- 1. How many orderings are there for a deck of 52 cards if all the cards of the same suit are together?
- 2. How many distinct positive divisors does the number $3^4 * 5^2 * 7^6 * 11^1$ have?
- 3. A committee of five people is to be chosen from a club that boasts a membership of 10 men and 12 women. How many ways can the committee be formed if it is to contain at least two women? How many ways if, in addition, one particular man and one particular woman who are members of the club refuse to serve together on the committee?
- 4. How many sets of 3 integers between 1 and 20 are possible if no two consecutive integers are to be in a set?
- 5. How many permutations are there of the letters of the word ADDRESSES? How many 8-permutations are there of these 9 letters?
- 6. List all 5-permutations, 3-combinations, and 4-combinations of the multiset {2 * a, 1 * b, 3 * c}.
- 7. How many integral solutions of $x_1 + x_2 + x_3 + x_4 = 30$ satisfy the following conditions:
 - a. $x_i \ge 0, \forall i$ b. $x_1 \ge 2, x_2 \ge 0, x_3 \ge -3, x_4 \ge 4$
- 8. Find a one-to-one correspondence between the permutations of the set $\{1, 2, ... n\}$ and the towers $A_0 \subset A_1 \subset ... A_n$, where $|A_k| = k$ for $k \in \{1, 2, ... n\}$
- 9. Provide an algebraic proof of Pascal's Formula.
- 10. What is the coefficient of x^5y^{13} in the expansion of $(3x 2y)^{18}$?
- 11. Use the binomial theorem to prove:

$$3^n = \sum_{k=0}^n \binom{n}{k} 2^k$$

12. Provide a combinatorial argument that

$$\binom{n}{k} - \binom{n-3}{k} = \binom{n-1}{k-1} + \binom{n-2}{k-1} + \binom{n-3}{k-1}$$

13. Provide two proofs (one algebraic, one combinatorial) that

$$\binom{n}{m} \binom{m}{k} = \binom{n}{k} \binom{n-k}{m-k}$$

14. What is the coefficient of

$$x_1^3 x_2^3 x_3^1 x_4^2$$
 in $(x_1 - x_2 + 2x_3 - 2x_4)^9$?

15. Prove by induction on n that, for a positive integer n,

$$\frac{1}{(1-x)^n} = \sum_{k=0}^{\infty} \binom{n+k-1}{k} x^k$$