

fminunc

Find minimum of unconstrained multivariable function

Syntax

```
x = fminunc(fun,x0)
x = fminunc(fun,x0,options)
x = fminunc(problem)
[x,fval] = fminunc(...)
[x,fval,exitflag] = fminunc(...)
[x,fval,exitflag,output] = fminunc(...)
[x,fval,exitflag,output,grad] = fminunc(...)
[x,fval,exitflag,output,grad,hessian] = fminunc(...)
```

Description

fminunc attempts to find a minimum of a scalar function of several variables, starting at an initial estimate. This is generally referred to as unconstrained nonlinear optimization.

`x = fminunc(fun,x0)` starts at the point `x0` and attempts to find a local minimum `x` of the function described in `fun`. `x0` can be a scalar, vector, or matrix.

`x = fminunc(fun,x0,options)` minimizes with the optimization options specified in `options`. Use `optimoptions` to set these options.

`x = fminunc(problem)` finds the minimum for `problem`, where `problem` is a structure described in Input Arguments.

Create the problem structure by exporting a problem from Optimization app, as described in Exporting Your Work.

`[x,fval] = fminunc(...)` returns in `fval` the value of the objective function `fun` at the solution `x`.

`[x,fval,exitflag] = fminunc(...)` returns a value `exitflag` that describes the exit condition.

`[x,fval,exitflag,output] = fminunc(...)` returns a structure `output` that contains information about the optimization.

`[x,fval,exitflag,output,grad] = fminunc(...)` returns in `grad` the value of the gradient of `fun` at the solution `x`.

`[x,fval,exitflag,output,grad,hessian] = fminunc(...)` returns in `hessian` the value of the Hessian of the objective function `fun` at the solution `x`. See Hessian.

Examples

Minimize the function $f(x) = 3x_1^2 + 2x_1x_2 + x_2^2$.

Create a file `myfun.m`:

```
function f = myfun(x)
f = 3*x(1)^2 + 2*x(1)*x(2) + x(2)^2;    % Cost function
```

Then call `fminunc` to find a minimum of `myfun` near `[1,1]`:

```
x0 = [1,1];
[x,fval] = fminunc(@myfun,x0);
```

After a few iterations, `fminunc` returns the solution, `x`, and the value of the function at `x`, `fval`:

```
x,fval

x =
    1.0e-006 *
    0.2541    -0.2029

fval =
    1.3173e-013
```

To minimize this function with the gradient provided, modify `myfun.m` so the gradient is the second output argument:

```
function [f,g] = myfun(x)
f = 3*x(1)^2 + 2*x(1)*x(2) + x(2)^2;    % Cost function
if nargin > 1
    g(1) = 6*x(1)+2*x(2);
    g(2) = 2*x(1)+2*x(2);
end
```

Indicate that the gradient value is available by creating optimization options with the `GradObj` option set to 'on' using `optimoptions`. Choose the 'trust-region' algorithm, which requires a gradient.

```

options = optimoptions('fminunc','GradObj','on','Algorithm','trust-region');
x0 = [1,1];
[x,fval] = fminunc(@myfun,x0,options);

```

After several iterations `fminunc` returns the solution, `x`, and the value of the function at `x`, `fval`:

```

x,fval

x =
    1.0e-015 *
    0.1110    -0.8882

fval =
    6.2862e-031

```

To minimize the function $f(x) = \sin(x) + 3$ using an anonymous function

```

f = @(x) sin(x)+3;
x = fminunc(f,4);

```

`fminunc` returns a solution

```

x

x =
    4.7124

```