

# TRIGONOMETRY FORMULA LIST

by joyyntls

## common values

$\theta / ^\circ$	$0^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$
$\theta / \text{rad}$	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$
$\sin \theta$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0
$\tan \theta$	0	$\frac{\sqrt{3}}{3}$	1	$\sqrt{3}$	undefined

## reciprocal

$$\begin{aligned}\csc A &= \frac{1}{\sin A} \\ \sec A &= \frac{1}{\cos A} \\ \cot A &= \frac{1}{\tan A}\end{aligned}$$

## periodicity

$$\begin{aligned}\sin(A \pm 2\pi) &= \sin A \\ \cos(A \pm 2\pi) &= \cos A \\ \tan(A \pm \pi) &= \tan A\end{aligned}$$

## co-function

$$\begin{aligned}\sin\left(\frac{\pi}{2} - A\right) &= \cos A \\ \cos\left(\frac{\pi}{2} - A\right) &= \sin A \\ \tan\left(\frac{\pi}{2} - A\right) &= \cot A\end{aligned}$$

## sum & difference

$$\begin{aligned}\sin(A \pm B) &= \sin A \cos B \pm \cos A \sin B \\ \cos(A \pm B) &= \cos A \cos B \mp \sin A \sin B \\ \tan(A \pm B) &= \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}\end{aligned}$$

## pythagorean identities

$$\begin{aligned}\sin^2 A + \cos^2 A &= 1 \\ \sec^2 A - \tan^2 A &= 1 \\ \csc^2 A - \cot^2 A &= 1\end{aligned}$$

## double angle

$$\begin{aligned}\sin(2A) &= 2 \sin A \cos A \\ &= \frac{2 \tan A}{1 + \tan^2 A} \\ \cos(2A) &= \cos^2 A - \sin^2 A \\ &= 1 - 2 \sin^2 A \\ &= 2 \cos^2 A - 1 \\ &= \frac{1 - \tan^2 A}{1 + \tan^2 A} \\ \tan(2A) &= \frac{2 \tan A}{1 - \tan^2 A}\end{aligned}$$

## product to sum

$$\begin{aligned}\sin A \sin B &= \frac{1}{2} \left[ \cos(A - B) - \cos(A + B) \right] \\ \cos A \cos B &= \frac{1}{2} \left[ \cos(A - B) + \cos(A + B) \right] \\ \sin A \cos B &= \frac{1}{2} \left[ \sin(A + B) + \sin(A - B) \right] \\ \cos A \sin B &= \frac{1}{2} \left[ \sin(A + B) - \sin(A - B) \right]\end{aligned}$$

## sum to product

$$\begin{aligned}\sin A \pm \sin B &= 2 \sin \left( \frac{A \pm B}{2} \right) \cos \left( \frac{A \mp B}{2} \right) \\ \cos A + \cos B &= 2 \cos \left( \frac{A + B}{2} \right) \cos \left( \frac{A - B}{2} \right) \\ \cos A - \cos B &= -2 \sin \left( \frac{A + B}{2} \right) \sin \left( \frac{A - B}{2} \right)\end{aligned}$$

## geometry

### sine rule

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

### cosine rule

$$\begin{aligned}a^2 &= b^2 + c^2 - 2bc \cos A \\ A &= \cos^{-1} \left( \frac{b^2 + c^2 - a^2}{2bc} \right)\end{aligned}$$

### area of triangle

$$\frac{1}{2} ab \sin C$$

### Heron's formula

$$\begin{aligned}\text{area} &= \sqrt{s(s-a)(s-b)(s-c)} \\ \text{where } s &= \frac{1}{2}(a+b+c)\end{aligned}$$

## differentiation

$f(x)$	$f'(x)$
$\tan x$	$\sec^2 x$
$\csc x$	$-\csc x \cot x$
$\sec x$	$\sec x \tan x$
$\cot x$	$-\csc^2 x$
$\sin^{-1} f(x)$	$\frac{f'(x)}{\sqrt{1-[f(x)]^2}}, \quad  f(x)  < 1$
$\cos^{-1} f(x)$	$-\frac{f'(x)}{\sqrt{1-[f(x)]^2}}, \quad  f(x)  < 1$
$\tan^{-1} f(x)$	$\frac{f'(x)}{1+[f(x)]^2}$
$\cot^{-1} f(x)$	$-\frac{f'(x)}{1+[f(x)]^2}$
$\sec^{-1} f(x)$	$\frac{f'(x)}{ f(x) \sqrt{[f(x)]^2-1}}$
$\csc^{-1} f(x)$	$-\frac{f'(x)}{ f(x) \sqrt{[f(x)]^2-1}}$

## integration

$f(x)$	$\int f(x)$
$\tan x$	$\ln(\sec x), \quad  x  < \frac{\pi}{2}$
$\cot x$	$\ln(\sin x), \quad 0 < x < \pi$
$\csc x$	$-\ln(\csc x + \cot x), \quad 0 < x < \pi$
$\sec x$	$\ln(\sec x + \tan x), \quad  x  < \frac{\pi}{2}$