# **TMA4268 Statistical Learning**

## Chapter 10: Unsupervised Learning

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# Lab 2: Clustering

## **K-Means Clustering**

#### Simulate data

Lets simulate data with the intention to create two clusters:

```
set.seed(2)
x=matrix(rnorm(50*2), ncol=2)
x[1:25,1]=x[1:25,1]+3
x[1:25,2]=x[1:25,2]-4
```

#### Perform k-means

The function kmeans() performs K-means clustering in R. We now perform K-means clustering with K = 2.

```
km.out=kmeans(x,2,nstart=20)
```

To run the kmeans() function in R with multiple initial cluster assignments, we use the nstart argument. The kmeans() function will report only the best results.

## **Cluster assignments**

The cluster assignments of the 50 observations are contained in km.out\$cluster:

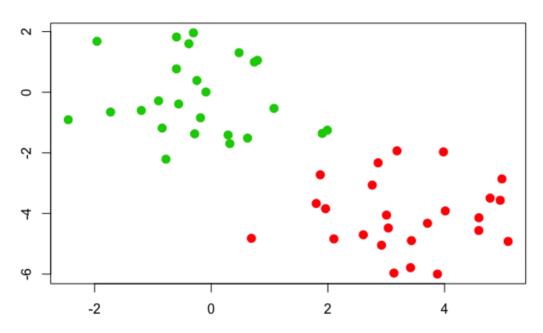
```
km.out$cluster
```

#### Plot the data

We can plot the data, with each observation colored according to its cluster assignment.

```
plot(x,
     col=(km.out$cluster+1),
     main="K-Means Clustering Results with K=2",
     xlab="", ylab="", pch=20, cex=2)
```

#### K-Means Clustering Results with K=2



#### kmeans with k = 3

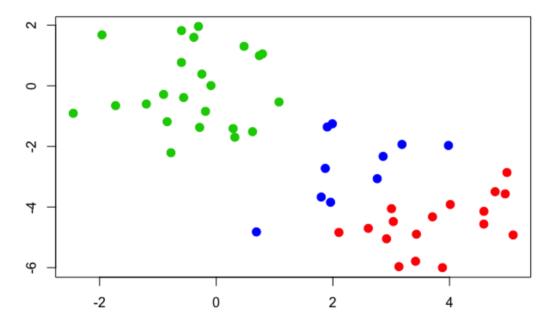
However, for real data, in general we do not know the true number of clusters. We could instead have performed K-means clustering on this example with K = 3.

```
set.seed(4)
km.out=kmeans(x,3,nstart=20)
km.out
```

```
## K-means clustering with 3 clusters of sizes 17, 23, 10
##
## Cluster means:
## [,1] [,2]
## 1 3.7789567 -4.56200798
## 2 -0.3820397 -0.08740753
## 3 2.3001545 -2.69622023
##
## Clustering vector:
```

```
plot(x, col=(km.out$cluster+1), main="K-Means Clustering Results with K=3",
    xlab="", ylab="", pch=20, cex=2)
```

#### K-Means Clustering Results with K=3



## **Multiple starting points**

We compare using nstart=1 to nstart=20.

```
set.seed(3)
km.out=kmeans(x,3,nstart=1)
km.out$tot.withinss
```

```
## [1] 97.97927
```

```
km.out=kmeans(x,3,nstart=20)
km.out$tot.withinss
```

```
## [1] 97.97927
```

Note that km.out\$tot.withinss is the total within-cluster sum of squares, which we seek to minimize by performing K-means clustering.

We strongly recommend always running K-means clustering with a large value of nstart, such as 20 or 50, since otherwise an undesirable local optimum may be obtained.

## **Hierarchical Clustering**

The hclust() function implements hierarchical clustering in R. We will use the data simulated in the K-means section.

Next, we will compute hierarchical clustering dendrogram using complete, single, and average linkage clustering, with Euclidean distance as the dissimilarity measure.

### Perform hierarchical clustering

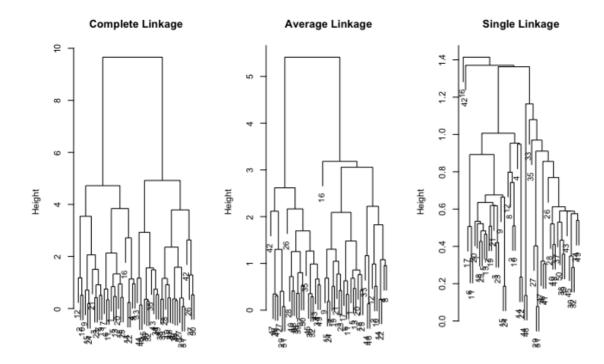
The dist() function is used to compute the  $50 \times 50$  inter-observation Euclidean distance matrix.

```
hc.complete=hclust(dist(x), method="complete")
hc.average=hclust(dist(x), method="average")
hc.single=hclust(dist(x), method="single")
```

## **Plot dendograms**

We can now plot the dendrograms obtained using the usual **plot()** function. The numbers at the bottom of the plot identify each observation.

```
par(mfrow=c(1,3))
plot(hc.complete,main="Complete Linkage", xlab="", sub="", cex=.9)
plot(hc.average, main="Average Linkage", xlab="", sub="", cex=.9)
plot(hc.single, main="Single Linkage", xlab="", sub="", cex=.9)
```



## **Cluster assignment**

To determine the cluster labels for each observation associated with a given cut of the dendrogram, we can use the cutree() function:

For this data, complete and average linkage generally separate the observations into their correct groups.

### Single linkage singletons

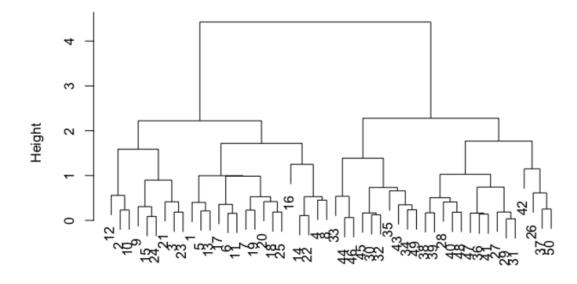
However, single linkage identifies one point as belonging to its own cluster. A more sensible answer is obtained when four clusters are selected, although there are still two singletons.

## **Scaling the variables**

To scale the variables before performing hierarchical clustering of the observations, we use the scale() function:

```
xsc=scale(x)
plot(hclust(dist(xsc), method="complete"), main="Hierarchical Clustering with
    Scaled Features")
```

### **Hierarchical Clustering with Scaled Features**



dist(xsc) hclust (\*, "complete")

### **Correlation-based distance**

Correlation-based distance can be computed using the <code>as.dist()</code> function, which converts an arbitrary square symmetric matrix into a form that the <code>hclust()</code> function recognizes as a distance

matrix.

However, this only makes sense for data with at least three features since the absolute correlation between any two observations with measurements on two features is always 1.

```
# Code below is to check the statement above.

x=matrix(rnorm(5*2), ncol=2)
dd=as.dist(1-cor(t(x)))
dd
```

```
## 1 2 3 4

## 2 2

## 3 2 0

## 4 2 0 0

## 5 0 2 2 2
```

```
x=matrix(rnorm(5*3), ncol=3)
dd=as.dist(1-cor(t(x)))
dd
```

```
## 1 2 3 4

## 2 1.765076e+00

## 3 1.638313e+00 1.595186e-02

## 4 1.630165e+00 1.788151e-02 5.554177e-05

## 5 1.954130e+00 7.722732e-02 1.605010e-01 1.662744e-01
```

Hence, we will cluster a three-dimensional data set.

## Complete Linkage with Correlation-Based Distance

