

14

15

17

18

23

25

29

31

32

Article

A machine learning model for forecast procurement of secondary reserve capacity in power systems with significant vRES penetrations

João Passagem Santos D and Hugo Algarvio

- ¹ Affiliation 1; e-mail@e-mail.com
- ² Affiliation 2; e-mail@e-mail.com

Abstract: The growing investment in variable renewable energy sources is changing how electricity markets operate. Players rely on forecasts to participate in markets closing between 1 and 37 hours ahead of real-time operation. Usually, transmission system operators (TSOs) use a symmetrical procurement of up and down secondary power reserves based on the expected demand. This work uses machine learning techniques that dynamically computes it using the day-ahead programmed and expected dispatches of variable renewables, demand, and other technologies. The study uses operational open data from the Spanish TSO from 2014 to 2023 for training. Benchmark and test data are from the period of 2019 to 2022. The proposed methodology improves the usage of the up and down secondary reserved power by almost 47% and 42%, respectively.

Keywords: reserve systems; energy markets; neural networks; forecast

1. Introduction

The European Union's energy and climate goals for 2030 and 2050 emphasize the transition to a carbon-neutral energy system, driven by the large-scale integration of variable Renewable Energy Systems (vRES), such as wind and solar photovoltaic (PV) technologies [1]. While vRES are critical for achieving sustainability targets, such as Sustainable Development Goals (SDG) 7 (Affordable and Clean Energy) and SDG 13 (Climate Action), their stochastic and intermittent nature poses significant challenges to power system operations, particularly in balancing energy supply and demand efficiently.[2][3]

The increasing penetration of vRES introduces greater uncertainty into energy markets, particularly in Day-Ahead (DA) forecasts, which are essential for the allocation of secondary reserves. These reserves, procured to address real-time imbalances between generation and consumption, often suffer from inefficient allocation methodologies. DA predictions frequently diverge from real-time conditions, leading to both over-allocation and underallocation of reserves. This inefficiency not only results in higher operational costs but also compromises the optimal utilization of resources, thereby undermining the economic and energy efficiency of the system.

This paper focuses on enhancing the accuracy of DA forecasts for secondary reserve allocation, addressing the inefficiencies caused by vRES uncertainty. By leveraging machine learning techniques, this work develops predictive models that incorporate historical data on vRES generation, demand patterns, and system behavior. The objective is to dynamically adjust reserve allocations, ensuring that grid stability is maintained while minimizing excess reserve procurement.

The work present on this paper analyzes the benefits of using of machine learning techniques for an idependent, up and down, forecast of capacity procurement of secondary reserves. Publicly available operational data from the Spanish Transmission System Operators (TSO) was utilized, ensuring the replicability of the analysis. Typically, TSOs rely on bilateral agreements to acquire additional reserves, which can drive up costs. Analyzing

Citation: Passagem Santos, J.; Algarvio, H. Title. *Journal Not Specified* 2024, 1, 0. https://doi.org/

Received: Revised: Accepted:

Published:

4.0/).

Copyright: © 2024 by the authors. Submitted to *Journal Not Specified* for possible open access publication under the terms and conditions of the Creative Commons Attribution (CC BY) license (https://creativecommons.org/licenses/by/

43

45

51

55

65

78

82

the underutilization of secondary reserves and the frequent need for extraordinary capacity in Portugal and Spain highlights the inefficiencies in current methods for determining reserve requirements. [4]

The remainder of this paper is structured as follows. Section 2 provides an overview of wholesale energy markets and reserve systems, highlighting existing inefficiencies. Section 3 outlines the proposed methodology for dynamic reserve allocation using machine learning techniques. Section 4 presents case studies and evaluates the performance of the developed models. Finally, Section 5 summarizes the findings and discusses the implications for future energy systems.

2. Literature review

The increasing integration of vRES in power systems has created significant challenges for electricity markets and ancillary services. Traditionally, TSO rely on symmetric allocation of upward and downward reserves based on deterministic forecasts of demand. However, with vRES like wind and solar introducing substantial variability and unpredictability, these conventional methods have proven inefficient in addressing the real-time balancing needs of modern power grids.

Numerous studies highlight the limitations of static reserve procurement methods under high vRES penetration. The European Network of Transmission System Operators for Electricity (ENTSO-E) framework [5] outlines standardized methodologies for reserve sizing, which are Frequency Containment Reserve (FCR), automatic Frequency Restoration Reserve (aFRR) and manual Frequency Restoration Reserve (mFRR), but these often fail to adapt dynamically to changing system conditions. In Portugal, for example, the secondary reserve allocation formula used by the TSO employs a fixed ratio applied to expected demand, resulting in excessive allocation and energy waste . Similar inefficiencies are observed in the Spanish market, where reserve procurement lacks symmetry and adaptability to vRES production.

Dynamic procurement of secondary reserves has been proposed as a solution to address these inefficiencies [6], with an improvement in 13% and 8% for up and down secondary capacities. By incorporating real-time or near real-time forecasts of demand and renewable generation, dynamic methodologies aim to optimize reserve allocation, reducing both operational costs and resource wastage. Machine learning techniques have emerged as a powerful tool to support this transition. Studies such as [7] and [8] demonstrate the potential of predictive models to estimate reserve needs with greater accuracy, leading to significant reductions in over-procurement.

The literature also underscores the importance of enhancing forecast accuracy for vRES generation and consumption patterns. Traditional statistical models, including ARMA and ARIMA, have been widely used for time series forecasting. However, recent advancements in machine learning, such as Long Short-Term Memory (LSTM) networks and Convolutional neural network (CNN), have shown superior performance in capturing the nonlinear and temporal characteristics of renewable energy data [9]. These models can adapt to complex patterns and improve prediction accuracy, enabling more efficient management of reserves.

In summary, the literature identifies three key areas of focus: the inefficiency of static reserve allocation methods, the potential of machine learning to improve forecasting accuracy, and the need for market design adaptations to support dynamic reserve procurement. This paper builds upon these insights by applying machine learning techniques to optimize secondary reserve allocation in the Spanish electricity market, addressing both forecast uncertainty and market inefficiencies.

3. Electricity Markets and Ancillary Services

The operation of modern electricity systems relies heavily on well-structured markets to ensure the balance between generation and consumption. These markets encompass wholesale electricity markets, where energy is traded, and ancillary services markets,

92

93

100

101

102

103

105

108

110

113

114

115

117

119

120

which guarantee the system's stability and reliability. The integration of vRES has added complexity to these operations, requiring more dynamic approaches to market design and reserve allocation.

3.1. Wholesale Electricity Markets

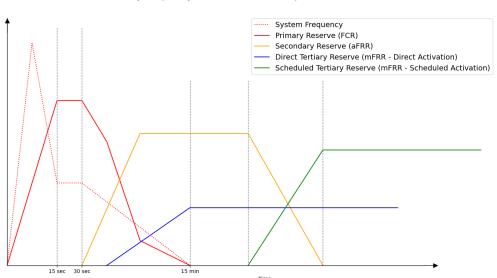
Wholesale electricity markets facilitate the trading of electricity between generators, suppliers, and other market participants. These markets are typically divided into three main categories: day-ahead markets (DAM), intraday markets (IDM), and real-time balancing markets. In the DAM, participants submit bids for energy delivery 12 to 37 hours before real-time operation. The market-clearing process determines the energy schedules and market prices based on supply and demand equilibrium [10]. While the DAM provides a foundation for energy trading, IDM allow participants to make adjustments closer to real-time, responding to unforeseen changes in demand or vRES generation.

Balancing markets, on the other hand, operate in near real-time to address deviations between scheduled and actual energy delivery. TSOs procure balancing services to ensure system equilibrium, activating reserves as needed. This process is particularly critical in systems with high vRES penetration, where forecasting errors can cause significant imbalances.[11] [12]

3.2. Ancillary Services and Reserve Requirements

Ancillary services are essential for maintaining grid stability and ensuring a reliable power supply. They include services such as frequency control, voltage regulation, and operating reserves. Among these, frequency control reserves play a crucial role in balancing supply and demand in real-time. These reserves are divided into three main categories:

- FCR: Activated automatically within seconds to stabilize frequency deviations.
- aFRR: Restore frequency to nominal levels and release FCR for subsequent use.
- mFRR: Address longer-term imbalances through manual activation.



Primary frequency deviation and subsequent activation of reserves

Figure 1. Ancillary Services response scheme. Adapted from [5]

3.3. Iberian Reserve Markets

Mercado Ibérico de Eletricidade (MIBEL) is the iberian example of energy market integration across countries. Acting as a bond between portuguese and spanish electricity markets, Operador do Mercado Ibérico de Energia Português, Sociedade Gestora do Mercado Regulamentado, S.A. (OMIP) and Operador del Mercado Ibérico de Energía - Pólo Espanhol, S.A (OMIE). This joint market consists of bilateral, derivatives, and spot markets.

123

124

125

127

129

131

133

138

141

142

143

144

145

146

148

149

Even though there is a joint market, each country's TSO, Red Eléctrica de España (REE) for Spain and *Redes Energéticas Nacionais* (REN) for Portugal, manages it's own ancillary services independently.

3.3.1. Static Reserve Procurement

In Europe, the ENTSO-E provides guidelines for the procurement and activation of these reserves. Traditionally, TSOs acquire reserves symmetrically (equal upward and downward capacities), based on deterministic demand forecasts. However, this approach often leads to inefficiencies in systems with high vRES variability.

For Secundary Reserve ENTSO-E proposes:

$$R = \sqrt{a \times L_{max} + b^2} - b \tag{1}$$

where:

- R: Secondary Control Reserve.
- $a \in b$: empiric coeficients, a=10MW and b=150MW.
- L_{max} : maximum anticipated consumer load.

The Spanish and Portuguese markets provide examples of differing reserve procurement methods. In Portugal, the TSO employs a fixed ratio formula for secondary reserve sizing. Creating a symmetrical distribution for Upward and Downward bands, respectively $\frac{2}{3}$ and $\frac{1}{3}$ of the Reserve band.

The given formula is based on ENTSO-E equation (1), adding an hourly ratio ρ :

$$R = \rho \times \sqrt{a \times L_{max} + b^2} - b \tag{2}$$

Conversely, the Spanish market lacks a standardized reserve procurement formula, relying instead on flexible procurement mechanisms [13]. Where the upward and downard bands distribuition is not directly symmetric. These differences highlight the need for market design improvements to better accommodate the variability of vRES.

4. Dynamic procurement of secondary power

This study proposes a dynamic procurement based on machine learning techniques trained with historical hourly data. With custom made model architectures

4.1. Methodology Implementation

The methodology aplied was a "brute force" choosing of better model, which can lead to better fine tuning results than a more complex architecture as shown in [14]. With multiple model related variables in study:

Table 1. Training and architecture variables.

Variables	Options
Architecture	CNN LSTM RNN UNET Transformer
Advance Loss function	Mirror Weights N/A
Loss function	MAE MSE MSLE
Activation	linear relu gelu
Weights	Temporal Distance to mean No Weights

Where each of the model variables in study where a layer of training, giving the best model within that scope we would go to the next variable with the given best option so far. Going back and forward as to not loose best possible choices.

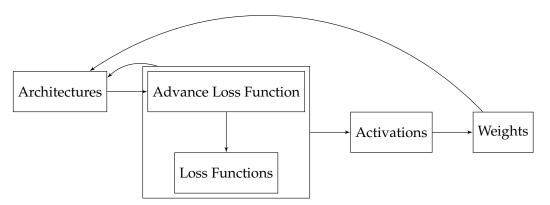


Figure 2. Model choice method scheme.

For the porpuse of controling and processing this experiment three python packages were created.

- Alquimodelia: A keras based model builder package, to create the necessary models
 with each different arch and variable.
- Alquitable: A keras based workshop package, to create custom callbacks, loss functions, data generators.
- MuadDib: A machine learning framework that uses alquimodelia to test and choose best models on given conditions automatically.

The experiments were done using keras>=3 with a torch backend on a CPU laptop.

4.2. Metrics

With distinct valorizations, the metrics, are used to choose best model on each iteration, and they can be divided into two groups: Model metric, where we just use the usual regression metrics adding a metric for how much did the model missed in alocating for the

150 151 152

159 160 161

158

163 164

170

171

172 173

174

177

178

179

180

182

183

186

188

validation periodo. And the comparative metrics, where we assert percentual gains over the current allocation method.

t: Real value. p: Forecast n: number of samples

4.2.1. Model Metrics

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (t_i - p_i)^2}$$
 (3)

$$SAE = \sum_{i=1}^{n} |t_i - p_i| \tag{4}$$

SAE can be divide into the following metrics, where we obtain the error, within the time period, of allocated energy not enough for the needs, and too much energy allocated, separatly.

AllocM - Missing Allocation:

$$AllocM = \begin{cases} 0 & \text{, if } p \ge t \\ t - p & \text{, if } p < t \end{cases}$$
 (5)

AllocS - Surplus Allocation

$$AllocS = \begin{cases} 0 & \text{, if } p \le t \\ p - t & \text{, if } p > t \end{cases}$$
 (6)

We need these metrics because we are not just looking to get a better error than the benchmark, we want to have both instances of less wasted allocated energy (AllocS), and less occurences of missing allocation (AllocS).

4.2.2. Model/benchmark comparative metrics

PPG - Performance Percentual Gain

$$PPG = \frac{SAE_{benchmark} - SAE_{modelo}}{SAE_{benchmark}} \times 100 \tag{7}$$

PPG is the percentage of how much better is the model over the benchmark. The following metrics are the same but for only missing allocation and surplus allocation. PPGM - Performance Percentual Gain Missing (allocation)

$$PPGM = \frac{AllocM_{benchmark} - AllocM_{modelo}}{AllocM_{benchmark}} \times 100$$
 (8)

PPGS - Performance Percentual Gain Surplus (allocation)

$$PPGS = \frac{AllocS_{benchmark} - AllocS_{modelo}}{AllocS_{benchmark}} \times 100$$
 (9)

The next metric is showing how much better is the model over the benchmark, but only if both condition are met. PPGM and PPGS positive. PPG Positive - Performance Percentual Gain Positive

$$PPGPositive = \begin{cases} PPG & \text{, if } PPGM \& PPGS \ge 0\\ 0 & \text{, if } PPGM \parallel PPGS < 0 \end{cases}$$
(10)

191

194

196

199

5. Case-study

To evaluate the aplicability of machine learning techniques for secondary reserve allocation the study was conducted using the Spanish electricity market historical data.

5.1. Data Sources and Preprocessing

The case study utilizes publicly available operational and historical data from the Spanish TSO, REE. Available at *Sistema de Información del Operador del Sistema* (ESIOS). The dataset includes the following key variables:

Table 2. ESIOS data used on the study.

ESIOS Code	ESIOS Name	Variable	Units
632	Secondary Reserve Allocation AUpward	Up Allocated	MW
633	Secondary Reserve Allocation ADownward	Down Allocated	MW
680	Upward Used Secondary Reserve Energy	Up Used	MWh
681	Downward Used Secondary Reserve Energy	Down Used	MWh
1777	Wind D+1 Daily Forecast	DA Wind	MWh
1779	Photovoltaic D+1 Daily Forecast	DA PV	MWh
1775	Demand D+1 Daily Forecast	DA Demand	MWh
10258	Total Base Daily Operating Schedule PBF Generation	DA Schedule Generation	MWh
14	Base Daily Operating Schedule PBF Solar PV	DA Schedule PV Generation	MWh
10073	Base Daily Operating Schedule PBF Wind Base Daily Operating	DA Schedule Wind Generation	MWh
10186	Shedule PBF Total Balance Interconnections	DA Scheduled Tie Lines	MWh

The data spans multiple years to account for seasonal variability and long-term trends in vRES generation and demand. Data preprocessing only handled missing values using interpolation methods, with IterativeImputer [15][16].:

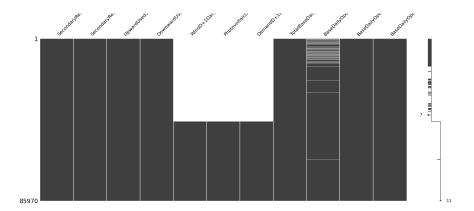


Figure 3. Missing Data

To choose the temporal space of the models temporal auto-correlations were checked: 200

Table 3. Temporal self correlation.

horas	1	2	24	23	25	168	144	192	48
Up	0.44	0.24	0.22	0.19	0.19	0.17	0.16	0.16	0.16
Down	0.43	0.22	0.25	0.20	0.19	0.21	0.19	0.20	0.19

We wanted to forecast DA values, so we will be forecasting 24 hours ahead. As for the input for that forecast the temporal correlactions present 168 hours as the next correlation after the one day period, which represents a week. We add also variable to account for each time range: day, day of year, month, day of week.

And so our models will receive data in (Batch Size, 168, 18) shape for input, and (Batch Size, 24, 1) shape for output.

5.1.1. Training Data

For training the full dataset from 2014 to 2023, inclusive was used. follows a description of said data:

Table 4. Training data summary.

	mean	std	min	max
Down Used	168.20	199.67	0.00	1721.40
Up Allocated	662.94	150.62	399.00	958.00
Down Allocated	549.27	126.67	312.00	956.00
Up Used	158.10	191.62	0.00	1654.80
DA Wind	5824.12	3413.15	71.33	20879.30
DA PV	1666.31	2719.60	0.00	14925.30
DA Demand	27944.24	4479.39	14170.00	41773.00
DA Schedule Generation	27249.43	4603.58	13470.50	42707.60
DA Schedule PV Generation	1714.09	2815.35	0.00	16358.90
DA Schedule Wind Generation	6525.51	3582.36	308.60	21619.60
DA Scheduled Tie Lines	290.58	2157.11	-7817.00	6858.50

With each variable correlation to used secondary reserve energy:

203

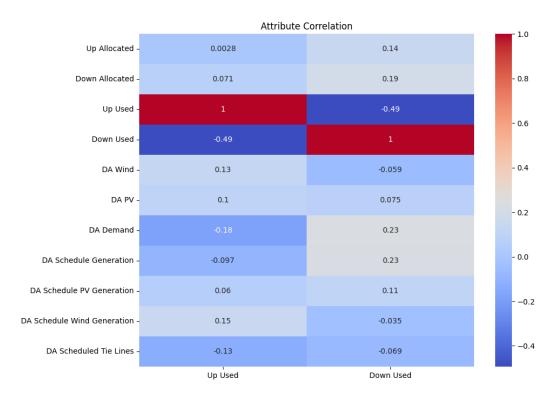


Figure 4. Attribute correlation

5.1.2. Validation Data

As for validation it was chosen the years 2019-2022, in direct comparison with validation from [17].

Using the non comparitive metrics we have the following results:

Table 5. Metric Results for validation data.

	RMSE	SAE	AllocF	AllocD
Up Allocation (MW)	536.55	17357826.75	152679.00	17205147.75
Down Allocation (MW)	408.99	12981575.55	479191.60	12502383.95

And the correlation between allocated energy in the current method to the used energy can be seen in the following image:

216

211

213

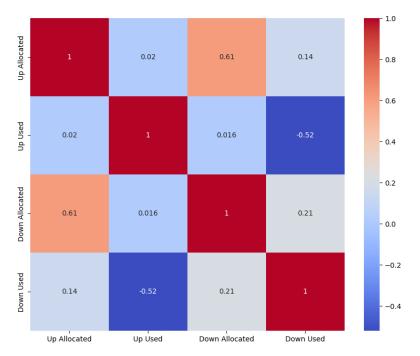


Figure 5. Attribute correlation benchmark

5.2. Results

The best results for each architeture can be seen below:

Table 6. Metric results for up and down forecast.

	Arquitetura	RMSE	SAE ×10 ⁶	AllocM ×10 ⁵	AllocS ×10 ⁶
	Aiquitetura		×10	×10	× 10
	UNET	304.34	9.19	1.47	9.05
	VanillaCNN	363.35	11.49	1.48	11.34
Up Allocation	VanillaFCNN	430.56	13.71	1.52	13.56
	StackedCNN	285.37	9.05	5.51	8.50
	Transformer	267.64	8.28	6.37	7.65
	UNET	262.71	7.52	4.71	7.05
	VanillaCNN	290.88	8.71	4.79	8.23
Down Allocation	onVanillaFCNN	345.38	10.50	4.77	10.03
	Transformer	351.15	10.69	4.59	10.23
	StackedCNN	270.28	8.16	9.92	7,17

Table 7. Comparative metric results for up and down forecast.

	Architecture	PPG %	PPG M %	PPG S %	PPG Positive %
	UNET	47.00	3.60	47.39	47.00
	VanillaCNN	33.83	2.76	34.11	33.83
Up Allocation	VanillaFCNN	21.01	0.69	21.19	21.01
•	StackedCNN	47.86	-261.16	50.60	0.00
	Transformer	52.27	-317.32	55.55	0.00
	UNET	42.07	1.65	43.62	42.07
	VanillaCNN	32.89	0.01	34.15	32.89
Down Allocation	onVanillaFCNN	19.09	0.40	19.81	19.09
	Transformer	17.63	4.18	18.15	17.63
	StackedCNN	37.12	-106.92	42.64	0.00

217 218

Table 8. Model Results and (allocated) values wthin 2019-2022.

	mean	std	min	max
D 411 (* (4.674)	(542.59)	(126.09)	(363.00)	(946.00)
Down Allocation (MW)	387.28	189.23	0.00	1711.80
Up Allocation (MW)	(623.68)	(152.39)	(419.00)	(958.00)
	391.31	157.08	0.00	1797.19
II 1 G	(1166.27)	(250.19)	(816.00)	(1891.00)
Hourly Capacity (MW)	778.59	213.68	174.85	2281.04
F. ((169.93)	(153.95)	(0.10)	(1226.40)
Extraordinary Down Er	nergy (MWh) 82.20	60.80	0.01	333.51
	(120.21)	(136.45)	(0.40)	(922.80)
Extraordinary Up Energ	59 56.46	41.46	0.03	212.13

The proposed model presente an overall improvement of \sim 47% in upward allocation amd \sim 42% in downward allocation, comparing to current allocation methods.

Where the hourly means differences between benchmark and validation results are:

Table 9. Mean Δ % between model and benchmark

	Δ%	
Down Allocation (MW)	-28.62	
Up Allocation (MW)	-37.26	
Hourly Capacity (MW)	-33.24	
Extraordinary Down Energy (MWh)	-51.62	
Extraordinary Up Energy (MWh)	-59.47	

Average hourly improvements are of \sim 37% and \sim 29% respectively, which also is an improvement on state of the art [17] with 13% and 8%. The current study can free in average \sim 33% of hourly resources, lowering the need to activate the third reserve in \sim 52% and \sim 59%.

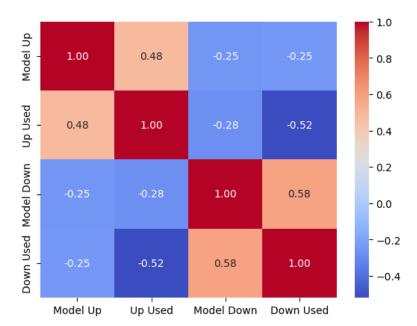


Figure 6. Attribute correlation

We can also check that the correlation between used and alocated is bigger than in the current method, achieving 48% in upward energy and 58% in downward.

219

223 224 225

220

222

232

233

234

237

238

239

241

243

244

245

247 248

6. Conclusions 229

The results of the case study validate the effectiveness of machine learning techniques in improving the accuracy of reserve forecasts and optimizing reserve allocation. By dynamically adjusting upward and downward reserves based on real-time forecasts, the proposed methodology addresses the inefficiencies of static procurement methods. The observed cost savings and improved reserve utilization demonstrate the practical benefits of this approach for systems with high renewable penetration.

Additionally, the case study highlights the potential for asymmetrical reserve procurement to better reflect system needs, particularly during periods of extreme renewable generation variability. The integration of weather forecasts into the predictive models further enhances their reliability, ensuring that reserve procurement decisions are informed by real-time conditions.

In conclusion, the case study illustrates that dynamic reserve procurement, supported by machine learning techniques, can significantly improve the efficiency and costeffectiveness of balancing services in modern electricity systems. These findings provide a strong foundation for further research and potential implementation in other power markets with similar challenges.

Abbreviations 246

The following abbreviations are used in this manuscript:

aFRR automatic Frequency Restoration Reserve

CNN Convolutional neural network

DA Day-Ahead

DAM day-ahead markets

ENTSO-E European Network of Transmission System Operators for Electricity

ESIOS Sistema de Información del Operador del Sistema

FCR Frequency Containment Reserve

IDM intraday markets

LSTM Long Short-Term Memory MAE Mean Absolute Error

manual Frequency Restoration Reserve mFRR

MIBEL Mercado Ibérico de Eletricidade

MSE Mean Squared Error

MSLE Mean Squared Logarithmic Error

OMIE Operador del Mercado Ibérico de Energía - Pólo Espanhol, S.A

OMIP Operador do Mercado Ibérico de Energia Português

PV solar photovoltaic REE Red Eléctrica de España **REN** Redes Energéticas Nacionais SDG Sustainable Development Goals **TSO** Transmission System Operators vRES variable Renewable Energy Systems

References

Perissi, I.; Jones, A. Investigating European Union Decarbonization Strategies: Evaluating the Pathway to Carbon Neutrality by

2050. Sustainability (Switzerland) 2022, 14, 4728. https://doi.org/10.3390/SU14084728/S1.

- 2. Ocker, F.; Ehrhart, K.M. The "German Paradox" in the balancing power markets. Renewable and Sustainable Energy Reviews 2017, 67, 892–898. https://doi.org/10.1016/J.RSER.2016.09.040.
- 3. Frade, P.M.; Pereira, J.P.; Santana, J.J.; Catalão, J.P. Wind balancing costs in a power system with high wind penetration - Evidence from Portugal. Energy Policy 2019, 132, 702-713. https://doi.org/10.1016/J.ENPOL.2019.06.006.
- 4. Estanqueiro, A.; et al.. D5.3 Performance assessment of current and new market designs and trading mechanisms for national and regional markets, 2022.
- 5. Handbook, U.O. Policy 1: Load-frequency control and performance. Final policy 2009, 2.
- Algarvio, H. Multi-step optimization of the purchasing options of power retailers to feed their portfolios of consumers. International Journal of Electrical Power and Energy Systems 2022, 142. https://doi.org/10.1016/J.IJEPES.2022.108260.

249

250 251 252

253

259

268

269

270

274

275

276

277

278

279

280

284

285

- 7. Vos, K.D.; Stevens, N.; Devolder, O.; Papavasiliou, A.; Hebb, B.; Matthys-Donnadieu, J. Dynamic dimensioning approach for operating reserves: Proof of concept in Belgium. *Energy Policy* **2019**, *124*, 272–285. https://doi.org/10.1016/J.ENPOL.2018.09.031.
- 8. Kruse, J.; Schäfer, B.; Witthaut, D. Secondary control activation analysed and predicted with explainable AI. *Electric Power Systems Research* **2022**, 212. https://doi.org/10.1016/J.EPSR.2022.108489.
- 9. Benti, N.E.; Chaka, M.D.; Semie, A.G. Forecasting Renewable Energy Generation with Machine Learning and Deep Learning: Current Advances and Future Prospects. *Sustainability (Switzerland)* **2023**, *15*. https://doi.org/10.3390/SU15097087.
- Mercado de Serviço de Sistemas.
- 11. Rassid, H.A.; Fernando, O..; Lopes, J.F. Mercado de Reservas: Simulador Multiagente SIMREEL e Caso de Estudo Envolvendo o Mercado Ibérico, 2017.
- 12. Carneiro, C. Mecanismos de funcionamento do Mercado de Serviços de Sistema aplicação ao MIBEL 2016.
- 13. Frade, P.M.; Shafie-khah, M.; Santana, J.J.; Catalão, J.P. Cooperation in ancillary services: Portuguese strategic perspective on replacement reserves. *Energy Strategy Reviews* **2019**, 23, 142–151. https://doi.org/10.1016/J.ESR.2018.12.011.
- 14. Liu, Z.; Mao, H.; Wu, C.Y.; Feichtenhofer, C.; Darrell, T.; Xie, S. A ConvNet for the 2020s. *Proceedings of the IEEE Computer Society Conference on Computer Vision and Pattern Recognition* **2022**, 2022-June, 11966–11976. https://doi.org/10.1109/CVPR52688.2022.01 167.
- 15. van Buuren, S.; Groothuis-Oudshoorn, K. mice: Multivariate Imputation by Chained Equations in R. *Journal of Statistical Software* **2011**, 45, 1–67. https://doi.org/10.18637/JSS.V045.I03.
- 16. Buck, S.F. A Method of Estimation of Missing Values in Multivariate Data Suitable for use with an Electronic Computer. *Journal of the Royal Statistical Society. Series B (Methodological)* **1960**, 22, 302–306.
- 17. Algarvio, H.; Couto, A.; Estanqueiro, A. A Methodology for Dynamic Procurement of Secondary Reserve Capacity in Power Systems with Significant vRES Penetrations. *International Conference on the European Energy Market, EEM* **2024**. https://doi.org/10.1109/EEM60825.2024.10608904.

Disclaimer/Publisher's Note: The statements, opinions and data contained in all publications are solely those of the individual author(s) and contributor(s) and not of MDPI and/or the editor(s). MDPI and/or the editor(s) disclaim responsibility for any injury to people or property resulting from any ideas, methods, instructions or products referred to in the content.