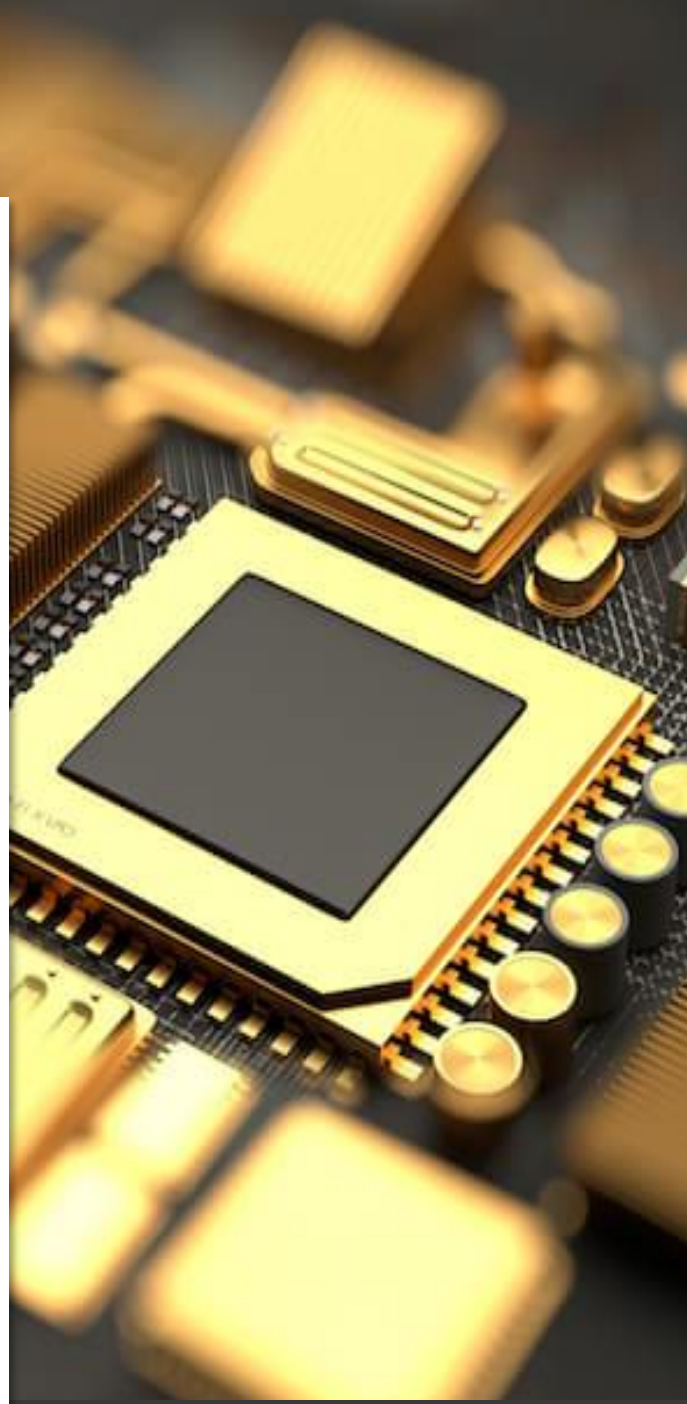


OpenMP Vector Sorting

COMPUTER ARCHITECTURE

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Introduction

For this assignment we have used two different kind of processors, the ones that we had available at the moment of doing the measures. These processors are ' **Intel Core i7-8750H** ' and ' **Intel Core i5-7200U** ' respectively.

We thought that taking measures with both of them could be interesting, in order to also show what is the difference between two different kinds of processors exetucing the same program, and how do they improve their preformance with the parallelization of the program.

Furthermore we have depicted in some plots how the execution time behaves when we 'play' with different vector sizes, these plots are, in a more precise way, dot plots with a line that shows in a better what we have said.

One thing to take into account is that the Task 2 is not explained in this document, as it was required to be explained as comments in the source code.

Task 1

For this task, as it is stated in the assignment, we have taken some measures and collected the more significant of them in the following charts. Time is measured in **ms** and size of the vector refers to the number of elements that the vector. (The complete set of measures is placed at the end of this document)

Intel Core i5-7200U

Size Alg	10	100	1000	10000	100000	200000
A	0.03025799	0.11798233	1.95284766	106.1719299	5644.5460390	20460.150972
B	0.02289666	0.08530766	2.29401566	83.91503000	8314.5898930	31102.613464
C	0.02942833	0.20012600	6.97919060	312.0844530	37636.218750	140526.68696
D	0.02826400	0.19659600	7.38811933	262.3261896	29729.957390	114154.29732

Intel Core i7-8750H

Size Alg	10	100	1000	10000	100000	200000
A	0.01012366	0.03917133	1.17783200	63.29890433	3878.0865746	15561.694973
B	0.00769933	0.02525733	1.43228333	58.73236433	5878.2683309	23695.176663
C	0.00900966	0.05991400	3.83168433	223.6413363	26977.390251	109398.75507
D	0.00994266	0.06362633	4.12101699	182.0911991	20388.736503	83265.275556

As we can see, there is, in fact, a difference between the two processors that we are testing. But this difference is only visible on the response times while executing the different algorithms. Therefore as we can also see, the algorithms have the same behavior independently of the Architecture.

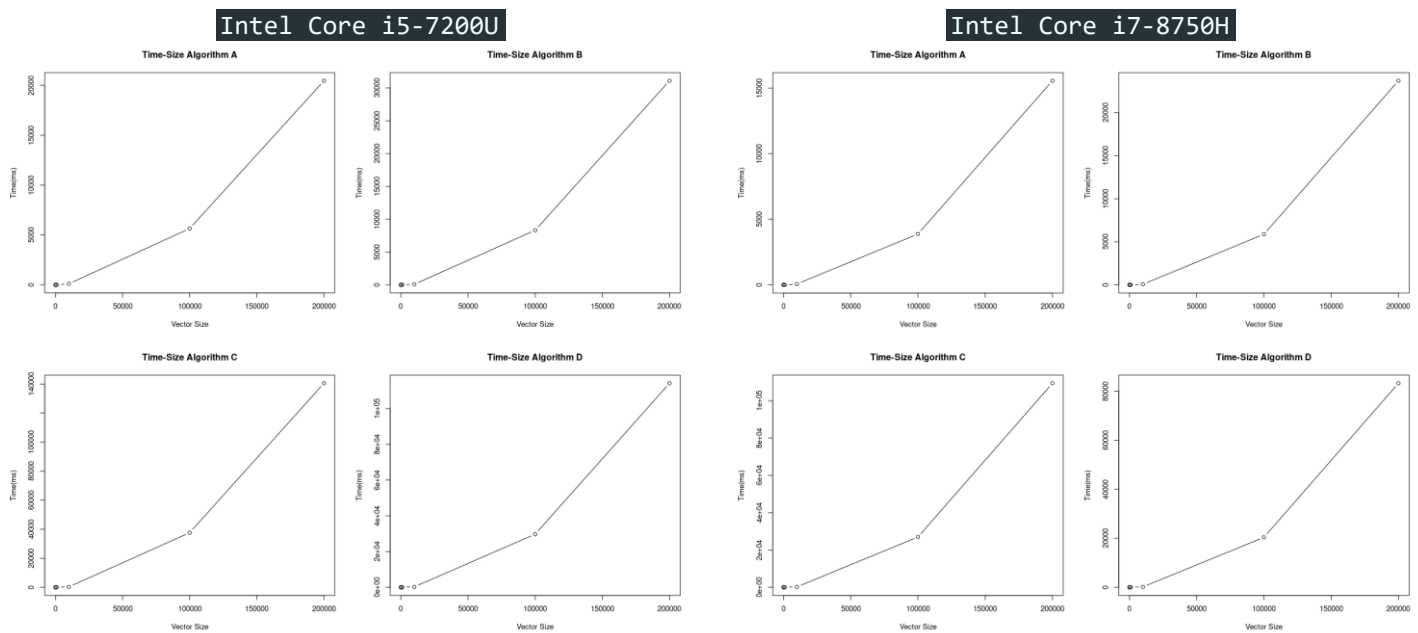
So, analyzing every algorithm in a more exhaustive way we can observe these facts:

1. Using small vector sizes, we can not appreciate a big difference between one and another algorithm, as they have very similar response times. But the difference between them appears when we set a large vector size, where both Algorithm C and D increments dramatically the response time in comparison to the other algorithms.
2. The behaviors of the algorithms are very close to the Exponential behavior as they don't grow following a straight line (what happens if the response time would have growth in a proportional way). So we can state that multiplying the input by 10 does not imply that the response time will grow 10 times too, it will grow much more.
3. There is not an absolute 'winner', there is not an algorithm that is always the fastest one, as it depends on the vector size, in very low vector sizes the fastest Algorithm is B but when the input grows the fastest algorithm is A. That leads to think that if you want to compute very small vector sizes you should use the Algorithm B and if you want to compute very large vector you should use A, but it is a little bit tricky as if

we look the difference on the response times, there is not a notorious difference between A and B in small vector sizes. So this can generally be insignificant, but if we are trying to be as precise as possible (for example in real time programs or distributed systems) it is a fact that algorithm B is faster than A in the very beginning.

A very different situation exist talking about the 'looser', as the worse algorithm talking about response times is Algorithm C, this algorithm has proved that is very unnefficient as it's response time is the one tha grows faster and faster with respect to the others.

We have represented the algorithm Time-Size plots:



Task 3

For this task, as it is stated in the assignment, we have taken again some measures and collected the more significant of them in the following charts but, with the main difference that in this time we have taken the measures with the parallelized source code. Time is measured in **ms** and size of the vector reffers to the number of elements that the vector. (The complete set of measures is placed at the end of this document)

Intel Core i5-7200U

Size Alg	10	100	1000	10000	100000	200000
A	0.05035433	0.39354566	0.62213433	51.31171699	4157.4183153	16356.7031736
B	0.01720600	0.02897066	0.92546300	73.45548100	7211.3050546	28191.0550566
C	0.01270233	0.04832933	2.50017300	273.4751610	33189.870487	132822.440236
D	0.03248133	0.18695233	3.64057499	109.7173650	11466.426697	43237.7163926

Intel Core i7-8750H

Size Alg	10	100	1000	10000	100000	200000
A	0.02755333	0.06028066	0.46698333	38.05365033	2814.8695793	11225.2330333
B	0.01431200	0.04213366	0.70653833	55.77766633	5368.1400043	21242.2937066
C	0.01461666	0.06046333	1.89549333	207.4096066	24970.167456	100109.238919
D	0.05795233	0.21679099	1.83298366	38.99261433	3343.9230059	15970.4816176

As we see, there is a markable difference between the parallelized code and the non-parallelized, this difference is even more evident when we watch at the larger vector sizes. So, for that reason, we will focus on this larger vector sizes (specifically 200000), as we can prove in a more detailed way, how much improvement exists.

Now by using Amdahl's law we can calculate the speed gain for algorithms A and D, and only those, as algorithms B and C are non parallelizables as they have different kinds of dependences.

Speed gain A

$$S_{gA} = \frac{T_o}{T_i} = \frac{T_{sA}}{T_{pA}} = \frac{15561.694973}{11225.233033} = 1.3863 \quad \text{Intel Core i7-8750H}$$

$$S_{gA} = \frac{T_o}{T_i} = \frac{T_{sA}}{T_{pA}} = \frac{20460.150972}{16356.703173} = 1.2509 \quad \text{Intel Core i5-7200U}$$

Speed gain D

$$S_{gD} = \frac{T_o}{T_i} = \frac{T_{sD}}{T_{pD}} = \frac{83265.275556}{15970.481617} = 5.2137 \quad \text{Intel Core i7-8750H}$$

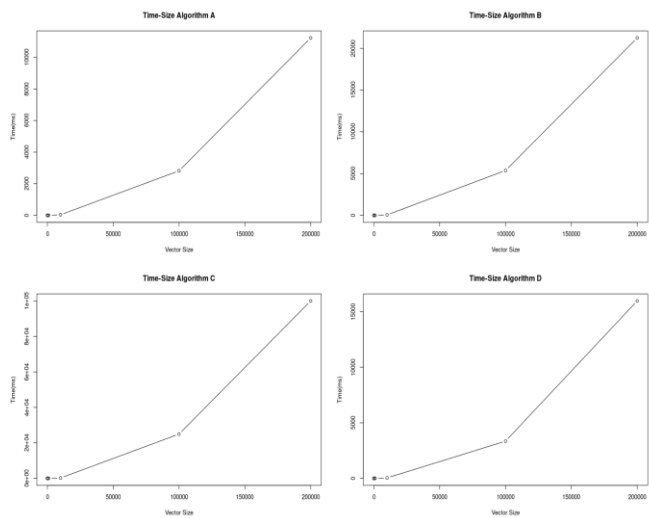
$$S_{gD} = \frac{T_o}{T_i} = \frac{T_{sD}}{T_{pD}} = \frac{114154.29725}{43237.716392} = 2.6406 \quad \text{Intel Core i5-7200U}$$

As we can see there is, in fact, an improvement between the non-parallelized and the parallelized code. And we can also see that the fact of having more cores, helps with the fact of increasing the performance even more. As we can have more things happening at the same time.

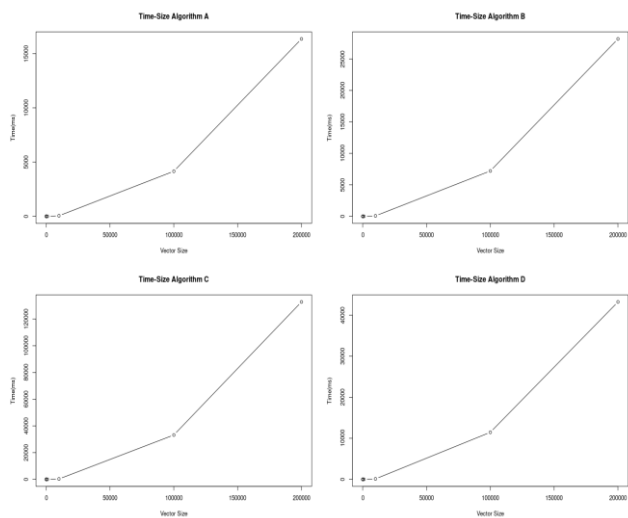
Therefore we can answer the questions made in the presentation segment. It's a fact that two different processors with different architectures neither increase the performance in the same proportion nor have the same speed executing the algorithms.

This time we have depicted the Time-Size dot plots to show how the algorithms behave.

Intel Core i5-7200U



Intel Core i7-8750H



Annex

Sequential Complete Measurements

Intel Core i7-8750H

Measurement 10:

A:

- 1: 0.01039600 milliseconds
- 2: 0.01408500 milliseconds (slowest)
- 3: 0.01030600 milliseconds
- 4: 0.00592100 milliseconds (fastest)
- 5: 0.00966900 milliseconds

B:

- 1: 0.00734600 milliseconds
- 2: 0.01408500 milliseconds (slowest)
- 3: 0.00828500 milliseconds
- 4: 0.00615900 milliseconds (fastest)
- 5: 0.00746700 milliseconds

C:

- 1: 0.00967500 milliseconds
- 2: 0.01274500 milliseconds (slowest)
- 3: 0.00713000 milliseconds
- 4: 0.00595600 milliseconds (fastest)
- 5: 0.01022400 milliseconds

D:

- 1: 0.01015300 milliseconds
- 2: 0.01131600 milliseconds (slowest)
- 3: 0.00877000 milliseconds
- 4: 0.00796600 milliseconds (fastest)
- 5: 0.01090500 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(0.01039600 + 0.01030600 + 0.00966900) / 3 = 0.010123666666666666$

B: $(0.00734600 + 0.00828500 + 0.00746700) / 3 = 0.007699333333333333$

C: $(0.00967500 + 0.00713000 + 0.01022400) / 3 = 0.009009666666666668$

D: $(0.01015300 + 0.00877000 + 0.01090500) / 3 = 0.009942666666666667$

Measurement 100:

A:

- 1: 0.03900600 milliseconds
- 2: 0.04384300 milliseconds
- 3: 0.02517900 milliseconds (fastest)
- 4: 0.04787600 milliseconds (slowest)
- 5: 0.03466500 milliseconds

B:

- 1: 0.02695700 milliseconds
- 2: 0.02620000 milliseconds
- 3: 0.01770100 milliseconds (fastest)
- 4: 0.02977200 milliseconds (slowest)
- 5: 0.02261500 milliseconds

C:

- 1: 0.06100300 milliseconds
- 2: 0.06554400 milliseconds
- 3: 0.04175500 milliseconds (fastest)
- 4: 0.07483000 milliseconds (slowest)
- 5: 0.05319500 milliseconds

D:

- 1: 0.06211800 milliseconds
- 2: 0.06996100 milliseconds
- 3: 0.04224500 milliseconds (fastest)
- 4: 0.07208400 milliseconds (slowest)
- 5: 0.05880000 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(0.03900600 + 0.04384300 + 0.03466500) / 3 = 0.039171333333333336$

B: $(0.02695700 + 0.02620000 + 0.02261500) / 3 = 0.025257333333333333$

C: $(0.06100300 + 0.06554400 + 0.05319500) / 3 = 0.059914$

D: $(0.06211800 + 0.06996100 + 0.05880000) / 3 = 0.063626333333333333$

Measurement 1000:

A:

- 1: 0.68390500 milliseconds (fastest)
- 2: 1.42196900 milliseconds (slowest)
- 3: 1.12428100 milliseconds
- 4: 1.20408300 milliseconds
- 5: 1.20513200 milliseconds

B:

- 1: 0.88215500 milliseconds (fastest)
- 2: 1.88515300 milliseconds (slowest)
- 3: 1.30627500 milliseconds
- 4: 1.48693000 milliseconds
- 5: 1.50364500 milliseconds

C:

- 1: 2.24796800 milliseconds (fastest)
- 2: 4.83558700 milliseconds (slowest)
- 3: 3.69439600 milliseconds
- 4: 3.81240100 milliseconds
- 5: 3.98825600 milliseconds

D:

- 1: 2.32730300 milliseconds (fastest)
- 2: 4.93812600 milliseconds (slowest)
- 3: 3.87867200 milliseconds
- 4: 4.04516500 milliseconds
- 5: 4.43921400 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(1.12428100 + 1.20408300 + 1.20513200) / 3 = 1.1778320000000002$

B: $(1.30627500 + 1.48693000 + 1.50364500) / 3 = 1.4322833333333334$

C: $(3.69439600 + 3.81240100 + 3.98825600) / 3 = 3.8316843333333333$

D: $(3.87867200 + 4.04516500 + 4.43921400) / 3 = 4.1210169999999999$

Measurement 10000:

A:

- 1: 64.97279100 milliseconds (slowest)
- 2: 64.19168400 milliseconds
- 3: 63.41531600 milliseconds
- 4: 49.45484300 milliseconds (fastest)
- 5: 62.28971300 milliseconds

B:

- 1: 57.81129200 milliseconds (fastest)
- 2: 58.73213600 milliseconds
- 3: 58.46788200 milliseconds
- 4: 59.61375800 milliseconds (slowest)
- 5: 58.99707500 milliseconds

C:

- 1: 219.09739000 milliseconds (fastest)
- 2: 227.46944000 milliseconds (slowest)
- 3: 226.63727600 milliseconds
- 4: 223.32350000 milliseconds
- 5: 220.96323300 milliseconds

D:

- 1: 175.14914200 milliseconds (fastest)
- 2: 186.44133300 milliseconds (slowest)
- 3: 182.75133400 milliseconds
- 4: 179.04777700 milliseconds
- 5: 184.47448600 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(64.19168400 + 63.41531600 + 62.28971300) / 3 = 63.29890433333333$

B: $(58.73213600 + 58.46788200 + 58.99707500) / 3 = 58.73236433333333$

C: $(226.63727600 + 223.32350000 + 220.96323300) / 3 = 223.64133633333336$

D: $(182.75133400 + 179.04777700 + 184.47448600) / 3 = 182.09119900000005$

Measurement 100000:

A:

- 1: 3924.43045100 milliseconds
- 2: 3863.09089300 milliseconds
- 3: 3834.38163800 milliseconds (fastest)
- 4: 3943.90602400 milliseconds (slowest)
- 5: 3846.73838000 milliseconds

B:

- 1: 5915.61565300 milliseconds
- 2: 5825.32269000 milliseconds (fastest)
- 3: 5843.26538500 milliseconds
- 4: 6046.89200100 milliseconds (slowest)
- 5: 5875.92395500 milliseconds

C:

- 1: 26943.56309300 milliseconds
- 2: 26905.27193500 milliseconds
- 3: 26873.29061900 milliseconds (fastest)
- 4: 27146.60216700 milliseconds (slowest)
- 5: 27083.33572500 milliseconds

D:

- 1: 20291.91485000 milliseconds (fastest)
- 2: 20350.22445000 milliseconds
- 3: 20446.95861100 milliseconds (slowest)
- 4: 20438.90855700 milliseconds
- 5: 20377.07650400 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(3924.43045100 + 3863.09089300 + 3846.73838000) / 3 = 3878.0865746666664$

B: $(5915.61565300 + 5843.26538500 + 5875.92395500) / 3 = 5878.2683309999999$

C: $(26943.56309300 + 26905.27193500 + 27083.33572500) / 3 = 26977.390251$

D: $(20350.22445000 + 20438.90855700 + 20377.07650400) / 3 = 20388.7365036666663$

Measurement 200000:

A:

- 1: 15611.59104100 milliseconds
- 2: 15498.32431600 milliseconds
- 3: 15629.13347700 milliseconds (slowest)
- 4: 15575.16956300 milliseconds
- 5: 15028.67622300 milliseconds (fastest)

B:

- 1: 23702.88593300 milliseconds
- 2: 23697.32919500 milliseconds
- 3: 23826.00264400 milliseconds (slowest)
- 4: 23685.31486200 milliseconds
- 5: 21712.29571300 milliseconds (fastest)

C:

- 1: 109164.76463800 milliseconds
- 2: 109391.60571600 milliseconds
- 3: 109398.22876900 milliseconds (slowest)
- 4: 109639.89487900 milliseconds
- 5: 101041.97649700 milliseconds (fastest)

D:

- 1: 83039.38122900 milliseconds
- 2: 83271.19046700 milliseconds
- 3: 83485.25497400 milliseconds
- 4: 83638.08041700 milliseconds (slowest)
- 5: 75778.99928700 milliseconds (fastest)

Delete the slowest and the fastest and average of the other three

A: $(15611.59104100 + 15498.32431600 + 15575.16956300) / 3 = 15561.694973333331$

B: $(23702.88593300 + 23697.32919500 + 23685.31486200) / 3 = 23695.17666333333$

C: $(109164.76463800 + 109391.60571600 + 109639.89487900) / 3 = 109398.75507766668$

D: $(83039.38122900 + 83271.19046700 + 83485.25497400) / 3 = 83265.27555666666$

Intel Core i5-7200U

Measurement 10:

A:

- 1: 0.04789200 milliseconds (slowest)
- 2: 0.02926600 milliseconds
- 3: 0.02086400 milliseconds (fastest)
- 4: 0.02747000 milliseconds
- 5: 0.03403800 milliseconds

B:

- 1: 0.02791100 milliseconds
- 2: 0.01754400 milliseconds (fastest)
- 3: 0.01817900 milliseconds
- 4: 0.02260000 milliseconds
- 5: 0.03184400 milliseconds (slowest)

C:

- 1: 0.03082100 milliseconds
- 2: 0.03009300 milliseconds
- 3: 0.02352300 milliseconds (fastest)
- 4: 0.04102900 milliseconds (slowest)
- 5: 0.02737100 milliseconds

D:

- 1: 0.02492700 milliseconds
- 2: 0.02916300 milliseconds
- 3: 0.02357000 milliseconds (fastest)
- 4: 0.03676200 milliseconds (slowest)
- 5: 0.03070200 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(0.02926600+0.02747000+0.03403800) / 3 = 0.030257999999999997$

B: $(0.02791100+0.01817900+0.02260000) / 3 = 0.022896666666666666$

C: $(0.03082100+0.03009300+0.02737100) / 3 = 0.029428333333333334$

D: $(0.02492700+0.02916300+0.03070200) / 3 = 0.028264$

Measurement 100:

A:

1: 0.11278200 milliseconds

2: 0.13496100 milliseconds

3: 0.05250400 milliseconds (fastest)

4: 0.10620400 milliseconds

5: 0.19603500 milliseconds (slowest)

B:

1: 0.07614500 milliseconds

2: 0.09286800 milliseconds

3: 0.02710600 milliseconds (fastest)

4: 0.08691000 milliseconds

5: 0.13861300 milliseconds (slowest)

C:

1: 0.20096300 milliseconds

2: 0.19111600 milliseconds

3: 0.09713800 milliseconds (fastest)

4: 0.20829900 milliseconds

5: 0.27409900 milliseconds (slowest)

D:

1: 0.21114900 milliseconds

2: 0.19245800 milliseconds

3: 0.15323400 milliseconds (fastest)

4: 0.18618100 milliseconds

5: 0.30385500 milliseconds (slowest)

Delete the slowest and the fastest and average of the other three

A: $(0.11278200+0.13496100+0.10620400) / 3 = 0.11798233333333334$

B: $(0.07614500+0.09286800+0.08691000) / 3 = 0.08530766666666667$

C: $(0.20096300+0.19111600+0.20829900) / 3 = 0.20012600000000003$

D: $(0.21114900+0.19245800+0.18618100) / 3 = 0.196596$

Measurement 1000:

A:

1: 5.57368300 milliseconds (slowest)

2: 1.86236000 milliseconds

3: 2.29279300 milliseconds

4: 1.70339000 milliseconds

5: 1.69719400 milliseconds (fastest)

B:

- 1: 5.41146800 milliseconds (slowest)
- 2: 2.06240100 milliseconds
- 3: 2.73795000 milliseconds
- 4: 2.05725300 milliseconds (fastest)
- 5: 2.08169600 milliseconds

C:

- 1: 14.54388900 milliseconds (slowest)
- 2: 6.04039000 milliseconds
- 3: 9.25284000 milliseconds
- 4: 5.64434200 milliseconds
- 5: 4.30718000 milliseconds (fastest)

D:

- 1: 9.79168100 milliseconds (slowest)
- 2: 5.88649300 milliseconds
- 3: 9.73108300 milliseconds
- 4: 6.54678200 milliseconds
- 5: 3.92546800 milliseconds (fastest)

Delete the slowest and the fastest and average of the other three

A: $(1.86236000 + 2.29279300 + 1.70339000) / 3 = 1.9528476666666668$

B: $(2.06240100 + 2.73795000 + 2.08169600) / 3 = 2.2940156666666667$

C: $(6.04039000 + 9.25284000 + 5.64434200) / 3 = 6.9791906666666668$

D: $(5.88649300 + 9.73108300 + 6.54678200) / 3 = 7.3881193333333333$

Measurement 10000:

A:

- 1: 109.25207400 milliseconds
- 2: 97.63302400 milliseconds (fastest)
- 3: 110.63868000 milliseconds
- 4: 112.98691400 milliseconds (slowest)
- 5: 98.62503600 milliseconds

B:

- 1: 84.14285200 milliseconds
- 2: 86.85032200 milliseconds (slowest)
- 3: 82.15001300 milliseconds
- 4: 80.31590400 milliseconds (fastest)
- 5: 85.45222500 milliseconds

C:

- 1: 316.97606300 milliseconds
- 2: 326.95380900 milliseconds (slowest)
- 3: 303.84590900 milliseconds (fastest)
- 4: 304.26317400 milliseconds
- 5: 315.01412200 milliseconds

D:

- 1: 266.00106800 milliseconds
- 2: 265.96868600 milliseconds
- 3: 245.49389200 milliseconds (fastest)
- 4: 255.00881500 milliseconds
- 5: 272.03367800 milliseconds (slowest)

Delete the slowest and the fastest and average of the other three

A: $(109.25207400 + 110.63868000 + 98.62503600) / 3 = 106.17192999999999$

B: $(84.14285200 + 82.15001300 + 85.45222500) / 3 = 83.91503$

C: $(316.97606300 + 304.26317400 + 315.01412200) / 3 = 312.084453$

D: $(266.00106800 + 265.96868600 + 255.00881500) / 3 = 262.32618966666666$

Measurement 100000:

A:

- 1: 5365.43000600 milliseconds (fastest)
- 2: 5724.46013600 milliseconds
- 3: 5812.30752500 milliseconds (slowest)
- 4: 5632.61628900 milliseconds
- 5: 5576.56169400 milliseconds

B:

- 1: 8233.84477700 milliseconds
- 2: 8417.49496600 milliseconds
- 3: 8520.75287700 milliseconds (slowest)
- 4: 8292.42993800 milliseconds
- 5: 8195.77333700 milliseconds (fastest)

C:

- 1: 37467.53372700 milliseconds (fastest)
- 2: 37814.11073600 milliseconds (slowest)
- 3: 37797.61288200 milliseconds
- 4: 37494.21686400 milliseconds
- 5: 37616.82650800 milliseconds

D:

- 1: 29682.94504100 milliseconds
- 2: 30225.44848800 milliseconds (slowest)
- 3: 29267.47120300 milliseconds (fastest)
- 4: 29890.15135700 milliseconds
- 5: 29616.77579900 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(5724.46013600 + 5632.61628900 + 5576.56169400) / 3 = 5644.546039666667$

B: $(8233.84477700 + 8417.49496600 + 8292.42993800) / 3 = 8314.589893666665$

C: $(37797.61288200 + 37494.21686400 + 37616.82650800) / 3 = 37636.218751333334$

D: $(29682.94504100 + 29890.15135700 + 29616.77579900) / 3 = 29729.957398999995$

Measurement 200000:

A:

- 1: 22777.58730800 milliseconds
- 2: 23021.42176000 milliseconds (slowest)
- 3: 19006.40999000 milliseconds (fastest)
- 4: 19109.34519000 milliseconds
- 5: 19493.52041800 milliseconds

B:

- 1: 33149.57607400 milliseconds
- 2: 34149.45030100 milliseconds (slowest)
- 3: 29173.34608700 milliseconds (fastest)
- 4: 29329.18235800 milliseconds
- 5: 30829.08196000 milliseconds

C:

- 1: 152230.99320800 milliseconds (slowest)
- 2: 148376.38411800 milliseconds
- 3: 135095.29466500 milliseconds (fastest)
- 4: 137464.46489400 milliseconds
- 5: 135739.21187700 milliseconds

D:

- 1: 127526.09602400 milliseconds (slowest)
- 2: 120767.69417300 milliseconds
- 3: 100963.64701000 milliseconds (fastest)
- 4: 102505.21123700 milliseconds
- 5: 119189.98656500 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(22777.58730800 + 19109.34519000 + 19493.52041800) / 3 = 20460.150972$

B: $(33149.57607400 + 29329.18235800 + 30829.08196000) / 3 = 31102.613464$

C: $(148376.38411800 + 137464.46489400 + 135739.21187700) / 3 = 140526.686963000001$

D: $(120767.69417300 + 102505.21123700 + 119189.98656500) / 3 = 114154.297325$

Parallel Complete Measurements

Intel Core i7-8750H

Measurement 10:

A:

- 1: 0.01248100 milliseconds (fastest)
- 2: 0.04412200 milliseconds
- 3: 0.01988400 milliseconds
- 4: 0.01865400 milliseconds
- 5: 0.08978900 milliseconds (slowest)

B:

- 1: 0.00447000 milliseconds (fastest)
- 2: 0.02201300 milliseconds
- 3: 0.01043400 milliseconds
- 4: 0.01048900 milliseconds
- 5: 0.05212800 milliseconds (slowest)

C:

- 1: 0.00445000 milliseconds (fastest)
- 2: 0.02192000 milliseconds
- 3: 0.01108600 milliseconds
- 4: 0.01084400 milliseconds
- 5: 0.05136700 milliseconds (slowest)

D:

- 1: 0.01888900 milliseconds (fastest)
- 2: 1.03387900 milliseconds (slowest)
- 3: 0.02535300 milliseconds
- 4: 0.02557400 milliseconds
- 5: 0.12293000 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(0.04412200 + 0.01988400 + 0.01865400) / 3 = 0.027553333333333336$

B: $(0.02201300 + 0.01043400 + 0.01048900) / 3 = 0.014312$

C: $(0.02192000 + 0.01108600 + 0.01084400) / 3 = 0.014616666666666667$

D: $(0.02535300 + 0.02557400 + 0.12293000) / 3 = 0.057952333333333333$

Measurement 100:

A:

- 1: 0.02988900 milliseconds
- 2: 0.07564300 milliseconds
- 3: 0.07531000 milliseconds
- 4: 0.02940900 milliseconds (fastest)
- 5: 0.14737700 milliseconds (slowest)

B:

- 1: 0.01750200 milliseconds (fastest)
- 2: 0.06405600 milliseconds
- 3: 0.04406500 milliseconds
- 4: 0.01828000 milliseconds
- 5: 0.08624400 milliseconds (slowest)

C:

- 1: 0.03432600 milliseconds
- 2: 0.07839800 milliseconds
- 3: 0.06866600 milliseconds
- 4: 0.03370200 milliseconds (fastest)
- 5: 0.16101000 milliseconds (slowest)

D:

- 1: 0.16653800 milliseconds
- 2: 0.20850400 milliseconds
- 3: 0.27533100 milliseconds
- 4: 0.16361400 milliseconds (fastest)
- 5: 0.43648200 milliseconds (slowest)

Delete the slowest and the fastest and average of the other three

A: $(0.02988900 + 0.07564300 + 0.07531000) / 3 = 0.06028066666666667$

B: $(0.06405600 + 0.04406500 + 0.01828000) / 3 = 0.04213366666666666$

C: $(0.03432600 + 0.07839800 + 0.06866600) / 3 = 0.06046333333333334$

D: $(0.16653800 + 0.20850400 + 0.27533100) / 3 = 0.21679099999999998$

Measurement 1000:

A:

1: 0.47139800 milliseconds

2: 0.44409000 milliseconds

3: 0.48546200 milliseconds

4: 0.53848700 milliseconds (slowest)

5: 0.41745800 milliseconds (fastest)

B:

1: 0.70087400 milliseconds

2: 0.69907400 milliseconds

3: 0.71966700 milliseconds

4: 0.87331400 milliseconds (slowest)

5: 0.66968600 milliseconds (fastest)

C:

1: 1.89537800 milliseconds

2: 1.88250000 milliseconds

3: 1.90860200 milliseconds

4: 1.92862800 milliseconds (slowest)

5: 1.85987100 milliseconds (fastest)

D:

1: 1.98383400 milliseconds (slowest)

2: 1.81747500 milliseconds

3: 1.94989000 milliseconds

4: 1.71877400 milliseconds (fastest)

5: 1.73158600 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(0.47139800 + 0.44409000 + 0.48546200) / 3 = 0.4669833333333333$

B: $(0.70087400 + 0.69907400 + 0.71966700) / 3 = 0.7065383333333334$

C: $(1.89537800 + 1.88250000 + 1.90860200) / 3 = 1.8954933333333335$

D: $(1.81747500 + 1.94989000 + 1.73158600) / 3 = 1.8329836666666666$

Measurement 10000:

A:

1: 35.95244400 milliseconds (fastest)

2: 40.80395100 milliseconds

3: 41.60670800 milliseconds (slowest)

4: 36.91932000 milliseconds

5: 36.43768000 milliseconds

B:

- 1: 55.26651700 milliseconds (fastest)
- 2: 55.72184500 milliseconds
- 3: 56.05269600 milliseconds
- 4: 55.55845800 milliseconds
- 5: 56.08673700 milliseconds (slowest)

C:

- 1: 207.28626100 milliseconds (fastest)
- 2: 207.39735900 milliseconds
- 3: 208.34786300 milliseconds
- 4: 206.48359800 milliseconds
- 5: 209.27298400 milliseconds (slowest)

D:

- 1: 39.69119100 milliseconds
- 2: 36.83044100 milliseconds (fastest)
- 3: 38.17354200 milliseconds
- 4: 39.11311000 milliseconds
- 5: 39.88995400 milliseconds (slowest)

Delete the slowest and the fastest and average of the other three

A: $(40.80395100 + 36.91932000 + 36.43768000) / 3 = 38.05365033333333$

B: $(55.72184500 + 56.05269600 + 55.55845800) / 3 = 55.777666333333336$

C: $(207.39735900 + 208.34786300 + 206.48359800) / 3 = 207.4096066666667$

D: $(39.69119100 + 38.17354200 + 39.11311000) / 3 = 38.992614333333336$

Measurement 100000:

A:

- 1: 2908.61869400 milliseconds (slowest)
- 2: 2824.74016100 milliseconds
- 3: 2785.01909400 milliseconds (fastest)
- 4: 2794.57509300 milliseconds
- 5: 2825.29348400 milliseconds

B:

- 1: 5410.88241100 milliseconds
- 2: 5423.03718200 milliseconds (slowest)
- 3: 5301.08004000 milliseconds (fastest)
- 4: 5343.69249100 milliseconds
- 5: 5349.84511100 milliseconds

C:

- 1: 25311.24818200 milliseconds (slowest)
- 2: 25110.63779300 milliseconds
- 3: 24944.89910600 milliseconds
- 4: 24902.14547600 milliseconds
- 5: 24897.71910100 milliseconds (fastest)

D:

- 1: 3289.19256100 milliseconds
- 2: 3266.58956700 milliseconds (fastest)
- 3: 3669.08366600 milliseconds (slowest)
- 4: 3412.69223100 milliseconds
- 5: 3329.88422600 milliseconds

Delete the slowest and the fastest and average of the other three

$$A: (2824.74016100 + 2794.57509300 + 2825.29348400) / 3 = 2814.869579333333$$

$$B: (5410.88241100 + 5343.69249100 + 5349.84511100) / 3 = 5368.140004333333$$

$$C: (25110.63779300 + 24902.14547600 + 24897.71910100) / 3 = 24970.167456666666$$

$$D: (3289.19256100 + 3412.69223100 + 3329.88422600) / 3 = 3343.9230059999995$$

Measurement 200000:

A:

- 1: 11257.44863600 milliseconds (slowest)
- 2: 11232.00675400 milliseconds
- 3: 11238.27032800 milliseconds
- 4: 11205.42201800 milliseconds
- 5: 11157.11326200 milliseconds (fastest)

B:

- 1: 21254.62607300 milliseconds
- 2: 21242.69950900 milliseconds
- 3: 21229.55553800 milliseconds
- 4: 21267.98886200 milliseconds (slowest)
- 5: 21214.29985000 milliseconds (fastest)

C:

- 1: 100182.61500700 milliseconds (slowest)
- 2: 100100.02078200 milliseconds
- 3: 100170.27975800 milliseconds
- 4: 100057.41621700 milliseconds
- 5: 99841.46536900 milliseconds (fastest)

D:

- 1: 15733.19340200 milliseconds
- 2: 15550.93918500 milliseconds (fastest)
- 3: 16048.67282700 milliseconds
- 4: 16479.94229400 milliseconds (slowest)
- 5: 16129.57862400 milliseconds

Delete the slowest and the fastest and average of the other three

$$A: (11232.00675400 + 11238.27032800 + 11205.42201800) / 3 = 11225.233033333332$$

$$B: (21254.62607300 + 21242.69950900 + 21229.55553800) / 3 = 21242.293706666667$$

$$C: (100100.02078200 + 100170.27975800 + 100057.41621700) / 3 = 100109.23891900001$$

$$D: (15733.19340200 + 16048.67282700 + 16129.57862400) / 3 = 15970.481617666666$$

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Measurement 10:

A:

- 1: 0.06670300 milliseconds
- 2: 0.01486800 milliseconds (fastest)
- 3: 0.02801600 milliseconds
- 4: 0.11082200 milliseconds (slowest)
- 5: 0.05634400 milliseconds

B:

- 1: 0.02771800 milliseconds
- 2: 0.00817900 milliseconds (fastest)
- 3: 0.01113700 milliseconds
- 4: 0.06372500 milliseconds (slowest)
- 5: 0.01276300 milliseconds

C:

- 1: 0.02841600 milliseconds (slowest)
- 2: 0.00811900 milliseconds (fastest)
- 3: 0.01117800 milliseconds
- 4: 0.01420200 milliseconds
- 5: 0.01272700 milliseconds

D:

- 1: 0.12824800 milliseconds (slowest)
- 2: 0.02090100 milliseconds (fastest)
- 3: 0.04004000 milliseconds
- 4: 0.03061400 milliseconds
- 5: 0.02679000 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(0.06670300 + 0.02801600 + 0.05634400) / 3 = 0.05035433333333334$

B: $(0.02771800 + 0.01113700 + 0.01276300) / 3 = 0.017206$

C: $(0.01117800 + 0.01420200 + 0.01272700) / 3 = 0.01270233333333335$

D: $(0.04004000 + 0.03061400 + 0.02679000) / 3 = 0.03248133333333334$

Measurement 100:

A:

- 1: 0.03436900 milliseconds (fastest)
- 2: 0.04475600 milliseconds
- 3: 1.10100100 milliseconds
- 4: 2.86040600 milliseconds (slowest)
- 5: 0.03488000 milliseconds

B:

- 1: 0.02211300 milliseconds (fastest)
- 2: 0.02429000 milliseconds
- 3: 0.08517500 milliseconds (slowest)
- 4: 0.03949200 milliseconds
- 5: 0.02313000 milliseconds

C:

- 1: 0.04245400 milliseconds (fastest)
- 2: 0.05837900 milliseconds
- 3: 0.10296900 milliseconds (slowest)
- 4: 0.05795000 milliseconds
- 5: 0.04458400 milliseconds

D:

- 1: 0.16278600 milliseconds (fastest)
- 2: 0.26195500 milliseconds (slowest)
- 3: 0.22170800 milliseconds
- 4: 0.16766000 milliseconds
- 5: 0.17148900 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(0.04475600 + 1.10100100 + 0.03488000) / 3 = 0.3935456666666666$

B: $(0.02429000 + 0.03949200 + 0.02313000) / 3 = 0.02897066666666667$

C: $(0.04245400 + 0.05795000 + 0.04458400) / 3 = 0.04832933333333335$

D: $(0.22170800 + 0.16766000 + 0.17148900) / 3 = 0.18695233333333333$

Measurement 1000:

A:

- 1: 0.57259800 milliseconds
- 2: 0.66636000 milliseconds
- 3: 0.56567500 milliseconds (fastest)
- 4: 0.69060500 milliseconds (slowest)
- 5: 0.62744500 milliseconds

B:

- 1: 0.82741100 milliseconds (fastest)
- 2: 0.97361600 milliseconds
- 3: 0.85241600 milliseconds
- 4: 1.03269200 milliseconds (slowest)
- 5: 0.95035700 milliseconds

C:

- 1: 2.38671800 milliseconds
- 2: 2.57299000 milliseconds
- 3: 2.36105200 milliseconds (fastest)
- 4: 2.66008200 milliseconds (slowest)
- 5: 2.54081100 milliseconds

D:

- 1: 2.42979500 milliseconds
- 2: 2.23074100 milliseconds (fastest)
- 3: 5.48405000 milliseconds (slowest)
- 4: 4.99323900 milliseconds
- 5: 3.49869100 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(0.57259800 + 0.66636000 + 0.62744500) / 3 = 0.6221343333333333$

B: $(0.97361600 + 0.85241600 + 0.95035700) / 3 = 0.925463$

C: $(2.38671800 + 2.57299000 + 2.54081100) / 3 = 2.500173$

D: $(2.42979500 + 4.99323900 + 3.49869100) / 3 = 3.6405749999999997$

Measurement 10000:

A:

- 1: 50.02389800 milliseconds (fastest)
- 2: 50.09122000 milliseconds
- 3: 51.43956100 milliseconds
- 4: 52.83681500 milliseconds (slowest)
- 5: 52.40437000 milliseconds

B:

- 1: 72.71324100 milliseconds (fastest)
- 2: 73.53724900 milliseconds
- 3: 73.81418500 milliseconds (slowest)
- 4: 73.23794300 milliseconds
- 5: 73.59125100 milliseconds

C:

- 1: 272.41097100 milliseconds (fastest)
- 2: 273.61119300 milliseconds (slowest)
- 3: 273.33708600 milliseconds
- 4: 273.59779100 milliseconds
- 5: 273.49060600 milliseconds

D:

- 1: 102.50148700 milliseconds (fastest)
- 2: 109.09236100 milliseconds
- 3: 112.25615700 milliseconds (slowest)
- 4: 111.85549400 milliseconds
- 5: 108.20424000 milliseconds

Delete the slowest and the fastest and average of the other three

A: $(50.09122000 + 51.43956100 + 52.40437000) / 3 = 51.3117169999999994$

B: $(73.53724900 + 73.23794300 + 73.59125100) / 3 = 73.455481$

C: $(273.33708600 + 273.59779100 + 273.49060600) / 3 = 273.475161$

D: $(109.09236100 + 111.85549400 + 108.20424000) / 3 = 109.717365000000002$

Measurement 100000:

A:

- 1: 4216.48310300 milliseconds
- 2: 4114.46901100 milliseconds (fastest)
- 3: 4124.32188000 milliseconds
- 4: 4131.44996300 milliseconds
- 5: 4258.64411800 milliseconds (slowest)

B:

- 1: 7201.44162900 milliseconds
- 2: 7205.84123600 milliseconds
- 3: 7226.63229900 milliseconds
- 4: 7159.72950700 milliseconds (fastest)
- 5: 7271.28447200 milliseconds (slowest)

C:

- 1: 33096.25428500 milliseconds (fastest)
- 2: 33131.06523600 milliseconds
- 3: 33241.59186000 milliseconds
- 4: 33196.95436500 milliseconds
- 5: 33464.89452900 milliseconds (slowest)

D:

- 1: 11467.38410300 milliseconds
- 2: 11487.33056400 milliseconds
- 3: 11444.56542600 milliseconds
- 4: 10706.74630500 milliseconds (fastest)
- 5: 11839.44780200 milliseconds (slowest)

Delete the slowest and the fastest and average of the other three

A: $(4216.48310300 + 4124.32188000 + 4131.44996300) / 3 = 4157.418315333333$

B: $(7201.44162900 + 7205.84123600 + 7226.63229900) / 3 = 7211.305054666667$

C: $(33131.06523600 + 33241.59186000 + 33196.95436500) / 3 = 33189.870487$

D: $(11467.38410300 + 11487.33056400 + 11444.56542600) / 3 = 11466.426697666668$

Measurement 200000:

A:

- 1: 16337.37880000 milliseconds
- 2: 16259.46421000 milliseconds (fastest)
- 3: 16402.96622300 milliseconds
- 4: 16329.76449800 milliseconds
- 5: 16438.21989800 milliseconds (slowest)

B:

- 1: 28026.05121500 milliseconds (fastest)
- 2: 28234.73145000 milliseconds (slowest)
- 3: 28221.49599700 milliseconds
- 4: 28153.07239400 milliseconds
- 5: 28185.36132600 milliseconds

C:

- 1: 132535.57325000 milliseconds (fastest)
- 2: 132765.17177100 milliseconds
- 3: 132622.94696100 milliseconds
- 4: 133079.20197700 milliseconds
- 5: 133554.64992200 milliseconds (slowest)

D:

- 1: 43217.16676200 milliseconds
- 2: 42256.73874500 milliseconds (fastest)
- 3: 43201.65890900 milliseconds
- 4: 43294.32350700 milliseconds
- 5: 45067.96703800 milliseconds (slowest)

Delete the slowest and the fastest and average of the other three

$$A: (16337.37880000 + 16402.96622300 + 16329.76449800) / 3 = 16356.703173666669$$

$$B: (28234.73145000 + 28153.07239400 + 28185.36132600) / 3 = 28191.055056666664$$

$$C: (132765.17177100 + 132622.94696100 + 133079.20197700) / 3 = 132822.44023633332$$

$$D: (43217.16676200 + 43201.65890900 + 43294.32350700) / 3 = 43237.71639266666$$