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Homework Due 10/12/17: (13 problems)
Section 4.2 pages 177 - 178; 1, 2, 4, 5(a)(c)(e)(g)(i)(k), 9, 10, 17, 18
Test up to 4.2.4 on 10/5/17
(theorem 4.2.1 is a possibility on test)
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Since 4.2.1 is a possibility, I'm going to redo it here:

Theorem 4.2.1

Assume that (s_n) and (t_n) are convergent sequences with $\lim s_n = s$ and $\lim t_n = t$. If $s_n \le t_n \ \forall \ n \in \mathbb{N}$, then $s \le t$.

Proof.

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Suppose, instead, that s > t. 

Let: \epsilon = \frac{(s-t)}{2} > 0

Now, we have 2\epsilon = s - t

t = s - 2\epsilon

s = t + 2\epsilon

t + \epsilon = s - \epsilon

By the definition of convergent sequences,

\exists \ N_1 \in \mathbb{N} \text{ st } n \geq N_1 \text{ implies } s - \epsilon > s_n > s + \epsilon

and, similarly

\exists \ N_2 \in \mathbb{N} \text{ st } n \geq N_2 \text{ implies } t - \epsilon > t_n > t + \epsilon

Let: N = \max{\{N_1, N_2\}}

Then, for n \geq N, we have

t_n > t + \epsilon = s - \epsilon > s_n

Which contradicts the assumption that s_n \leq t_n \ \forall \ n \in \mathbb{N}

Thus, we conclude that s \leq t
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Figure 1 shows a boat.



Figure 1: A boat.