

Rolaton: To a called h-do found
Roberty: The control of M (Very har) s.t. Yo Har: her (For W) = \$\phi\$ or (phxp)
(F; >) ntx(*)
EX: Flor lines of a non-various Vector titeld are n-transacra toleratures
If h=n-n =) 5 = V TeF(P) D a hyperpione foold
"every foliation of color of whice a home a foliation?"
Q'helen doos a hyperpleire come hom a foliation?"
Teom 2 [framius]
ker (a) = & (T) is manced by a foram (=) and a = 0
digressivi en: tem 1- Form In lin
$\forall \rho \in (0, \cap)^{\times}$
Let $x_1,, t_n$ be coordinates on \bigcap
$\Rightarrow \alpha_i = \sum_{i=1}^{n} c_i (a) x_i $ $\Rightarrow \alpha_i = \sum_{i=1}^{n} c_i (a) x_i $ $\Rightarrow \alpha_i = \sum_{i=1}^{n} c_i (a) x_i $
heron M: Bo: (Tom) x x (Tym) IR nutilities, alternating
A-Product:
$A = \{ c, d \};$ $A = \{ c, d \}$
Differential dx, 1 dx, = 0
d: h- Form -) (htn)-Forms
$\sum_{i} C_{i}(\rho) d = \longrightarrow d \alpha$ $\sum_{i} \frac{\partial C_{i}}{\partial x_{i}} d x_{i} \wedge d x_{i}$

 $\frac{t \cdot x}{d \cdot x} = \ln_{(yy,z)}^{2} \propto d \times d \times d \times d \times d \times d \times = 0$ =) \alpha / da con from a foliable $(2) \quad \alpha = \times d_{7} + d_{2}$ $d\alpha = d(xdy + dz) = d(xdy) + d(dz) = \frac{\partial^{*}}{\partial x} dx dy + \frac{\partial^{*}}{\partial y} dydy$ ornda= (xdy Ldz)n (lxndy)= xdyn(dxndy) + dzndxndy an (da) - andan. ndo * of D carled contact form If the reels vector fireld R_{α} of α is demy $\begin{cases} \lambda_{\alpha}(\Lambda_{\alpha_{1}}) \equiv 0 \\ \alpha(\Lambda_{\alpha}) \equiv 1 \end{cases}$ nervh: 91 (da)" is a sol fun =) (o new Nor * $\frac{1}{3}$ = her (α) - her (α) - (α) α = $f(\alpha)$ for f: -> In {o} $\Rightarrow \alpha \wedge (d\alpha)^n = (+\alpha) \wedge (d(+\alpha))^n =$ fan (far + dfna)" $= \int_{0}^{n+2} \sqrt{(Ja)^{n}}$ Rais well-defined;

or N (day) fo =) (day) fo =) day his rank zn

zndamon =) rev (day) is n-dn

zm/le & or fo on ker(day)

Worston (on : (closed =) It control for a an or la a perote orst 10 (+1, 41, 1-1/2, 17m, Z) Ex (1) (ononler Standard contact Structure Sst = Ker (Ost) $\alpha_{st} = \left(\begin{array}{c} 2 \\ 5 \end{array} \times \lambda_{\gamma_i} \right) + \lambda_{z}$ = ({ x,dy, +dz) / (d({ x, 1, + 1, 2))" = ({ x, 1, + 1, 2 }) / ({ d x, 1, dy,)" and a (dast)" = dz / n (d x, ndyn / duz/ drin... n / h, n / n) - n | d x, ndyn / duz/ drin... n / h, n / n / z & f 0 Compre Rost = $(\{A, J, +B, \partial_{7}\}) + C \partial_{7}$ $d_{est}\left(\bigcap_{st} st, e \right) = \left(\bigwedge_{st} A_{s} d_{s} - B_{s} d_{s} \right) = 0$ $A_{t} = (n_{st}) = c + c_{sin} = 1$ One solution: $N_{orst} = \partial_{\frac{1}{2}}$ (2) $S_{yy} = her \left(\frac{S_{yy}}{S_{yy}} \left(\frac{S_{yy}}{S_{yy}} - \frac{S_{yy}}{S_{yy}} \right) + dz \right)$ Horsework: This is a constact smuchne · Ra = 72. · for n=1: toan this · read milher: Topology for a alternal very int Jelby Lee

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\frac{\text{New }(1)}{\text{CD}} \cdot \left( \frac{\text{New }(2)}{\text{New }(2)} - \frac{3^{2} \text{New }(2)}{\text{CD}} \right) \cdot \left( \frac{\text{Cornel confold}}{\text{CD}} \right)
\frac{\text{Cornel confold}}{\text{CD}} \cdot \left( \frac{\text{New }(2)}{\text{CD}} - \frac{3^{2} \text{New }(2)}{\text{CD}} \right) \cdot \left( \frac{\text{Cornel confold}}{\text{CD}} - \frac{3^{2} \text{New }(2)}{\text{CD}} \right)
                                                                                                                   (19, 23
   (x1, 41, 1..., xn, 4n, 2)

(x1, 41, 1..., xn, 4n, 2)

(x1, 41, 1..., xn, 4n, 2)

(x1, 41, 1..., xn, 4n, 2)
                                       (2) \alpha_{s_7-} = (\frac{7}{2} \times \lambda_1 - 7, h_{s_1}) + \lambda_7 = ) \alpha_{s_7-} \wedge (\lambda \alpha_{s_7-})^{-} + 0
 (3) 1h3 un combred worders (0,1,2)
          \int_{07}^{\infty} = \ker (\alpha_{07}) = \ker (\cos(r)^{1/2} + r \sin(r) d\theta)
                      αοΤΛ ΔασΤ = [(r 5-2 r) - (~ (052 r)) landr Λ 12
                                 = - [1+ sin (1) (10)(1)] r d d A d ( A d 2 to)
bress: f: ((10,2) (1,4,2) (1 you pull that back, you get.

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Admin: [Contacto noiphism;)
    · f: (m, S) - (mz (3)) o caned Contacton orphism
      (i.e. f^*(a_2) = g \cdot a_1 for y = g \cdot a_1)

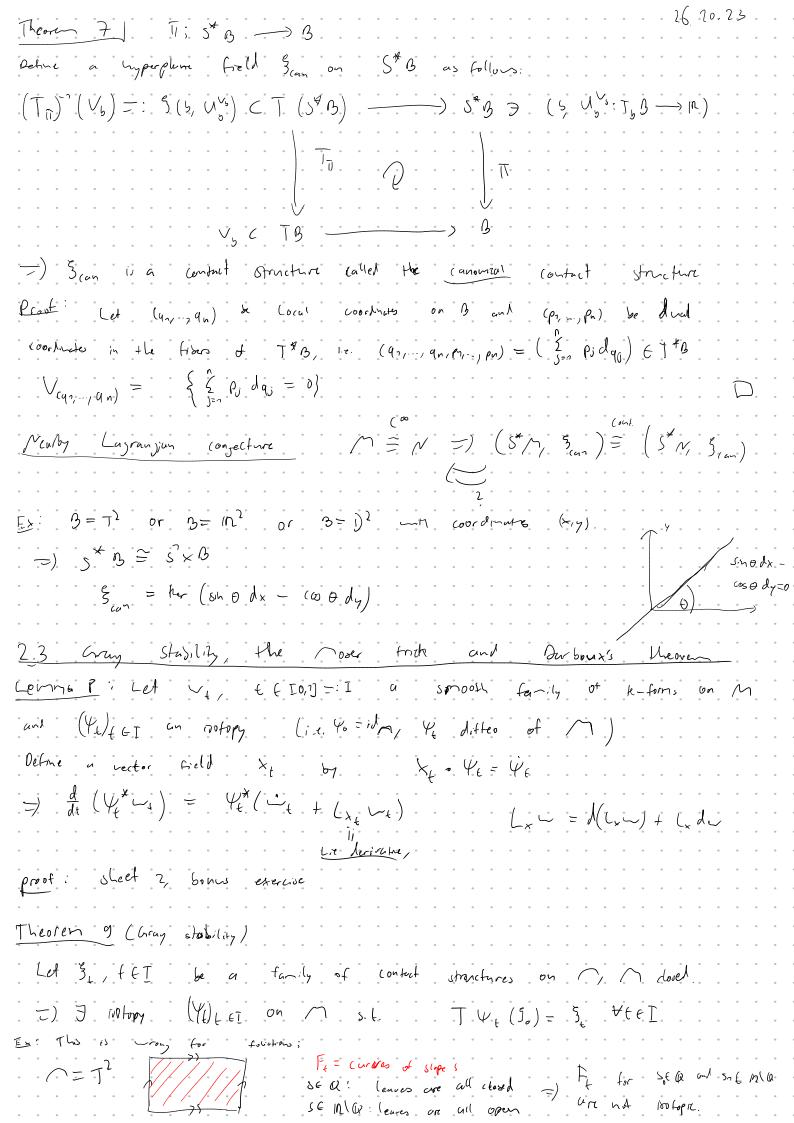
(i.e. f^*(a_2) = g \cdot a_1 for y = g \cdot a_1)

f(g_1) = g_2
     pollousi for y _____
          02 a 7- for on 12
      SHORT: f * \alpha_1(x) = \alpha_2 (f(x))
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Empty:
$$f:(n^{2n}, 5_{1}) \longrightarrow (n^{2n}, 5_{1})$$
 $f:(n_{1}, 2) \mapsto (n^{2n}, 5_{1}) \longrightarrow (n^{2n}, 5_{1})$
 $f:(n_{1}, 2) \mapsto (n^{2n}, 5_{1}) \longrightarrow (n^{2n}, 5_{1})$
 $f:(n_{1}, 2) \mapsto (n^{2n}, 5_{1}) \longrightarrow (n^{2n}, 5_{1}) \mapsto (n^{2n}$

Det: A symplate form 0 a 2-form w dw = 0 & m 0 a volume form ξ_{κ} : $(N_{5}n)$ $W_{5+} := \xi$ $d_{5+} V d_{5+}$ Del: a Louville vector Geld y on $(W_{l} u)$ is a vector buy $S_{l} + d(u(y, \cdot)) = d(lyu) = u$ l := plug inEx: Y= ? ([x: dx: + y: dy:) 15 lookentle on (n2 _ st) Ly Lost = 7 (2 x d7; -7; dx) =) d (4 Vst) = Vst Let y se Lioning on (Will) a:= ly l 13 a comprét for on every hypersortage 2002 W transverse to y S247 (Pin (Ust) o transverse to y===r2r 122 =) a= iy~st s a contact form = 2 5 Azi - 4. Azi Honeren; check directly that as a contact form on 529-3 oslet): $\ker(\alpha) = 3$ 84

proof (Lemis 5): $\alpha \wedge (d \alpha)^n = (d (y -))^{n-2}$ compre & explishy $= \frac{7}{5} \left(y C^{n} \right)$ $(Ja)^{n-1} to$ on 1 trajune 19 9 $\left(f_{\sigma} \sim (4, 4) = 0\right)$ Cover a manfold of the space of contact elements (b, Vb) | b & B D Vb C To B Coonword hypromin Spice of contact elemb = 5th (changet) (b, vb) min Vo Top Sir hocary Vs ormed & coonered Crob is wright up to suly



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Droof (the of an moser truth)

Let at smooth s.f. he (at) = 3t. Need to construct:
                                                                                                                                                                                               Y_t \sim 11 \quad Y_t^*(a_t) = \lambda_t a_0,
                                                                                                                                                                                                Assume 4t is the flow of a rector field X_t
                                                                                                                                                                                               =) \frac{d}{dt} \left( Y_t^* (\alpha_t) \right) = \lambda_t \alpha_0 = \frac{\lambda_t}{\lambda_t} \cdot Y_t^{*} \alpha_t = Y_t^* (\mu_t \alpha_t)
 with Cerna P, on the steer hand, we have
                      \frac{d}{d+}\left(\psi_{\ell}^{\star}(\alpha_{\ell})\right) = \psi_{\ell}^{\star}\left(\alpha_{\ell} + L_{\chi_{\ell}}^{\star}\alpha_{\ell}\right) = \psi_{\ell}^{\star}\left(\alpha_{\ell}^{\star} + \lambda(\alpha_{\ell}(\chi_{\ell})) + L_{\chi_{\ell}}(\lambda_{\ell})\right).
    As \psi_f is a diffeomorphism, this is equivalent to
(=) p_t \cdot \alpha_t = \dot{\alpha_t} + d(\alpha_t(x_t)) + \iota_{x_t}(d\alpha_t)

[t further one x_t \in \mathcal{A}_t = ter(\alpha_t)
Fluxying in Ray we ustrin \mu_{\xi} = \alpha_{\xi} (Rat).
 · Define V_t := \dot{\alpha}_t(N_{Ot})
· Roy Ehr (M, Ox - ax) & day | 5 to on degenerate =) Il solution XI & g of & Ox (Lover >) that Yx of Xx or Boronly defined
Det A vector field on ( ) 3= her (a) ) or culted contact vator field ( on the total field ) = 5 to the (3) = 5
    (=) Lx a = Ma for M: M->IN
\times = \star d \star + y d y
                              L_{x} = d \alpha(x) + l_{x} d \alpha
                                                       = (0) 0 dx + m + dy - x sn + de + y con + de + zh + y - (0) + y + 1 = (0) + (x (0) + dx + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) + (0) +
                 =) X s a contact rector Grd/
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This 10: Lot or with 3 = her or. Then $\begin{pmatrix}
\text{output} \\
\text{vector} \\
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\begin{pmatrix}
\text{n:7} \\
\text{co}(\text{n}) \\
\text{mills}
\end{pmatrix}$ $\propto (x) = 1 + x$ $(x_{H}) = A + (N_{\alpha})^{\alpha - 1/4} = x_{H}$ $\int d^{4}x (\Omega_{\alpha}) + \lambda_{\alpha}(\lambda_{1}\Omega_{\alpha}) = \mu \cdot \frac{\alpha(\Omega_{0})}{2}$ $=) \quad (\times \wedge \circ = \wedge H^{x}(\, \mathbb{N}^{\circ}) \cdot \wedge - \wedge H^{x}$ " Cuch H. Detine XH as a sovi • $L_{\times_{H}} \alpha = d(\alpha(\times_{H})) + (x_{H} d\alpha = d + (n_{\sigma}) \alpha =) \times_{H} ,$ • HxH = Q(XA)=H Then is (Darboux) Let or be a contact form on M2nn and let pEM -) I NOHO UCA of P & coordinates (1, ..., x, y,..., yn, t) on U S.t. $\rho := (0, ..., 0)$ and $\alpha |_{U} = (\hat{f}, \kappa, \lambda_{13}) + \lambda_{2}$ proof (via root fith) W(09 n=1020+1) (because he are worting locally) and p=0 (house coordinates c.f. on $T_0(\Omega^{2n+2}: \alpha(\partial_{\bar{x}})=\gamma)$ ($\partial_{\bar{x}} d\alpha = 0$; $\partial_{x_{j-1}} y_j \in d\alpha$ and $\partial_{x_{j-1}} \partial_{x_{j-1}} \partial_{x_{j$ Define $\propto 0 := \left(\sum_{j=1}^{2} \times_{j} dy_{j}\right) + dz$ $x \in (1-t) \propto t + t \propto t$ =) of: (1-t) as + ta, te] Moder frich: Assume Yt at = as for Yt fle flow of xt Lemma ($\forall_{t} (\alpha_{t} + L_{x_{t}} \alpha_{t}) = 0$ (=) $\alpha_{t} + d(\alpha_{t} (x_{t})) + C_{x_{t}} d\alpha_{t} = 0$ where $x_{t} = H_{t} R_{\alpha_{t}} + y_{t}$ for $y_{t} \in \ker(\alpha_{t})$ & plus in that; $\alpha_{t}(R_{\alpha_{t}}) + dH_{t}(R_{\alpha_{t}}) = 0$ On a NBHD of poor ver not his no closed onthe of the city He (0)-0 difference of the long Define Y_t by $\alpha_t + \lambda H_t + (y_t \lambda \alpha_t = 0) = \lambda_t(0) = 0$) $Y_t := F_t \circ \lambda_t \circ$

2.4 July of contrict long a: let [(/ 2 m) t) $\Rightarrow \sim (C) \leq h$ (f nm (L) = n =) L Cayron Broot: i; L C > C (= hv(a) TL L 9 (=) (*a=0 TpL (5 5, 1 d als,) Te L (To L) dals, = { v ∈ 1, $d\alpha (U,U) = 2$ $\forall \alpha \in \{p \downarrow \}$ Conor I : 3, -) î, L. V (V) | () | () | () | > 2n = 0in (9,)= Din (m) + on (m) > 2 (ToL) dal 90 Let 3 be a 5- 11 2 52 a 2- Plane fresh on ... Cot I (M A swifing & (U,V) coul. on { near P = (0,0) } { 0 (4,0)1= 4 (Tu,0) [, 5,00) 3 has contact & order at least K wh E at p (Es d(4,1)) is at true 0 (|(h)) hr (u,v) -> (v,0), i.e. $\frac{\partial(u,v)}{(u,v)^h}$ & c to (u,v) -> (0,0).

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Thom 13: 5 is contract at pEN E) & S CN 1/4 pE &:

This order of contract at most n m & st p.
prost: Llas = (N3) pro 2 90 = (x17) - Plane
  3=hr(dz + a(x,1,2) dx + s(27,2) dy)
~ (0)=0=S(0)
 f is contact at p \in (\alpha \wedge 1) p
                                                           (- 39 (0) + 35 (0)) 8 x y x y x y F
                  (o)
             = \begin{cases} \begin{cases} f & \text{order of control at less} \\ f & \text{order of } \end{cases} 
= \begin{cases} f & \text{order of } \\ f & \text{order of } \end{cases} 
    f(0,0) = f_{x}(0,0) = f_{y}(0,0) = 0
  3 = xd = -a)z/25-b/z >
      -) ng(x17)= a(v17, f(74)) 2x + b(x4, 6(514))My + 2z
          h_{\xi}(y_{1}) = - (x(x_{1})) \times - (y(y_{1})) = \frac{[y_{1}(y_{1}) \times y_{2}(y_{1})]^{2}}{[y_{1}(y_{1}) \times y_{2}(y_{1})]^{2}}
     h(x,y):= sm2(0(xy)) =
                                          [ng [2 | 1 ng 2
                     (3+62)^{2}+(a+f_{x})^{2}+(5f_{x}-af_{y})^{2}
5) of (n) compact who I of order at last I E ((44) units to order (
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l_{1}(l_{1}(y)) \cdot l_{1}(y) + l_{2}(y) = 0 \\
l_{2}(y) \cdot l_{2}(y) + l_{2}(y) = 0
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l_{3}(y) \cdot l_{3}(y) + l_{3}(y) = 0 \\
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