

$$\oint \mathbf{B} \cdot d\vec{s} = \mu_0 I \quad (\text{Ampere's Law})$$

↓
constant electric field

Maxwell $\Rightarrow \oint \mathbf{B} \cdot d\vec{s} = \mu_0 (I + I_d)$ → displacement current
(due to non uniform \vec{E})

$$I_d = \epsilon_0 \frac{d\Phi_E}{dt}$$

Ampere's Law $\oint \mathbf{B} \cdot d\vec{s} = \mu_0 I + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt} \Rightarrow$ Maxwell's Equations I ↑ Ampere's Maxwell Law

Electric flux $\Phi_E = \oint \mathbf{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$ Gauss's Law " " II

Magnetic Flux $\Phi_B = \oint \mathbf{B} \cdot d\vec{A} = 0$ Gauss's Law in magnetism " " III

emf $= \oint \mathbf{E} \cdot d\vec{s} = -N \frac{d\Phi_B}{dt}$ " " IV

Faraday's Law

$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$ Lorentz's Law

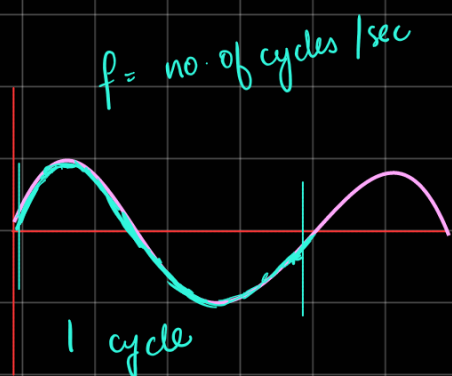
Basis of
electromagnetism

Properties of Electromagnetic wave

1. c (speed of light) $= \frac{1}{\sqrt{\epsilon_0 \mu_0}} \approx 3 \times 10^8 \text{ m/s}$

2. Transverse Wave $\Rightarrow \vec{E} \quad \vec{B}$ direction of propagation are all \perp to each other

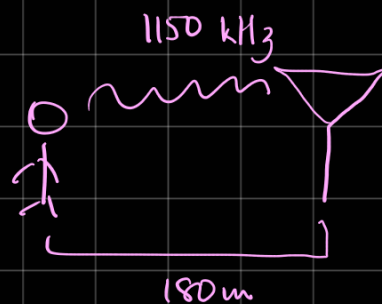
3 $c = \frac{E}{B}$; Wavelength $\lambda = \frac{c}{f}$ (m)
 $f \rightarrow$ frequency



Example

$$\lambda = \frac{c}{f} = \frac{3 \times 10^8}{1150 \times 10^3}$$

Wavelengths = $\frac{180}{\lambda}$



Poynting Vector \vec{S}

$$\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B} \quad (\text{W/m}^2)$$

\rightarrow direction

same as direction of propagation

(W/m²)

$$\text{Intensity} = S_{\text{avg}} = \frac{E_{\text{max}} B_{\text{max}}}{2 \mu_0} = \frac{B_{\text{max}}^2 c}{2 \mu_0} = \frac{E_{\text{max}}^2}{2 \mu_0 c}$$

Energy Density

$$U_E = \frac{1}{2} \epsilon_0 E^2$$

$$U_B = \frac{B^2}{2 \mu_0}$$

Total Energy Density in em wave

$$U_E + U_B$$

$$= \frac{1}{2} \epsilon_0 E^2 + \frac{B^2}{2\mu_0}$$

For electromagnetic wave

$$U_E = U_B$$

$\frac{1}{2}$ here $\frac{1}{2}$ here

Total energy density

$$= 2U_E = 2U_B$$

$$= \epsilon_0 E^2 = \frac{B^2}{\mu_0}$$

Total

Avg Energy Density

$$= U_{avg} = \frac{1}{2} \epsilon_0 E_{max}^2 = \frac{B_{max}^2}{2\mu_0}$$

$$\text{Intensity} = \frac{E_{max} B_{max}}{2\mu_0} = \frac{B_{max}^2 c}{2\mu_0}$$

$$= c \cdot U_{avg}$$

$$P = \frac{F}{A} = \frac{1}{A} \frac{dp}{dt}$$

\rightarrow momentum

$$= \frac{1}{A} \frac{d}{dt} (T_{ER} / dt)$$



Time derivative of the rate of energy transferred to the surface

$$= \frac{1}{A} \left[\frac{d T_{\text{em}} / dt}{c} \right] \rightarrow \frac{\text{Power}}{\text{Area}} = \text{Intensity}$$

$$= S_{\text{avg}} / c$$

$$= I / c \quad (\text{perfectly absorbing surface})$$

perfectly reflecting surface

$$P = \frac{2I}{c}$$

