

Assigned: Page 54, Exercise 2, 4, 23, 25, 33

Exercise 2

Which of the following binary operations are associative?

- a. subtraction of integers
- b. division of nonzero rationals
- c. function composition of polynomials with real coefficients
- d. multiplication of 2×2 matrices with integer entries
- e. exponentiation of integers

Exercise 4

Which of the following sets are closed under the given operation?

- a. 0, 4, 8, 12 addition mod 16
- b. 0, 4, 8, 12 addition mod 15
- c. 1, 4, 7, 13 multiplication mod 15
- d. 1, 4, 5, 7 multiplication mod 9

Exercise 23

(Law of Exponents for Abelian Groups)

Let a and b be elements of an Abelian group and let n be any integer. Show that $(ab)^n = a^n b^n$.

Is this also true for non-Abelian groups?

Exercise 25

Prove that a group G is Abelian iff $(ab)^{-1} = a^{-1}b^{-1}$, $\forall a, b \in G$.

Exercise 33

Suppose the table below is a group table. Fill in the blank entries.

	e	a	b	c	d			e	a	b	c	d
e	e	-	-	-	-			e	-	-	-	-
a	-	b	-	-	e	→		a	-	b	-	e
b	-	c	d	e	-			b	-	c	d	e
c	-	d	-	a	b			c	-	d	-	a
d	-	-	-	-	-			d	-	-	-	-