

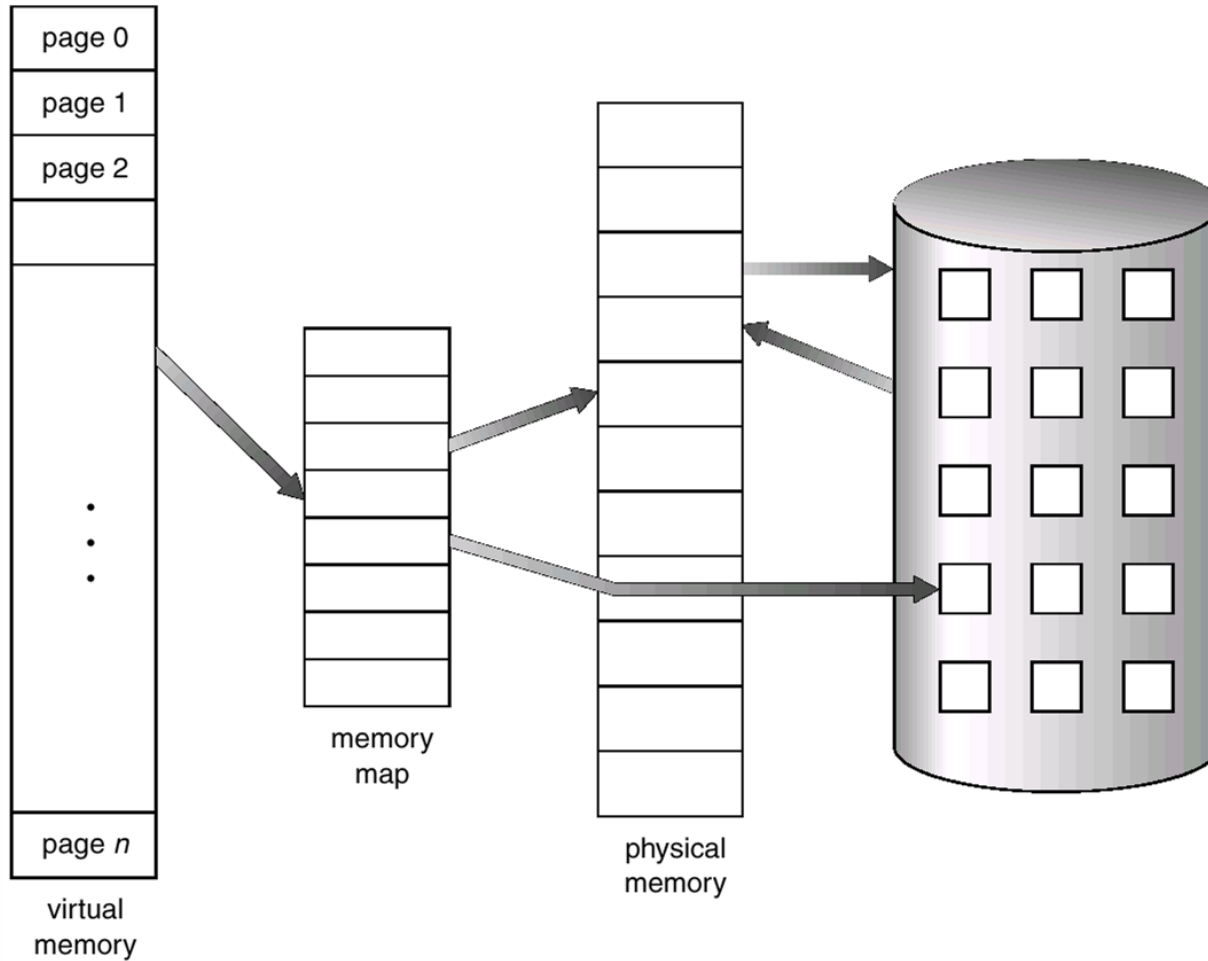
# Virtual Memory

# Background

- **Virtual memory** – separation of user logical memory from physical memory.
  - Only part of the program needs to be in memory for execution
  - Logical address space can therefore be much larger than physical address space
  - Allows address spaces to be shared by several processes
  - Allows for more efficient process creation
- Virtual memory can be implemented via:
  - Demand paging
  - Demand segmentation

# Virtual memory:

result of a mechanism which combines  
main memory and secondary memories



Virtual Memory That is Larger Than  
Physical Memory

# Demand Paging

- Bring a page into memory only when it is needed
  - Less I/O needed
  - Less memory needed
  - Faster response
  - More users
- **Lazy swapper** – never swaps a page into memory unless page will be needed
  - Swapper that deals with pages is a **pager**

# Valid-Invalid Bit

- With each page table entry a valid–invalid bit is associated (**v**  $\Rightarrow$  in-memory, **i**  $\Rightarrow$  not-in-memory)
- Initially valid–invalid bit is set to **i** on all entries
- Example of a page table snapshot:

Frame #	valid-invalid bit
	<b>v</b>
	<b>v</b>
	<b>v</b>
	<b>v</b>
	<b>i</b>
	<b>i</b>
	<b>i</b>

page table

- During address translation (logical to physical), if valid–invalid bit in page table entry is **i**  $\Rightarrow$  page fault

# Page Table When Some Pages Are Not in Main Memory

0	A
1	B
2	C
3	D
4	E
5	F
6	G
7	H

logical  
memory

valid-invalid bit	
frame	bit
0	4 v
1	i
2	6 v
3	i
4	i
5	9 v
6	i
7	i

page table

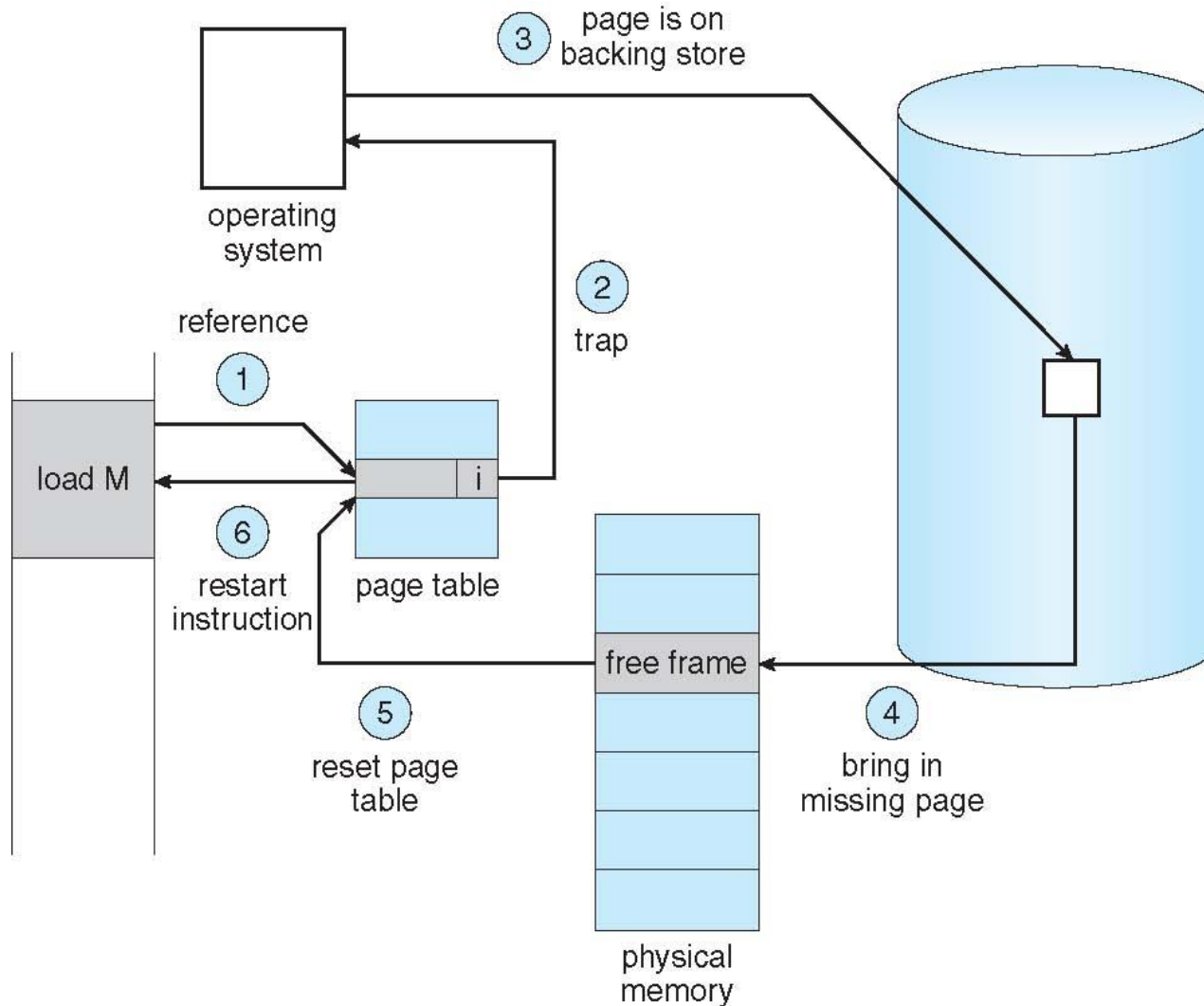
0	
1	
2	
3	
4	A
5	
6	C
7	
8	
9	F
10	
11	
12	
13	
14	
15	

physical memory

# Page Fault

- An interruption is generated when the logical address refers to a part which is not in the resident set
  - defect of paging, fault page
- 1. Operating system looks at another table to decide:
  - - Invalid reference  $\Rightarrow$  abort
  - Just not in memory
- 2. Get empty frame
- 3. Swap page into frame
- 4. Reset tables
- 5. Set validation bit = **v**
- 6. Restart the instruction that caused the page fault

# Steps in Handling a Page Fault





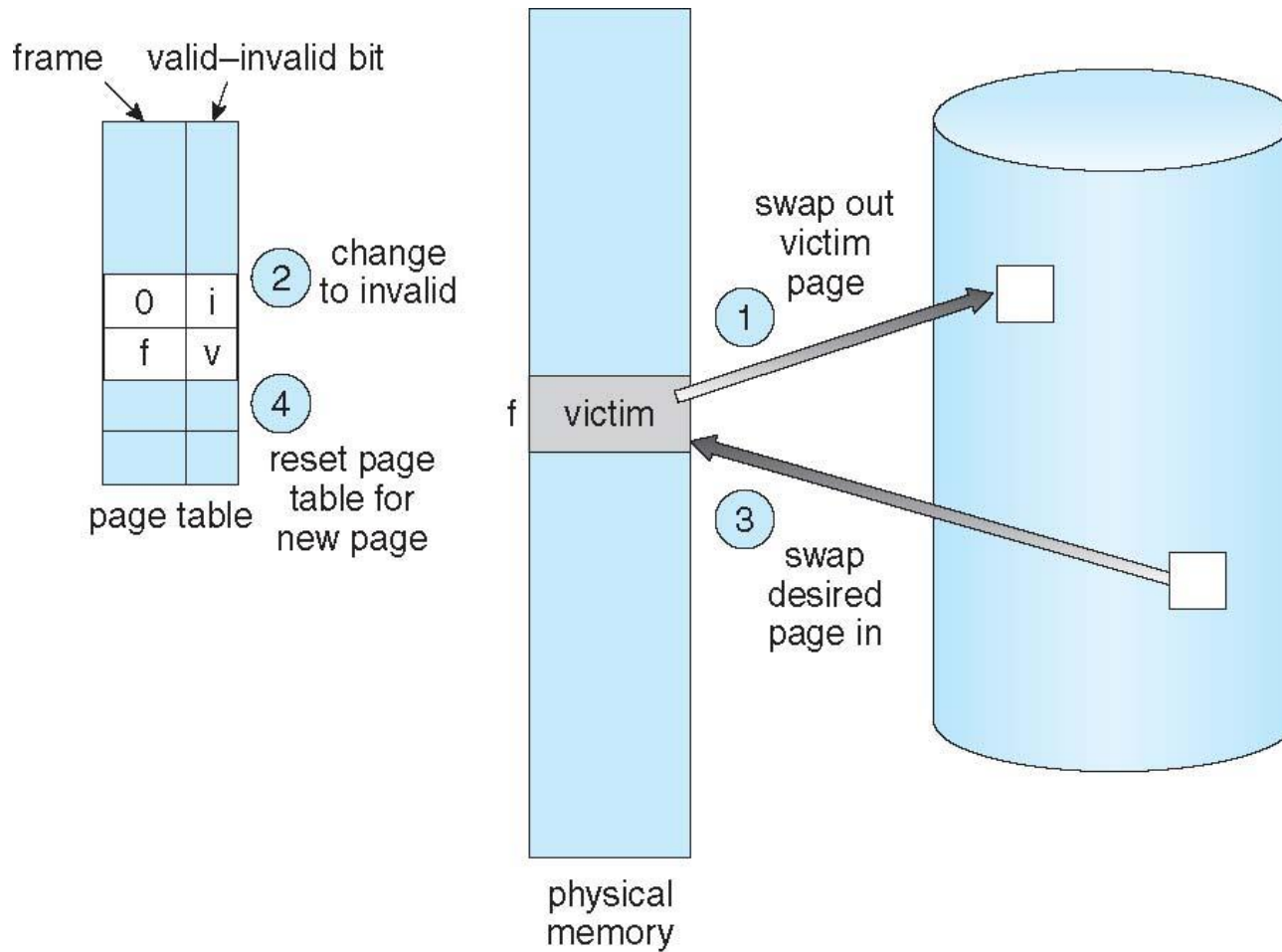
# What happens if there is no free frame?

- Page replacement – find some page in memory, but not really in use, swap it out
  - algorithm
  - performance – want an algorithm which will result in minimum number of page faults
- Same page may be brought into memory several times

# Basic Page Replacement

1. Find the location of the desired page on disk
2. Find a free frame:
  - If there is a free frame, use it
  - If there is no free frame, use a page replacement algorithm to select a **victim** frame
3. Bring the desired page into the (newly) free frame; update the page and frame tables
4. Restart the process

# Page Replacement



# Page Replacement Algorithms

- Want lowest page-fault rate
- Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string
- In all our examples, the reference string is

**1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5**

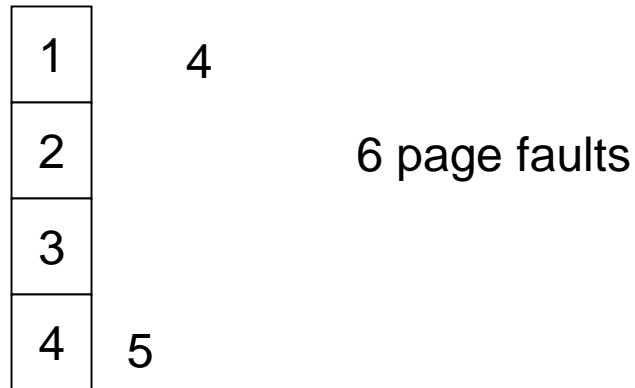
# Algorithms for the policy of replacement

- The optimal algorithm (OPT) chooses for page to replace that will be referred **most tardily** (late)
  - produces the fewest number of page faults.
  - impossible to implement (need to know the future)
    - but serves as a standard to compare with the other algorithms we shall study.

# Optimal Algorithm

- Replace page that will not be used for longest period of time
- 4 frames example

1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5



- How do you know this?
- Used for measuring how well your algorithm performs
- IMPOSSIBLE to implement
- We need to know the future
- Used to test the performance of other algorithms

# Optimal Page Replacement

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2																
	0	0	0																
		1	1																

page frames

# First In, First Out (FIFO)

- Logic: a page which was a long time in memory had already its chance to be executed
- When the memory is full, the **oldest** page is replaced.
  - Thus: “first-in, first-out”
- Simple to apply
- But: A frequently used page is often the oldest,
  - it will be replaced by FIFO!



# FIFO Page Replacement

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2																	
	0	0	0																	
		1	1																	

page frames

# Implementation of FIFO

- Easily implemented by using a queue of memory frameworks
  - Who should be updated at each defect of page
  - Exercise: Conceive this queue (previous example)

**Page address  
stream**

2      3      2      1      5      2      4      5      3      2      5      2

2	3		1	5	2	4		3		5	2
	2		3	1	5	2		4		3	5
			2	3	1	5		2		4	3

**FIFO**

2	2	2	2	5	5	5	5	3	3	3	3
	3	3	3	3	2	2	2	2	2	5	5
			1	1	1	4	4	4	4	4	2
				<b>F</b>	<b>F</b>	<b>F</b>		<b>F</b>		<b>F</b>	<b>F</b>

# First-In-First-Out (FIFO) Algorithm

- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
- 3 frames (3 pages can be in memory at a time per process)

1	1	4	5	9 page faults
2	2	1	3	
3	3	2	4	

- 4 frames

1	1	5	4	10 page faults
2	2	1	5	
3	3	2		
4	4	3		

- Belady's Anomaly: more frames  $\Rightarrow$  more page faults

# Algorithms for the policy of replacement

## ■ Chronological order of use (LRU)

- Least Recently Used

- Replace the page whose last reference goes back to the most remote time

  - past is used to predict the future

# LRU Page Replacement

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		4	4	4	0			1		1		1		
	0	0	0		0		0	0	3	3			3		0		0		
		1	1		3		3	2	2	2			2		2		7		

page frames

# Comparison between FIFO and LRU

Page address stream	2	3	2	1	5	2	4	5	3	2	5	2																																				
LRU	<table><tr><td>2</td></tr><tr><td></td></tr><tr><td></td></tr></table>	2			<table><tr><td>2</td></tr><tr><td>3</td></tr><tr><td></td></tr></table>	2	3		<table><tr><td>2</td></tr><tr><td>3</td></tr><tr><td></td></tr></table>	2	3		<table><tr><td>2</td></tr><tr><td>3</td></tr><tr><td>1</td></tr></table>	2	3	1	<table><tr><td>2</td></tr><tr><td>5</td></tr><tr><td>1</td></tr></table> F	2	5	1	<table><tr><td>2</td></tr><tr><td>5</td></tr><tr><td>1</td></tr></table>	2	5	1	<table><tr><td>2</td></tr><tr><td>5</td></tr><tr><td>4</td></tr></table> F	2	5	4	<table><tr><td>2</td></tr><tr><td>5</td></tr><tr><td>4</td></tr></table>	2	5	4	<table><tr><td>3</td></tr><tr><td>5</td></tr><tr><td>4</td></tr></table> F	3	5	4	<table><tr><td>3</td></tr><tr><td>5</td></tr><tr><td>2</td></tr></table> F	3	5	2	<table><tr><td>3</td></tr><tr><td>5</td></tr><tr><td>2</td></tr></table>	3	5	2	<table><tr><td>3</td></tr><tr><td>5</td></tr><tr><td>2</td></tr></table>	3	5	2
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- Contrary to FIFO, LRU recognizes that the pages 2 and 5 are frequently used
- In this case, the performance of FIFO is worse:
  - LRU = 3+4, FIFO = 3+6

# Comparison OPT-LRU

- Example: A process of 5 pages, and there are only 3 available physical pages.
- In this example, OPT causes 3+3 defects, LRU 3+4.

Page address  
stream

2 3 2 1 5 2 4 5 3 2 5 2

OPT

2	2	2	2	2	2	4	4	4	2	2	2
	3	3	3	3	3	3	3	3	3	3	3
			1	5	5	5	5	5	5	5	5
				F		F			F		

LRU

2	2	2	2	2	2	2	2	3	3	3	3
	3	3	3	5	5	5	5	5	5	5	5
			1	1	1	4	4	4	2	2	2
				F		F		F	F		