

Page 27, Exercise 38, 58**Exercise 38**

Prove that $\forall n \in \mathbb{Z}, n^3 \bmod 6 = n \bmod 6$.

Page 24 Exercise 11

Let n and a be positive integers and let $d = \gcd(a, n)$. Show that the equation $ax \bmod n = 1$ has a solution iff $d = 1$. (This exercise is referred to in Chapter 2.

Let $a, n \in \mathbb{Z}^+$.

Let $d = \gcd(a, n)$

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Want to show: $ax \bmod n = 1 \Rightarrow d = 1$

Suppose $ax \bmod n = 1$.

\longleftarrow

Want to show: $d = 1 \Rightarrow ax \bmod n = 1$ Suppose $d = 1$.