

Transformar a la forma polar

a) $2 + j3$

$$C = \sqrt{A^2 + B^2} = \sqrt{2^2 + 3^2} = \sqrt{13}$$
$$\theta = \tan^{-1}\left(\frac{B}{A}\right) = \tan^{-1}\left(\frac{3}{2}\right) = 56.31^\circ$$

Respuesta $\rightarrow \sqrt{13} < 56.31^\circ$

b) $-8 + j6.2$

$$C = \sqrt{A^2 + B^2} = \sqrt{(-8)^2 + 6.2^2} = 10.12$$
$$\theta = \tan^{-1}\left(\frac{B}{A}\right) = \tan^{-1}\left(\frac{6.2}{-8}\right) = -37.77^\circ$$

Respuesta $\rightarrow 10.12 < -37.77^\circ$

c) $4.3 - j2.8$

$$C = \sqrt{A^2 + B^2} = \sqrt{4.3^2 + 2.8^2} = 5.13$$
$$\theta = \tan^{-1}\left(\frac{B}{A}\right) = \tan^{-1}\left(\frac{2.8}{4.3}\right) = 33.07^\circ$$

Respuesta $\rightarrow 5.13 < 33.07^\circ$

d) $-6 - j3.2$

$$C = \sqrt{A^2 + B^2} = \sqrt{(-6)^2 + (-3.2)^2} = 6.8$$
$$\theta = \tan^{-1}\left(\frac{B}{A}\right) = \tan^{-1}\left(\frac{-3.2}{-6}\right) = 28.07^\circ$$

Respuesta $\rightarrow 6.8 < 28.07^\circ$

Transformar a la forma rectangular

a) $36 < -10^\circ$

$$A = C \cos(\theta) = 36 \cos(-10) = 35.45$$
$$B = C \sin(\theta) = 36 \sin(-10) = -6.25$$

Respuesta $\rightarrow 35.45 - j6.25$

b) $28.7 < 135^\circ$

$$A = C \cos(\theta) = 28.7 \cos(135) = -20.29$$
$$B = C \sin(\theta) = 28.7 \sin(135) = 20.29$$

Respuesta $\rightarrow -20.29 + j20.29$

c) $11.2 < 28^\circ$

$$A = C \cos(\theta) = 11.2 \cos(28) = 9.88$$
$$B = C \sin(\theta) = 11.2 \sin(28) = 5.25$$

$$\text{Respuesta} \rightarrow 9.88 + j5.25$$

$$d) 45 < -117.9^\circ$$

$$A = C \cos(\theta) = 45 \cos(-117.9) = -21.05$$

$$B = C \sin(\theta) = 45 \sin(-117.9) = -39.76$$

$$\text{Respuesta} \rightarrow -21.05 - j39.76$$

Transformar a la forma rectangular y polar

$$a) 10 + j3 - (7 + j2)(3 < -115^\circ) - 2j$$

$$C = \sqrt{A^2 + B^2} = \sqrt{7^2 + 2^2} = 7.28$$

$$\theta = \tan^{-1}\left(\frac{B}{A}\right) = \tan^{-1}\left(\frac{2}{7}\right) = 15.94^\circ$$

$$\text{Respuesta} \rightarrow 7.28 < 15.94^\circ$$

$$(7.28 < 15.94^\circ)(3 < -115^\circ) = 21.84 < -99.06^\circ$$

$$* 21.84 < -99.06^\circ \text{ a rectangular}$$

$$A = C \cos(\theta) = 21.84 \cos(-99.06) = -3.44$$

$$B = C \sin(\theta) = 21.84 \sin(-99.06) = -21.57$$

$$\text{Respuesta} \rightarrow -3.44 - j21.57$$

$$10 + j3 + 3.44 + j21.57 - 2j = 0$$

$$\text{Respuesta} \rightarrow 13.44 + j22.57$$

$$* 13.44 + j22.57 \text{ a polar}$$

$$C = \sqrt{A^2 + B^2} = \sqrt{13.44^2 + 22.57^2} = 26.26$$

$$\theta = \tan^{-1}\left(\frac{B}{A}\right) = \tan^{-1}\left(\frac{22.57}{13.44}\right) = 59.22^\circ$$

$$\text{Respuesta} \rightarrow 26.26 < 59.22^\circ$$

$$b) 6.8 < 125.3^\circ + \frac{4.5 < -11.5^\circ}{7.6 - j1.2}$$

$$* 7.6 - j1.2 \text{ a polar}$$

$$C = \sqrt{A^2 + B^2} = \sqrt{7.6^2 + (-1.2)^2} = 7.69$$

$$\theta = \tan^{-1}\left(\frac{B}{A}\right) = \tan^{-1}\left(\frac{-1.2}{7.6}\right) = -8.97^\circ$$

$$\text{Respuesta} \rightarrow 7.69 < -8.97^\circ$$

$$6.8 < 125.3^\circ + \frac{4.5 < -11.5^\circ}{7.69 < -8.97^\circ}$$

$$\frac{4.5 < -11.5^\circ}{7.69 < -8.97^\circ} = \frac{4.5}{7.69} < -11.5 + 8.97^\circ$$

Respuesta $\rightarrow 0.58 < -2.53^\circ$

* $(6.8 < 125.3^\circ) + (0.58 < -2.53^\circ)$ a rectangular

$$A = C \cos(\theta) = 6.8 \cos(125.3) = -3.92$$

$$B = C \sin(\theta) = 6.8 \sin(125.3) = 5.54$$

Respuesta $\rightarrow -3.92 + j5.54$

$$A = C \cos(\theta) = 0.58 \cos(-2.53) = 0.57$$

$$B = C \sin(\theta) = 0.58 \sin(-2.53) = -0.02$$

Respuesta $\rightarrow 0.57 - j0.02$

$$(-3.92 + j5.54) + (0.57 - j0.02)$$

***Respuesta* $\rightarrow -3.35 + j5.52$**

* $-3.35 + j5.52$ a polar

$$C = \sqrt{A^2 + B^2} = \sqrt{(-3.35)^2 + 5.52^2} = 6.45$$

$$\theta = \tan^{-1}\left(\frac{B}{A}\right) = \tan^{-1}\left(\frac{5.52}{-3.35}\right) = -58.74^\circ$$

***Respuesta* $\rightarrow 6.45 < -58.74^\circ$**

c) $\frac{34 + j28.6}{4 < -20.8^\circ} - 51.2 < 215^\circ$

* $34 + j28.6$ a polar

$$C = \sqrt{A^2 + B^2} = \sqrt{34^2 + 28.6^2} = 44.43$$

$$\theta = \tan^{-1}\left(\frac{B}{A}\right) = \tan^{-1}\left(\frac{28.6}{34}\right) = 40.07^\circ$$

Respuesta $\rightarrow 44.43 < 40.07^\circ$

$$\frac{44.42 < 40.06^\circ}{4 < -20.8^\circ} = \frac{44.43}{4} < 40.06^\circ + 20.8^\circ$$

Respuesta $\rightarrow 11.10 < 60.87^\circ$

* $(11.10 < 60.87^\circ) - (51.2 < 215^\circ)$ a rectangular

$$A = C \cos(\theta) = 11.10 \cos(60.87) = 5.40$$

$$B = C \sin(\theta) = 11.10 \sin(60.87) = 9.70$$

Respuesta $\rightarrow 5.4 + j9.70$

$$A = C \cos(\theta) = 51.2 \cos(215) = -41.94$$

$$B = C \sin(\theta) = 51.2 \sin(215) = -29.36$$

$$\text{Respuesta} \rightarrow -41.94 - j29.36$$

$$(5.4 + j9.70) - (-41.94 - j29.36)$$

$$\text{Respuesta} \rightarrow 47.34 + j39.06$$

$$* 47.34 + j39.06 \text{ a polar}$$

$$C = \sqrt{A^2 + B^2} = \sqrt{47.34^2 + 39.06^2} = 61.37$$

$$\theta = \tan^{-1}\left(\frac{B}{A}\right) = \tan^{-1}\left(\frac{39.06}{47.34}\right) = 39.52^\circ$$

$$\text{Respuesta} \rightarrow 61.37 < 39.52^\circ$$

Fórmulas usadas para los cálculos:

** Forma Rectangular a Polar*

$$A \pm jB$$

$$C = \sqrt{A^2 + B^2}$$

$$\theta = \tan^{-1}\left(\frac{B}{A}\right)$$

$$C < \theta$$

** Forma Polar a Rectangular*

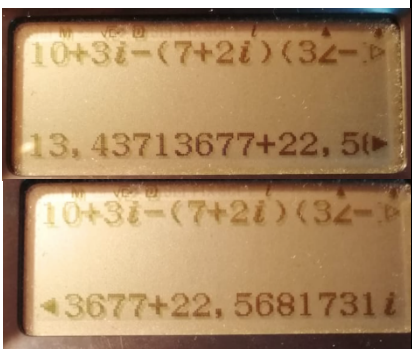
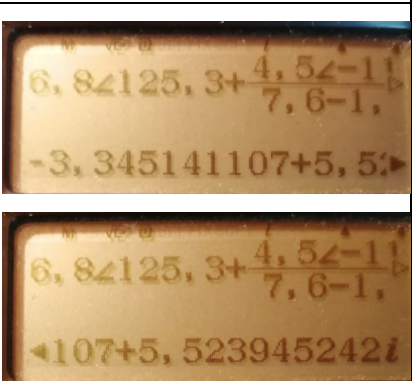
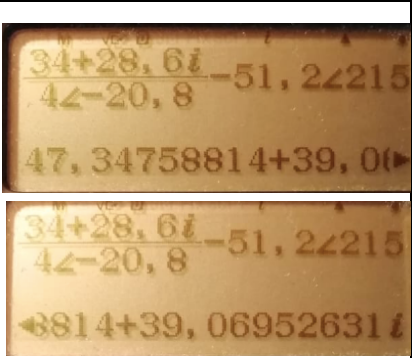
$$C < \theta$$

$$A = C \cos(\theta)$$

$$B = C \sin(\theta)$$

$$A \pm jB$$

- Resuelva las operaciones anteriores por medio de la calculadora y compare resultados.

$a) 10 + j3 - (7 + j2)(3 \angle -115^\circ) - 2j$	<p>Respuesta $\rightarrow 13.44 + j22.57$</p>	
$b) 6.8 \angle 125.3^\circ + \frac{4.5 \angle -11.5^\circ}{7.6 - j1.2}$	<p>Respuesta $\rightarrow -3.35 + j5.52$</p>	
$c) \frac{34 + j28.6}{4 \angle -20.8^\circ} - 51.2 \angle 215^\circ$	<p>Respuesta $\rightarrow 47.34 + j39.06$</p>	

- Los resultados obtenidos tanto para el literal a,b y c se asemejan a lo que sale en la calculadora, ya que al realizar los pasos uno por uno los decimales no se los toma en cuenta y la calculadora lo que hace es tomar todos los decimales de los cálculos y mostrar el resultado completo.