

## Preconditions

System definition, quantitative emergence

## Objectives

Terminology for self-organization, robustness, and adaptivity

Quantitative approach

## Content

- ☐ Self-organization and autonomy
- ☐ 5 aspects of autonomous systems
- ☐ Measuring robustness
- ☐ Measuring adaptivity: Configuration space and variability
- ☐ Control and degree of autonomy
- ☐ Controlled self-organization

## Preconditions

System definition, quantitative emergence

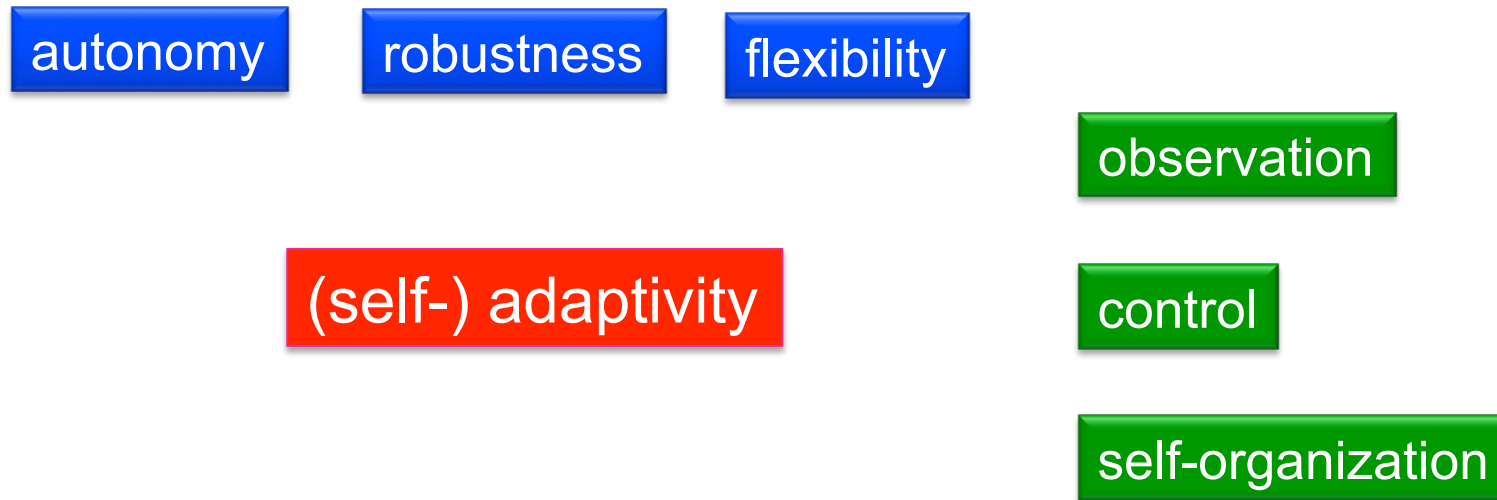
## Objectives

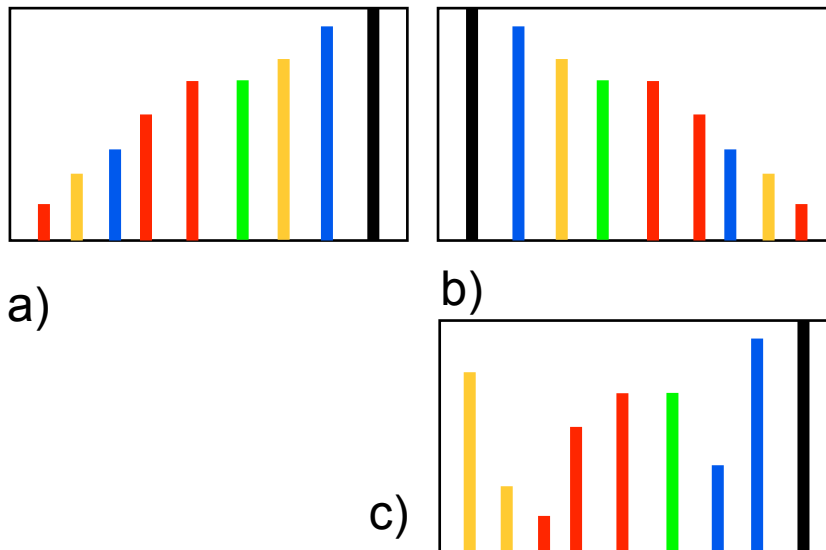
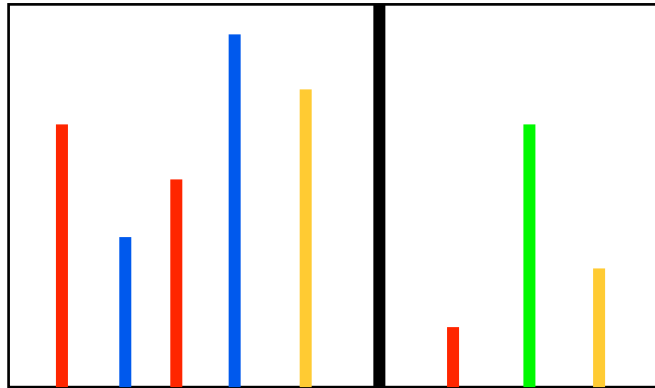
Terminology for self-organization and adaptivity

Quantitative approach

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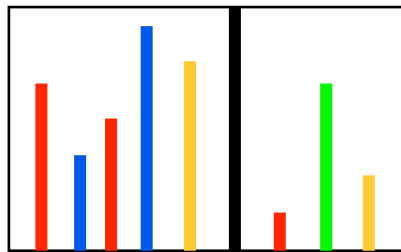
□ Properties of each stick:

- height
- color

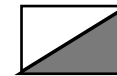
□ Ordering objectives

- a) increasing height
- b) decreasing height
- c) color clusters

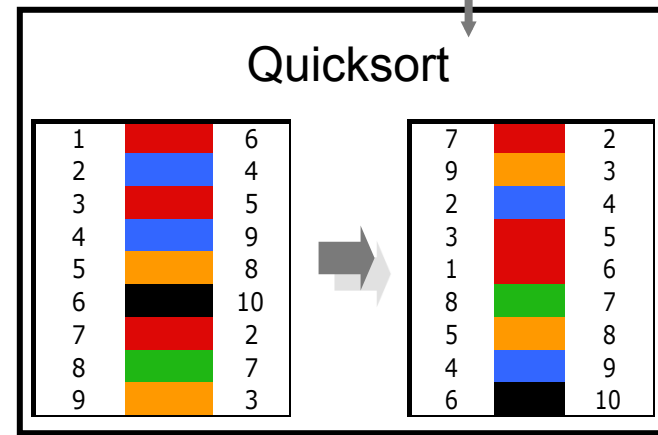
□ Ordering process?



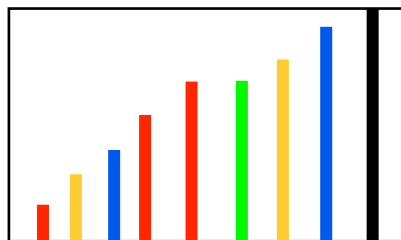
Global objective  $a := \text{increasing height}$

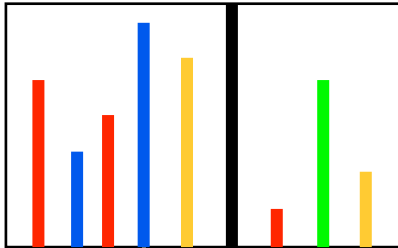


- 1 Observation
- 2 Model building
- 3 Simulation



- 4 Enactment

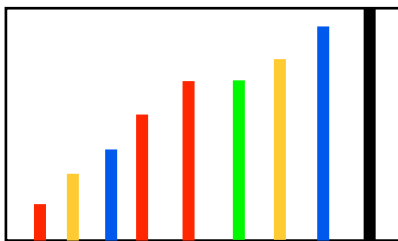




Global objective  $a := \text{increasing height}$

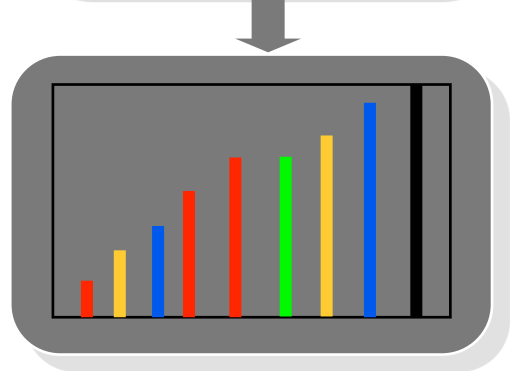
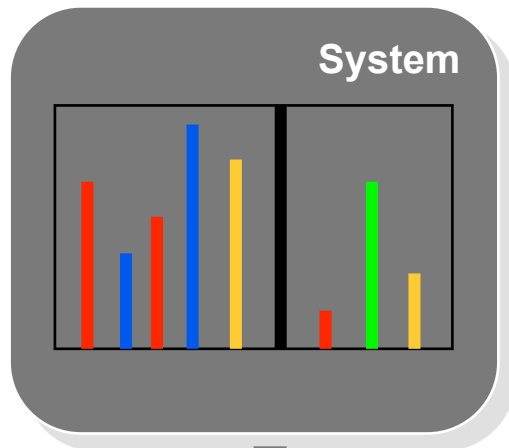
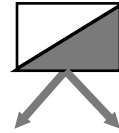


1. Local objective:  $\text{right} > \text{myself}$
2. Local observation:  $\text{right} < \text{myself}$
3. Local decision:  
if  $\text{right} < \text{myself}$  then Switch  
places; else: nil
4. Local enactment
5. Go to 2

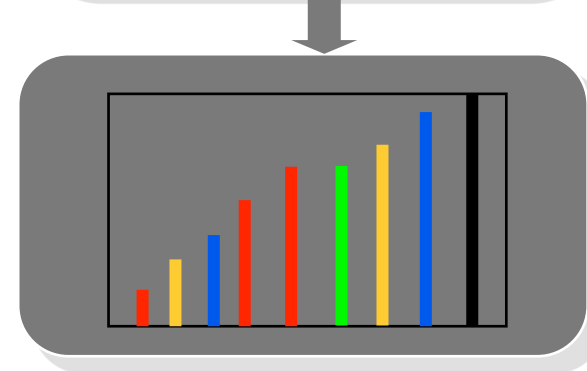
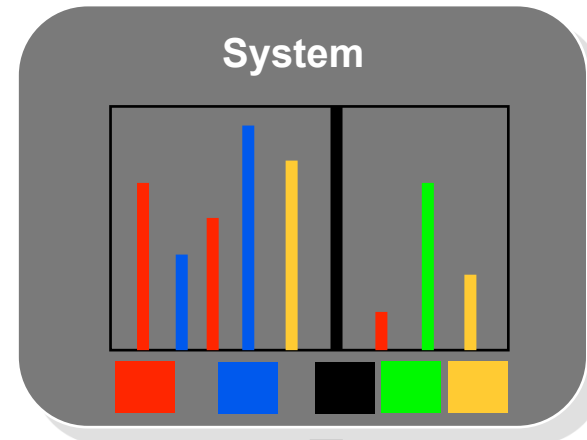
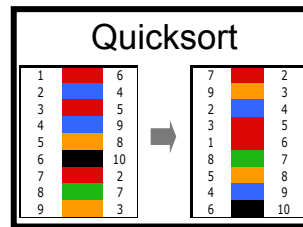


enactment = Ausführung, Umsetzung

Global objective := increasing height

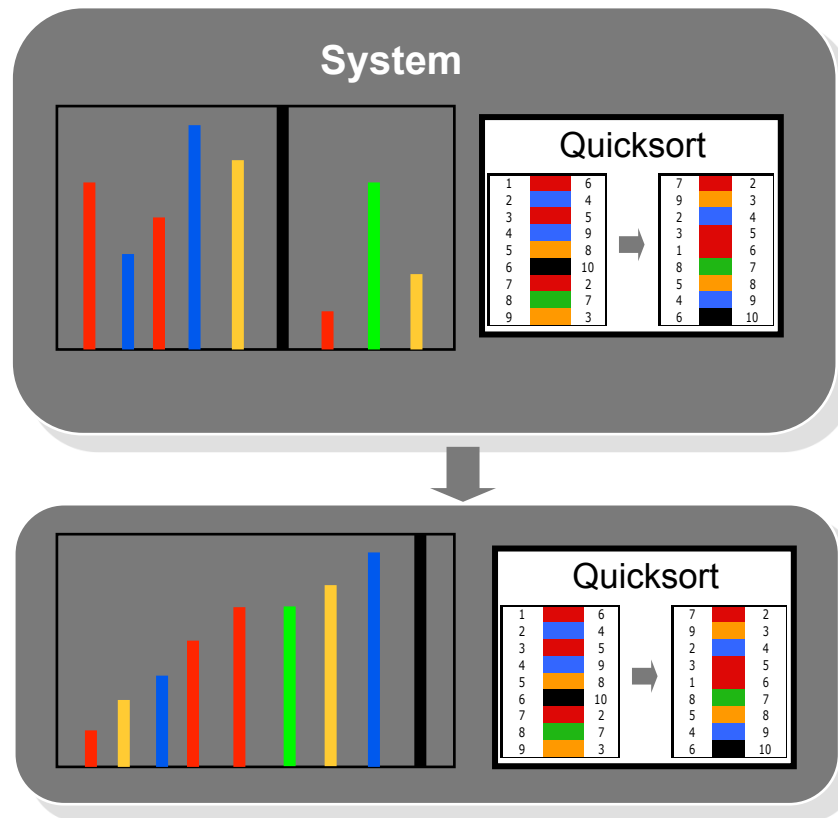


Autonomy? No  
SO? No



Autonomy? Yes  
SO? Yes

Global objective := increasing height

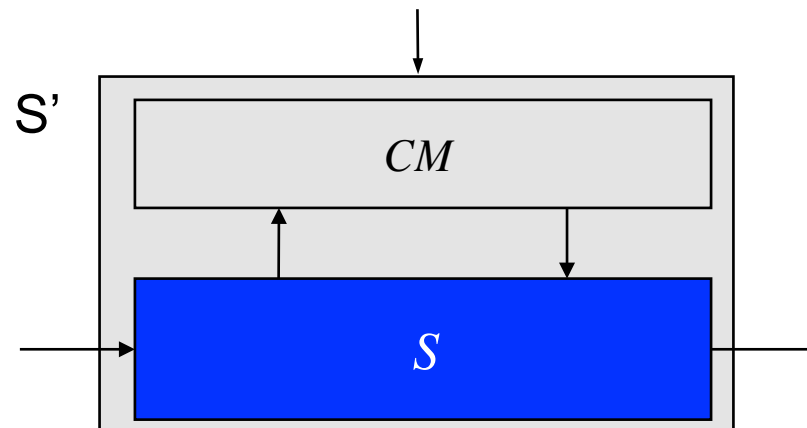


Autonomy? yes  
Self-organization? Maybe



- ❑ **Autonomy**: A system  $S'$  changes its structure without explicit external control.
  - There must be some kind of **internal** control mechanism  $CM$ !
- ❑ **Self-organization**: The internal control mechanism is distributed (to a certain degree).
- ❑ **Adaptivity**: A system  $S$  allows to be changed (passive property).

These definitions have to be refined and formulated quantitatively!



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Terminology framework for self-organization and adaptivity

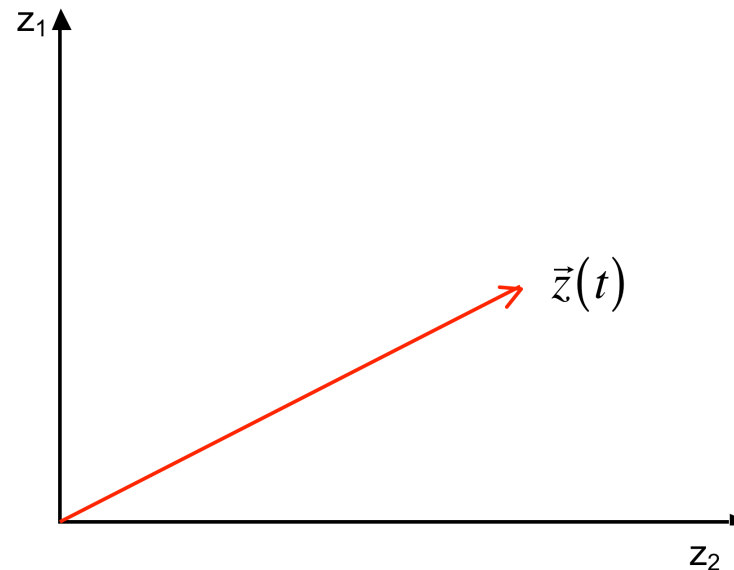
Quantitative approach

## Content

- ☐ Self-organization and autonomy
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- ☐ Measuring robustness
- ☐ Measuring adaptivity: Configuration space and variability
- ☐ Control and degree of autonomy
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- ❑ An autonomous system  $S$  is characterized by 5 aspects:
  1. System state
  2. Utility and Acceptance space
  3. Disturbance
  4. Control mechanism
  5. Recovery (process)

- ❑ At any given time  $t$ , the system  $S$  is in state  $z(t)$ .
- ❑ If there are  $n$  attributes used to describe the state of  $S$ ,  $\mathbf{z}(t)$  is a vector in  $n$ -dimensional state space  $Z^n$ .



- ❑ We assign a **utility**  $U$  to each state  $\mathbf{z}$  by the evaluation functions  $\eta_i$ :

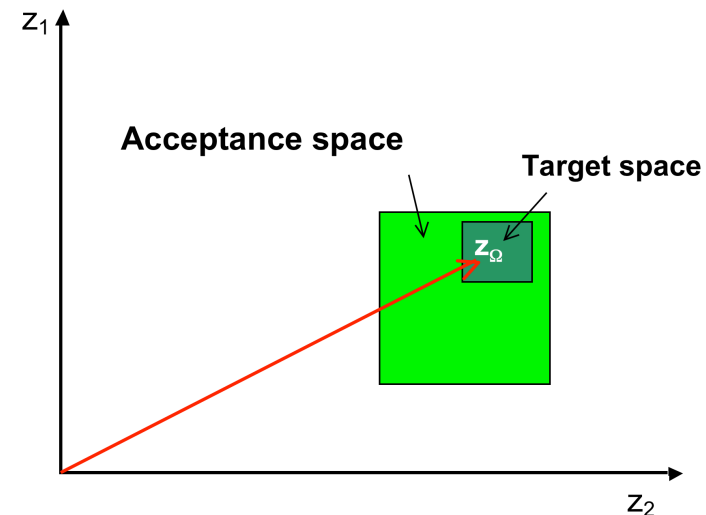
$$U = \eta(\mathbf{z}). U_i \in \mathbb{R}$$

- ❑ The set of acceptable states (the **acceptance space**) corresponds to a minimal acceptable utility

$$U_{i, \text{ acceptable}} = \eta_i(\mathbf{z}_{\text{acceptable}}) \text{ and } U_{i, \text{ acceptable}} \geq U_{\min} \quad \forall \mathbf{z}_{\text{acceptable}}.$$

- ❑ The set of **ideal** states (the **target space**) is denoted by  $Z_\Omega$ . In some cases, it might be a single state  $\mathbf{z}_\Omega$ .
- ❑ The target space is a subset of the acceptance space.

cf. Objective function



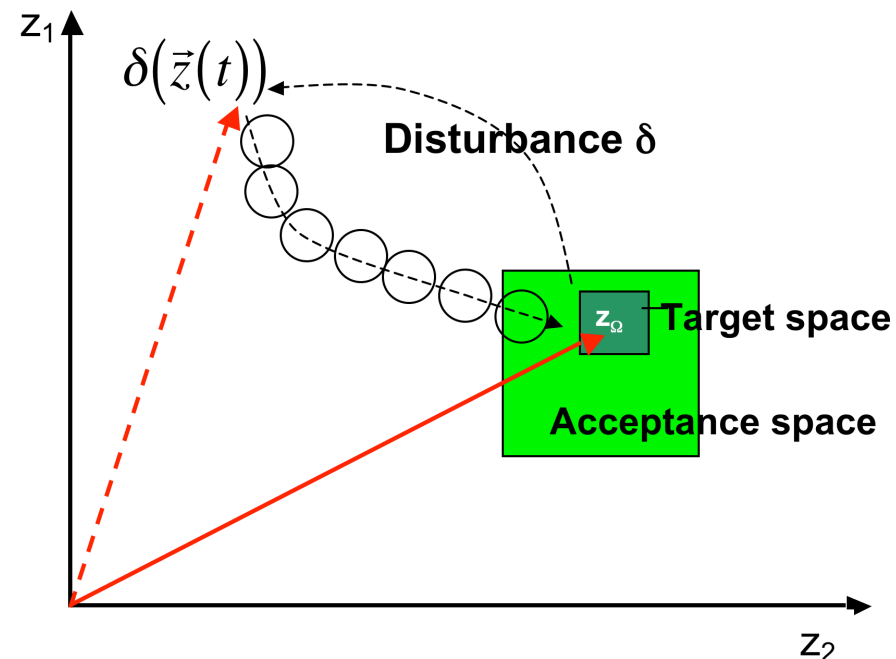
❑ The system might be disturbed by environmental influences or disturbances  $\delta$ .

❑ A disturbance  $\delta$  changes the state  $\mathbf{z}(t)$  into the disturbed state  $\mathbf{z}_{\delta}(t) = \delta(\mathbf{z}(t))$ .

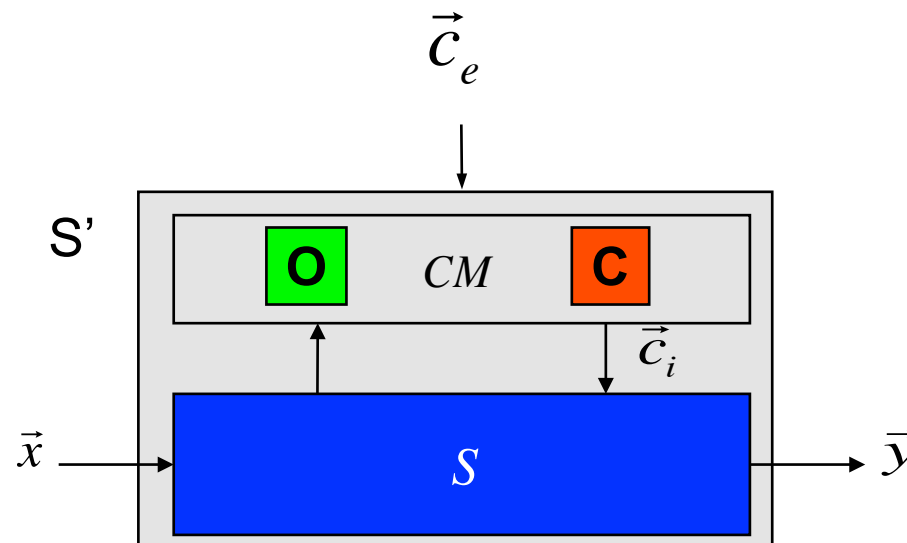
❑ Consequently the utility changes to

$$U_{\delta} = \eta(\mathbf{z}_{\delta}(t))$$

❑ If  $U_{\delta} < U_{\text{acceptable}}$  the system is outside the acceptance space.

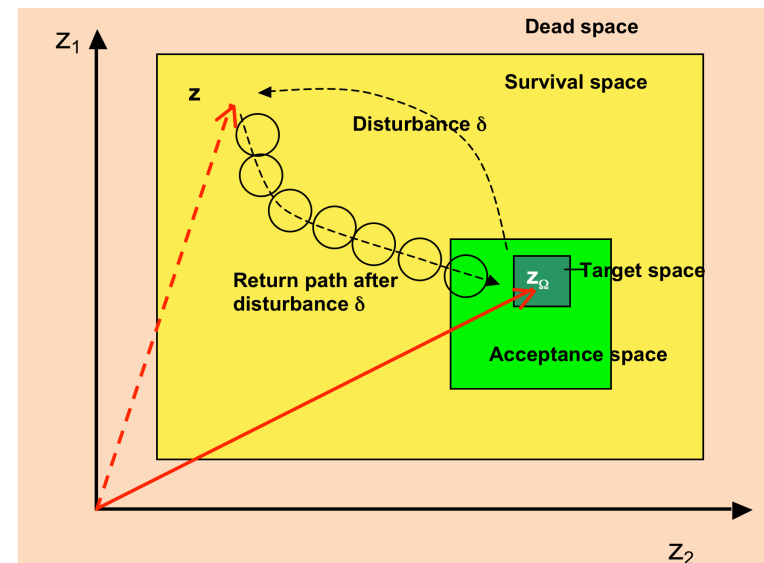


- ❑ An internal control mechanism  $CM$  to controls the behavior of the system  $S$  by changing some of its attributes  $\mathbf{c}_i$ .
  - See: Configuration space
- ❑ The control mechanism  $CM$  consists of an **Observer**  $O$  and a **Controller**  $C$ .
- ❑  $S'$  can be controlled via  $\mathbf{c}_e$ .



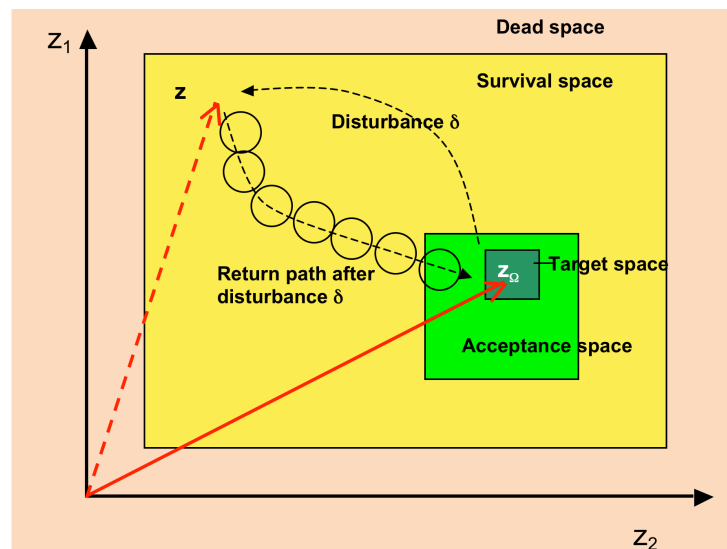
## □ Disturbance and **recovery** behavior in state space

- Phase I: A disturbance of strength  $\delta$  is applied to the system, which changes its state to  $\mathbf{z}_\delta$  and its utility to  $U_\delta < U_{\text{acceptable}}$ .
- Phase II: A control mechanism (which in the case of an adaptive self-organizing system is part of the system itself) actively guides the system back into the acceptance space (recovery process).
- The time needed for this recovery is  $t_{\text{rec}}$ .





- ❑ An adaptive system  $S$  will always try to return to the acceptance space.
- ❑ Such a recovery is possible only from a certain subset of states, the **Survival space**.
- ❑ Any disturbance  $\delta$  moving  $z$  outside the survival space will be **lethal** for  $S$ : **Dead Space**.



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- ☐ Self-organization and autonomy
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- ☐ **Measuring Robustness**
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- ❑ It is a common misunderstanding that the goal of building OC systems is primarily the construction of (self-) adaptive or self-organizing systems or that OC systems generally have a higher performance (more general: utility) than conventional systems.
- ❑ OC systems are **not per se** faster than conventional systems.
  - But they return to a certain accepted utility in the presence of internal and/or external disturbances. We call this property “**robustness**”.
  - Or they adapt to new goals (a new acceptance space). We call this property “**flexibility**”.
- ❑ **Active** correction mechanisms (such as an observer/controller) counteract the temporary deviation of a system from an acceptable state (or in case of a multi-dimensional state space: the acceptance space).

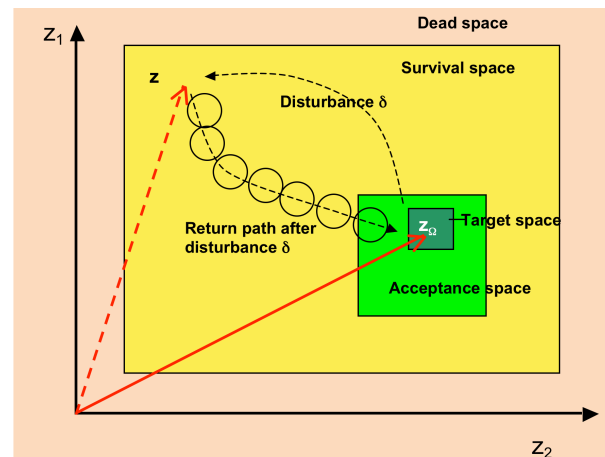
## □ Robustness

- The system  $S'$  is expected to maintain a required behavior or functionality in spite of certain disturbances.
- The standard notion for this behavior is **robustness**.

## □ Flexibility

- The requirement to modify the behavior because of changed **objectives** corresponds to the notion of **flexibility**.

- Both capabilities, robustness and flexibility, are enabled by the **(self-) adaptivity** of the system.



- ❑ We call a system more robust if it has a large number of states that do not lead to a permanently reduced utility.
- ❑ Definition: Let  $D$  be a non-empty set of disturbances.
  - a) A system  $S$  is called **strongly robust** with respect to  $D$ , iff all the disturbances  $\delta \in D$  map the **target** space into itself.
  - b) A system  $S$  is called **weakly robust** with respect to  $D$ , iff all the disturbances  $\delta \in D$  map the target space into the **acceptance** space.
- ❑ Flexibility can be treated like robustness if we define a change of goals (i.e. a change of acceptance space) as a special case of a disturbance.

## □ Observations

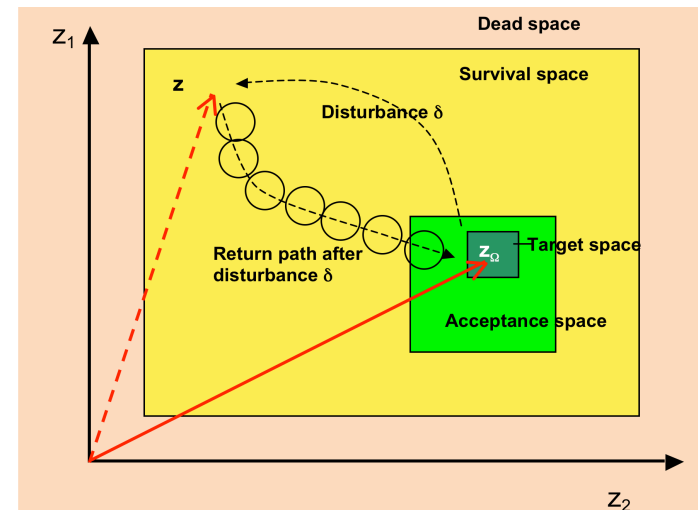
- The (degree of) robustness of a system increases with the **size** of the set of disturbances  $D$  and the **strength** of the disturbance  $\delta$  the system can handle (i.e. fulfilling the requirements a or b above).
- A system A is more robust than a system B if it returns to the target or the acceptance space in a **shorter** time after the disturbance occurs.

## □ If we want to quantify robustness (for comparison between different systems) we have to take into account the following observables:

- the strength of the disturbance,  $\delta$
- the deviation of the system utility  $U_\delta$  from the acceptable utility  $U_{\text{acceptable}}$ ,  $\Delta U$ , and
- the duration of the deviation (the recovery time  $t_{\text{rec}}$ ).

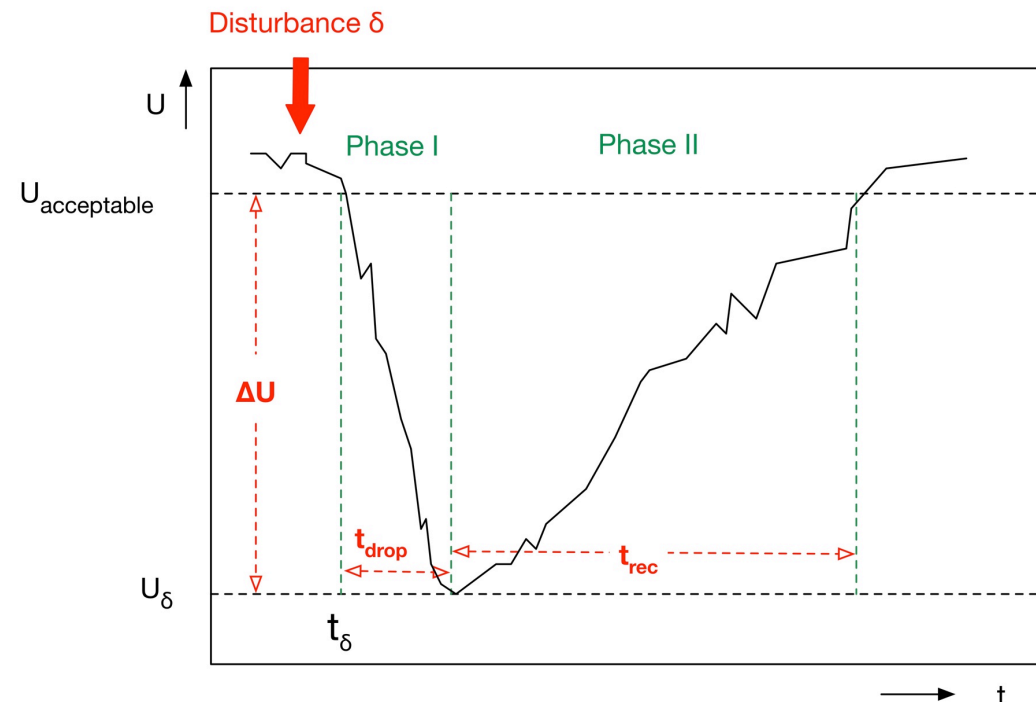
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- The time needed for this recovery is  $t_{\text{rec}}$ .



### □ Utility degradation behavior over time

- The deviation begins when the utility drops below  $U_{\text{acceptable}}$ , i.e. at time  $t_{\delta}$  (and not when the disturbance occurs).
- A disturbance taking effect at time  $t_{\delta}$  will lead to a utility drop from  $U \geq U_{\text{acceptable}}$  to  $U_{\delta}$ . The drop occurs within  $t_{\text{drop}}$ .
- Given an effective control mechanism the system will return back to  $U \geq U_{\text{acceptable}}$  within time  $t_{\text{rec}}$ .
- Phases I and II are called deviation phase.



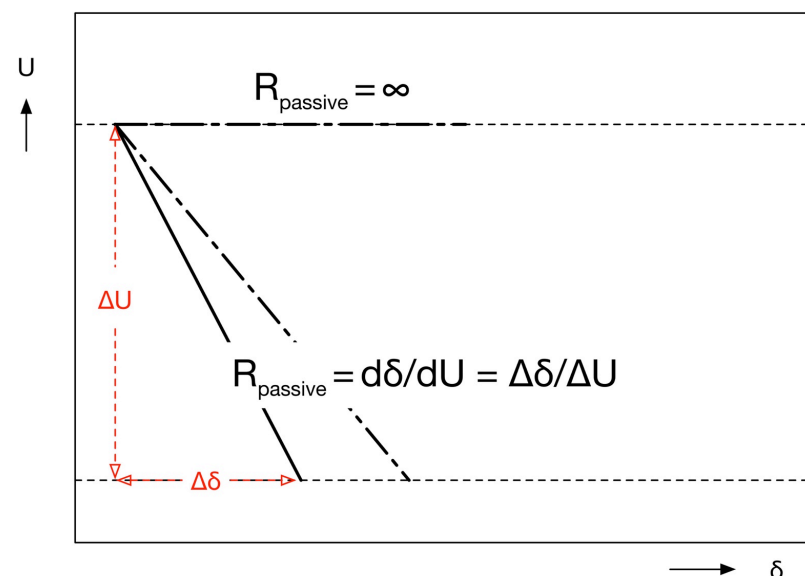


- The deviation phase shows 2 sub-phases:
  - **Phase I: Passive robustness (or drop) phase:** There is not yet a control mechanism active. The system utility drops by  $\Delta U$ . The drop  $\Delta U$  and the time  $t_{\text{drop}}$  are a function (1) of the strength of the disturbance,  $\delta$ , and (2) of the structural stability of the system.
  - **Phase II: Active robustness phase:** The active O/C mechanism tries to reorganize/repair the system.
- It might be difficult to discriminate between the 2 phases, they might overlap.
- Usually  $t_{\text{drop}}$  is very short, the drop occurs “instantaneously” in many cases.

The utility deviation  $\Delta U$  is the cost caused by the disturbance.

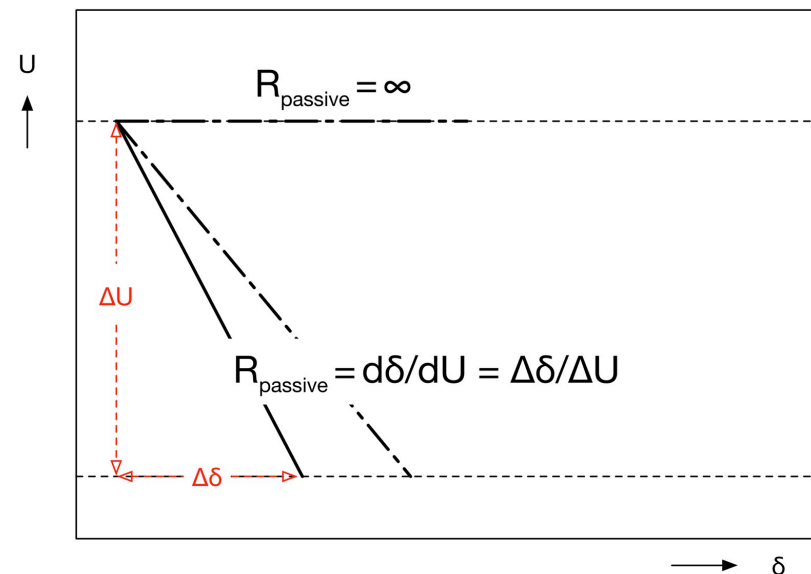
## □ Passive robustness

- Passive robustness  $R_{\text{passive}}$  is the sensitivity of  $U$  against a change of  $\delta$ , i.e.  $dU/d\delta = 1/R_{\text{passive}}$
- $R_{\text{passive}}$  is a measure of the *structural* stability of a system in the presence of a disturbance  $\delta$ .
- If  $\delta$  has no effect on a system ( $\Delta U = 0$ ) its structural stability  $R_{\text{passive}} = \infty$ .



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- ❑ Example 1: A very stable concrete tower, which does not move ( $\Delta U = 0$ ) under a storm of strength  $\delta$ , is structurally infinitely stable.
- ❑ Example 2: A communication link with an error correcting code, which corrects errors up to 3 bits, is structurally infinitely stable under a disturbance of strength  $\delta = 1$  bit.



### □ Active robustness $R_{\text{active}}$

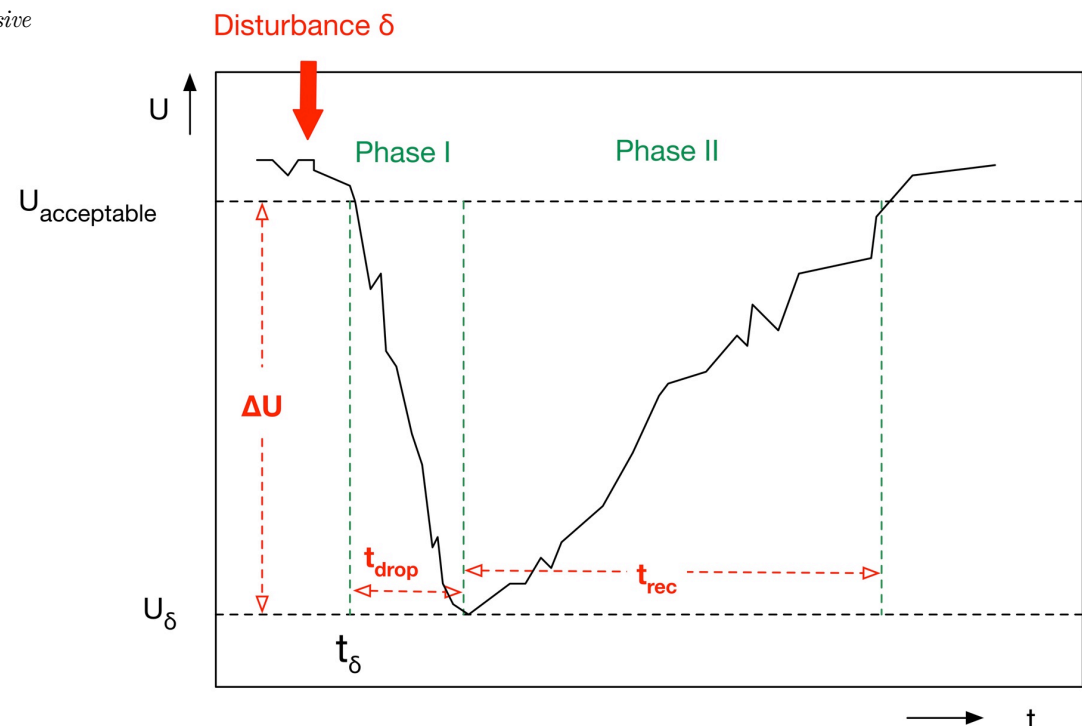
- $R_{\text{active}}$  is defined as the (averaged) recovery speed of the system, i.e.

$$R_{\text{active}} = \frac{dU}{dt} \text{ or } R_{\text{active}} = \frac{\Delta U}{t_{\text{rec}}} \text{ (in case of a full recovery)}$$

$$t_{\text{rec}} = \frac{\Delta U}{R_{\text{active}}}$$

$$t_{\text{rec}} = \frac{\delta}{R_{\text{passive}} \times R_{\text{active}}} \text{ with } \Delta U = \frac{\delta}{R_{\text{passive}}}$$

- $R_{\text{active}}$  is a property of the Observer/Controller
- Without an O/C the system stays at  $U_{\delta}$  as long as the disturbance remains.

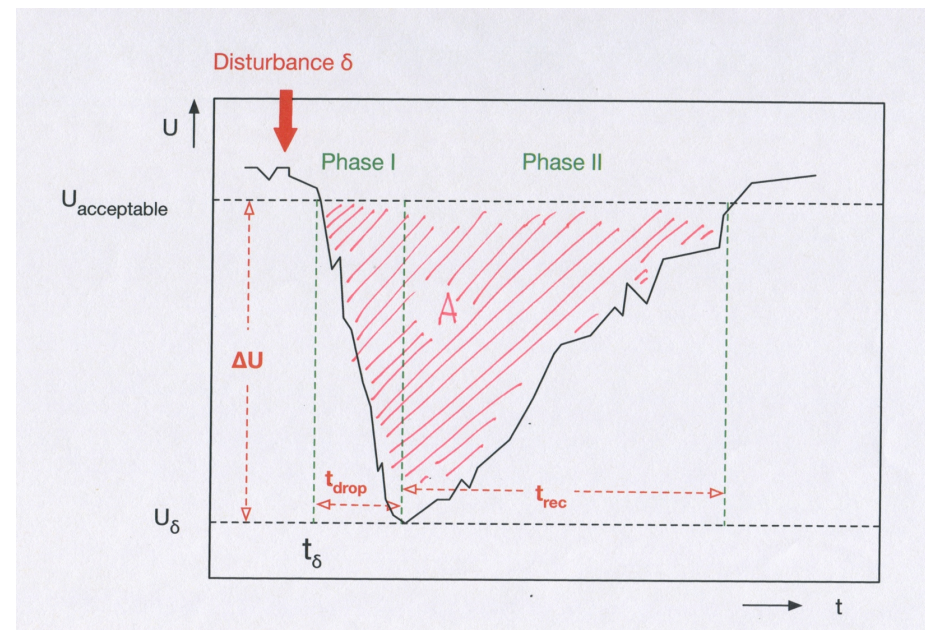


- The robustness of a system under a given disturbance of strength  $\delta$  is characterized by the triple  $(\delta, \Delta U, t_{\text{rec}})$  or  $(\delta, R_{\text{passive}}, R_{\text{active}})$ .
- We can use the area  $A$  of the utility deviation from  $U_{\text{acceptable}}$  until full recovery to  $U_{\text{acceptable}}$  as a measure for the effective **utility degradation**:

▪ Effective utility degradation 1) 
$$A = \Delta U \times (t_{\text{drop}} + t_{\text{rec}}) - \int_{t_{\delta}}^{t_{\delta} + t_{\text{rec}}} U(t) dt$$

- To achieve a minimal degradation we have to minimize  $A$  (i.e.  $\Delta U$  and  $t_{\text{rec}}$ ).

1) for  $U_{\delta} = 0$



□ For simplification we **approximate** the deviation area by a triangle:

- The drop occurs very fast, hence  $t_{\text{drop}} = 0$ .
- The recovery is assumed to be linear.

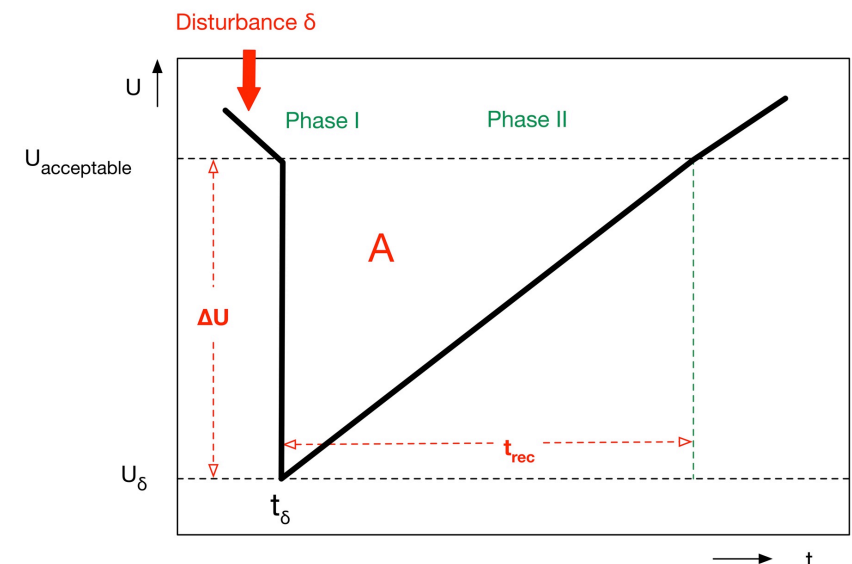
□ Then 
$$A = \frac{\Delta U \times t_{\text{rec}}}{2} = \frac{1}{2} \frac{\delta}{R_{\text{passive}}} \times \frac{\delta}{R_{\text{passive}} \times R_{\text{active}}}$$

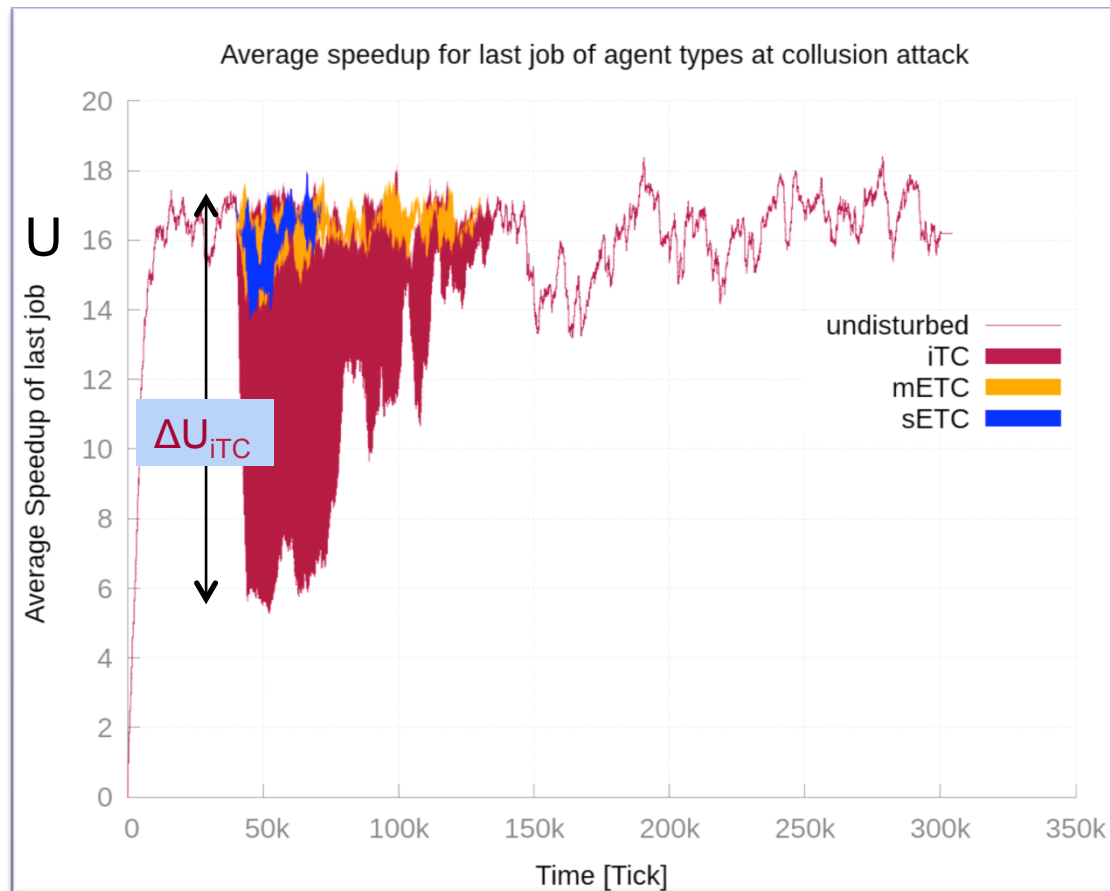
□ **Effective utility degradation** 
$$A = \frac{1}{2} \frac{\delta^2}{R_{\text{passive}}^2 \times R_{\text{active}}}$$

A is a cost x time product

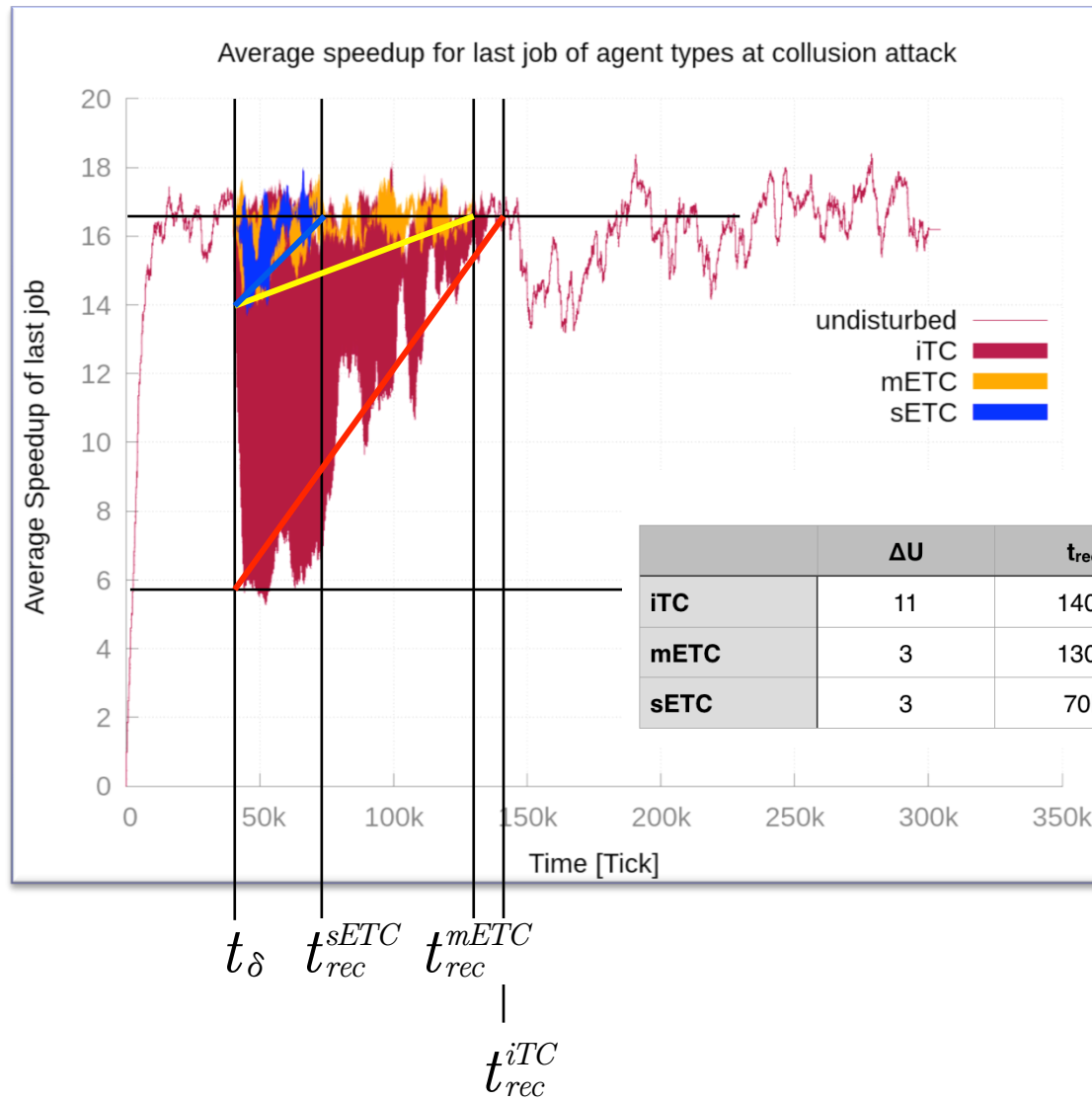
□ Observations

- An increase of  $R_{\text{passive}}$  decreases A more effectively than a  $R_{\text{active}}$  increase. The reason is that  $R_{\text{passive}}$  influences  $\Delta U$  as well as  $t_{\text{rec}}$ .
- There is a trade-off possible between  $R_{\text{passive}}$  and  $R_{\text{active}}$ .





- ❑ Trust Community experiments: 3 experimental recovery behaviors
  - with identical  $\delta$  (attack size)
  - 3 different O/C solutions
- ❑ The O/C solutions mETC and sETC counteract the attack so fast, that  $\Delta U$  is reduced as well.
- ❑ For the practical comparison of experimental evaluations the determination of A (the colored areas under the 3 curves) seems to be best suited.



Evaluation

	$\Delta U$	$t_{rec}$	$A [x10^3]$	$R_{passive}$	$R_{active}$	$\delta$
iTC	11	140k	770	4.5.	$8 \cdot 10^{-5}$	50
mETC	3	130k	195	17	$2.3 \cdot 10^{-5}$	50
sETC	3	70k	105	17	$4.3 \cdot 10^{-5}$	50



## Evaluation

	$\Delta U$	$t_{\text{rec}}$	$A [x10^3]$	$R_{\text{passive}}$	$R_{\text{active}}$	$\delta$
<b>iTC</b>	11	140k	770	4.5.	$8 \cdot 10^{-5}$	50
<b>mETC</b>	3	130k	195	17	$2.3 \cdot 10^{-5}$	50
<b>sETC</b>	3	70k	105	17	$4.3 \cdot 10^{-5}$	50

A is a cost x time product:  $[A] = [\text{speed-up} \times \text{time}]$

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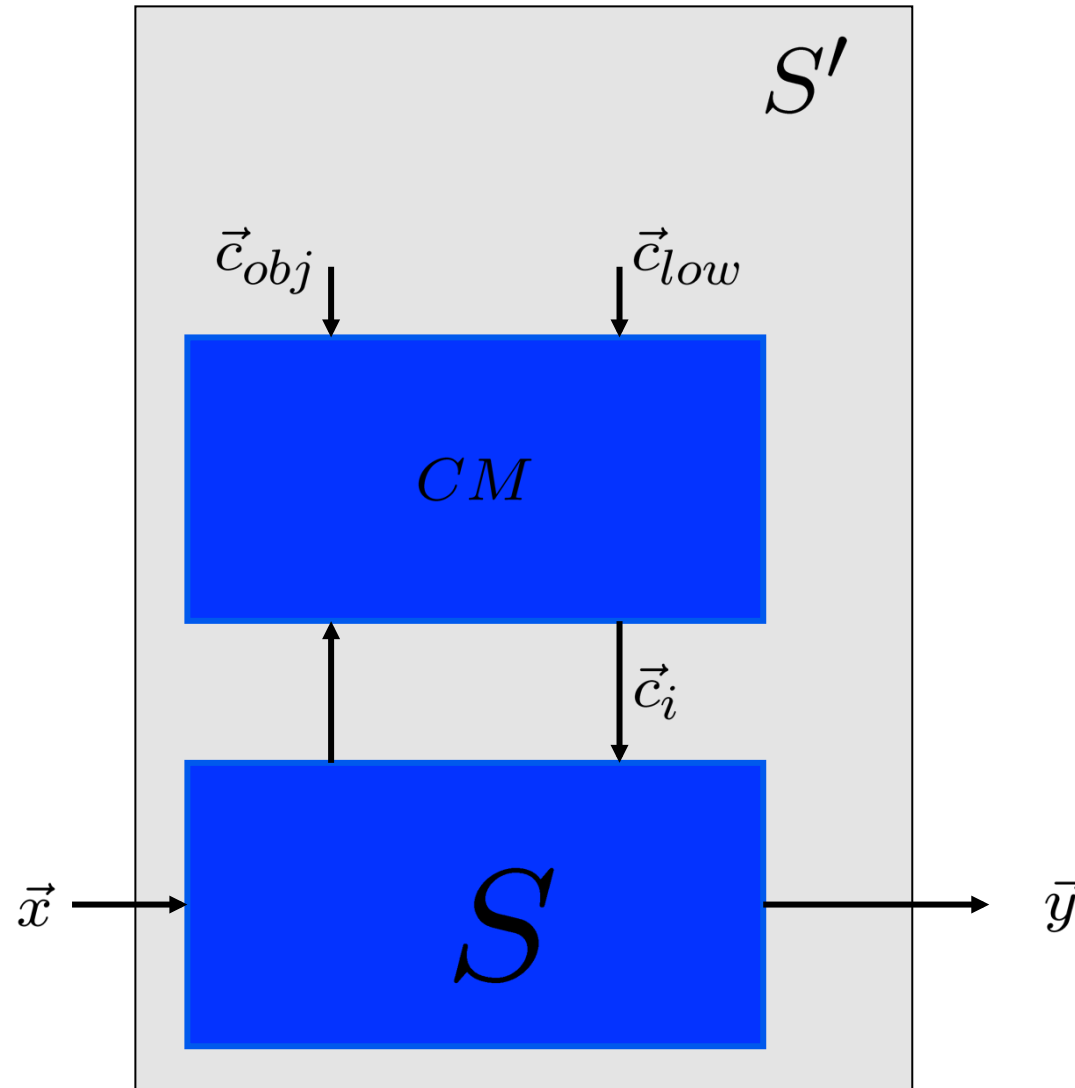
Terminology for self-organization and adaptivity

Quantitative approach

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S is adaptable.  
S' is adaptive.

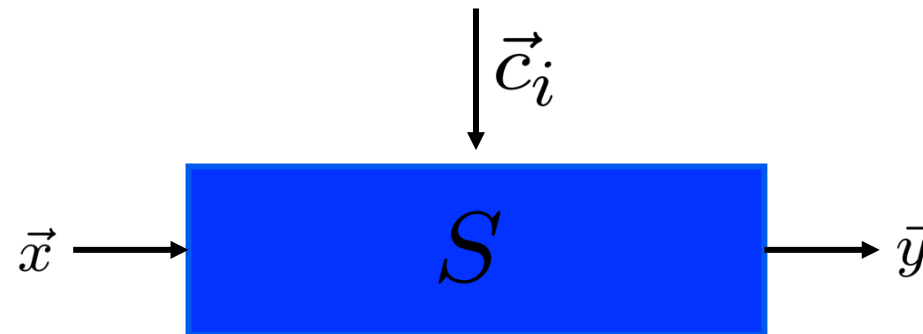


- ❑ Definition: Let  $D$  be a non-empty set of disturbances.
- ❑ A system is called (self-) **adaptive** iff it is capable to move into the acceptance space after any of the disturbances  $D$  **without\*** needing external control.
  - That means for a **robust** system  $S$ , if  $\delta$  transforms state  $\mathbf{z}(t)$  of  $S$  into state  $\delta(\mathbf{z}(t))$  then, after some time interval  $t_{\text{rec}}$  the state of  $S$  will be acceptable.
  - That means for a **flexible** system  $S$ , if  $\delta$  is a change of goals (i.e. a change of acceptance space) then, after some time interval  $t_{\text{rec}}$  the state of  $S$  will be acceptable.
- ❑ The adaptivity of a system is quantitatively specified by its degree of autonomy (see below).

adaptive = robust or flexible!

\* “without” must be quantified!

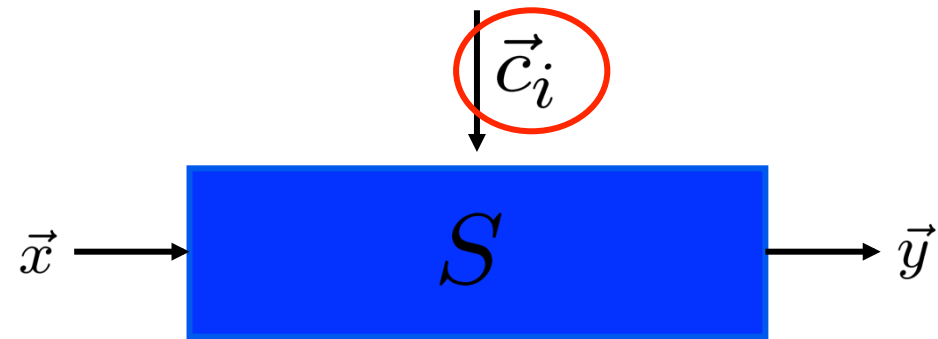
- A system  $S$  is called **adaptable** or **controllable** iff explicit (external) control actions are possible.
- The behavior of an adaptable system  $S$  can be modified from the outside via control inputs  $\mathbf{c}_i$  by
    - changing parameters and/or
    - changing its structure (elements and links).



$S$  is adaptable.

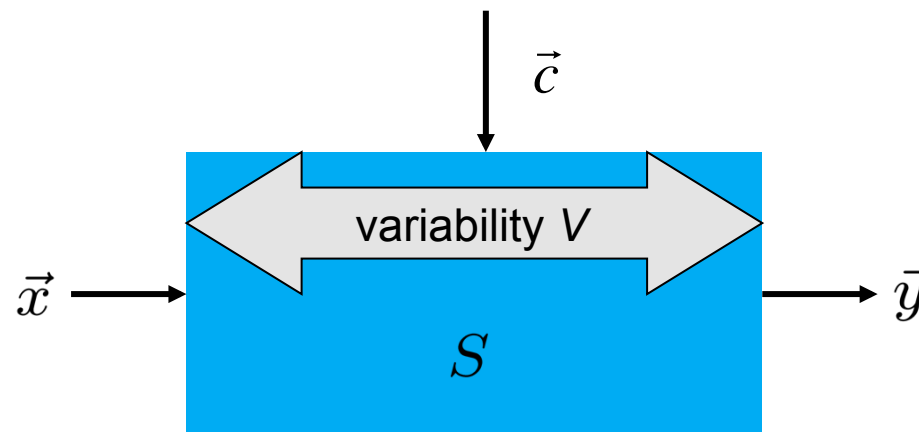
Adaptability is a passive property!

Notation:  $\mathbf{c}_i$  is equivalent to  $\vec{c}_i$  !



- ❑ We have to specify the range of possibilities for **influencing the SuOC**. This changeability (or plasticity) is described by the **configuration space** representing the capability of  $S$  to be changed (passively!).
- ❑ It is determined by the **control parameters  $\mathbf{c}$**  of the system that can be changed directly by the external control mechanism CM.
  - These control parameters refer to all the components of the system structure and to further parameters.
- ❑ A control input  $\mathbf{c}$  selects a certain configuration.
- ❑ In the following we assume that  $S$  is an adaptable system.

- ❑ The configuration space comprises the set of configurations that  $S$  can assume.
- ❑ Every configuration is specified by the values of a collection of system or environmental parameters  $\mathbf{c}$ , which are open to be modified by control actions.
- ❑ These parameters are called **configuration parameters**.
- ❑  $\mathbf{c}$  can be regarded as a pointer into the configuration space. The dimension of this pointer corresponds to the dimension of the configuration space.



- ❑ The Variability  $V$  equals the number of bits necessary to address all the different configurations in the configuration space.
  - The variability of a system is measured by  $V = \lg(\text{number of configurations})$ . This is the **number of bits** in  $\mathbf{c}$ .
- ❑ The configuration space and the variability represent the **possible** modifications by CM.
- ❑ Every control action modifies the values of a **subset** of the configuration attributes.
- ❑ We denote the number of bits **actually** modified by a specific control action  $\mathbf{c}$  by  $\#c$ .
  - ❑  $\#c$  can be less than  $V$  (only some attributes are modified).
  - ❑  $\#c$  can be greater than  $V$  (multiple steps of modifications).

Possible modifications  $\neq$  Actual modifications



## Preconditions

System definition, quantitative emergence

## Objectives

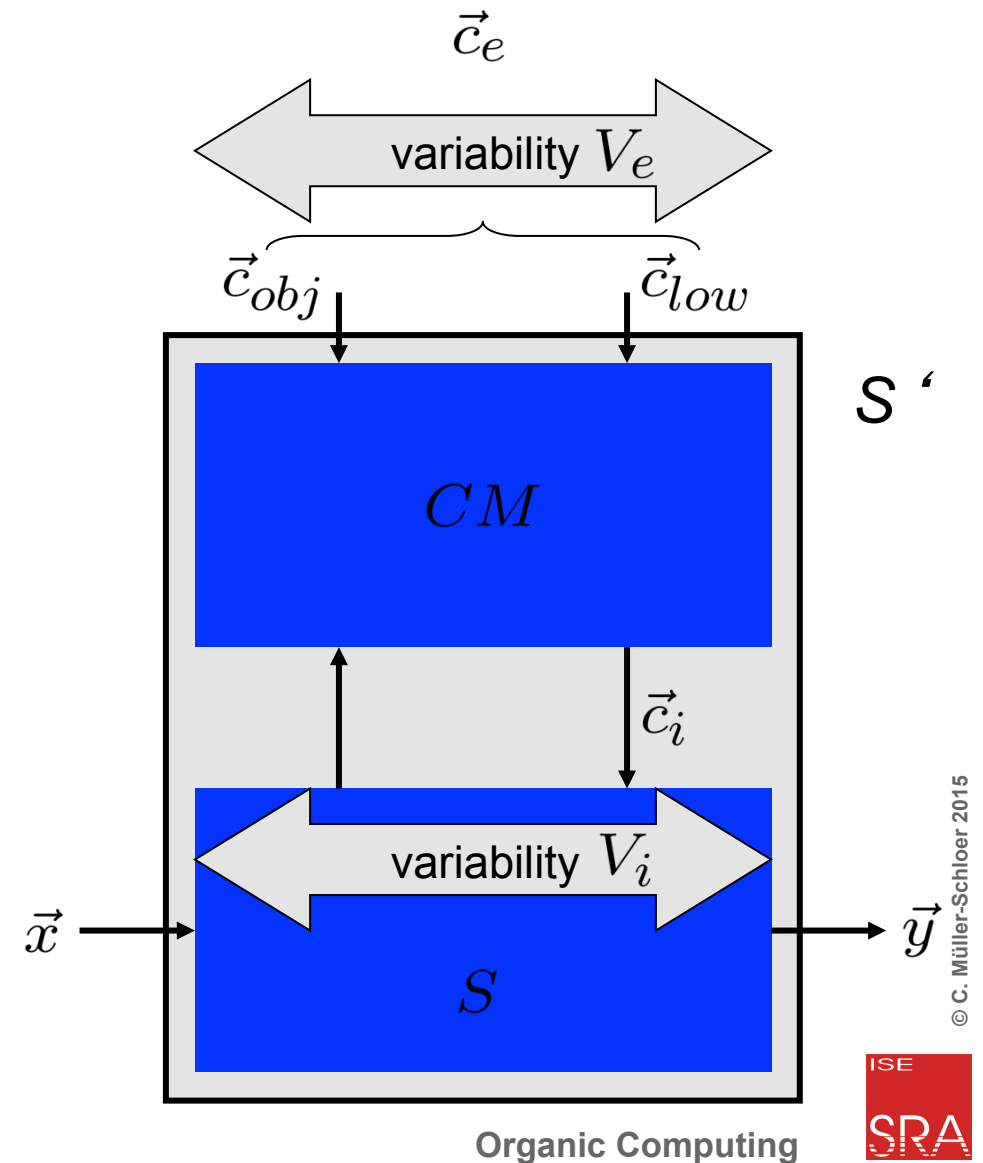
Terminology for self-organization and adaptivity

Quantitative approach

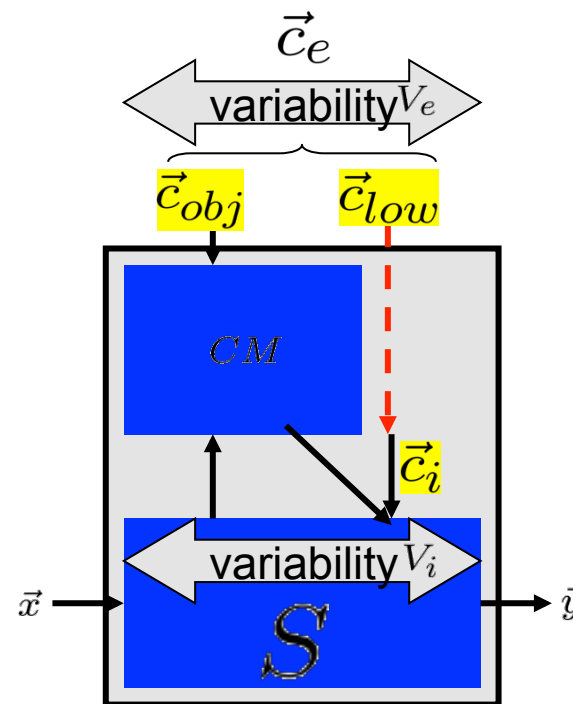
## Content

- ☐ Self-organization and autonomy
- ☐ 5 aspects of autonomous systems
- ☐ Measuring robustness
- ☐ Measuring adaptivity: Configuration space and variability
- ☐ **Control and degree of autonomy**
- ☐ Controlled self-organization

- With respect to  $S'$  we can distinguish two types of configuration spaces:
- The **internal configuration** space is the configuration space of  $S$ , its variability is denoted by  $V_i$ .
  - The **external configuration** space is the configuration space of  $S'$ , its variability is denoted by  $V_e$ .



- We distinguish between high-level control inputs  $\mathbf{c}_{obj}$ , specifying **system objectives** to be followed by the control mechanism  $CM$ ,
- and control actions  $\mathbf{c}_{low}$  directly controlling attributes of the internal configuration space (**low-level control**).

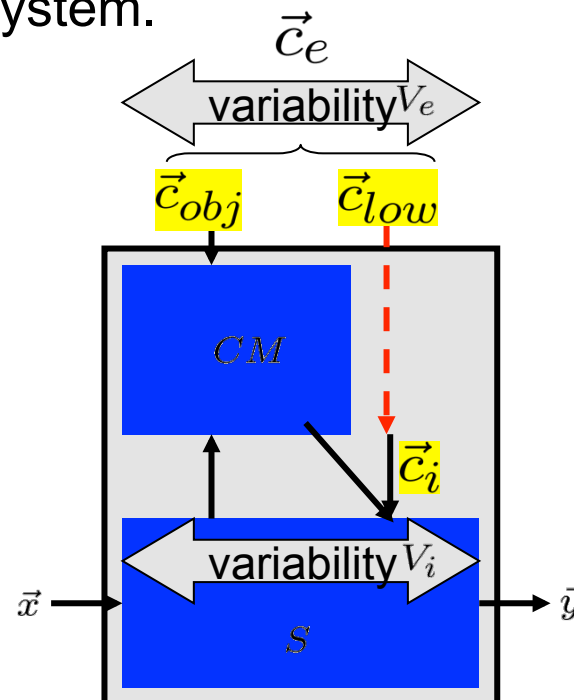


- ❑ We use the relation between external and internal control actions to characterize the **degree of autonomy**.
- ❑ The **origin** of the control actions  $c_i$  determines how autonomous a system is:
  - **External** origin of  $c_i$ , i. e.  $c_i = c_{low}$ : direct control by an external (e. g. human) operator, no autonomy.
  - **Internal** origin of  $c_i$ :  $S$  is fully controlled by  $CM$ .  $CM$  is part of the system  $S'$ . Full autonomy.
  - **Intermediate**: Control actions of type  $c_i$  and  $c_{low}$  are both used to control  $S$ .

- The autonomy of the system  $S'$  can be characterized by the complexity reduction  $R$

$$R = V_i - V_e$$

- If the system has been designed with the objective of having increasingly higher levels of abstraction,  $R$  will be a **positive** value.
- A **negative** value of  $R$  would indicate that the control mechanism leads to an **additional complexity** of the system.



- The (static) degree of autonomy  $\alpha$  of system  $S'$  is defined by

$$\alpha = \frac{R}{V_i} = \frac{V_i - V_e}{V_i}$$

- The value of  $\alpha$  will be at most 1 (if  $V_e = 0$ ).
- In this case, there is no external variability, i. e. there is no possibility to modify any attributes of  $S'$  by external control actions.
  - Such a system is called fully autonomous.

- ❑ If  $\alpha = 0$ , the internal and the external variabilities are the same, which indicates that there is no complexity reduction.
- ❑ If  $\alpha$  drops below zero, we have a situation where the external configuration space contains more controllable attributes than the internal configuration space.

- ❑ To characterize the **actual** degree of autonomy we must consider the total number of bits that have been actually used in all control actions over some time period  $[t_1, t_2]$ .
- ❑ **Definition:** Let  $\#c_e(t_i)$  and  $\#c_i(t_i)$  be the number of bits of the external and internal control actions at a certain discrete time  $t_i$ .
- ❑ The **dynamic complexity reduction**  $r$  in  $S'$  over some time interval  $[t_1, t_2]$  is defined as

$$r = \sum_{t_1}^{t_2} [\#c_i(t_i) - \#c_e(t_i)]$$

- ❑ The **dynamic degree of autonomy**  $\beta$  in  $S'$  over some time interval  $[t_1, t_2]$  is defined as

$$\beta = \frac{\sum_{t_1}^{t_2} [\#c_i(t_i) - \#c_e(t_i)]}{\sum_{t_1}^{t_2} [\#c_i(t_i)]}$$



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Quantitative approach

## Content

- ☐ Self-organization and autonomy
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- ☐ **Controlled self-organization**

- Intuition suggests that a self-organizing system is
  - a **multi-element system** (consisting of  $m$  elements,  $m > 1$ )
  - which needs no external control to restructure itself (i. e. it has a high degree of autonomy).
  
- A common assumption is that the control mechanism  $CM$  of a self-organizing system is (to a certain degree) **distributed over the  $m$  elements**.

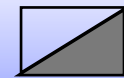
- The control mechanism (CM) can be:
  - centralized (one CM)
  - distributed over the  $m$  elements ( $m$  CMs)
  - distributed over a hierarchy of CMs
  
- Definition: Degree of self-organization
  - Count the number of CMs ( $= k$ ) in relation to the number of elements  $m$  of the system ( $k : m$ ).

- **Definition:** Let  $S$  be an adaptive system consisting of  $m$  elements ( $m > 1$ ) with large degrees of autonomy ( $\alpha$  and  $\beta$ ) and fully or partially distributed  $k$  control mechanisms  $CM$  ( $k \geq 1$ ) leading to a degree of self-organization of  $(k : m)$ .
- $S$  is called **strongly self-organised**, if  $k = m$ , i. e. the degree of self-organization is  $(m : m)$ .
  - $S$  is called **self-organised**, if  $k > 1$ , i. e. it has a medium degree of self-organization  $(k : m)$ .
  - $S$  is called **weakly self-organised**, if  $k = 1$ , i. e. there is a central control mechanism and the degree of self-organization is  $(1 : m)$ .

□ **Definition:** A self-organized system  $S'$  allows for controlled self-organization, iff:

- it has a nonempty external configuration space, i. e. we have  $V_e > 0$ , and
- it allows for external control actions of type  $\mathbf{c}_{obj}$ . (This implies an internal control mechanism CM!)

Goal := increasing height



$\vec{c}_{obj}$

