ S = signal power
- ▶ I_k = power of the k -th interferer

Inserting the path loss formula for signal and interference

$$\frac{S}{I} = \frac{\frac{\text{const.}}{R^\gamma}}{6 \frac{\text{const.}}{D^\gamma}} = \frac{1}{6} \left(\frac{D}{R} \right)^\gamma$$



Inserting $D/R = \sqrt{3N}$ it follows that

$$N = \frac{1}{3} \left(6 \frac{S}{I} \right)^{2/\gamma}$$

- ▶ $S/I \geq 13 \text{ dB} \Rightarrow S/I \geq 10^{1.3}$
- ▶ $\gamma = 2.5$
- ▶ cluster size $N \geq 16$
- ▶ smaller path loss $\gamma \Rightarrow$ larger cluster size $N \Rightarrow$ more channels