

**The City College Of New York  
Grove School of Engineering**



**Civil Engineering Department**

**Mechanics of Deformable Bodies (CE 334)-Fall 2018**

**New Jersey Transit Authority  
Beam Design Project**

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NJ TRANSIT  
BAY HEAD YARD SUBSTATION  
30% SUBMITTAL  
BOROUGH OF BAY HEAD, OCEAN COUNTY, N.J.

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## **Abstract**

Our company has been hired by the New Jersey Transit Authority to provide engineering services for their new building project which is located in Borough of Bay Head, Ocean County, NJ. The following report contains calculations regarding the design of specific portions of the New Jersey Transit Authority's new Substation Service Building design project.

As specified by the client, the flexural design, maximum deflection limit, revised flexural design, lightest W-shaped column, max footing size and revised calculations for all portions of the design are included. As per the request of the client, we have also considered the inclusion of a generator on the roof in our calculations. Explanations are also included along with the calculations in the report so that the client can have a better understanding of the design project.

This report is the next step to the 30% design package submitted and fulfills all of the client's requirements. Our engineers went through all of the questions and have provided answers with detailed analysis and design calculations.

Known: For lightest W-Shapes on 1<sup>st</sup> floor.

\* The Factor of Safety = 2.0  $\rightarrow \frac{\sigma_{ult}}{\sigma_{all}}$

\* Ignore deflection

\* USE "1<sup>st</sup> Floor Drawings" (S-102) for Beams 1 and 2

\* USE "Roof Drawings" (S-104) for Beams 3 and 4

- Location of Beam 1: Electrical Room. (See figure 1)

• Based on Beam Type table: Rolled Shapes: ASTM A922  
 $\rightarrow$  Stress:  $\sigma_y = 50000 \text{ psi}$

- knowing total load; by using General Notes (S-001)-

• Design loads for electrical room: Dead load =  $75 \frac{\text{lb}}{\text{ft}^2}$       Live load =  $100 \frac{\text{lb}}{\text{ft}^2}$       Total load =  $175 \frac{\text{lb}}{\text{ft}^2}$

$$L_{tot} = L_D + L_L$$

$$\text{Load total} = \left(175 \frac{\text{lb}}{\text{ft}^2}\right) \left(\frac{1 \text{ ft}}{12 \text{ in}}\right)^2 = 1.2152 \text{ psf}$$

• The weight of the concrete itself:

$$\text{If } \rho \text{ of concrete is } = \left(150 \frac{\text{lb}}{\text{ft}^3}\right) \left(\frac{1 \text{ ft}}{12 \text{ in}}\right)^3 = 0.08680 \frac{\text{lb}}{\text{in}^3}$$

then, the weight for slab with 6" thickness:

$$(0.08680 \frac{\text{lb}}{\text{in}^3})(6 \text{ in}) = 0.52083 \frac{\text{lb}}{\text{in}^2}$$

$$L_{tot} = 1.2152 \frac{\text{lb}}{\text{in}^2} \text{ and } L_{self} = 0.52083 \frac{\text{lb}}{\text{in}^2}$$

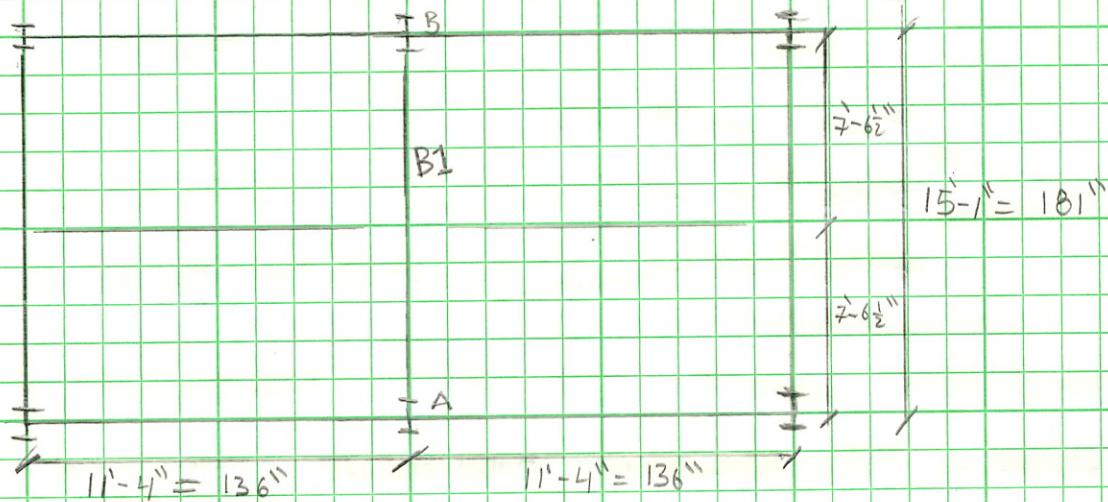
- Distributed Load:  $W = L_{tot} + L_{self} = (L_{tot} + L_{self}) (\text{length of section})$  at B1

• See figure 1 for more details: length of section for B1: 11'-4" = 136"

$$W = (1.2152 + 0.52083) \frac{\text{lb}}{\text{in}^2} (136 \text{ in}) = [236 \cdot 100 \frac{\text{lb}}{\text{in}} = W]$$

- Allowable stress: since  $SOF = 2.0 = \frac{\sigma_{ult}}{\sigma_{all}} \rightarrow \sigma_{all} = \frac{50000 \text{ psi}}{2.0} = 25 \text{ ksi}$

Figure 1: Beam 1 (NTS)



$\Sigma 56.100 \text{ lb/in}$

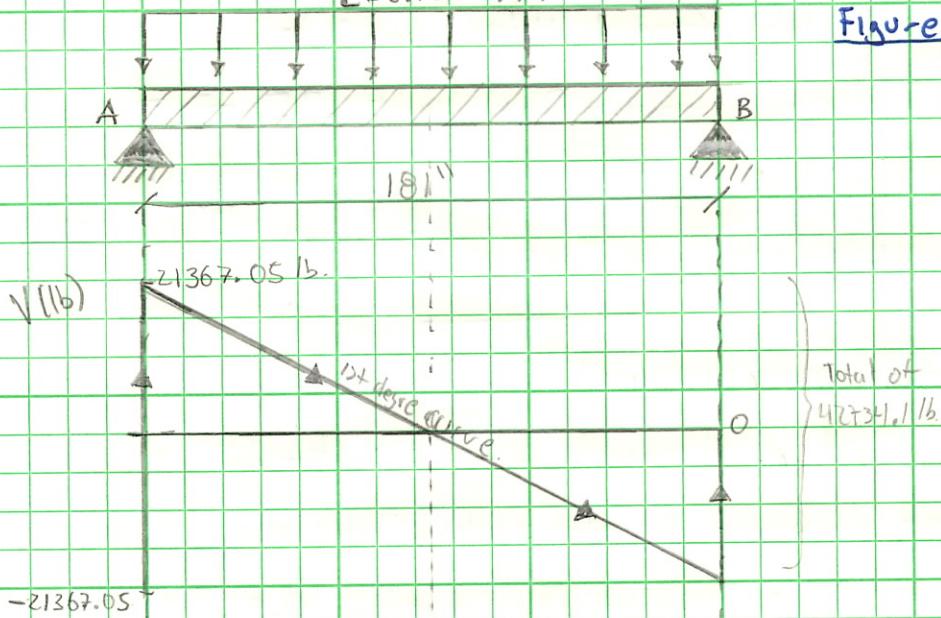


Figure 2: Load Distribution on Beam 1

Figure 3:

Shear Diagram.  
Total of  $47734.1 \text{ lb.}$

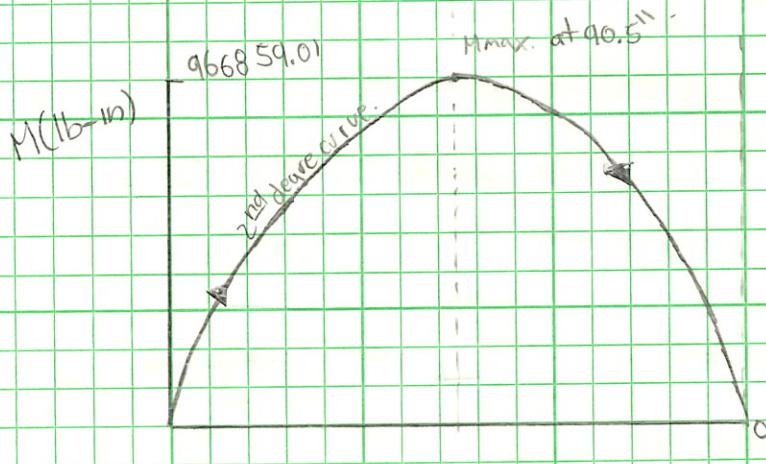


Figure 4:

Moment Diagram.  
 $M(\text{lb-in})$

$M_{\max.} \text{ at } 90.5''$

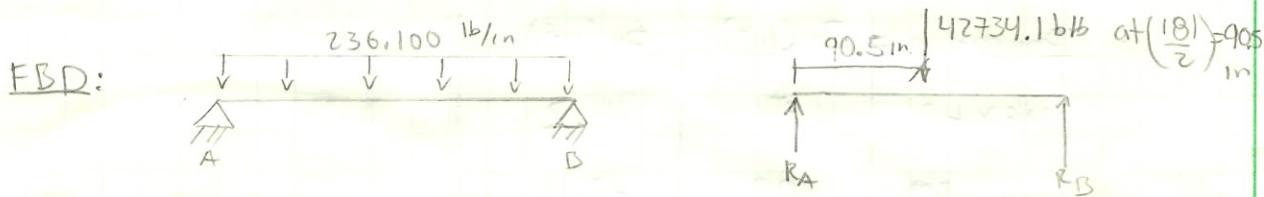
$966859.01$

21

## 2.1) Flexural Design

## Calculations for M-V diagrams Beam 1

- Since our  $W$  is Distributed along the Beam (B1). (see figure 2).



- To Find Reactions: Use Basic Statics knowledge.

- Because of symmetry:  $\frac{42734.1 \text{ lb}}{2} = 21367.05 \text{ lb} = R_A = R_B$ .

OR

$$\sum M_A = 0 \rightarrow R_B(18 \text{ in}) - (42734.1 \text{ lb})(9.5 \text{ in}) = 21367.05 = R_B$$

$$\sum F_y = 0 \rightarrow R_A + R_B = 42734.1 \text{ lb} \rightarrow R_A = 21367.05 \text{ lb}.$$

- From Reactions: we know  $V_{max} = 21367.05 \text{ lb}$  since  $R_A$  is pointing upward

- For Shear Diagram, since the Beam only experiences an evenly distributed load, then our graph will look linear with negative slope until it reaches  $R_B$ . which then brings it back to zero. (see figure 3)

- In order to graph out Moment Diagram!

- Max Moment:  $(V_{max})(\frac{18}{2})$  (since its at the center) =

$$M_{max} = \frac{(21367.05 \text{ lb})(9.5 \text{ in})}{2} = 966859.01 \text{ lb.in}$$

- Because of symmetry: Total moment = 0 when we reach to 18"

(see figure 4)

- We can obtain out section Modulus. by using equation:  $\frac{I}{c} \geq \frac{M_{max}}{\sigma_{all}}$

But,  $\frac{I}{c} = S$  so  $\rightarrow S = \frac{M_{max}}{\sigma_{all}} \cdot \frac{5}{X} = \frac{966859.01 \text{ lb.in}}{(50000 \text{ lb/in}^2) \cdot \frac{1}{2}} = 38.674 \text{ in.}$

- The Beam options based on our  $S_x$ , and Based on the W-table: (choose slightly bigger  $S_x$ ).

(see table 1.1)

Table 1.1 - Beam Options.

Designation #	$I_x (in^4)$	$S_x (in^3)$	$d (in)$
W8X48	184	43.3	8.5
W10X39	209	42.1	9.92
W12X35	285	45.6	12.5
W14X30	291	42.0	13.8

(3)

## Z.1) Flexural Design.

## Calculations

## Beam 2.

Since Beam 2 is also located in the Electrical Room,

$$\text{The total load} = 175 \text{ lb/ft}^2 = 1.2152 \text{ lb/in}^2$$

We know from B1 that  $\sigma_{yield} = 50,000 \text{ psi}$  •  $\sigma_{all} = 25 \text{ ksi}$

$$\text{Load 1} = T_L (\text{length of section}) = (1.215 \text{ psi})(136 \text{ in}) = 165.280 \text{ lb}$$

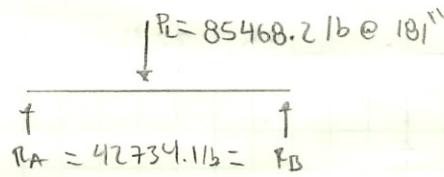
$$\text{Load 2} = (0.5268 \text{ psi})(136 \text{ in}) = 70.833 \text{ lb/in.}$$

$$W = L_1 + L_2 = 236.100 \text{ lb/in.}$$

-  $P_L = (W)(\text{Span length}) = (236.100 \text{ lb/in})(181 \text{ in} + 181 \text{ in}) = 85468.2 \text{ lb}$

- If we want to find the reactions: (see figure 5).

FBD



Because of symmetry:

$$R_A = R_B \quad \text{or we can use our Statics knowledge:}$$

$$R_A = R_B = \frac{1}{2}(85468.2 \text{ lb}) = 42734.1 \text{ lb.}$$

- For our Shear diagram: (see figure 6).

$$\bullet R_A = V_{max} = 42734.1 \text{ lb (T)}$$

$$\bullet M_{max} = \underline{\underline{V_{max}(181 \text{ in})}} =$$

- For our Moment diagram  
(see figure 7).

$$= \underline{\underline{(42734.1 \text{ lb})(181 \text{ in})}} =$$

$$= 3867436.05 \text{ lb.in.}$$

- For our Section Modulus:  $S_x = \frac{M_{max}}{\sigma_{all}} = \frac{3867436.05 \text{ lb.in}}{\frac{(50000 \text{ lb/in}^2)}{2}} =$

$\downarrow$

$$S_x = 154.601 \text{ in}^3$$

- We want to find Beam Options: (see table Z.1).

Figure 5: Load Distribution on Beam 2.

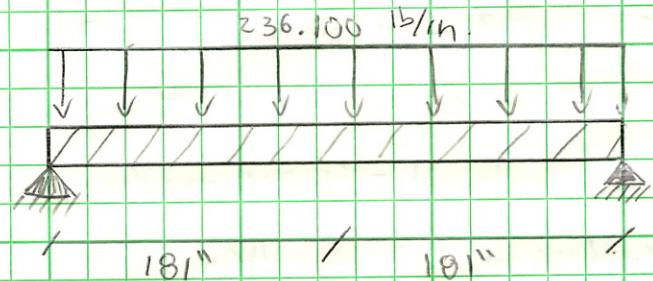


Figure 6: Shear Diagram for Beam 2.

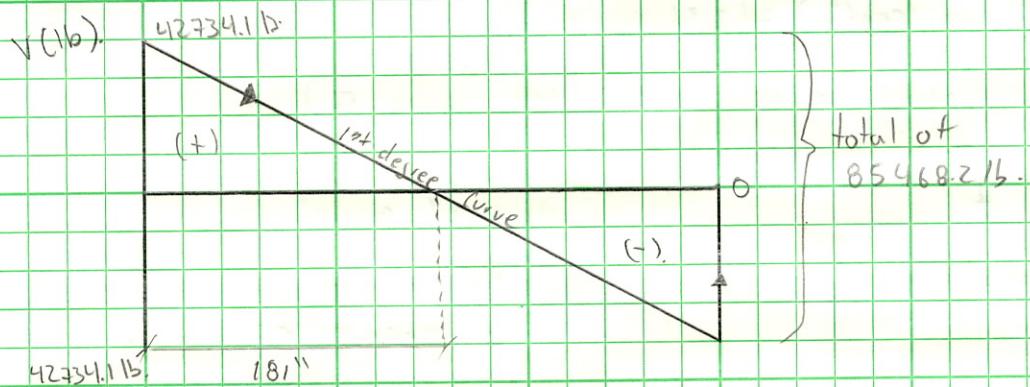


Figure 7: Moment Diagram of Beam 2.

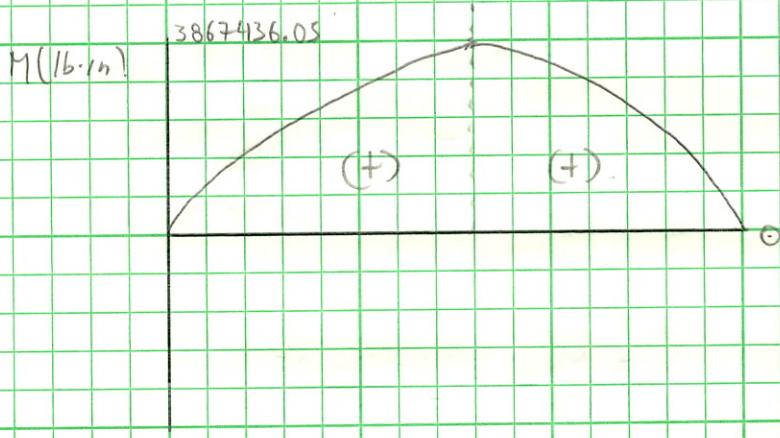


Table 2.1 - Beam Options.

Designation #	$I_x(\text{in}^4)$	$S_x(\text{in}^3)$	$d(\text{in})$
W24X68	1830	154	23.7
W16X89	1300	155	16.75
W14X99	1110	157	14.16
W18X86	1530	166	18.4
W21X93	1930	171	21.4

(4)

## 2.1) Flexural Design

## Calculations

## Beam 3.

$$\sigma_y = 50,000 \text{ psi}$$

$$\sigma_{all} = 25,000 \text{ psi}$$

$$\text{Loads: Dead} = 25 \text{ lb/ft}^2$$

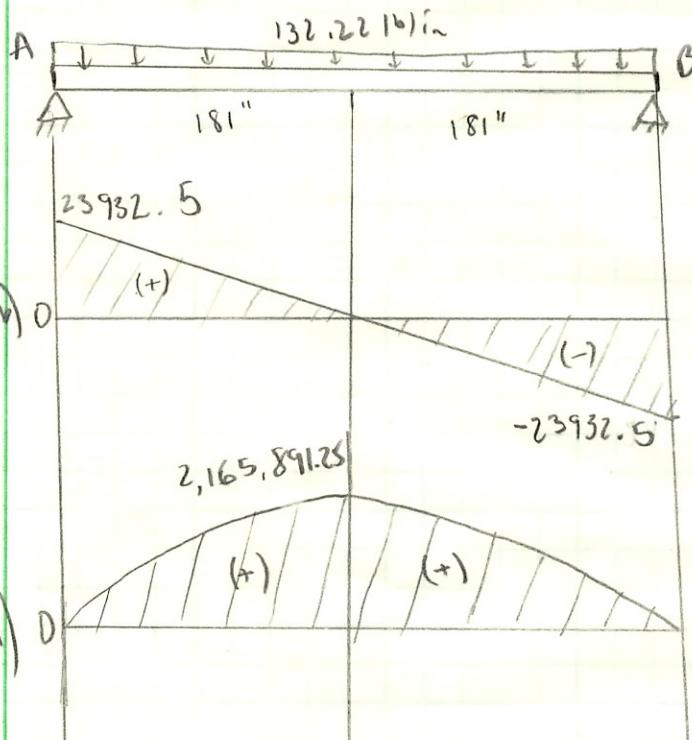
$$\text{Live} = 40 \text{ lb/ft}^2$$

$$\text{Total} = 65 \text{ lb/ft}^2 \left( \frac{1 \text{ ft}^2}{144 \text{ in}^2} \right) = 0.4514 \text{ psi}$$

$$w_1 = (0.4514)(136) = 61.39 \text{ lb/in}$$

$$w_2 = (150 \text{ lb/ft}^3) \left( \frac{1 \text{ ft}^3}{1728 \text{ in}^3} \right) (6 \text{ in}) (136 \text{ in}) = 70.83 \text{ lb/in}$$

$$w = w_1 + w_2 = 61.39 + 70.83 = 132.223 \text{ lb/in}$$



$$P_L = (L)(w) = (362)(132.223)$$

$$P_L = 47865 \text{ lb}$$

$$R_A = R_B = \frac{P_L}{2}$$

$$R_{A,B} = \frac{47865}{2} = 23932.5 \text{ lb}$$

$$M_{max} = \frac{(V_{max})(181)}{2}$$

$$M_{max} = \frac{(23932.5)(181)}{2}$$

$$S_x = \frac{M_{max}}{\sigma_x} = \frac{2165891.25}{25000} = 2165891.25$$

$$S_x = 86.636 \text{ in}^3$$

Table 3.1 - Beam Options

Designation	$I_x$ (in <sup>4</sup> )	$S_x$ (in <sup>3</sup> )	$d$ (in)
W12x72	597	97.4	12.3
W16x57	758	92.2	16.4
W18x50	800	88.9	18.0
W14x68	722	103	14.0

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## 2.1) Flexural Design

## Calculations

## Beam 4.

$$\text{Total load} = 0.4514 \text{ lb/in}^2$$

$$\text{Concrete Density} = 150 \text{ lb/ft}^3$$

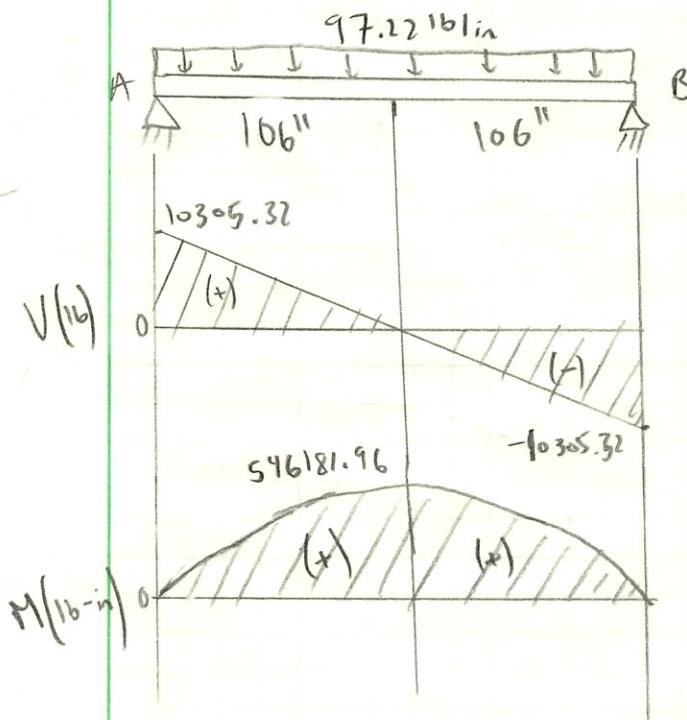
$$\sigma_{all} = 25 \text{ ksi}$$

Distributed loads:

$$w_1 = (0.4514)(100) = 45.139 \text{ lb/in}$$

$$w_2 = (150 \text{ lb/ft}^3) \left( \frac{1 \text{ ft}^3}{1728 \text{ in}^3} \right) (6 \text{ in}) (100 \text{ in}) = 52.0833 \text{ lb/in}$$

$$w = w_1 + w_2 = 45.139 + 52.0833 = 97.22 \text{ lb/in}$$



$$P_L = C(\omega) = (212)(97.22)$$

$$P_L = 20610.6 \text{ lb}$$

$$R_A = R_B = \frac{P_L}{2}$$

$$R_{A,B} = \frac{20610.6}{2} = 10305.32 \text{ lb}$$

$$M_{max} = \frac{|V_{max}|(l/2)}{2}$$

$$M_{max} = \frac{(10305.32)(106)}{2}$$

$$M_{max} = 546181.96 \text{ lb-in}$$

$$S_x = \frac{M_{max}}{\delta_x} = \frac{546181.96}{25000} = 21.84 \text{ in}^3$$

Table 4.1 - Beam options

<u>Designations</u>	$I_x (\text{in}^4)$	$S_x (\text{in}^3)$	$d (\text{in})$
W14 x 22	199	29	13.7
W12 x 22	156	25.4	12.3
W10 x 22	118	23.2	10.2
W8 x 28	98	24.3	8.06

⑥

2.2) Revise Flexural Design.

Calculations

Beam. 3.

$$\text{Live Load} = \left(40 \frac{\text{lb}}{\text{ft}^2}\right) \left(\frac{1 \text{ ft}^2}{144 \text{ in}^2}\right) (136 \text{ in}) = 37.78 \text{ lb/in}$$

$$\frac{L}{360} = \frac{362}{360} = 1.0056$$

$$\delta_{\max} = \frac{5 w L^4}{384 EI}$$

① W12x72

$$\delta_{\max} = \frac{5 (37.78) (362)^4}{(384) (29 \times 10^6) (597)} = 0.488 < 1.0056 \quad \underline{\text{Pass}}$$

② W16x57

$$\delta_{\max} = \frac{5 (37.78) (362)^4}{(384) (29 \times 10^6) (758)} = 0.3843 < 1.0056 \quad \underline{\text{Pass}}$$

③ W16x50

$$\delta_{\max} = \frac{5 (37.78) (362)^4}{(384) (29 \times 10^6) (800)} = 0.364 < 1.0056 \quad \underline{\text{Pass}}$$

④ W14x68

$$\delta_{\max} = \frac{5 (37.78) (362)^4}{(384) (29 \times 10^6) (722)} = 0.4034 < 1.0056 \quad \underline{\text{Pass}}$$

(7)

## 2.2) Revise Flexural Design Calculations

## Beam 4

We know from our flexural design calculations that:

The total load =  $w = w_1 + w_2 = 97.22 \text{ lb/in}$ . But we want

$$\text{Live load} = \left( 40 \frac{\text{lb}}{\text{ft}^2} \right) \left( \frac{1\text{ft}}{12\text{in}} \right)^2 (100\text{in}) = 27.7778 \text{ lb/in} \text{ Live!}$$

Not use Dead Load

$$E = 29 \times 10^6 \text{ psi}$$

If a max deflection limit of  $\frac{L}{360}$  under live loads.

$$\text{Live load} = \frac{L}{360} = \frac{181}{360} = 0.5027$$

Use  $\frac{5W14}{384EI}$  (chart from book)

Using our beam options: Our  $S_x = 21.84 \text{ in}^3$ .

$$\text{W14 X 22: } I_x(1\text{m}^4) = 199, S_x(1\text{m}^3) = 29.$$

$$\text{Live load: } \frac{5(\text{Load})(181\text{in})^4}{384(E)(I_x)} = \frac{5(27.7778 \text{ lb/in})(181\text{in})^4}{384(29 \times 10^6 \text{ lb/in}^2)(199\text{in}^4)} = 0.06723.$$

$$0.06723 < 0.5027 \text{ (Good)}$$

$$\text{W12 X 22: } I_x(1\text{m}^4) = 156, S_x(1\text{m}^3) = 25.4$$

$$\text{Live load: } \frac{5(27.7778 \text{ lb/in})(181\text{in})^4}{384(29 \times 10^6 \text{ lb/in}^2)(156\text{in}^4)} = 0.0858 > 0.5027 \text{ (Good)}$$

$$\text{W10 X 22: } I_x(1\text{m}^4) = 118, S_x(1\text{m}^3) = 23.2$$

$$\text{Live load: } \frac{5(27.7778 \text{ lb/in})(181\text{in})^4}{384(29 \times 10^6 \text{ lb/in}^2)(118\text{in}^4)} = 0.11344 > 0.5027 \text{ (Good)}$$

$$\text{W8 X 28: } I_x(1\text{m}^4) = 98, S_x(1\text{m}^3) = 24.3$$

$$\text{Live load: } \frac{5(27.7778 \text{ lb/in})(181\text{in})^4}{384(29 \times 10^6 \text{ lb/in}^2)(98\text{in}^4)} = 0.13659 > 0.5027 \text{ (Good)}$$

(8)

## 2.3) Revise Flexural Design. | Calculations for lightest bot/Beam | Beam 3.

We use our previous tables. (table 3.1).

B3

$$\frac{L}{d} = 16 \Rightarrow d = \frac{L}{16} = \frac{362}{16} = 22.625 \text{ in}$$

① W12x72

$$d = 12.3 < 22.625 \quad \underline{\text{fail}}$$

② W16x72

$$d = 16.4 < 22.625 \quad \underline{\text{fail}}$$

③ W18x50

$$d = 18 < 22.625 \quad \underline{\text{fail}}$$

④ W14x68

$$d = 14 < 22.625 \quad \underline{\text{fail}}$$

New choice : W24x68

$$\delta_{\max} = \frac{5(37.78)(362)^4}{(384)(6 \times 10^6)(1830)} = 0.1592 < 1.005 \quad \underline{\text{Pass}}$$

$$d = 23.7 > 22.625 \quad \underline{\text{Pass}}$$

(9)

2.3) Revise Flexural Design

Calculations for lightest W Beam

Beam 4.

Use table 4.1 with "d" values.

B4

$$\frac{L}{d} = 16 \Rightarrow d = \frac{L}{16} = \frac{212}{16} = 13.25 \text{ in}$$

① W14 x 22

$$d = 13.7 > 13.25 \quad \underline{\text{Pass}}$$

② W12 x 22

$$d = 12.3 < 13.25 \quad \underline{\text{fail}}$$

③ W10 x 22

$$d = 10.2 < 13.25 \quad \underline{\text{fail}}$$

④ W8 x 28

$$d = 8.06 < 13.25 \quad \underline{\text{Pass}}$$

(10)

## 2.4) Design Calculations

Calculation for lightest W-column

B/4 column.

Under axial loads, ignore deflection limits in previous questions.

and no buckling. eccentricity of 12".  $\phi = 2.0$ .

$$\sigma_{eff} = \frac{50000 \text{ psi}}{2.0} = 25 \text{ ksi}$$

From our flexural design calculations: we said that: the load distribution:

$$R_R = R_A = R_B = 21367.05 \text{ lb}; \text{ load applied then is } 2 \times R_A \\ = 42734.1 \text{ lb.}$$

For the column conditions:

- Total load = Live load + Dead load =  $w_1$

$$= (75 \text{ lb/ft}^2) + (100 \text{ lb/ft}^2) = 175 \text{ lb/ft}^2 \left( \frac{1 \text{ ft}^2}{144 \text{ in}^2} \right) = 1.2152 \frac{\text{lb}}{\text{in}^2}$$

$$w_1 = (1.2152 \frac{\text{lb}}{\text{in}^2})(90.5 \text{ in}) = 109.985 \text{ lb/in.}$$

- Concrete:  $w_2 = (\text{Density concrete})(\text{thickness of slab}) \times (\text{length of col.}) =$

$$(150 \frac{\text{lb}}{\text{ft}^3})(6 \text{ in})(90.5 \text{ in}) \left( \frac{1 \text{ ft}}{12 \text{ in}} \right)^3 = 47.1354 \frac{\text{lb}}{\text{in.}}$$

(see figure 9) for reference.

$$w_T = 109.985 + 47.1357 = 157.120 \text{ lb.}$$

From Distributed load:

- $P_L = w(\text{Span length}) = (157.12 \frac{\text{lb}}{\text{in}})(136 \text{ in}) =$

- $P_{tot} = P_L + P_R$       21,368.32 lb.

$$P_{tot} = 21368.32 \text{ lb} + 21367.05 \text{ lb} = 42,735.37 \text{ lb.}$$

- Reactions from a total force  $P$ :  $R_A = R_B = \frac{21,368.32 \text{ lb}}{2} = 10684.16 \text{ lb.}$

- $R_A = V_{max}$ .       $M_{max} = 363261.1 \text{ lb.in.}$

(see figure 9) for distributed load.

- Shear Diagram (Figure 10).

FBD.

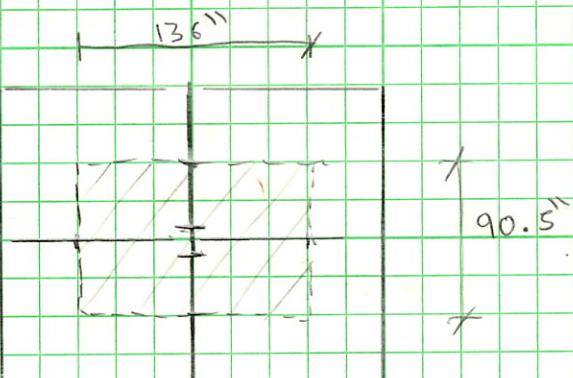
$$\downarrow 21,368 \text{ lb} @ 34"$$

$$A \quad A \\ f \quad f \\ R_A = 10684.16 \text{ lb}$$

- Moment Diagram (Figure 11).

$$\star S_y = \frac{M}{C_{eff}} = \frac{(P_{tot})(12 \text{ in})}{25000 \frac{\text{lb}}{\text{in}^2}} = \frac{(42735.37 \text{ lb})(12 \text{ in})}{25000 \frac{\text{lb}}{\text{in}^2}} = 25.64 \text{ in}^3.$$

Figure 8: Column



Problem states eccentricity of 12"

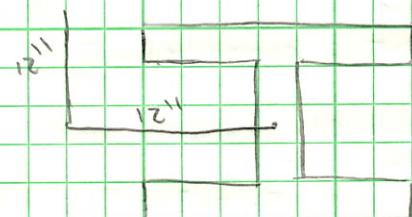


Figure 9: Distributed load.

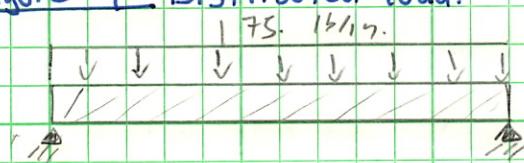


Figure 10: Shear Diagram

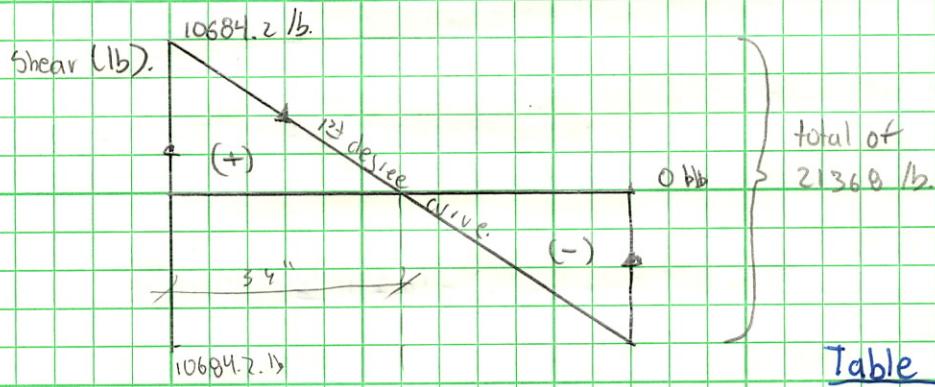
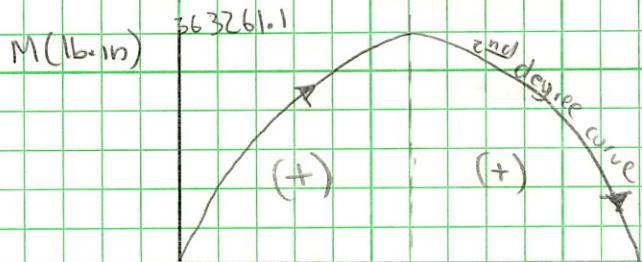


Table 4.1:

Figure 11: Moment Diagram



Designation #	$I_x (in^4)$	$I_y (in^4)$	$S_y (in^3)$
W16X77	1106	138	26.9
W14X74	796	134	26.6
W10X68	394	134	26.4

d (cm)	Area	Width (cm)
16.77	22.6	10.295
14.17	21.8	10.070
10.40	20.0	10.130

(11)

## 24) Design Calculations.

Calculation for lightest W-col.

B/g

\* From our table 4.1, test our W shape beam

$$\sigma = \frac{P_0}{A} + \frac{M_x(Y_{max})}{I_x} + \frac{M_y(X_{max})}{I_y} \quad M_y = M_x = (42735.35 lb)(12 in) \\ = 512836.2 lb \cdot in$$

\* W16 X 77     $I_x(1n^4) = 1100$ ,  $I_y(1n^4) = 138$ ,  $S_y(1n^3) = 26.9$ ,  $d = 16.77$   
 $A = 22.6 \text{ in}^2$ , width =  $10.295 \text{ in.}$

$$Y_{max} = \frac{d}{2} = \frac{16.77}{2} = 8.385 \text{ in.}$$

$$X_{max} = \frac{\text{width}}{2} = \frac{10.295}{2} = 5.147 \quad \sigma = \frac{(42735.35 lb)}{22.6 \text{ in}^2} + \frac{(512836.2 lb \cdot in)(8.385 in)}{1100 \text{ in}^4} + \frac{(512836.2)(5.145)}{138}$$

$$\sigma = 24,920 \frac{lb}{in^2} < \sigma_{all}(25 k_{s1}) \quad \underline{\text{Good}}$$

\* W14 X 74     $I_x(1n^4) = 796$ ,  $I_y(1n^4) = 134$ ,  $S_y(1n^3) = 26.6$ ,  $d = 14.17$ , width =  $10.070$

$$\text{Area} = 21.8 \text{ in}^2$$

$$Y_{max} = 14.17/2 = 7.085 \quad \left. \begin{array}{l} \\ X_{max} = 10.070/2 = 5.035 \end{array} \right\} \sigma = \frac{(42735.35 lb)}{21.8 \text{ in}^2} + \frac{(512836.2 lb \cdot in)(7.085 in)}{796 \text{ in}^4} + \frac{(512836.2 lb \cdot in)(5.035 in)}{134 \text{ in}^4}$$

$$\sigma = 25,794.5 \frac{lb}{in^2} > 25 k_{s1}(\sigma_{all}) \quad \underline{\text{Failure}}$$

\* W10 X 68     $I_x = 394 \text{ in}^4$ ,  $I_y = 134 \text{ in}^4$ ,  $S_y = 26.4 \text{ in}^3$ ,  $d = 10.40 \text{ in}$ ,  $A = 26 \text{ in}^2$ ,

$$\text{width} = 10.130 \text{ in.}$$

$$Y_{max} = 10.40/2 = 5.2 \text{ in} \quad \left. \begin{array}{l} \\ X_{max} = 10.130/2 = 5.065 \text{ in} \end{array} \right\} \sigma = \frac{(42735.35 lb)}{20 \text{ in}^2} + \frac{(512836.2 lb \cdot in)(5.2 in)}{394 \text{ in}^4} + \frac{(512836.2 lb \cdot in)(5.065 in)}{134 \text{ in}^4}$$

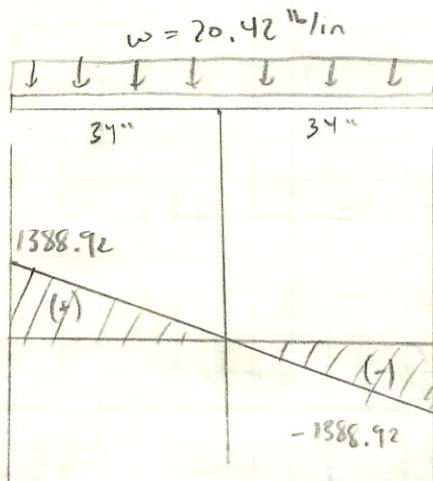
$$\sigma = 28,284.6 > \sigma_{all} \quad \underline{\text{Failure.}}$$

(12)

## 2.4) Design Calculations

## Calculation for lightest W-column

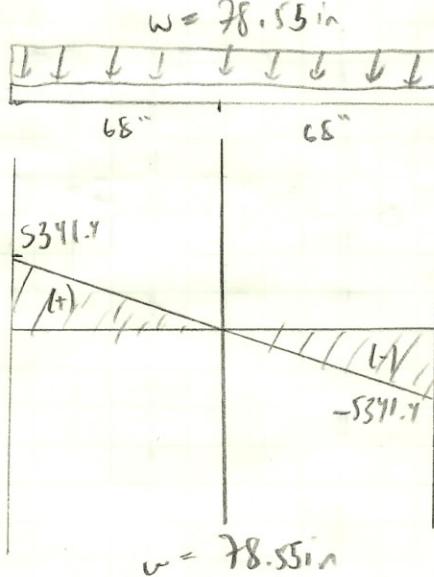
P/L

Roof

$$P_1 = 27021.05 \text{ lb}$$

$$P_2 = 2777.8 \text{ lb}$$

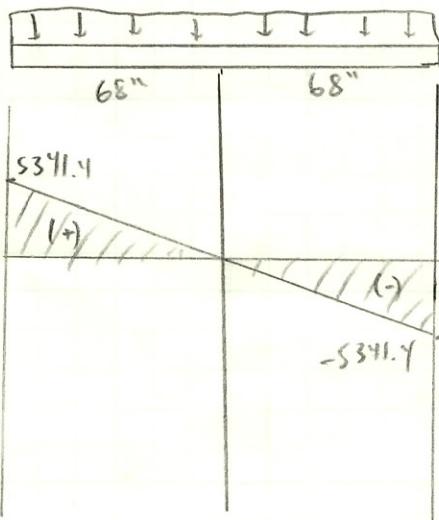
$$P = P_1 + P_2 = 26799 \text{ lb}$$

1st FL

$$P_1 = 42735.97 \text{ lb}$$

$$P_2 = 10682.8 \text{ lb}$$

$$P = P_1 + P_2 = 53418.8 \text{ lb}$$

2nd FL

$$P_1 = 21368 \text{ lb}$$

$$P_2 = 10682.8 \text{ lb}$$

$$P = P_1 + P_2 = 32050.8 \text{ lb}$$

$$P_{\text{total}} = 112268.5 \text{ lb}$$

$$M_x = M_y = (112 \text{ lb/in}^2)(112) = 1347221.5 \text{ lb-in}$$

$$S_y = \frac{M}{\sigma_{all}} = \frac{1347221.5}{25000} = 53.889 \text{ in}^3$$

Designation	$A(\text{in}^2)$	$d (\text{in})$	$b_f (\text{in})$	$I_x (\text{in}^4)$	$I_y (\text{in}^4)$	$S_y (\text{in}^3)$
W27x146	43.1	27.4	14	5660	443	63.5
W14x145	42.7	14.8	15.5	1710	677	87.3
W30x173	51	30.4	15	8230	598	79.8

(13)

2.4) Design Calculations

Calculations for lightest Ws-cold

D/4

$$\sigma = \frac{P}{A} + \frac{M_x(Y_{max})}{I_x} + \frac{M_y(X_{max})}{I_y}$$

① W 27x146

$$\sigma = \frac{32050}{(43.1)} + \frac{(1347221.04)(27.4/2)}{(5660)} + \frac{(1347221.04)(14/2)}{443}$$

$$\sigma = 743.62 + 3260.94 + 21287.9 = 25292.48 > \sigma_{all}$$

fail

② W 14x145

$$\sigma = \frac{32050}{42.7} + \frac{(1347221.04)(14.8/2)}{1710} + \frac{(1347221.04)(15.5/2)}{677}$$

$$\sigma = 750.6 + 5830.08 + 15422.4 = 22003 < \sigma_{all}$$

Pass

③ W 30x173

$$\sigma = \frac{32050}{51} + \frac{(1347221.04)(30.4/2)}{8230} + \frac{(1347221.04)(15/2)}{598}$$

$$= 628.43 + 24888.18 + 16896.58 = 20013.2 < \sigma_{all}$$

Choose W14x145 because it is lightestPass

(14)

2.5) Determine min size of 18" thick sqr footings.  
B/4 and D/4 columns.

$$\sigma_{a||} = \frac{7000}{2} = 3500 \frac{\text{lb}}{\text{ft}^2} \left( \frac{1}{144} \right) = 24.31 \text{ psi}$$

$$\sigma_c = (18") \left( 15.16/\text{ft}^3 \right) \left( \frac{1 \text{ ft}^3}{1728 \text{ in}^3} \right) = 0.156 \text{ psi}$$

$$P = 42736.6 \text{ lb}$$

$$\sigma_{a||} = \sigma_c + \frac{P}{A} = 24.31 = 0.156 + \frac{42736.6}{A}$$

B41

$$\frac{42736.6}{A} = 24.15 \rightarrow A = 1769.36 \text{ in}^2$$

$$S = \sqrt{1769.36} = 42.06 \text{ in} \approx \underline{42 \text{ in}}$$

D41

$$A = \frac{P}{A} = \frac{11268.46}{24.31} = 4618.2 \text{ in}^2$$

$$S = \sqrt{4618.2} = 67.95 \text{ in} \approx \underline{68 \text{ in}}$$

## 2.6) Investigation of impact Calculations.

- New Request: 250 psf on roof by adding a new generator

$$\sum MA = (66,669 \text{ lb}) (96.5 \text{ in}) + (23935 \text{ lb})(0.75) + RB = 0$$

RB = 34,519 lb.

$$\sum F_y = RB + RA - (66,669 \text{ lb}) - (23935 \text{ lb}) = 0$$

RA = 55.989 lb

$w_1$  = total weight = 236.096 lb/in

$w_2$  = 132.7 lb/in

$$S_{min} = \frac{4.254.775 \text{ lb-in}}{23,690 \frac{\text{lb}}{\text{in}^2}} = 170.191 \text{ in}$$

$$D_{ref} = \frac{-5w_2L^4}{384EI} + \frac{w_1y}{24EIL} (a^24l^2a^2 - 2ax^2 2La + Lx^3)$$

$$L = 181 \text{ in.}$$

when,  $\frac{dy}{dx} = 0$ ,  $x = 166.4 \text{ in.}$

live load definition

$$\text{total } S = \frac{5w_2L^4}{384EI} + \frac{w_1(9.79 \times L'')}{24EIL}$$

$$\text{live } S = \frac{5w_2L^4}{384EI}$$

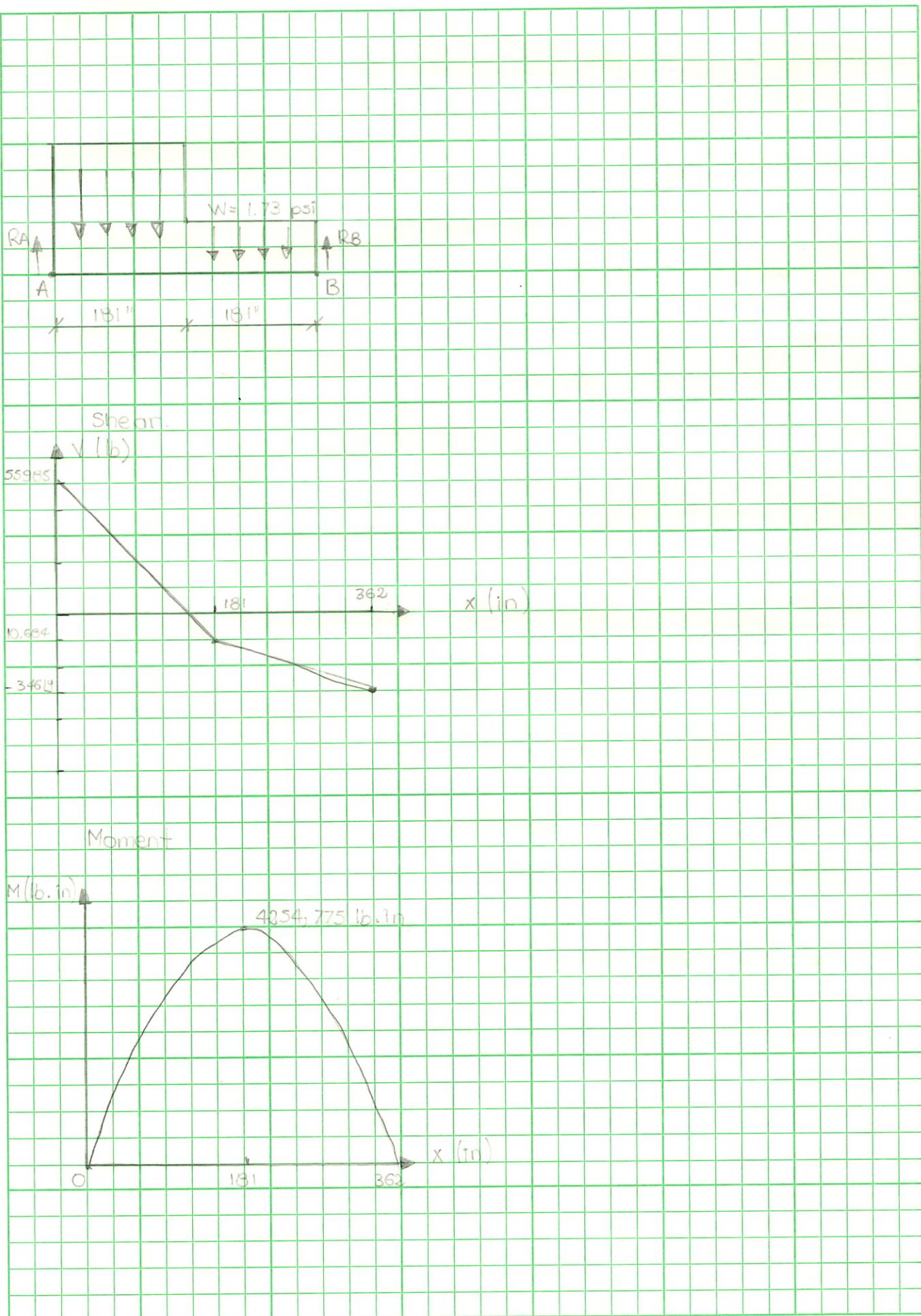
$$\text{total live load} = 274 \frac{\text{lb}}{\text{in}}$$

- So the lighter beams vertre going to test die?

W 10x76

W 24x68

W 27x84



## 2.6) Investigation of Impact Calculations.

criterion live:  $\frac{362 \text{ in}}{360 \text{ in}} = 1.005$

total =  $\frac{362 \text{ in}}{240 \text{ in}} = 1.51$

test.

- W 19x75

$$\text{Ix} = 1330 \text{ in}^4$$

$$\text{live} = \frac{(5)(229 \text{ lb/in})(362 \text{ in})^4}{384(29 \times 10^6 \text{ lb/in}^2)(1330 \text{ in}^4)} = 1.6 > 1.005 \quad (\text{fail})$$

- W 24x68

$$\text{Ix} = 1830 \text{ in}^4$$

$$\text{live} = \frac{(5)(274 \text{ lb/in})(363 \text{ in})^4}{384(29 \times 10^6 \text{ lb/in}^2)(1830 \text{ in}^4)} = 1.157 > 1.005 \quad (\text{fail})$$

- W 27x84

$$\text{Ix} = 2850 \text{ in}^4$$

$$\text{total} = \frac{5(132.7 \text{ lb/in})(362 \text{ in}^4)}{384(29 \times 10^6 \text{ lb/in}^2)(2850 \text{ in}^4)} + \frac{(236 \text{ lb/in})(9.29 \times 10^4)}{24(29 \times 10^6 \text{ lb/in})(2850 \text{ in}^4)} = 68$$

$$\text{live} = \frac{5(274 \text{ lb/in})(362 \text{ in}^4)}{384(29 \times 10^6 \text{ lb/in}^2)(2850 \text{ in}^4)} = 0.74 < 1.005 \quad (\text{pass})$$

Depth of W 27x84

$$\frac{362 \text{ in}}{16} \leq \text{depth}$$

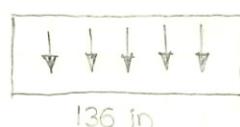
$$26.7 \text{ in} \leq 22.625 \text{ in} \quad (\text{pass})$$

- W 27x84 ✓

### Columns

B4 supported by generator

B4



$$\begin{aligned} \text{total weight} &= (.4514 \text{ lb/in}^2)(45.25 \text{ in}) \\ &+ (190 \text{ lb/in}^2)(1 \text{ lb}/12 \text{ in})^3 (6 \text{ in})(45.25 \text{ in}) \\ &+ (1.73 \text{ lb/in}^2)(45.25 \text{ in}) = 122.28 \text{ lb/in} \end{aligned}$$

$$P = (122.28 \text{ lb/in})(136 \text{ in}) = 16,630.08 \text{ lb}$$

Total depth on all floors = 138.121 ft

$$M_N = (158.121 \text{ ft})(2 \text{ in}) = 1897468.4 \text{ lb.in}$$

$$\therefore S_y = \frac{1897468.4 \text{ lb.in}}{23,060 \text{ lb.in}^2} = 75.9 \text{ in}^3$$

Steel shapes to be examined:

- W 30 x 173

- W 14 x 145

- W 33 x 201

$$\text{f}_y = 36,000 \text{ lb/in}^2$$

• W 30 x 173

$$A = 41 \text{ in}^2, C_y = 15.2 \text{ in}, C_x = 7.5 \text{ in}, I_y = 8230 \text{ in}^4, I_x = 592 \text{ in}^4$$

$$S = \frac{(158.121 \text{ ft})}{51.0 \text{ in}^2} + \left( \frac{1897468.4 \text{ lb.in}}{8230 \text{ in}^4} \right) + \left( \frac{(1897468.4 \text{ lb.in})(36 \text{ in})}{592 \text{ in}^4} \right)$$

$$S = 30,402.5 \text{ psi} > 25,060 \text{ psi} \quad (\text{fail})$$

• W 14 x 143

$$A = 42.7 \text{ in}^2, C_y = 7.4 \text{ in}, C_x = 7.76 \text{ in}, I_y = 1710 \text{ in}^4, I_x = 677 \text{ in}^4$$

$$S = \frac{(158.121 \text{ ft})}{42.7 \text{ in}^2} + \left( \frac{(1897468.4 \text{ lb})(7.9 \text{ in})}{1710 \text{ in}^4} \right) + \left( \frac{(18974624 \text{ lb.in})(7.72 \text{ in})}{677 \text{ in}^4} \right)$$

$$S = 33,635.7 \text{ psi} > 25,060 \text{ psi}$$

(fail)

• W 33 x 201

$$A = 59.2 \text{ in}^2, C_y = 16.85 \text{ in}, C_x = 7.25 \text{ in}, I_y = 7445 \text{ in}^4, I_x = 1466 \text{ in}^4$$

$$S = \frac{(158.121 \text{ ft})}{59.2 \text{ in}^2} + \left( \frac{(187468.4 \text{ lb.in})(16.185 \text{ in})}{7445 \text{ in}^4} \right) + \left( \frac{(147469.41 \text{ lb.in})(7.85 \text{ in})}{1466 \text{ in}^4} \right)$$

$$S = 2015.24 \text{ psi} < 25,000 \text{ psi}$$

(pass)

- W 33 x 201 ✓

footing:

- B/4 is not offered by generator

- D/4 fail = 24.81 psi

New area:  $A = 7150.75 \text{ in}^2$

$$S = \sqrt{7150.75 \text{ in}^2} = 84.36 \text{ in} \neq 85 \text{ in}$$

## **2.7 – Composite Action**

As stated within the instructions of the project, we are to assume all beams are simply supported, steel has elasto-plastic stress-strain characteristics, ignore any lateral load, and ignore any composite action between the concrete slabs and steel beams. However, in a more realistic approach to the design project where the concrete slabs and beams would be connected (by bolts, etc) then you would have to take composite action into consideration.

If the two materials were in composite action, it would result in an overall stronger member because materials that are in composite action are considered as one material. Composite action increases the strength of the beams which increases the yielding stress and allowable stress.

If the member is stronger, it means that it can support a greater allowable load. This greater allowable load would result in a smaller sectional modulus (compared to the one calculated in the report) because allowable stress and section modulus are inversely proportional. As allowable stress increases, section modulus decreases. With a smaller section modulus, we have more choices for beams to choose from for our design. This allows us to choose a beam that is lighter, more economical and supports a greater load.