

Let  $W_{DS} \in \mathbb{R}^{|V_{DS}| \times d_1}$  and  $W_G \in \mathbb{R}^{|V_G| \times d_2}$  be the domain specific and generic word embedding matrices.

Let  $w_{i,DS}$  and  $w_{i,G}$  be the embedding of the word  $i \in V_\cap = V_{DS} \cap V_G$

Let  $\phi_{DS}$  and  $\phi_G$  be the projection directions of  $w_{i,DS}$  and  $w_{i,G}$ , respectively.

For each embedding of each word, we will project it like so (the  $\phi$ 's are like the  $a$  and  $b$  in the CCA tutorial):

$$\bar{w}_{i,DS} = w_{i,DS} \phi_{DS} \text{ and } \bar{w}_{i,G} = w_{i,G} \phi_G$$

and we'll maximize the correlation of this projection like so:

$$\rho(\phi_{DS}, \phi_G) = \max \frac{\mathbb{E}[\langle \bar{w}_{i,DS}, \bar{w}_{i,G} \rangle]}{\sqrt{\mathbb{E}[\bar{w}_{i,DS}^2] \mathbb{E}[\bar{w}_{i,G}^2]}}$$

We can repeat this process up to  $d = \min(d_1, d_2)$  times, such that each canonical variable is uncorrelated with the previous ones.

Once we do that, we have two matrices of projection vectors:  $\Phi_{DS} \in \mathbb{R}^{d_1 \times d}$  and  $\Phi_G \in \mathbb{R}^{d_2 \times d}$

Finally, for a particular word  $i$ , we achieve its domain-adapted word embedding like so:

$$w_{i,DA} = \frac{1}{2} w_{i,DS} \phi_{DS} + \frac{1}{2} w_{i,G} \phi_G$$