

1.7 Parametric Equation

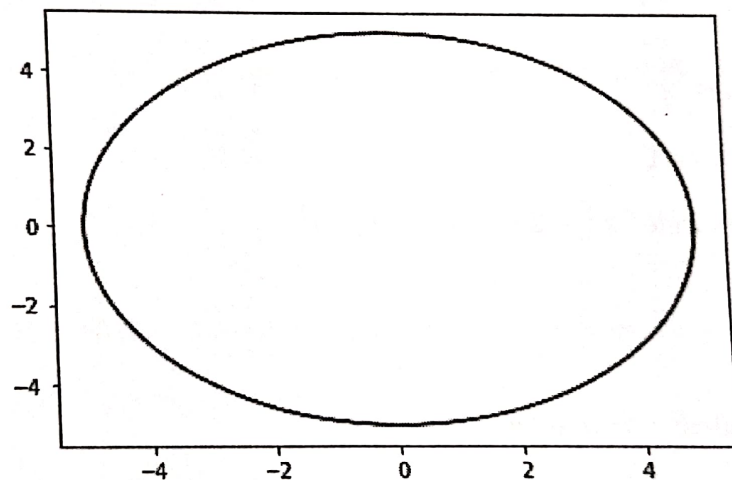
1. Circle: $x = a \cos(\theta)$; $y = a \sin(\theta)$

```
import numpy as np
import matplotlib.pyplot as plt
def circle(r):
    x = [] #create the list of x coordinates
    y = [] #create the list of y coordinates

    for theta in np.linspace(-2*np.pi, 2*np.pi, 100):
        #loop over a list of theta, which ranges from -2 pi to 2 pi
        x.append(r*np.cos(theta))
        #add the corresponding expression of x to the x list
        y.append(r*np.sin(theta))
        #same for y

    plt.plot(x,y) #plot using matplotlib.pyplot
    plt.show() #show the plot

circle(5) #call the function
```



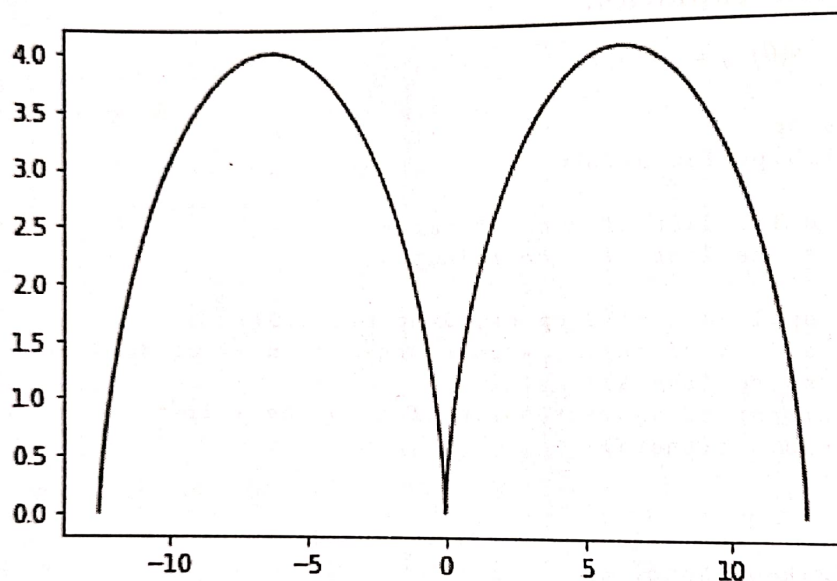
✓ 2. Cycloid: $x = a(\theta - \sin\theta)$; $y = a(1 - \sin\theta)$

```
def cycloid(r):
    x = [] #create the list of x coordinates
    y = [] #create the list of y coordinates

    for theta in np.linspace(-2*np.pi, 2*np.pi, 100):
        #loop over a list of theta, which ranges from -2 pi to 2 pi
        x.append(r*(theta - np.sin(theta)))
        #add the corresponding expression of x to the x list
        y.append(r*(1 - np.cos(theta))) #same for y

    plt.plot(x,y) #plot using matplotlib.pyplot
    plt.show() #show the plot

cycloid(2) #call the function
```



1.8 Exercise:

Plot the following:

1. Parabola $y^2 = 4ax$
2. Hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$
3. Lower half of the circle: $x^2 + 2x = 4 + 4y - y^2$
4. $\cos(\frac{\pi x}{2})$
5. $1 + \sin(x + \frac{\pi}{4})$
6. Spiral of Archimedes: $r = a + b\theta$
7. Limacon: $r = a + b \cos\theta$