

MATH1023-01: Lecture Notes

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Author's Note

I have loosely based my notes on the format on the Feynman Lectures on Physics (<https://www.feynmanlectures.caltech.edu/>). All of the questions in this document are found in the book *Calculus Volume One* by Strang et al. [1].

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Chapter 1

Important Formulas

1.1 Linear Functions

1.1.1 Slope-Intercept Form

$$f(x) = mx + b \quad (1.1)$$

1.1.2 Point-Slope Form

$$y - y_1 = m(x - x_1) \quad (1.2)$$

1.1.3 Standard Form

$$ax + by = c, \quad (1.3)$$

$$a + b \neq 0 \quad (1.4)$$

1.1.4 Slope Formula

$$m = \frac{y_2 - y_1}{x_2 - x_1} \quad (1.5)$$

1.2 Quadratic Functions

1.2.1 Vertex Form

$$f(x) = a(x - h)^2 + k \quad (1.6)$$

1.2.2 Standard Form

$$f(x) = ax^2 + bx + c \quad (1.7)$$

1.3 Exponential Functions

1.3.1 Exponential Growth

$$f(x) = ab^x \tag{1.8}$$

1.3.2 Exponential Decay

$$f(x) = ab^{-x} \tag{1.9}$$

1.4 Logarithmic Functions

1.4.1 Common Logarithm

$$f(x) = \log_b(x) \tag{1.10}$$

1.4.2 Natural Logarithm

$$f(x) = \ln(x) \tag{1.11}$$

1.5 Trigonometric Functions

1.5.1 Sine Function

$$f(x) = \sin(x) \tag{1.12}$$

1.5.2 Cosine Function

$$f(x) = \cos(x) \tag{1.13}$$

1.5.3 Tangent Function

$$f(x) = \tan(x) \tag{1.14}$$

1.6 Limits

1.6.1 Definition of a Limit

$$\lim_{x \rightarrow a} f(x) = L \tag{1.15}$$

1.6.2 Limit Laws

$$\lim_{x \rightarrow a} [f(x) + g(x)] = \lim_{x \rightarrow a} f(x) + \lim_{x \rightarrow a} g(x) \quad (1.16)$$

$$\lim_{x \rightarrow a} [f(x) - g(x)] = \lim_{x \rightarrow a} f(x) - \lim_{x \rightarrow a} g(x) \quad (1.17)$$

$$\lim_{x \rightarrow a} [cf(x)] = c \lim_{x \rightarrow a} f(x) \quad (1.18)$$

$$\lim_{x \rightarrow a} [f(x)g(x)] = \lim_{x \rightarrow a} f(x) \lim_{x \rightarrow a} g(x) \quad (1.19)$$

$$\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \frac{\lim_{x \rightarrow a} f(x)}{\lim_{x \rightarrow a} g(x)} \quad (1.20)$$

$$\lim_{x \rightarrow a} [f(x)]^n = [\lim_{x \rightarrow a} f(x)]^n \quad (1.21)$$

$$\lim_{x \rightarrow a} \sqrt[n]{f(x)} = \sqrt[n]{\lim_{x \rightarrow a} f(x)} \quad (1.22)$$

$$\lim_{x \rightarrow a} \sqrt[n]{f(x)} = \sqrt[n]{\lim_{x \rightarrow a} f(x)} \quad (1.23)$$

$$\lim_{x \rightarrow a} f(x)^{g(x)} = \left[\lim_{x \rightarrow a} f(x) \right]^{\lim_{x \rightarrow a} g(x)} \quad (1.24)$$

$$\lim_{x \rightarrow a} \frac{1}{f(x)} = \frac{1}{\lim_{x \rightarrow a} f(x)} \quad (1.25)$$

$$\lim_{x \rightarrow a} \frac{1}{f(x)} = \frac{1}{\lim_{x \rightarrow a} f(x)} \quad (1.26)$$

$$\lim_{x \rightarrow a} \frac{1}{f(x)} = \frac{1}{\lim_{x \rightarrow a} f(x)} \quad (1.27)$$

$$\lim_{x \rightarrow a} \frac{1}{f(x)} = \frac{1}{\lim_{x \rightarrow a} f(x)} \quad (1.28)$$

$$\lim_{x \rightarrow a} \frac{1}{f(x)} = \frac{1}{\lim_{x \rightarrow a} f(x)} \quad (1.29)$$

Chapter 2

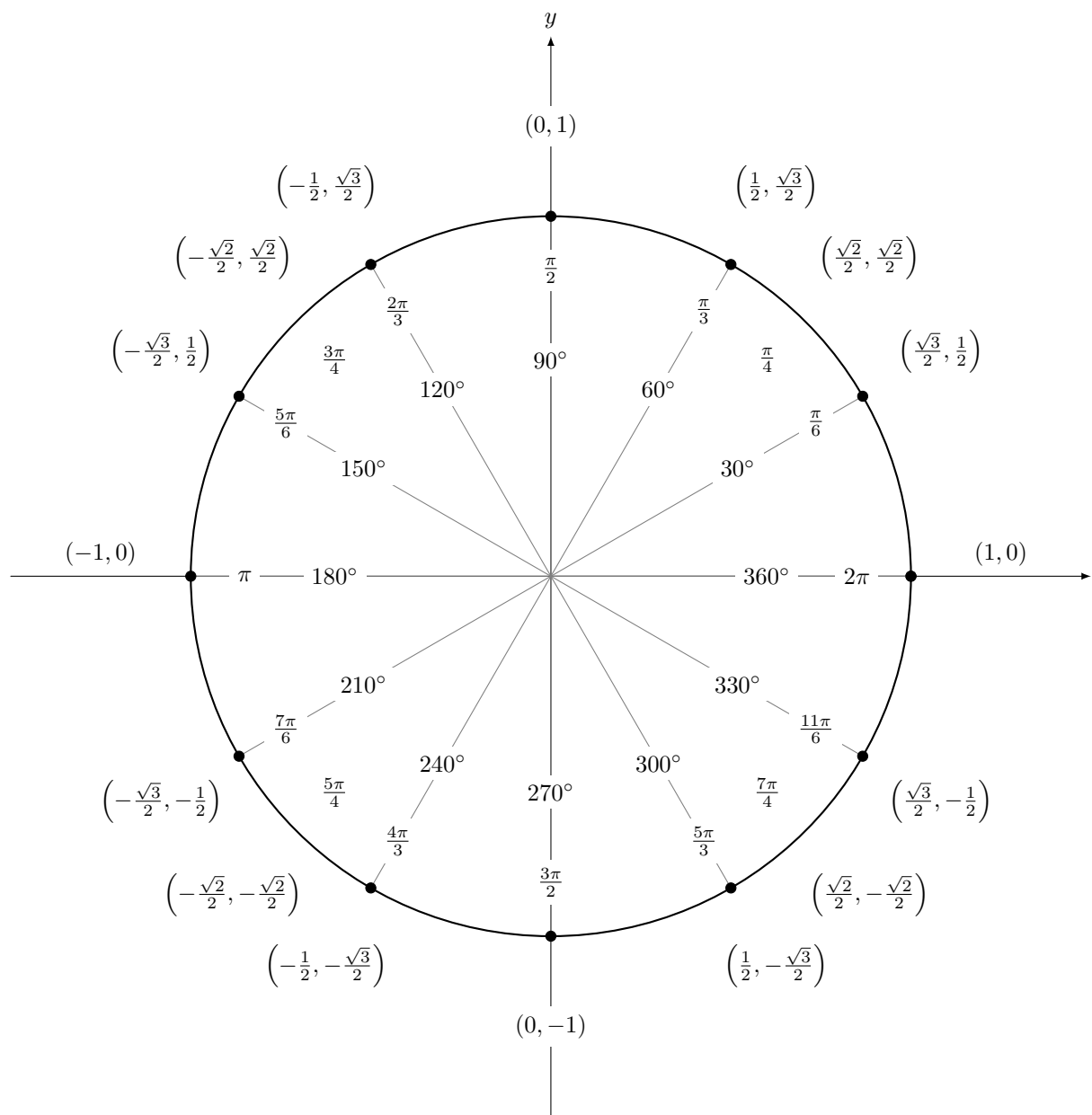
Definitions

2.1 Linear Functions

One of the most important functions in mathematics is the linear function. A linear function is a function that can be written in the form $f(x) = mx + b$, where m is the slope of the line and b is the y -intercept.

2.2 Unit Circle

The unit circle is a circle with a radius of 1. It is centered at the origin of the coordinate plane and is used to define the trigonometric functions.



Chapter 3

Review of Functions

3.1 Introduction

This is the introduction section of my document.

3.2 Linear Functions

A linear function is a function that can be written in the form $f(x) = mx + b$, where m is the slope of the line and b is the y -intercept.

3.2.1 Hyperbolic Functions

Hyperbolic cosine

$$\cosh x = \frac{e^x + e^{-x}}{2} \tag{3.1}$$

Chapter 4

Limits

4.1 Introduction

This is the introduction section of my document.

4.2 Intutive Definition of a Limit

$$\lim_{x \rightarrow a} f(x) = L \quad (4.1)$$

Definition of a Limit. The limit of a function $f(x)$ as x approaches a is L if for every $\epsilon > 0$ there exists a $\delta > 0$ such that if $0 < |x - a| < \delta$, then $|f(x) - L| < \epsilon$.

Example 1. Enter an example here.

Important. It is important that...

Formula. Enter a formula here.

Proof. This is a proof

$$s(t) = \text{position of the object at time } t \quad (4.2)$$

Example 2.2.

$$s(t) = 16t^2 + 64$$

a) $[0.49, 0.50]$

$$\frac{s(0.5) - s(0.49)}{0.5 - 0.49} = -15.84 \quad (4.3)$$

b) $[0.50, 0.51]$

$$\frac{s(0.51) - s(0.5)}{0.51 - 0.5} = 16.16u \quad (4.4)$$

Bibliography

- [1] Gilbert Strang et al. *Calculus Volume 1*. EN. OpenStax, Mar. 2016. ISBN: 978-1-947172-13-5. URL: <https://openstax.org/details/books/calculus-volume-1/>.