EXAMINATION COVERSHEET

Spring 2022 Final Examination



THIS EXAMINATION CONTENT IS STRICTLY CONFIDENTIAL	
Students must comply with requirements stated in the Examination Policy & Procedures	
Student Number:	
First Name:	
Family Name:	
Date of Examination:	27/06/22
(DD/MM/YY)	
Subject Code:	Math 142
Subject Title:	Essentials of Engineering Mathematics
Time Permitted to Write Exam:	2 Hours
Total Number of Questions:	6 MCQs + 5 Written Questions
Total Number of Pages (including this page):	9

INSTRUCTIONS TO STUDENTS FOR THE EXAM

- 1. Please note that subject lecturer/tutor will be unavailable during exams. If there is a doubt in any of the exam questions i.e. problem solving etc. students should proceed by assuming values etc. Students should mention their assumption on the question paper.
- 2. Answers must be written (and drawn) in black or blue ink
- 3. Any mistakes must be crossed out. Whitener and ink erasers must not be used.
- 4. Part A: MCQs. Answer ALL questions. The marks for each question are shown next to each question.
- 5. Part B: Written. Answer ALL questions. The marks for each question are shown next to each question.
- 6. You must show your work in detail.
- 7. Total marks: 100. This Exam is worth 40% of your final marks for Math 142.

EXAMINATION MATERIALS/AIDS ALLOWED

Approved Calculators and Formula Sheet

<u>Exam Unauthorised Items</u> - Students bringing these items to the examination room must follow the instructions of the invigilators with regards to these items.

- 8. Bags, including carrier bags, backpacks, shoulder bags and briefcases
- 9. Any form of electronic device including but not limited to mobile phones, smart watches, MP3 players, handheld computers and unauthorised calculators;
- 10. Calculator cases and covers, opaque pencil cases
- 11. Blank paper
- 12. Any written material

NOTE: The University does not guarantee the safe-keeping of students' personal items during examinations. Students concerned about the safety of their valuable items should make alternative arrangements for their care.

Part A MCQ (30%) (circle your choice)

(5pts) Problem 1

Evaluate the improper integral $L = \int_2^\infty \frac{dx}{x \ln^2 x}$.

- (a) $L = \ln 2$
- $(b) \quad L = \frac{1}{\ln 2}$
- (c) $L = +\infty$
- $(d) \quad L=2$
- (e) $L = e^2$

(5pts) Problem 2

Evaluate the improper integral $A = \int_0^1 \frac{x}{\sqrt{1-x^2}} dx$

- $(a) \quad A = 1$
- (b) A = 2
- (c) A = -1
- $(d) A = \frac{1}{2}$
- (e) $A = -\infty$

(5pts) Problem 3

Let a_n be the sequence given by

$$\cos(\pi)$$
, $\cos\left(\frac{\pi}{2}\right)$, $\cos\left(\frac{\pi}{3}\right)$, $\cos\left(\frac{\pi}{4}\right)$, ...

If $L = \lim_{n \to \infty} a_n$, then

- (a) L = 4
- (b) L = 3
- (c) L = 2
- (d) L = 1
- (e) L=0

(5pts) Problem 4

The series

$$\sum_{n=1}^{\infty} \frac{(-1)^n}{\sqrt[3]{n}}$$

- (a) converges absolutely
- (b) converges conditionally
- (c) diverges
- (d) is a convergent geometric series
- (e) is a divergent telescoping series

(5pts) Problem 5

The radius of convergence of the power series $\sum_{n=1}^{\infty} \frac{x^n}{n2^n}$ is

- (a) $\sqrt{2}$
- $(b) \quad \frac{1}{2}$
- (c) 1
- (d) ∞
- (e) 2

(5pts) **Problem 6**

The coefficient of x^3 in Maclaurin series of the function $f(x) = \sin(\pi - x)$ equal to

- $(a) \quad \frac{-1}{3}$
- $(b) \quad \frac{-1}{6}$
- (c) 1
- (d) 6
- $(e) \quad \frac{-1}{2}$

Part B Written Questions (70%)

(15pts)Problem 1

Find the interval of convergence of the following power series

1.
$$\sum_{n=0}^{\infty} \frac{(x+2)^n}{\sqrt{n}}$$
 2. $\sum_{n=0}^{\infty} \frac{x^n}{n^n}$.

$$2. \sum_{n=0}^{\infty} \frac{x^n}{n^n}.$$

(10pts)Problem 2

Show that the equation is separable and solve it.

$$y\frac{dy}{dx} - \left(1 + y^2\right)x^2 = 0$$

(15pts)Problem 3

Show that the differential equation is exact and solve the initial value problem.

$$(y-x^3) dx + (x+y^3) dy = 0, \quad y(0) = \sqrt{2}$$

(15pts)Problem 4

Show that the equation is Bernoulli and solve it.

$$\frac{dy}{dx} = \frac{2y}{x} - x^2y^2$$

(15pts)Problem 5

Show that the equation is homogeneous and solve it.

$$x^2 \frac{dy}{dx} = xy - y^2$$