FS22 Data Visualization and Analysis

Exercise Session 4 Vector Field Visualization in Python





Vector Field Features

Vector Field Features Divergence

- Think of vector field as encoding a fluid flow
- Is a local measure of its "outgoingness", at a point in D
- Given a field $\mathbf{v}: \mathbf{R}^3 \to \mathbf{R}^3$, div $\mathbf{v}: \mathbf{R}^3 \to \mathbf{R}$ is

$$\operatorname{div} \mathbf{v} = \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} + \frac{\partial v_z}{\partial z}$$

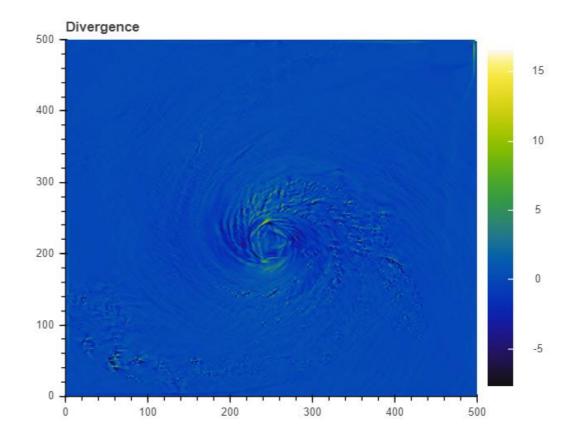
For 2D case, the divergence degenerates to:

$$\operatorname{div} \mathbf{v} = \frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y}$$

Vector Field Features Divergence

- Compute using numpy.gradient() function. Calculates the gradient of a vector field w.r.t. all directions. Carefully choose which part of the result you actually need for the divergence calculation.
- Visualize the divergence using bokeh image() function





Vector Field Features Vorticity

- Consider again a vector field as encoding a fluid flow
- Measures how quickly the flow 'rotates' around each point
- Given a field $\mathbf{v}: \mathbf{R}^3 \to \mathbf{R}^3$

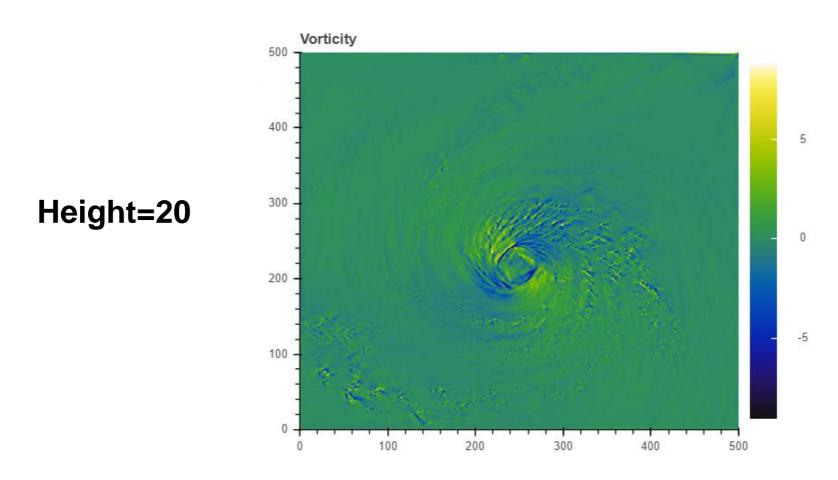
$$\operatorname{rot} \mathbf{v} = \left(\frac{\partial v_z}{\partial y} - \frac{\partial v_y}{\partial z}, \frac{\partial v_x}{\partial z} - \frac{\partial v_z}{\partial x}, \frac{\partial v_y}{\partial x} - \frac{\partial v_x}{\partial y} \right)$$

 For 2D cases, the derivations of the z-component and the derivation of the x- and y-component w.r.t. the z-direction become 0. Therefore, the magnitude of the vorticity can be computed using the following equation:

$$rot \mathbf{v} = \frac{\partial v_y}{\partial x} - \frac{\partial v_x}{\partial y}$$

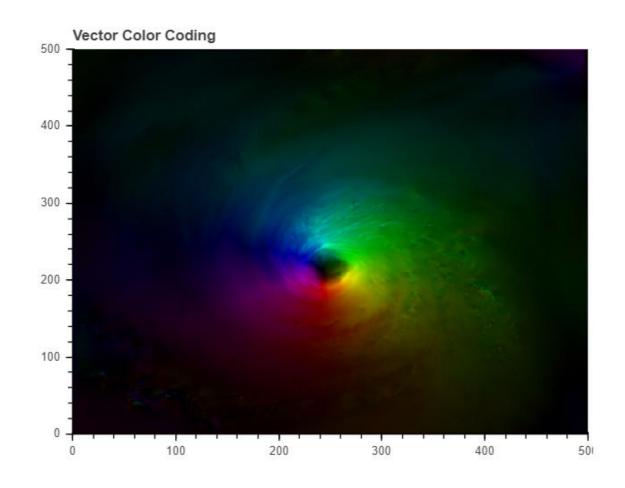
Vector Field Features Vorticity

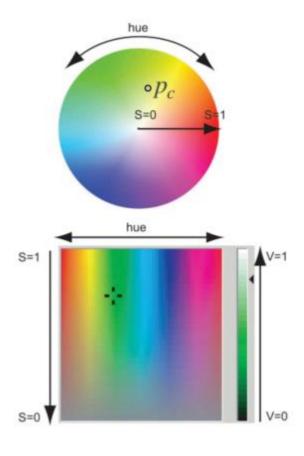
- Compute using definition with partial derivatives. Find out how you can use the numpy.gradient() results to achieve this.
- Visualize angular velocity using bokeh image() function



Vector Field Features Vector Color Coding

- Associates the orientation and magnitude of a vector with a color.
- Find angle between x-axis and a given vector. Perform an HSV to RGB color conversion. Formula: https://www.rapidtables.com/convert/color/hsv-to-rgb.html

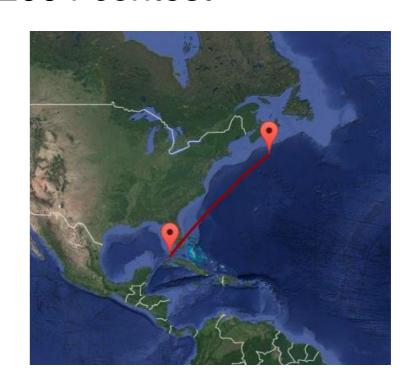




Exercise 4 Instructions

Exercise 4 Instructions Hurricane Dataset

- Dataset was used in IEEE Visualization 2004 contest
 - http://vis.computer.org/vis2004contest/data.html
- Summary of the data information
 - Hurricane Isabel (2003)
 - 13 Variables, 48 timesteps, data size 500 x 500 x 100
 - Each height point is 0.2km, max 19.8km
 - Format: Brick-of-Floats



Exercise 4 Instructions Hurricane Dataset

- Visualization of X, Y wind speed at time step 20
 - shows the wind speed as images at a certain height
 - Positive x-direction is West to East and positiv y-direction is South to North

