MTK: Mimetic Methods Toolkit

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Contents

Chapter 1

Introduction

We define numerical methods that are based on discretizations preserving the properties of their continuum counterparts to be **mimetic**.

The **Mimetic Methods Toolkit (MTK)** is a C++ library for mimetic numerical methods. It is arranged as a set of classes for **mimetic quadratures**, mimetic interpolation$**$, and **mimetic finite differences** methods for the numerical solution of ordinary and partial differential equations.

An older version of this library is available outside of GitHub... just email me about it, and you can have it... it is ugly, yet functional and more complete.

1.1 MTK Concerns

Since collaborative development efforts are definitely important in achieving the level of generality we intend the library to possess, we have divided the library's source code according to the designated purpose the classes possess within the library. These divisions (or concerns) are grouped by layers, and are hierarchically related by the dependence they have among them.

One concern is said to depend on another one, if the classes the first concern includes, rely on the classes the second concern includes.

In order of dependence these are:

1. Roots.
2. Enumerations.
3. Tools.
4. Data Structures.
5. Numerical Methods.
6. Grids.
7. Mimetic Operators.

1.2 MTK Flavors

The MTK collection of wrappers is:

1. MMTK: MATLAB wrappers collection for MTK; intended for sequential computations.

Others are being designed and developed.

1.3 Contact, Support and Credits

The MTK is developed by researchers and adjuncts to the Computational Science Research Center (CSRC) at San Diego State University (SDSU).

Developers are members of:

1. Mimetic Numerical Methods Research and Development Group.
2. Computational Geoscience Research and Development Group.
3. Ocean Modeling Research and Development Group.

Currently the developers are:

1. **Eduardo J. Sanchez, Ph.D. - esanchez at mail dot sdsu dot edu** - ejspeiro
2. Jose E. Castillo, Ph.D. - jcastillo at mail dot sdsu dot edu
3. Guillermo F. Miranda, Ph.D. - unigrav at hotmail dot com
4. Christopher P. Paolini, Ph.D. - paolini at engineering dot sdsu dot edu
5. Angel Boada.
6. Johnny Corbino.
7. Raul Vargas–Navarro.

1.4 Acknowledgements and Contributions

The authors would like to acknowledge valuable advising, contributions and feedback, from research personnel at the Computational Science Research Center at San Diego State University, which were vital to the fruition of this work. Specifically, our thanks go to (alphabetical order):

1. Mohammad Abouali, Ph.D.
2. Dany De Cecchis, Ph.D.
3. Julia Rossi.

Chapter 2

Programming Tools

The development of MTK has been made possible through the use of the following applications:

1. Editor: Kate - KDE Advanced Text Editor. Version 3.13.3. Using KDE Development Platform 4.13.3 (C) 2000-2005 The Kate Authors.
2. Compiler: gcc version 4.4.5 (Ubuntu/Linaro 4.4.4-14ubuntu5). Copyright (C) 2013 Free Software Foundation, Inc.
3. Debugger: GNU gdb (Ubuntu 7.7.1-0ubuntu5∼14.04.2) 7.7.1. Copyright (C) 2014 Free Software Foundation, Inc.
4. Memory Profiler: valgrind-3.10.0.SVN.

Chapter 3

Licensing and Modifications

Redistribution and use in source and binary forms, with or without modification, are permitted provided that the following conditions are met:

1. Modifications to source code should be reported to: `esanchez@mail.sdsu.edu` and a copy of the modified files should be reported once modifications are completed, unless these modifications are made through the project's GitHub page: `http://www.csrc.sdsu.edu/mtk`. Documentation related to said modifications should be developed and included in any deliverable.
2. Redistributions of source code must be done through direct downloads from the project's GitHub page: `http://www.csrc.sdsu.edu/mtk`
3. Redistributions in binary form must reproduce the above copyright notice, this list of conditions and the following disclaimer in the documentation and/or other materials provided with the distribution.
4. Usage of the binary form on proprietary applications shall require explicit prior written permission from the the copyright holders, and due credit should be given to the copyright holders.
5. Neither the name of the copyright holder nor the names of its contributors may be used to endorse or promote products derived from this software without specific prior written permission.

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THIS SOFTWARE IS PROVIDED BY THE COPYRIGHT HOLDERS AND CONTRIBUTORS "AS IS" AND ANY EXPRESS OR IMPLIED WARRANTIES, INCLUDING, BUT NOT LIMITED TO, THE IMPLIED WARRANTIES OF MERCHANTABILITY AND FITNESS FOR A PARTICULAR PURPOSE ARE DISCLAIMED. IN NO EVENT SHALL THE COPYRIGHT HOLDER OR CONTRIBUTORS BE LIABLE FOR ANY DIRECT, INDIRECT, INCIDENTAL, SPECIAL, EXEMPLARY, OR CONSEQUENTIAL DAMAGES (INCLUDING, BUT NOT LIMITED TO, PROCUREMENT OF SUBSTITUTE GOODS OR SERVICES; LOSS OF USE, DATA, OR PROFITS; OR BUSINESS INTERRUPTION) HOWEVER CAUSED AND ON ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT (INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.

Chapter 4

Read Me File and Installation Instructions

README File for the Mimetic Methods Toolkit (MTK)

By: **Eduardo J. Sanchez, Ph.D. - esanchez at mail dot sdsu dot edu**

1. Description

We define numerical methods that are based on discretizations preserving the properties of their continuum counterparts to be **mimetic**.

The **Mimetic Methods Toolkit (MTK)** is a C++ library for mimetic numerical methods. It is arranged as a set of classes for **mimetic quadratures**, **mimetic interpolation**, and **mimetic finite differences** methods for the numerical solution of ordinary and partial differential equations.

An older version of this library is available outside of GitHub... just email me about it, and you can have it... it is ugly, yet functional and more complete.

2. Dependencies

This README assumes all of these dependencies are installed in the following folder:

```
$(HOME)/Libraries/
```

```
In this version, the MTK optionally uses ATLAS-optimized BLAS and LAPACK
routines for the internal computation on some of the layers. However, ATLAS
requires both BLAS and LAPACK in order to create their optimized distributions.
Therefore, the following dependencies tree arises:
```

For Linux:

```
1. LAPACK - Available from:  http://www.netlib.org/lapack/
  1. BLAS - Available from:  http://www.netlib.org/blas/

2. GLPK - Available from:  https://www.gnu.org/software/glpk/

3. (Optional) ATLAS - Available from:  http://math-atlas.sourceforge.net/
  1. LAPACK - Available from:  http://www.netlib.org/lapack/
    1. BLAS - Available from:  http://www.netlib.org/blas

4. (Optional) Valgrind - Available from:  http://valgrind.org/

5. (Optional) Doxygen - Available from  http://www.stack.nl/~dimitri/doxygen/
```

For OS X:

```
1. GLPK - Available from:  https://www.gnu.org/software/glpk/
```

3. Installation

PART 1. CONFIGURATION OF THE MAKEFILE.

```
The following steps are required the build and test the MTK. Please use the
accompanying Makefile.inc file, which should provide a solid template to start
with. The following command provides help on the options for make:
```

```
$ make help
-----
Makefile for the MTK.

Options are:
- all: builds the library, the tests, and examples.
- mtklib: builds the library.
- test: builds the test files.
- example: builds the examples.

- testall: runs all the tests.

- gendoc: generates the documentation for the library.

- clean: cleans all the generated files.
- cleanlib: cleans the generated archive and object files.
- cleantest: cleans the generated tests executables.
- cleanexample: cleans the generated examples executables.
-----
```

PART 2. BUILD THE LIBRARY.

```
$ make
```

If successful you'll read (before building the examples):

```
----- Library created! Check in /home/ejspeiro/Dropbox/MTK/lib
```

Examples and tests will also be built.

4. Frequently Asked Questions

Q: Why haven't you guys implemented GBS to build the library?
A: I'm on it as we speak! ;)

Q: Is there any main reference when it comes to the theory on Mimetic Methods?
A: Yes! Check: http://www.csrc.sdsu.edu/mimetic-book

Q: Do I need to generate the documentation myself?
A: You can if you want to... but if you DO NOT want to, just go to our website.

5. Contact, Support, and Credits

```
The MTK is developed by researchers and adjuncts to the
 Computational Science Research Center (CSRC)
at  San Diego State University (SDSU).

Developers are members of:

1. Mimetic Numerical Methods Research and Development Group.
2. Computational Geoscience Research and Development Group.
3. Ocean Modeling Research and Development Group.

Currently the developers are:
```

1. **Eduardo J. Sanchez, Ph.D. - esanchez at mail dot sdsu dot edu** - ejspeiro
2. Jose E. Castillo, Ph.D. - jcastillo at mail dot sdsu dot edu
3. Guillermo F. Miranda, Ph.D. - unigrav at hotmail dot com
4. Christopher P. Paolini, Ph.D. - paolini at engineering dot sdsu dot edu
5. Angel Boada.
6. Johnny Corbino.
7. Raul Vargas-Navarro.

Finally, please feel free to contact me with suggestions or corrections:

Eduardo J. Sanchez, Ph.D. - esanchez at mail dot sdsu dot edu - ejspeiro

Thanks and happy coding!

Chapter 5

Tests and Test Architectures

Tests are given in the `files list` section. They are provided in the /tests/ folder within the distributed software.

In this page we intend to make a summary of all of the architectures in where the MTK has been tested. The MTK is intended to be as portable as possible throughout architectures. The following architectures have provided flawless installations of the API and correct execution of the examples:

```
1. Linux 3.2.0-23-generic-pae #36-Ubuntu SMP i386 GNU/Linux.
   Intel(R) Pentium(R) M CPU 1.73 GHz 2048 KB of cache and stepping of 8.
   gcc version 4.6.3 (Ubuntu/Linaro 4.6.3-1ubuntu5).

2. Linux 3.13.0-67-generic #110-Ubuntu SMP x86_64 GNU/Linux.
   Intel(R) Core(TM) i7-4700MQ CPU 2.40 GHz 6144 KB of cache and stepping of 3.
   gcc version 4.8.4 (Ubuntu 4.4.4-2ubuntu1~14.04).

3. Linux 3.16.7-29-desktop #1 SMP PREEMPT (6be6a97) x86_64 GNU/Linux
   Intel(R) Core(TM) i7-4600U CPU 2.10 GHz 4096 KB of cache and a stepping of 1.
   gcc (SUSE Linux) 4.8.3 20140627 [gcc-4_8-branch revision 212064].
```

Further architectures will be tested!

Chapter 6

Examples

Examples are given in the `files list` section. They are provided in the /examples/ folder within the distributed software.

Chapter 7

User Manual, References and Theory

The main source of references for this work can be found in:

http://www.csrc.sdsu.edu/mimetic-book/

However, a .PDF copy of this manual can be found here.

Chapter 8

Todo List

Member mtk::DenseMatrix::Kron (const DenseMatrix &aa, const DenseMatrix &bb)
Implement Kronecker product using the BLAS.

Member mtk::DenseMatrix::OrderColMajor ()
Improve this so that no new arrays have to be created.

Member mtk::DenseMatrix::OrderRowMajor ()
Improve this so that no new arrays have to be created.

Member mtk::DenseMatrix::Transpose ()
Improve this so that no extra arrays have to be created.

Class mtk::GLPKAdapter
Rescind from the GLPK as the numerical core for CLO problems.

Member mtk::Matrix::IncreaseNumNull () noexcept
Review the definition of sparse matrices properties.

Member mtk::Matrix::IncreaseNumZero () noexcept
Review the definition of sparse matrices properties.

Member mtk::RobinBCDescriptor2D::ImposeOnGrid (UniStgGrid2D &grid, const Real &time=kZero) const
Implement imposition for vector-valued grids. Need research here!

Member mtk::RobinBCDescriptor2D::ImposeOnSouthBoundaryNoSpace (const Lap2D &lap, const UniStg↩ Grid2D &grid, DenseMatrix &matrix, const Real &time=kZero) const
Impose the Neumann conditions on every pole, for every scenario.

Member mtk::RobinBCDescriptor2D::ImposeOnSouthBoundaryWithSpace (const Lap2D &lap, const UniStg↩ Grid2D &grid, DenseMatrix &matrix, const Real &time=kZero) const
Impose Harmonic mean on the corners for the case when the generated space is available, for all poles.

Member mtk::Tools::Prevent (const bool complement, const char ∗const fname, int lineno, const char ∗const fxname) noexcept
Check if this is the best way of stalling execution.

Member mtk::Tools::test_number_
Check usage of static methods and private members.

Member mtk::UniStgGrid1D::discrete_domain_x () const
Review const-correctness of the pointer we return.

Member mtk::UniStgGrid1D::discrete_field ()

Review const-correctness of the pointer we return. Look at the STL!

Member mtk::UniStgGrid2D::discrete_domain_x () const

Review const-correctness of the pointer we return.

Member mtk::UniStgGrid2D::discrete_domain_y () const

Review const-correctness of the pointer we return.

File mtk_div_1d.cc

Overload ostream operator as in mtk::Lap1D.

Implement creation of ■ w. mtk::BLASAdapter.

File mtk_glpk_adapter_test.cc

Test the mtk::GLPKAdapter class.

File mtk_grad_1d.cc

Overload ostream operator as in mtk::Lap1D.

Implement creation of ■ w. mtk::BLASAdapter.

File mtk_lapack_adapter.cc

Write documentation using LaTeX.

File mtk_lapack_adapter_test.cc

Test the mtk::LAPACKAdapter class.

File mtk_quad_1d.h

Implement this class.

File mtk_roots.h

Documentation should (better?) capture effects from selective compilation.

Test selective precision mechanisms.

File mtk_uni_stg_grid_1d.h

Create overloaded binding routines that read data from files.

File mtk_uni_stg_grid_2d.h

Create overloaded binding routines that read data from files.

Chapter 9

Bug List

Member mtk::Matrix::set_num_null (const int &in) noexcept

-nan assigned on construction time due to num_values_ being 0.

Member mtk::Matrix::set_num_zero (const int &in) noexcept

-nan assigned on construction time due to num_values_ being 0.

Chapter 10

Module Index

10.1 Modules

Here is a list of all modules:

Chapter 11

Namespace Index

11.1 Namespace List

Here is a list of all namespaces with brief descriptions:

Chapter 12

Class Index

12.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

Chapter 13

File Index

13.1 File List

Here is a list of all files with brief descriptions:

Chapter 14

Module Documentation

14.1 Roots.

Fundamental execution parameters and defined types.

Typedefs

- typedef float mtk::Real

  Users can simply change this to build a double- or single-precision MTK.

Variables

- const float mtk::kZero {0.0f}

  MTK's zero defined according to selective compilation.
- const float mtk::kOne {1.0f}

  MTK's one defined according to selective compilation.
- const float mtk::kTwo {2.0f}

  MTK's two defined according to selective compilation.
- const float mtk::kDefaultTolerance {1e-7f}

  Considered tolerance for comparisons in numerical methods.
- const int mtk::kDefaultOrderAccuracy {2}

  Default order of accuracy for mimetic operators.
- const float mtk::kDefaultMimeticThreshold {1e-6f}

  Default tolerance for higher-order mimetic operators.
- const int mtk::kCriticalOrderAccuracyDiv {8}

  At this order (and higher) we must use the CBSA to construct.
- const int mtk::kCriticalOrderAccuracyGrad {10}

  At this order (and higher) we must use the CBSA to construct.

14.1.1 Detailed Description

Fundamental execution parameters and defined types.

14.1.2 Typedef Documentation

14.1.2.1 mtk::Real

Definition at line 83 of file mtk_roots.h.

14.1.3 Variable Documentation

14.1.3.1 mtk::kCriticalOrderAccuracyDiv {8}

Definition at line 167 of file mtk_roots.h.

14.1.3.2 mtk::kCriticalOrderAccuracyGrad {10}

Definition at line 176 of file mtk_roots.h.

14.1.3.3 mtk::kDefaultMimeticThreshold {1e-6f}

Warning

Declared as double if MTK_PRECISION_DOUBLE is defined.

Definition at line 157 of file mtk_roots.h.

14.1.3.4 mtk::kDefaultOrderAccuracy {2}

Warning

Declared as double if MTK_PRECISION_DOUBLE is defined.

Definition at line 143 of file mtk_roots.h.

14.1.3.5 mtk::kDefaultTolerance {1e-7f}

Definition at line 131 of file mtk_roots.h.

14.1.3.6 mtk::kOne {1.0f}

Warning

Declared as double if MTK_PRECISION_DOUBLE is defined.

Definition at line 117 of file mtk_roots.h.

14.1.3.7 mtk::kTwo {2.0f}

Warning

Declared as double if MTK_PRECISION_DOUBLE is defined.

Definition at line 118 of file mtk_roots.h.

14.1.3.8 mtk::kZero {0.0f}

Warning

Declared as double if MTK_PRECISION_DOUBLE is defined.

Definition at line 116 of file mtk_roots.h.

14.2 Enumerations.

Enumerations.

Enumerations

- enum mtk::MatrixStorage { mtk::DENSE, mtk::BANDED, mtk::CRS }

  Considered matrix storage schemes to implement sparse matrices.
- enum mtk::MatrixOrdering { mtk::ROW_MAJOR, mtk::COL_MAJOR }

  Considered matrix ordering (for Fortran purposes).
- enum mtk::FieldNature { mtk::SCALAR, mtk::VECTOR }

  Nature of the field discretized in a given grid.
- enum mtk::DirInterp { mtk::SCALAR_TO_VECTOR, mtk::VECTOR_TO_SCALAR }

  Interpolation operator.

14.2.1 Detailed Description

Enumerations.

14.2.2 Enumeration Type Documentation

14.2.2.1 enum **mtk::DirInterp**

Used to tag different directions of interpolation supported.

Enumerator

SCALAR_TO_VECTOR Interpolations places scalar on vectors' location.

VECTOR_TO_SCALAR Interpolations places vectors on scalars' location.

Definition at line 127 of file mtk_enums.h.

14.2.2.2 enum **mtk::FieldNature**

Fields can be **scalar** or **vector** in nature.

See also

`https://en.wikipedia.org/wiki/Scalar_field`
`https://en.wikipedia.org/wiki/Vector_field`

Enumerator

SCALAR Scalar-valued field.

VECTOR Vector-valued field.

Definition at line 113 of file mtk_enums.h.

14.2.2.3 enum mtk::MatrixOrdering

Row-major ordering is used for most application in C/C++. For Fortran purposes, the matrices must be listed in a column-major ordering.

See also

https://en.wikipedia.org/wiki/Row-major_order

Enumerator

ROW_MAJOR Row-major ordering (C/C++).

COL_MAJOR Column-major ordering (Fortran).

Definition at line 95 of file mtk_enums.h.

14.2.2.4 enum mtk::MatrixStorage

The considered sparse storage schemes are selected so that these are compatible with some of the most used mathematical APIs, as follows: DENSE and BANDED for `BLAS`, `LAPACK`, and `ScaLAPACK`. Finally, CRS for `SuperLU`.

Enumerator

DENSE Dense matrices, implemented as a 1D array: DenseMatrix.

BANDED Banded matrices ala LAPACK and ScaLAPACK: Must be implemented.

CRS Compressed-Rows Storage: Must be implemented.

Definition at line 77 of file mtk_enums.h.

14.3 Execution tools.

Tools to ensure execution correctness.

Classes

- class mtk::Tools

  Tool manager class.

14.3.1 Detailed Description

Tools to ensure execution correctness.

14.4 Data structures.

Fundamental data structures.

Classes

- class mtk::DenseMatrix

  Defines a common dense matrix, using a 1D array.
- class mtk::Matrix

  Definition of the representation of a matrix in the MTK.

14.4.1 Detailed Description

Fundamental data structures.

14.5 Numerical methods.

Adapter classes and auxiliary numerical methods.

Classes

- class mtk::BLASAdapter

  Adapter class for the BLAS API.
- class mtk::GLPKAdapter

  Adapter class for the GLPK API.
- class mtk::LAPACKAdapter

  Adapter class for the LAPACK API.

14.5.1 Detailed Description

Adapter classes and auxiliary numerical methods.

14.6 Grids.

Uniform rectangular staggered grids.

Classes

- class mtk::UniStgGrid1D

  Uniform 1D Staggered Grid.
- class mtk::UniStgGrid2D

  Uniform 2D Staggered Grid.

14.6.1 Detailed Description

Uniform rectangular staggered grids.

14.7 Mimetic operators.

Mimetic operators.

Classes

- class mtk::Div1D

  Implements a 1D mimetic divergence operator.
- class mtk::Div2D

  Implements a 2D mimetic divergence operator.
- class mtk::Grad1D

  Implements a 1D mimetic gradient operator.
- class mtk::Grad2D

  Implements a 2D mimetic gradient operator.
- class mtk::Interp1D

  Implements a 1D interpolation operator.
- class mtk::Interp2D

  Implements a 2D interpolation operator.
- class mtk::Lap1D

  Implements a 1D mimetic Laplacian operator.
- class mtk::Lap2D

  Implements a 2D mimetic Laplacian operator.
- class mtk::Quad1D

  Implements a 1D mimetic quadrature.
- class mtk::RobinBCDescriptor1D

  Impose Robin boundary conditions on the operators and on the grids.
- class mtk::RobinBCDescriptor2D

  Impose Robin boundary conditions on the operators and on the grids.

Typedefs

- typedef Real(∗ mtk::CoefficientFunction0D)(const Real &tt)

  A function of a BC coefficient evaluated on a 0D domain and time.
- typedef Real(∗ mtk::CoefficientFunction1D)(const Real &xx, const Real &tt)

  A function of a BC coefficient evaluated on a 1D domain and time.

14.7.1 Detailed Description

Mimetic operators.

14.7.2 Typedef Documentation

14.7.2.1 mtk::CoefficientFunction0D

Warning

This definition implies that, for now, coefficients will depend on space and time, thus no extra parameters can influence their behavior. We will fix this soon enough.

Definition at line 111 of file mtk_robin_bc_descriptor_1d.h.

14.7.2.2 mtk::CoefficientFunction1D

Definition at line 97 of file mtk_robin_bc_descriptor_2d.h.

Chapter 15

Namespace Documentation

15.1 mtk Namespace Reference

Mimetic Methods Toolkit namespace.

Classes

- class BLASAdapter

  Adapter class for the BLAS API.
- class DenseMatrix

  Defines a common dense matrix, using a 1D array.
- class Div1D

  Implements a 1D mimetic divergence operator.
- class Div2D

  Implements a 2D mimetic divergence operator.
- class GLPKAdapter

  Adapter class for the GLPK API.
- class Grad1D

  Implements a 1D mimetic gradient operator.
- class Grad2D

  Implements a 2D mimetic gradient operator.
- class Interp1D

  Implements a 1D interpolation operator.
- class Interp2D

  Implements a 2D interpolation operator.
- class Lap1D

  Implements a 1D mimetic Laplacian operator.
- class Lap2D

  Implements a 2D mimetic Laplacian operator.
- class LAPACKAdapter

  Adapter class for the LAPACK API.
- class Matrix

  Definition of the representation of a matrix in the MTK.

- class Quad1D

  Implements a 1D mimetic quadrature.
- class RobinBCDescriptor1D

  Impose Robin boundary conditions on the operators and on the grids.
- class RobinBCDescriptor2D

  Impose Robin boundary conditions on the operators and on the grids.
- class Tools

  Tool manager class.
- class UniStgGrid1D

  Uniform 1D Staggered Grid.
- class UniStgGrid2D

  Uniform 2D Staggered Grid.

Typedefs

- typedef Real(∗ CoefficientFunction0D)(const Real &tt)

  A function of a BC coefficient evaluated on a 0D domain and time.
- typedef Real(∗ CoefficientFunction1D)(const Real &xx, const Real &tt)

  A function of a BC coefficient evaluated on a 1D domain and time.
- typedef float Real

  Users can simply change this to build a double- or single-precision MTK.

Enumerations

- enum MatrixStorage { DENSE, BANDED, CRS }

  Considered matrix storage schemes to implement sparse matrices.
- enum MatrixOrdering { ROW_MAJOR, COL_MAJOR }

  Considered matrix ordering (for Fortran purposes).
- enum FieldNature { SCALAR, VECTOR }

  Nature of the field discretized in a given grid.
- enum DirInterp { SCALAR_TO_VECTOR, VECTOR_TO_SCALAR }

  Interpolation operator.

Functions

- float snrm2_ (int ∗n, float ∗x, int ∗incx)
- void saxpy_ (int ∗n, float ∗sa, float ∗sx, int ∗incx, float ∗sy, int ∗incy)
- void sgemv_ (char ∗trans, int ∗m, int ∗n, float ∗alpha, float ∗a, int ∗lda, float ∗x, int ∗incx, float ∗beta, float ∗y, int ∗incy)
- void sgemm_ (char ∗transa, char ∗transb, int ∗m, int ∗n, int ∗k, double ∗alpha, double ∗a, int ∗lda, double ∗b, aamm int ∗ldb, double ∗beta, double ∗c, int ∗ldc)
- std::ostream & operator<< (std::ostream &stream, mtk::DenseMatrix &in)
- std::ostream & operator<< (std::ostream &stream, mtk::Div1D &in)
- std::ostream & operator<< (std::ostream &stream, mtk::Grad1D &in)
- std::ostream & operator<< (std::ostream &stream, mtk::Interp1D &in)
- std::ostream & operator<< (std::ostream &stream, mtk::Lap1D &in)
- void sgesv_ (int ∗n, int ∗nrhs, Real ∗a, int ∗lda, int ∗ipiv, Real ∗b, int ∗ldb, int ∗info)

- void sgels_ (char ∗trans, int ∗m, int ∗n, int ∗nrhs, Real ∗a, int ∗lda, Real ∗b, int ∗ldb, Real ∗work, int ∗lwork, int ∗info)

  Single-precision GEneral matrix Least Squares solver.
- void sgeqrf_ (int ∗m, int ∗n, Real ∗a, int ∗lda, Real ∗tau, Real ∗work, int ∗lwork, int ∗info)

  Single-precision GEneral matrix QR Factorization.
- void sormqr_ (char ∗side, char ∗trans, int ∗m, int ∗n, int ∗k, Real ∗a, int ∗lda, Real ∗tau, Real ∗c, int ∗ldc, Real ∗work, int ∗lwork, int ∗info)

  Single-precision Orthogonal Matrix from QR factorization.
- std::ostream & operator<< (std::ostream &stream, mtk::UniStgGrid1D &in)
- std::ostream & operator<< (std::ostream &stream, mtk::UniStgGrid2D &in)

Variables

- const float kZero {0.0f}

  MTK's zero defined according to selective compilation.
- const float kOne {1.0f}

  MTK's one defined according to selective compilation.
- const float kTwo {2.0f}

  MTK's two defined according to selective compilation.
- const float kDefaultTolerance {1e-7f}

  Considered tolerance for comparisons in numerical methods.
- const int kDefaultOrderAccuracy {2}

  Default order of accuracy for mimetic operators.
- const float kDefaultMimeticThreshold {1e-6f}

  Default tolerance for higher-order mimetic operators.
- const int kCriticalOrderAccuracyDiv {8}

  At this order (and higher) we must use the CBSA to construct.
- const int kCriticalOrderAccuracyGrad {10}

  At this order (and higher) we must use the CBSA to construct.

15.1.1 Function Documentation

15.1.1.1 std::ostream& mtk::operator<< (std::ostream & *stream*, mtk::Interp1D & *in*)

1. Print approximating coefficients for the interior.

Definition at line 66 of file mtk_interp_1d.cc.

15.1.1.2 std::ostream& mtk::operator<< (std::ostream & *stream*, mtk::UniStgGrid2D & *in*)

1. Print spatial coordinates.
2. Print scalar field.

Definition at line 67 of file mtk_uni_stg_grid_2d.cc.

15.1.1.3 std::ostream& mtk::operator<< (std::ostream & *stream*, mtk::UniStgGrid1D & *in*)

1. Print spatial coordinates.
2. Print scalar field.

Definition at line 68 of file mtk_uni_stg_grid_1d.cc.

15.1.1.4 std::ostream& mtk::operator<< (std::ostream & *stream*, mtk::Lap1D & *in*)

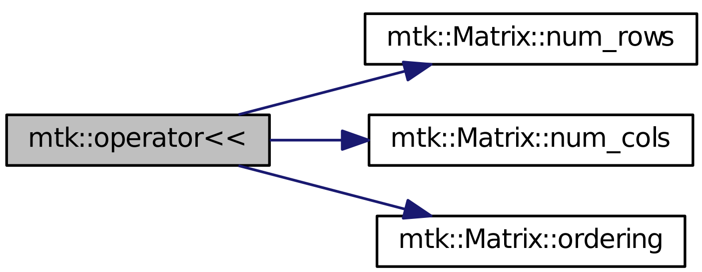
1. Print order of accuracy.
2. Print approximating coefficients for the interior.
3. No weights, thus print the mimetic boundary coefficients.

Definition at line 73 of file mtk_lap_1d.cc.

15.1.1.5 std::ostream& mtk::operator<< (std::ostream & *stream*, mtk::DenseMatrix & *in*)

Definition at line 77 of file mtk_dense_matrix.cc.

Here is the call graph for this function:



15.1.1.6 std::ostream& mtk::operator<< (std::ostream & *stream*, mtk::Grad1D & *in*)

1. Print order of accuracy.
2. Print approximating coefficients for the interior.
3. Print mimetic weights.
4. Print mimetic approximations at the boundary.

Definition at line 79 of file mtk_grad_1d.cc.

15.1.1.7 std::ostream& mtk::operator<< (std::ostream & *stream*, mtk::Div1D & *in*)

1. Print order of accuracy.
2. Print approximating coefficients for the interior.
3. Print mimetic weights.
4. Print mimetic approximations at the boundary.

Definition at line 79 of file mtk_div_1d.cc.

15.1.1.8 void mtk::saxpy_ (int ∗ *n*, float ∗ *sa*, float ∗ *sx*, int ∗ *incx*, float ∗ *sy*, int ∗ *incy*)

Here is the caller graph for this function:

15.1.1.9 void mtk::sgels_ (char ∗ *trans*, int ∗ *m*, int ∗ *n*, int ∗ *nrhs*, Real ∗ *a*, int ∗ *lda*, Real ∗ *b*, int ∗ *ldb*, Real ∗ *work*, int ∗ *lwork*, int ∗ *info*)

SGELS solves overdetermined or underdetermined real linear systems involving an M-by-N matrix A, or its transpose, using a QR or LQ factorization of A. It is assumed that A has full rank.

The following options are provided:

1. If TRANS = 'N' and m >= n: find the least squares solution of an overdetermined system, i.e., solve the least squares problem

```
minimize || B - A*X ||.
```

2. If TRANS = 'N' and m < n: find the minimum norm solution of an underdetermined system A ∗ X = B.
3. If TRANS = 'T' and m >= n: find the minimum norm solution of an undetermined system A∗∗T ∗ X = B.
4. If TRANS = 'T' and m < n: find the least squares solution of an overdetermined system, i.e., solve the least squares problem

```
minimize || B - A**T * X ||.
```

Several right hand side vectors b and solution vectors x can be handled in a single call; they are stored as the columns of the M-by-NRHS right hand side matrix B and the N-by-NRHS solution matrix X.

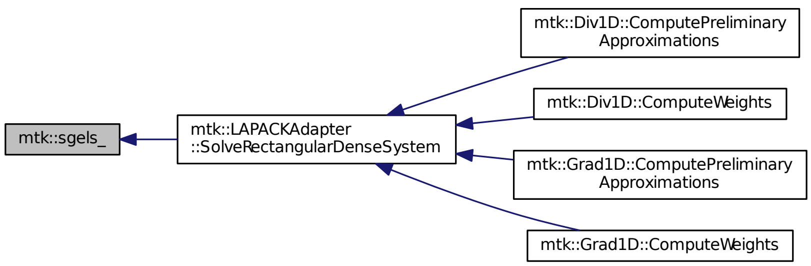
See also

http://www.math.utah.edu/software/lapack/lapack-s/sgels.html

Parameters

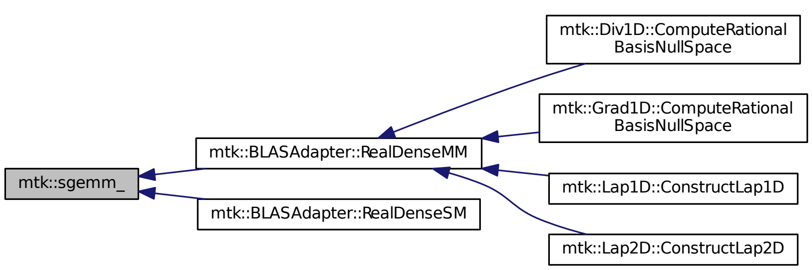
in	*trans*	Am I giving the transpose of the matrix?
in	*m*	The number of rows of the matrix a. m >= 0.
in	*n*	The number of columns of the matrix a. n >= 0.
in	*nrhs*	The number of right-hand sides.
in,out	*a*	On entry, the m-by-n matrix a.
in	*lda*	The leading dimension of a. lda >= max(1,m).
in,out	*b*	On entry, matrix b of right-hand side vectors.
in	*ldb*	The leading dimension of b. ldb >= max(1,m,n).
in,out	*work*	On exit, if info = 0, work(1) is optimal lwork.
in,out	*lwork*	The dimension of the array work.
in,out	*info*	If info = 0, then successful exit.

Here is the caller graph for this function:



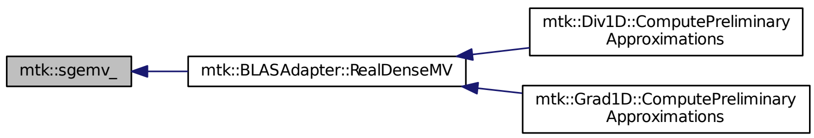
15.1.1.10 void mtk::sgemm_ (char * *transa*, char * *transb*, int * *m*, int * *n*, int * *k*, double * *alpha*, double * *a*, int * *lda*, double * *b*, aamm int * *ldb*, double * *beta*, double * *c*, int * *ldc*)

Here is the caller graph for this function:



15.1.1.11 void mtk::sgemv_ (char ∗ *trans,* int ∗ *m,* int ∗ *n,* float ∗ *alpha,* float ∗ *a,* int ∗ *lda,* float ∗ *x,* int ∗ *incx,* float ∗ *beta,* float ∗ *y,* int ∗ *incy*)

Here is the caller graph for this function:



15.1.1.12 void mtk::sgeqrf_ (int ∗ *m,* int ∗ *n,* Real ∗ *a,* int ∗ *lda,* Real ∗ *tau,* Real ∗ *work,* int ∗ *lwork,* int ∗ *info*)

Single-Precision Orthogonal Make Q from QR: dormqr_ overwrites the general real M-by-N matrix C with (Table 1):

```
SIDE = 'L'     SIDE = 'R'
```

TRANS = 'N': Q ∗ C C ∗ Q TRANS = 'T': Q∗∗T ∗ C C ∗ Q∗∗T
where Q is a real orthogonal matrix defined as the product of k elementary reflectors

```
Q = H(1) H(2) . . . H(k)
```

as returned by SGEQRF. Q is of order M if SIDE = 'L' and of order N if SIDE = 'R'.

See also

http://www.netlib.org/lapack/explore-html/df/d97/sgeqrf_8f.html

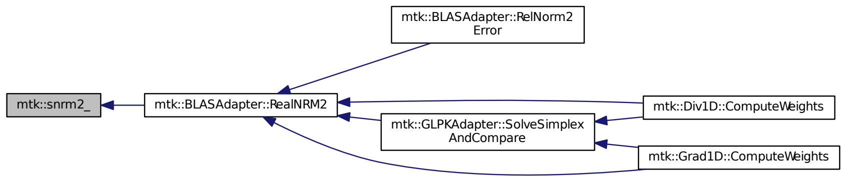
Parameters

in	*m*	The number of columns of the matrix a. n >= 0.
in	*n*	The number of columns of the matrix a. n >= 0.
in,out	*a*	On entry, the n-by-n matrix a.
in	*lda*	Leading dimension matrix. LDA >= max(1,M).
in,out	*tau*	Scalars from elementary reflectors. min(M,N).
in,out	*work*	Workspace. info = 0, work(1) is optimal lwork.
in	*lwork*	The dimension of work. lwork >= max(1,n).
in	*info*	info = 0: successful exit.

15.1.1.13 void mtk::sgesv_ (int ∗ *n,* int ∗ *nrhs,* Real ∗ *a,* int ∗ *lda,* int ∗ *ipiv,* Real ∗ *b,* int ∗ *ldb,* int ∗ *info*)

15.1.1.14 float mtk::snrm2_ (int * *n*, float * *x*, int * *incx*)

Here is the caller graph for this function:



15.1.1.15 void mtk::sormqr_ (char * *side*, char * *trans*, int * *m*, int * *n*, int * *k*, Real * *a*, int * *lda*, Real * *tau*, Real * *c*, int * *ldc*, Real * *work*, int * *lwork*, int * *info*)

Single-Precision Orthogonal Make Q from QR: sormqr_ overwrites the general real M-by-N matrix C with (Table 1):

```
SIDE = 'L'      SIDE = 'R'
```

TRANS = 'N': Q * C C * Q TRANS = 'T': Q**T * C C * Q**T

where Q is a real orthogonal matrix defined as the product of k elementary reflectors

```
Q = H(1) H(2) . . . H(k)
```

as returned by SGEQRF. Q is of order M if SIDE = 'L' and of order N if SIDE = 'R'.

See also

http://www.netlib.org/lapack/explore-html/d0/d98/sormqr_8f_source.html

Parameters

in	*side*	See Table 1 above.
in	*trans*	See Table 1 above.
in	*m*	Number of rows of the C matrix.
in	*n*	Number of columns of the C matrix.
in	*k*	Number of reflectors.
in,out	*a*	The matrix containing the reflectors.
in	*lda*	The dimension of work. lwork >= max(1,n).
in	*tau*	Scalar factors of the elementary reflectors.
in	*c*	Output matrix.
in	*ldc*	Leading dimension of the output matrix.
in,out	*work*	Workspace. info = 0, work(1) optimal lwork.
in	*lwork*	The dimension of work.

in,out	*info*	info = 0: successful exit.

Chapter 16

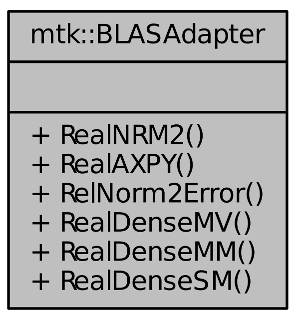
Class Documentation

16.1 mtk::BLASAdapter Class Reference

Adapter class for the BLAS API.

#include <mtk_blas_adapter.h>

Collaboration diagram for mtk::BLASAdapter:



Static Public Member Functions

- static Real RealNRM2 (Real ∗in, int &in_length)

  Compute the $||\mathbf{x}||_2$ *of given array* $\mathbf{x}$.
- static void RealAXPY (Real alpha, Real ∗xx, Real ∗yy, int &in_length)

  Real-Arithmetic Scalar-Vector plus a Vector.
- static Real RelNorm2Error (Real ∗computed, Real ∗known, int length)

  Computes the relative norm-2 of the error.
- static void RealDenseMV (Real &alpha, DenseMatrix &aa, Real ∗xx, Real &beta, Real ∗yy)

  Real-Arithmetic General (Dense matrices) Matrix-Vector Multiplier.

- static DenseMatrix RealDenseMM (DenseMatrix &aa, DenseMatrix &bb)

  Real-Arithmetic General (Dense matrices) Matrix-Matrix multiplier.
- static DenseMatrix RealDenseSM (Real alpha, DenseMatrix &aa)

  Real-Arithmetic General (Dense matrices) Scalar-Matrix multiplier.

16.1.1 Detailed Description

This class contains a collection of static classes, that posses direct access to the underlying structure of the matrices, thus allowing programmers to exploit some of the numerical methods implemented in the BLAS.

The **BLAS (Basic Linear Algebra Subprograms)** are routines that provide standard building blocks for performing basic vector and matrix operations. The Level 1 BLAS perform scalar, vector and vector-vector operations, the Level 2 BLAS perform matrix-vector operations, and the Level 3 BLAS perform matrix-matrix operations.

See also

`http://www.netlib.org/blas/`

Definition at line 96 of file mtk_blas_adapter.h.

16.1.2 Member Function Documentation

16.1.2.1 void mtk::BLASAdapter::RealAXPY (mtk::Real *alpha*, mtk::Real ∗ *xx*, mtk::Real ∗ *yy*, int & *in_length*) [static]

Performs

$$\mathbf{y} := \alpha \mathbf{A} mathbf{x} + \mathbf{y}$$

Parameters

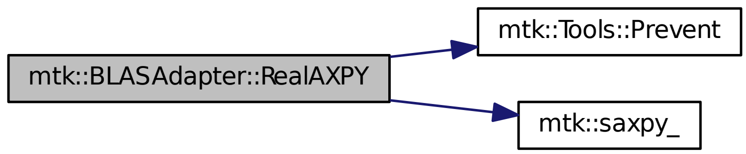
in	*alpha*	Scalar of the first array.
in	*xx*	First array.
in	*yy*	Second array.
in	*in_length*	Lengths of the given arrays.

Returns

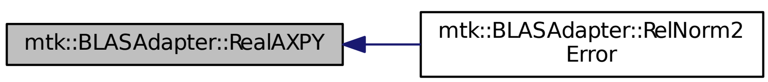
Norm-2 of the given array.

Definition at line 339 of file mtk_blas_adapter.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.1.2.2 mtk::DenseMatrix mtk::BLASAdapter::RealDenseMM (mtk::DenseMatrix & *aa*, mtk::DenseMatrix & *bb*) [static]

Performs:

$$\mathbf{C} := \mathbf{AB}$$

Parameters

in	*aa*	First matrix.
in	*bb*	Second matrix.

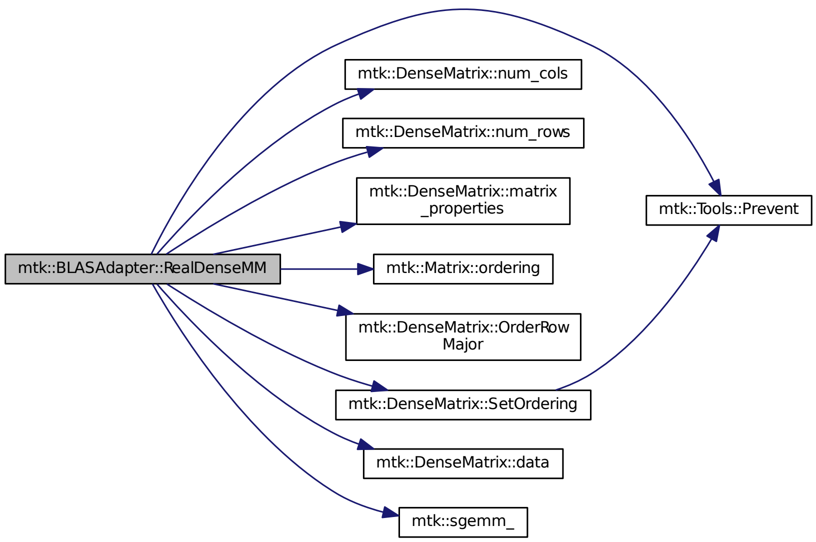
See also

http://ejspeiro.github.io/Netlib-and-CPP/

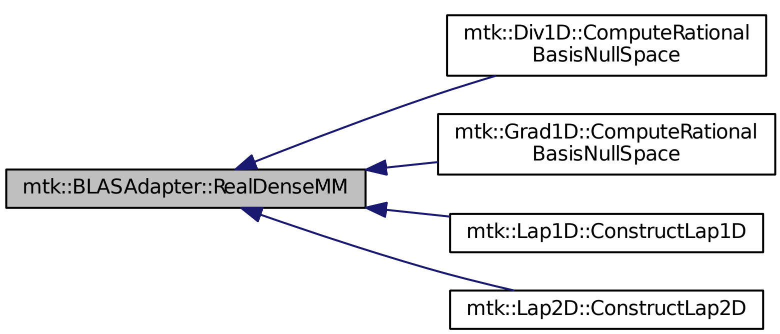
1. Make sure input matrices are row-major ordered.
2. Setup the problem.
3. Perform multiplication.

Definition at line 409 of file mtk_blas_adapter.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.1.2.3 void mtk::BLASAdapter::RealDenseMV (mtk::Real & *alpha*, mtk::DenseMatrix & *aa*, mtk::Real $*$ *xx*, mtk::Real & *beta*, mtk::Real $*$ *yy*) [static]

Performs

$$\mathbf{y} := \alpha \mathbf{A} \mathbf{x} + \beta \mathbf{y}$$

Parameters

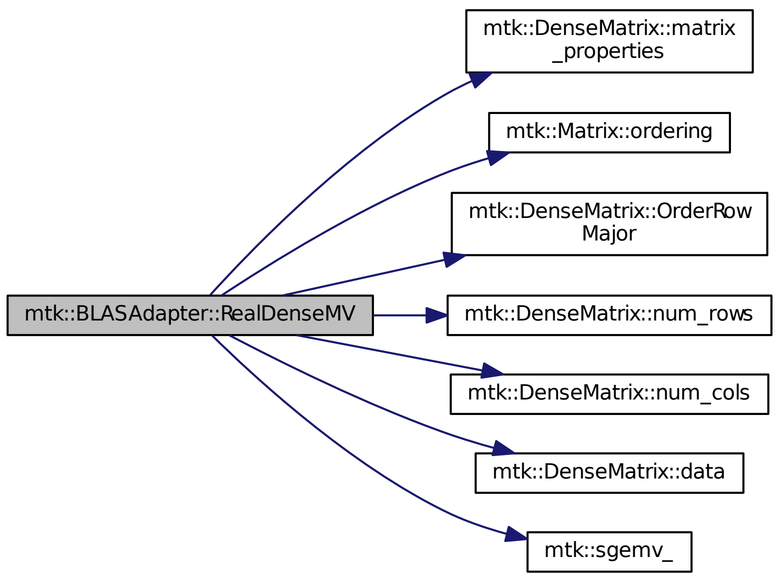
in	*alpha*	First scalar.
in	*aa*	Given matrix.
in	*xx*	First vector.
in	*beta*	Second scalar.
in,out	*yy*	Second vector (output).

See also

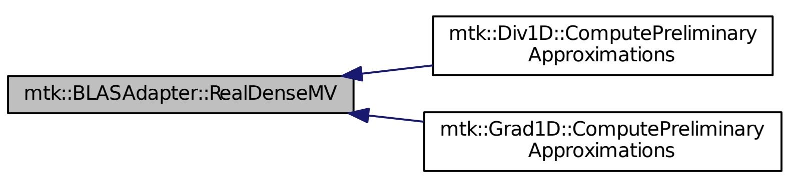
http://ejspeiro.github.io/Netlib-and-CPP/

Definition at line 378 of file mtk_blas_adapter.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.1.2.4 mtk::DenseMatrix mtk::BLASAdapter::RealDenseSM (mtk::Real *alpha*, mtk::DenseMatrix & *aa*) [static]

Performs:

$$\mathbf{B} := \alpha\mathbf{A}$$

Parameters

in	*alpha*	Input scalar.
in	*aa*	Input matrix.

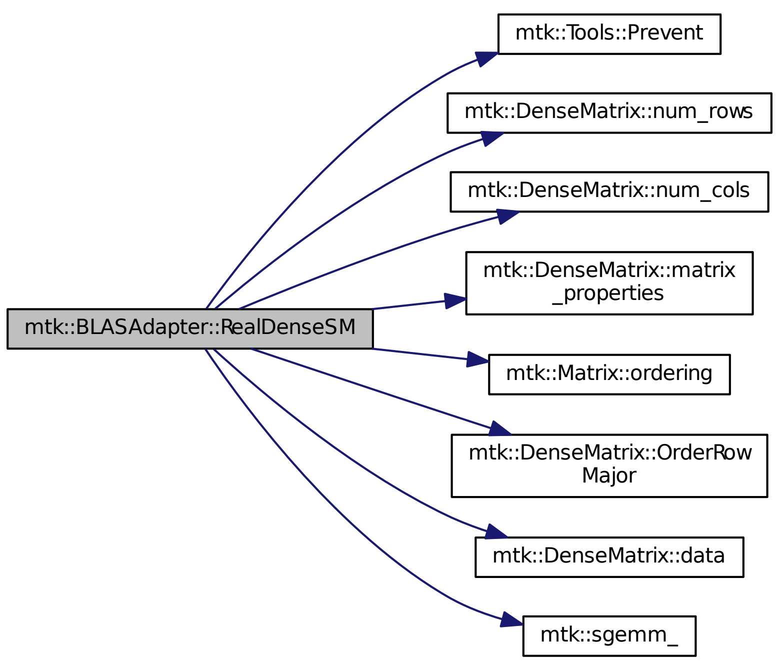
See also

http://ejspeiro.github.io/Netlib-and-CPP/

1. Make sure input matrices are row-major ordered.
2. Setup the problem.
3. Perform multiplication.

Definition at line 466 of file mtk_blas_adapter.cc.

Here is the call graph for this function:



16.1.2.5 mtk::Real mtk::BLASAdapter::RealNRM2 (Real * *in*, int & *in_length*) [static]

Parameters

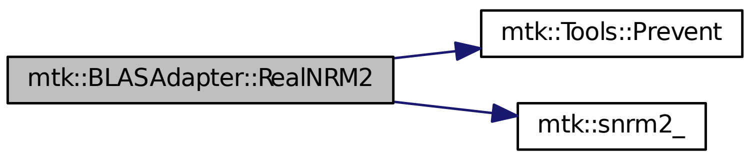
in	*in*	Input array.
in	*in_length*	Length of the array.

Returns

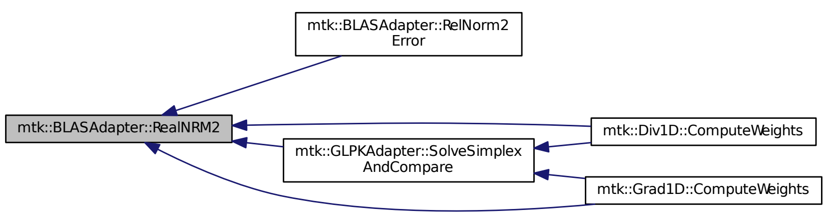
Norm-2 of the given array.

Definition at line 324 of file mtk_blas_adapter.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.1.2.6 mtk::Real mtk::BLASAdapter::RelNorm2Error (mtk::Real * *computed*, mtk::Real * *known*, int *length*) [static]

We compute

$$\frac{||\tilde{\mathbf{x}} - \mathbf{x}||_2}{||\mathbf{x}||_2}.$$

Parameters

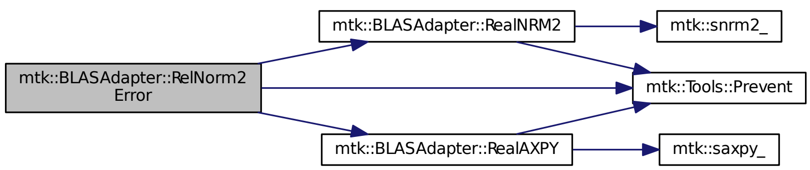
in	*known*	Array containing the computed solution.
in	*computed*	Array containing the known solution (ref. solution).

Returns

Relative norm-2 of the error, aka, the difference between the arrays.

Definition at line 358 of file mtk_blas_adapter.cc.

Here is the call graph for this function:



The documentation for this class was generated from the following files:

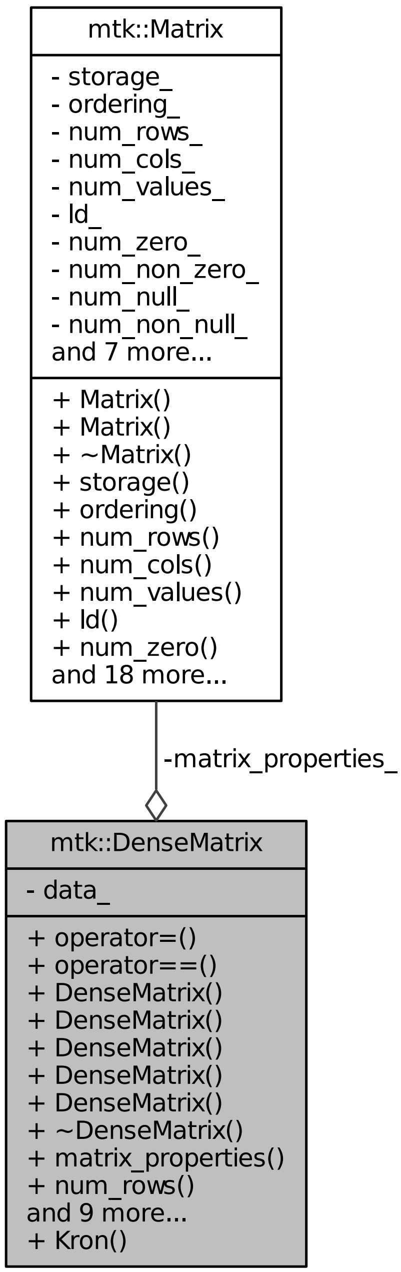
- include/mtk_blas_adapter.h
- src/mtk_blas_adapter.cc

16.2 mtk::DenseMatrix Class Reference

Defines a common dense matrix, using a 1D array.

`#include <mtk_dense_matrix.h>`

Collaboration diagram for mtk::DenseMatrix:



Public Member Functions

- DenseMatrix & operator= (const DenseMatrix &in)

Overloaded assignment operator.

- bool operator== (const DenseMatrix &in)

  Am I equal to the in matrix?

- DenseMatrix ()

  Default constructor.

- DenseMatrix (const DenseMatrix &in)

  Copy constructor.

- DenseMatrix (const int &num_rows, const int &num_cols)

  Construct a dense matrix based on the given dimensions.

- DenseMatrix (const int &rank, const bool &padded, const bool &transpose)

  Construct a zero-rows-padded identity matrix.

- DenseMatrix (const Real ∗const gen, const int &gen_length, const int &pro_length, const bool &transpose)

  Construct a dense Vandermonde matrix.

- ∼DenseMatrix ()

  Destructor.

- Matrix matrix_properties () const noexcept

  Provides access to the matrix data.

- int num_rows () const noexcept

  Gets the number of rows.

- int num_cols () const noexcept

  Gets the number of columns.

- Real ∗ data () const noexcept

  Provides access to the matrix value array.

- void SetOrdering (mtk::MatrixOrdering oo) noexcept

  Sets the ordering of the matrix.

- Real GetValue (const int &row_coord, const int &col_coord) const noexcept

  Gets a value on the given coordinates.

- void SetValue (const int &row_coord, const int &col_coord, const Real &val) noexcept

  Sets a value on the given coordinates.

- void Transpose ()

  Transpose this matrix.

- void OrderRowMajor ()

  Make the matrix row-wise ordered.

- void OrderColMajor ()

  Make the matrix column-wise ordered.

- bool WriteToFile (const std::string &filename) const

  Writes matrix to a file compatible with Gnuplot 4.6.

Static Public Member Functions

- static DenseMatrix Kron (const DenseMatrix &aa, const DenseMatrix &bb)

  Construct a dense matrix based on the Kronecker product of arguments.

Private Attributes

- Matrix matrix_properties_

  Data related to the matrix nature.
- Real ∗ data_

  Array holding the data in contiguous position in memory.

Friends

- std::ostream & operator<< (std::ostream &stream, DenseMatrix &in)

  Prints the matrix as a block of numbers (standard way).

16.2.1 Detailed Description

For developing purposes, it is better to have a not-so-intrincated data structure implementing matrices. This is the purpose of this class: to be used for prototypes of new code for small test cases. In every other instance, this should be replaced by the most appropriate sparse matrix.

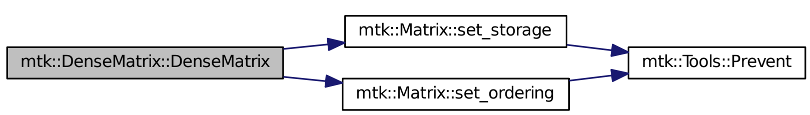
Definition at line 92 of file mtk_dense_matrix.h.

16.2.2 Constructor & Destructor Documentation

16.2.2.1 mtk::DenseMatrix::DenseMatrix ( )

Definition at line 162 of file mtk_dense_matrix.cc.

Here is the call graph for this function:



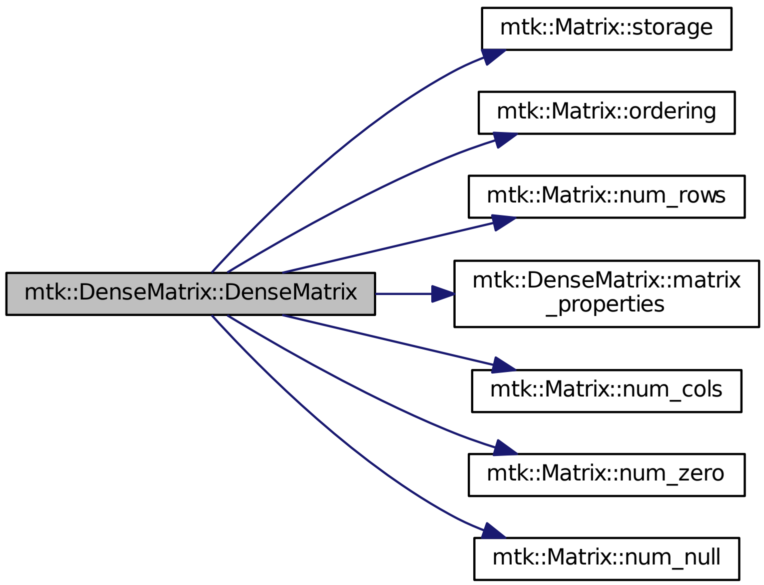
16.2.2.2 mtk::DenseMatrix::DenseMatrix (const DenseMatrix & *in*)

Parameters

in	*in*	Given matrix.

Definition at line 168 of file mtk_dense_matrix.cc.

Here is the call graph for this function:



16.2.2.3 mtk::DenseMatrix::DenseMatrix (const int & *num_rows*, const int & *num_cols*)

Parameters

in	*num_rows*	Number of rows of the required matrix.
in	*num_cols*	Number of rows of the required matrix.

Exceptions

std::bad_alloc	

Definition at line 201 of file mtk_dense_matrix.cc.

Here is the call graph for this function:

16.2.2.4 mtk::DenseMatrix::DenseMatrix (const int & *rank,* const bool & *padded,* const bool & *transpose*)

Used in the construction of the mimetic operators.

Def$**$. A **padded matrix** is a matrix with its first and last rows initialized to only zero values:

$$\bar{\mathbf{I}} = \begin{pmatrix} 0 & 0 & 0 & \dots & 0 \\ 1 & 0 & 0 & \dots & 0 \\ 0 & 1 & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & \dots & 1 \\ 0 & 0 & 0 & \dots & 0 \end{pmatrix}$$

Parameters

in	*rank*	Rank or number of rows/cols in square matrix.
in	*padded*	Should it be padded?
in	*transpose*	Should I return the transpose of the requested matrix?

Exceptions

std::bad_alloc	

Definition at line 223 of file mtk_dense_matrix.cc.

Here is the call graph for this function:

16.2.2.5 mtk::DenseMatrix::DenseMatrix (const Real $*$const *gen,* const int & *gen_length,* const int & *pro_length,* const bool & *transpose*)

Def$**$. In linear algebra, a **Vandermonde matrix** is a matrix with terms of a geometric progression in each row. This progression uses the terms of a given **generator vector**:

$$\mathbf{V} = \begin{pmatrix} 1 & \alpha_1 & \alpha_1^2 & \dots & \alpha_1^{n-1} \\ 1 & \alpha_2 & \alpha_2^2 & \dots & \alpha_2^{n-1} \\ 1 & \alpha_3 & \alpha_3^2 & \dots & \alpha_3^{n-1} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 1 & \alpha_m & \alpha_m^2 & \dots & \alpha_m^{n-1} \end{pmatrix}$$

This constructor generates a Vandermonde matrix, as defined above.

Obs$**$. It in important to understand that the generator vectors to be used are nothing but a very particular instance of a grid. These are little chunks, little samples, if you will, of a grid which is rectangular and uniform. So the selected samples, on the mtk::Div1D and mtk::Grad1D, basically represent the entire space, the entire grid. This is why nor the CRS nor the CBS algorithms may work for irregular geometries, such as curvilinear grids.

Parameters

in	*gen*	Given generator vector.
in	*gen_length*	Length generator vector.
in	*pro_length*	Length the progression.
in	*transpose*	Should the transpose be created instead?

Exceptions

std::bad_alloc	

Definition at line 264 of file mtk_dense_matrix.cc.

Here is the call graph for this function:

16.2.2.6 mtk::DenseMatrix::∼DenseMatrix ( )

Definition at line 312 of file mtk_dense_matrix.cc.

16.2.3 Member Function Documentation

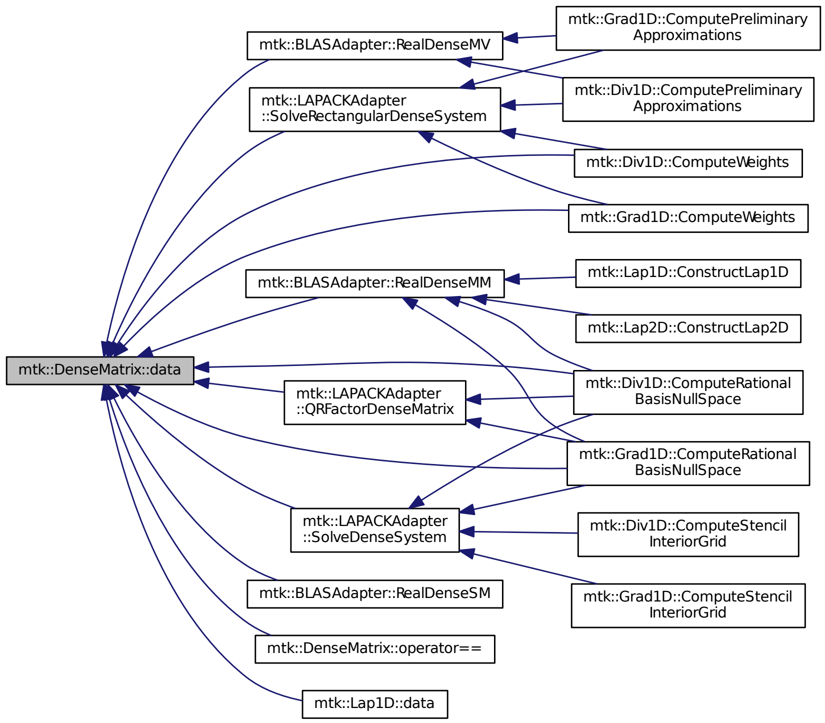
16.2.3.1 mtk::Real ∗ mtk::DenseMatrix::data ( ) const [noexcept]

Returns

Pointer to an array of mtk::Real.

Definition at line 343 of file mtk_dense_matrix.cc.

Here is the caller graph for this function:



16.2.3.2 mtk::Real mtk::DenseMatrix::GetValue (const int & *row_coord*, const int & *col_coord*) const [noexcept]

Parameters

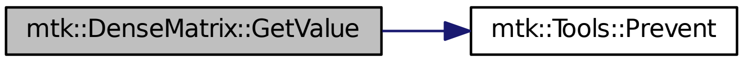
in	*row_coord*	Row coordinate.
in	*col_coord*	Column coordinate.

Returns

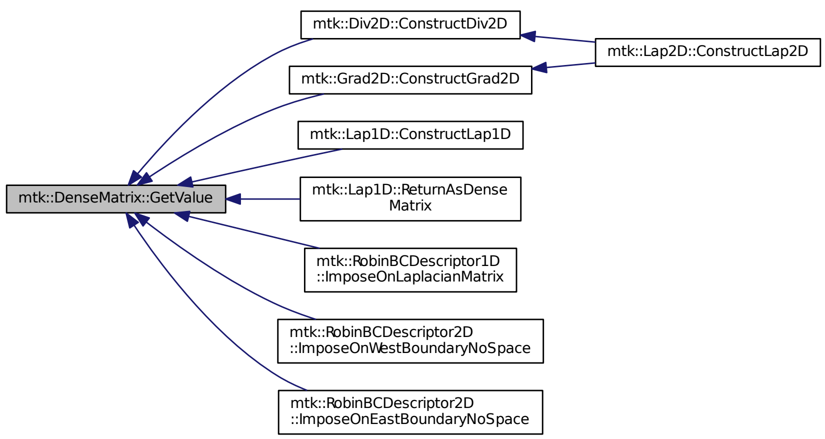
The required value at the specified coordinates.

Definition at line 348 of file mtk_dense_matrix.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.2.3.3 mtk::DenseMatrix mtk::DenseMatrix::Kron (const DenseMatrix & *aa*, const DenseMatrix & *bb*) [static]

Parameters

in	*aa*	First matrix.
in	*bb*	Second matrix.

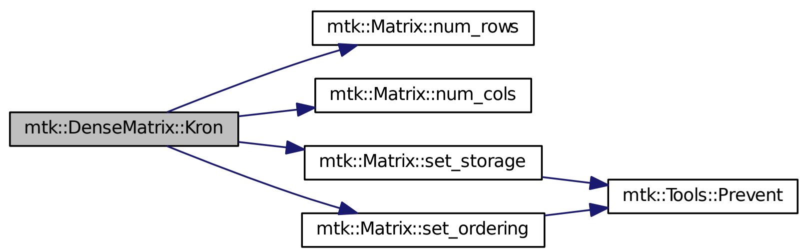
Exceptions

std::bad_alloc	

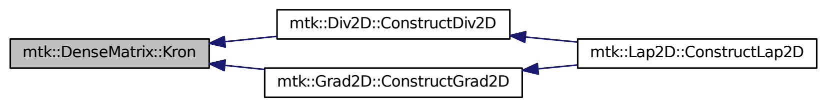
Todo Implement Kronecker product using the BLAS.

Definition at line 490 of file mtk_dense_matrix.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



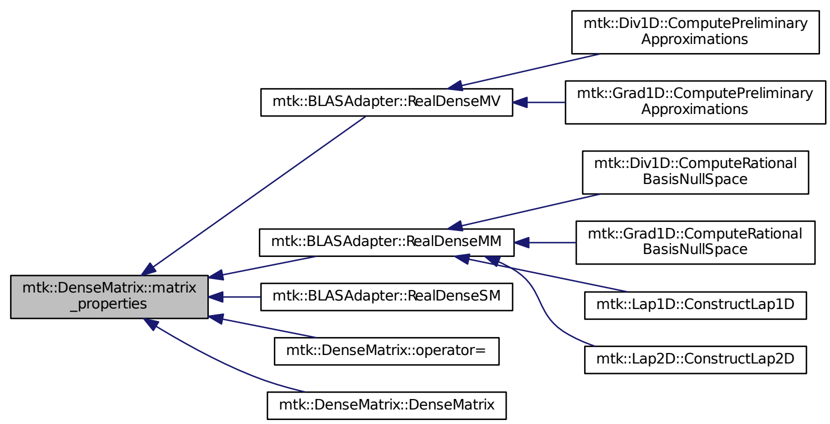
16.2.3.4 mtk::Matrix mtk::DenseMatrix::matrix_properties ( ) const [noexcept]

Returns

Pointer to a Matrix.

Definition at line 318 of file mtk_dense_matrix.cc.

Here is the caller graph for this function:



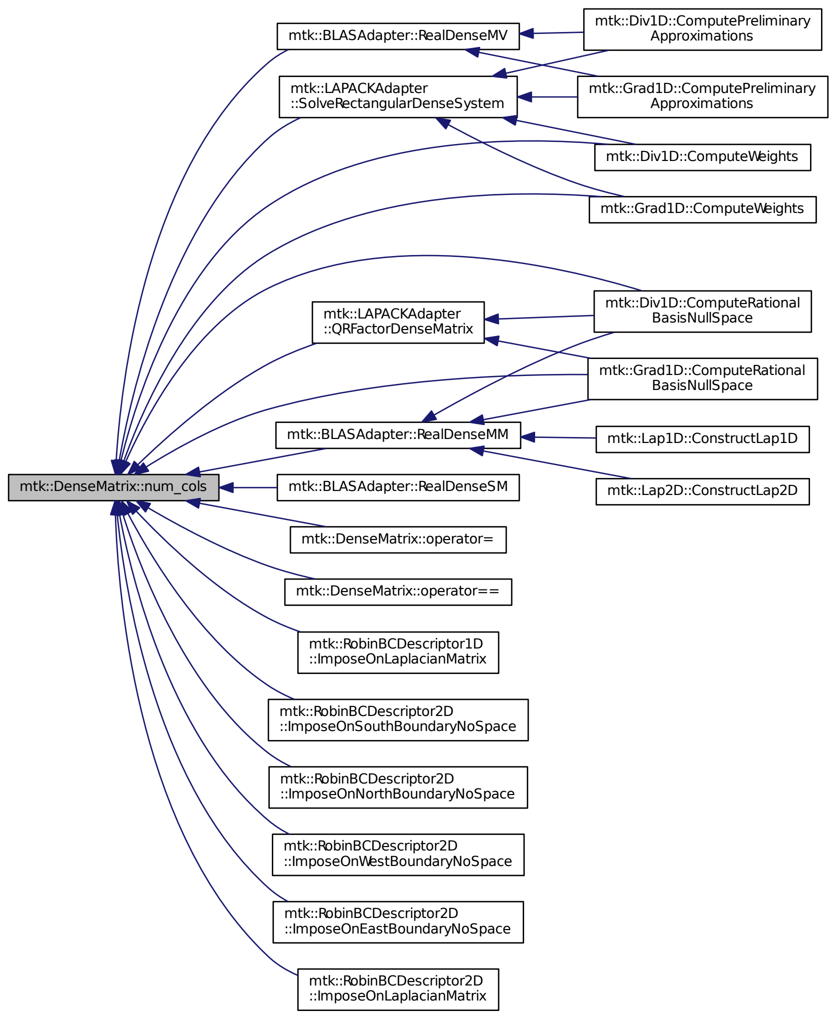
16.2.3.5 int mtk::DenseMatrix::num_cols ( ) const [noexcept]

Returns

Number of columns of the matrix.

Definition at line 338 of file mtk_dense_matrix.cc.

Here is the caller graph for this function:



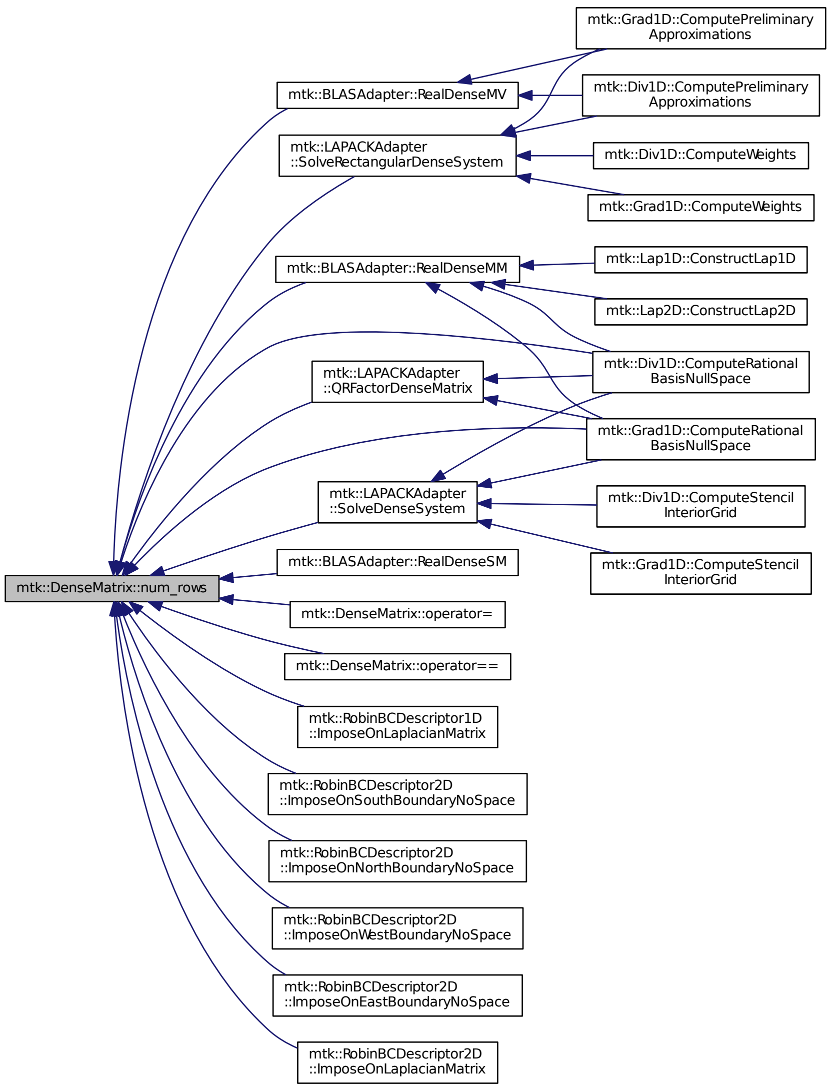
16.2.3.6 int mtk::DenseMatrix::num_rows ( ) const [noexcept]

Returns

Number of rows of the matrix.

Definition at line 333 of file mtk_dense_matrix.cc.

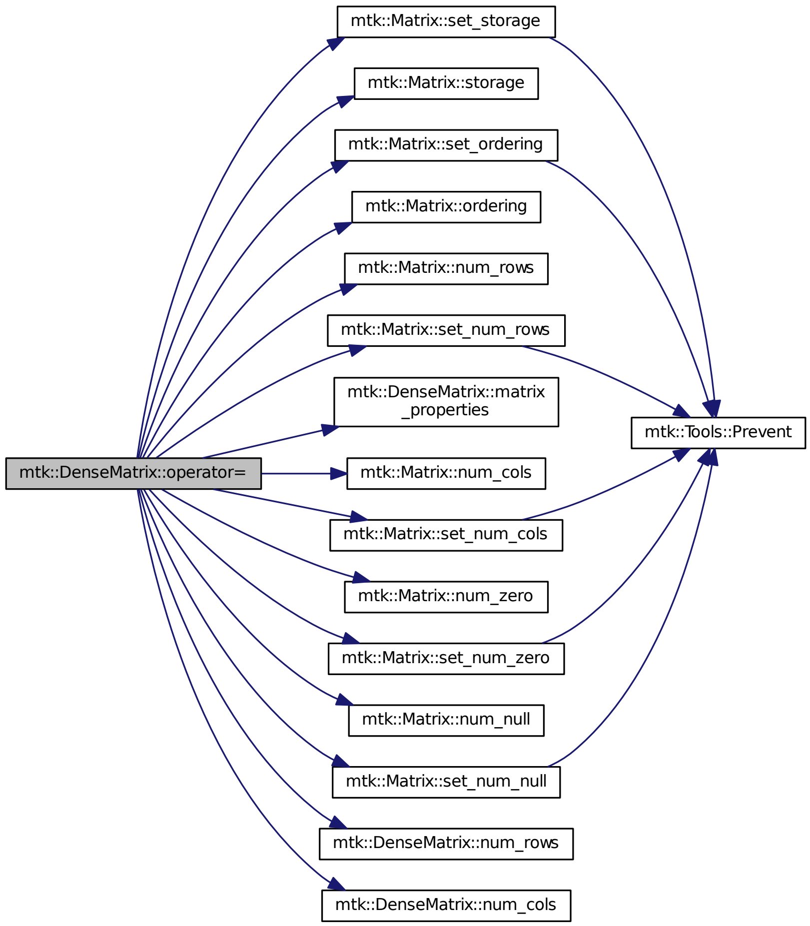
Here is the caller graph for this function:



16.2.3.7 mtk::DenseMatrix & mtk::DenseMatrix::operator= (const DenseMatrix & *in*)

Definition at line 100 of file mtk_dense_matrix.cc.

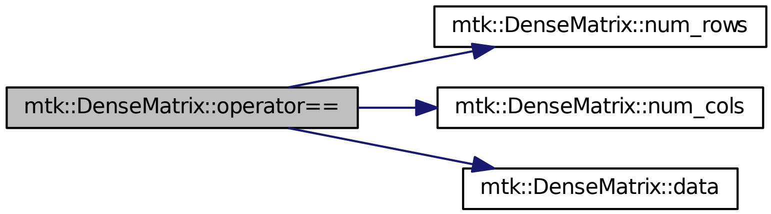
Here is the call graph for this function:



16.2.3.8 bool mtk::DenseMatrix::operator== (const DenseMatrix & *in*)

Definition at line 141 of file mtk_dense_matrix.cc.

Here is the call graph for this function:

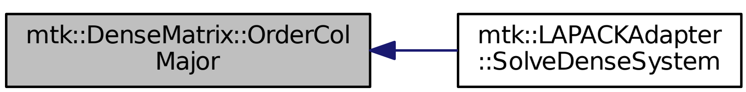


16.2.3.9 void mtk::DenseMatrix::OrderColMajor ( )

Todo Improve this so that no new arrays have to be created.

Definition at line 451 of file mtk_dense_matrix.cc.

Here is the caller graph for this function:

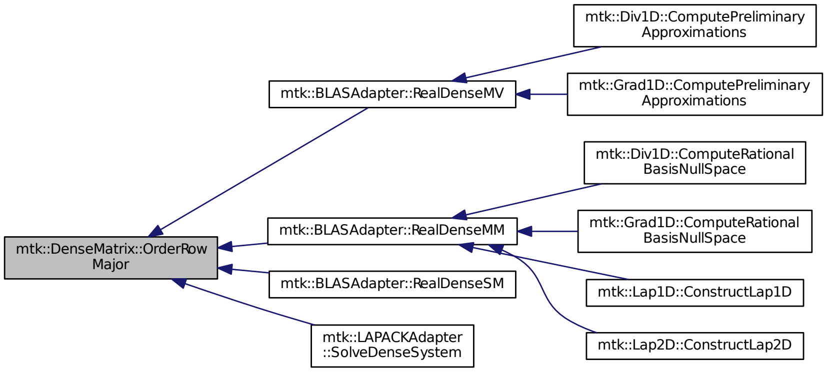


16.2.3.10 void mtk::DenseMatrix::OrderRowMajor ( )

Todo Improve this so that no new arrays have to be created.

Definition at line 410 of file mtk_dense_matrix.cc.

Here is the caller graph for this function:



16.2.3.11 void mtk::DenseMatrix::SetOrdering (**mtk::MatrixOrdering** *oo*) [noexcept]

Parameters

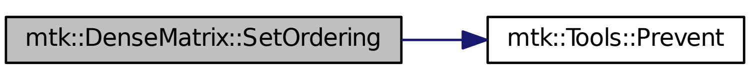
in	*oo*	Ordering.

Returns

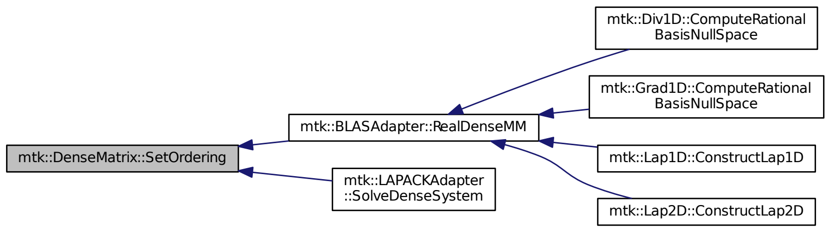
The required value at the specified coordinates.

Definition at line 323 of file mtk_dense_matrix.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



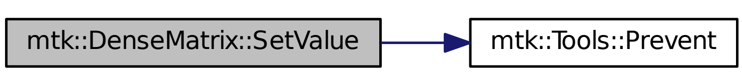
16.2.3.12 void mtk::DenseMatrix::SetValue (const int & *row_coord,* const int & *col_coord,* const Real & *val*) [noexcept]

Parameters

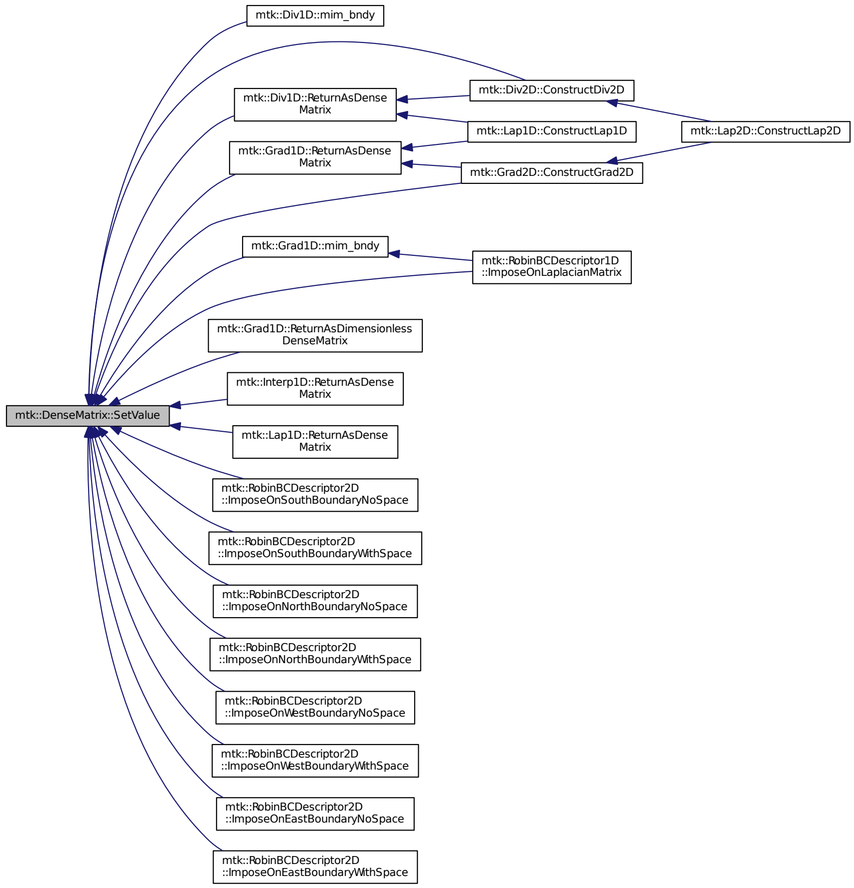
in	*row_coord*	Row coordinate.
in	*col_coord*	Column coordinate.
in	*val*	Row Actual value to be inserted.

Definition at line 360 of file mtk_dense_matrix.cc.

Here is the call graph for this function:



Here is the caller graph for this function:

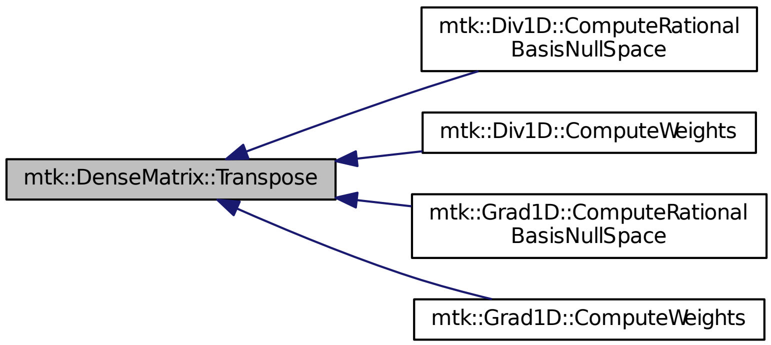


16.2.3.13 void mtk::DenseMatrix::Transpose ( )

Todo Improve this so that no extra arrays have to be created.

Definition at line 373 of file mtk_dense_matrix.cc.

Here is the caller graph for this function:



16.2.3.14 bool mtk::DenseMatrix::WriteToFile (const std::string & *filename*) const

Parameters

in	*filename*	Name of the output file.

Returns

Success of the file writing process.

See also

http://www.gnuplot.info/

Definition at line 531 of file mtk_dense_matrix.cc.

16.2.4 Friends And Related Function Documentation

16.2.4.1 std::ostream& operator<< (std::ostream & *stream*, mtk::DenseMatrix & *in*) [friend]

Definition at line 77 of file mtk_dense_matrix.cc.

16.2.5 Member Data Documentation

16.2.5.1 Real* mtk::DenseMatrix::data_ [private]

Definition at line 285 of file mtk_dense_matrix.h.

16.2.5.2 Matrix mtk::DenseMatrix::matrix_properties_ [private]

Definition at line 283 of file mtk_dense_matrix.h.

The documentation for this class was generated from the following files:

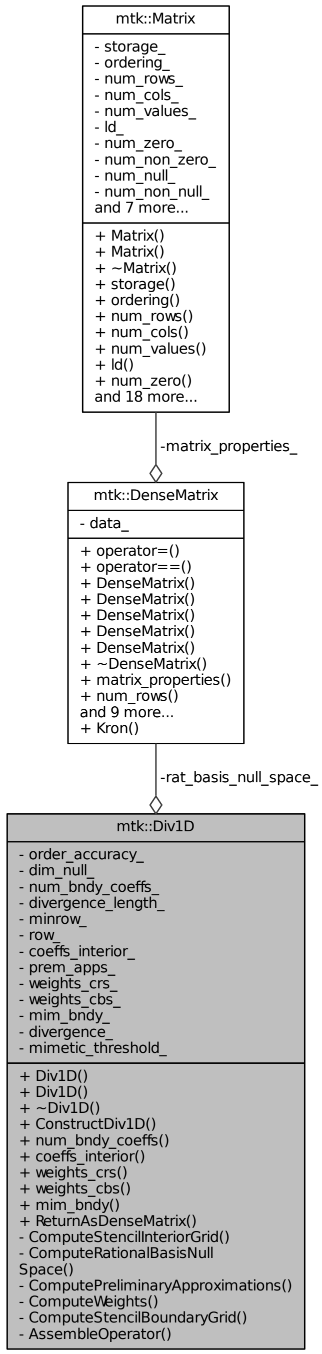
- include/mtk_dense_matrix.h
- src/mtk_dense_matrix.cc

16.3 mtk::Div1D Class Reference

Implements a 1D mimetic divergence operator.

```
#include <mtk_div_1d.h>
```

Collaboration diagram for mtk::Div1D:



Public Member Functions

- Div1D ()

Default constructor.
- Div1D (const Div1D &div)

  Copy constructor.
- ∼Div1D ()

  Destructor.
- bool ConstructDiv1D (int order_accuracy=kDefaultOrderAccuracy, Real mimetic_threshold=kDefaultMimetic←Threshold)

  Factory method implementing the CBS Algorithm to build operator.
- int num_bndy_coeffs () const

  Returns how many coefficients are approximating at the boundary.
- Real ∗ coeffs_interior () const

  Returns coefficients for the interior of the grid.
- Real ∗ weights_crs (void) const

  Return collection of weights as computed by the CRSA.
- Real ∗ weights_cbs (void) const

  Return collection of weights as computed by the CBSA.
- DenseMatrix mim_bndy () const

  Return collection of mimetic approximations at the boundary.
- DenseMatrix ReturnAsDenseMatrix (const UniStgGrid1D &grid) const

  Return the operator as a dense matrix.

Private Member Functions

- bool ComputeStencilInteriorGrid (void)

  Stage 1 of the CBS Algorithm.
- bool ComputeRationalBasisNullSpace (void)

  Stage 2.1 of the CBS Algorithm.
- bool ComputePreliminaryApproximations (void)

  Stage 2.2 of the CBS Algorithm.
- bool ComputeWeights (void)

  Stage 2.3 of the CBS Algorithm.
- bool ComputeStencilBoundaryGrid (void)

  Stage 2.4 of the CBS Algorithm.
- bool AssembleOperator (void)

  Stage 3 of the CBS Algorithm.

Private Attributes

- int order_accuracy_

  Order of numerical accuracy of the operator.
- int dim_null_

  Dim. null-space for boundary approximations.
- int num_bndy_coeffs_

  Req. coeffs. per bndy pt. uni. order accuracy.
- int divergence_length_

  Length of the output array.
- int minrow_

Row from the optimizer with the minimum rel. nor.

- int row_

  Row currently processed by the optimizer.

- DenseMatrix rat_basis_null_space_

  Rational b. null-space w. bndy.

- Real ∗ coeffs_interior_

  Interior stencil.

- Real ∗ prem_apps_

  2D array of boundary preliminary approximations.

- Real ∗ weights_crs_

  Array containing weights from CRSA.

- Real ∗ weights_cbs_

  Array containing weights from CBSA.

- Real ∗ mim_bndy_

  Array containing mimetic boundary approximations.

- Real ∗ divergence_

  Output array containing the operator and weights.

- Real mimetic_threshold_

  < Mimetic threshold.

Friends

- std::ostream & operator<< (std::ostream &stream, Div1D &in)

  Output stream operator for printing.

16.3.1 Detailed Description

This class implements a 1D divergence operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (CBSA).

Definition at line 81 of file mtk_div_1d.h.

16.3.2 Constructor & Destructor Documentation

16.3.2.1 mtk::Div1D::Div1D ( )

Definition at line 125 of file mtk_div_1d.cc.

16.3.2.2 mtk::Div1D::Div1D (const Div1D & *div*)

Parameters

in	*div*	Given divergence.

Definition at line 140 of file mtk_div_1d.cc.

16.3.2.3 mtk::Div1D::∼Div1D ( )

Definition at line 155 of file mtk_div_1d.cc.

16.3.3 Member Function Documentation

16.3.3.1 bool mtk::Div1D::AssembleOperator (void) [private]

Construct the output array with the operator and its weights.

1. The first entry of the array will contain the order of accuracy.
2. The second entry the collection of coefficients for interior of grid.
3. If order_accuracy_ $>$ 2, then third entry is the collection of weights.
4. If order_accuracy_ $>$ 2, next dim_null_ entries is approximating coefficients for the west boundary of the grid.

Definition at line 1342 of file mtk_div_1d.cc.

16.3.3.2 mtk::Real ∗ mtk::Div1D::coeffs_interior ( ) const

Returns

Coefficients for the interior of the grid.

Definition at line 320 of file mtk_div_1d.cc.

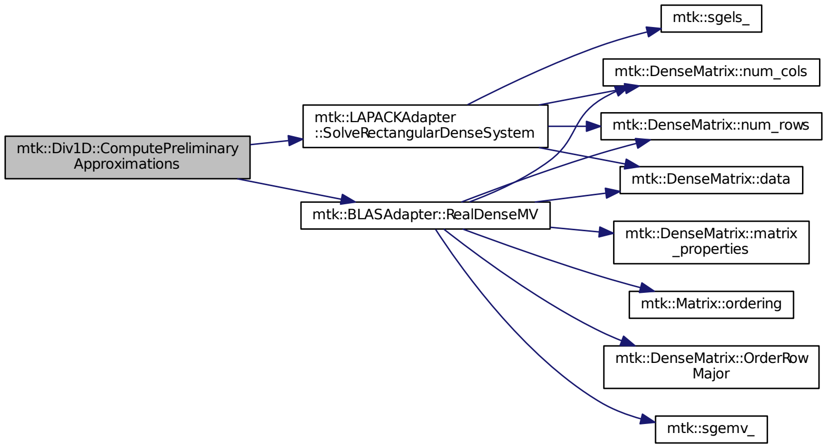
16.3.3.3 bool mtk::Div1D::ComputePreliminaryApproximations (void) [private]

Compute the set of preliminary approximations on the boundary neighborhood.

1. Create generator vector for the first approximation.
2. Compute the dim_null near-the-boundary columns of the pi matrix.
3. Create the Vandermonde matrix for this iteration.
4. New order-selector vector (gets re-written with LAPACK solutions).
5. Solving TT∗rr = ob yields the columns rr of the KK matrix.
6. Scale the KK matrix to make it a rational basis for null-space.
7. Extract the last dim_null values of the pre-scaled ob.
8. Once we posses the bottom elements, we proceed with the scaling.

Definition at line 691 of file mtk_div_1d.cc.

Here is the call graph for this function:



16.3.3.4 bool mtk::Div1D::ComputeRationalBasisNullSpace (void) [private]

Compute a rational basis for the null-space of the Vandermonde matrix approximating at the west boundary.

1. Create generator vector for the first approximation.

2. Create Vandermonde matrix.

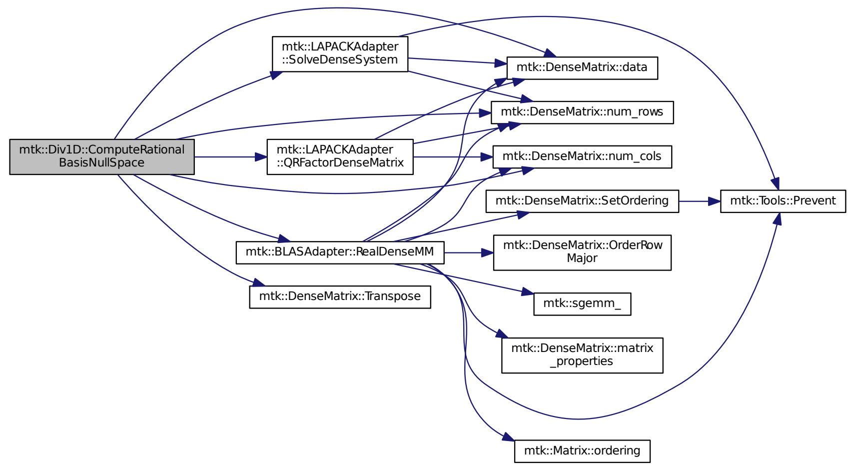
3. QR-factorize the Vandermonde matrix.

4. Extract the basis for the null-space from Q matrix.

5. Scale null-space to make it rational.

Definition at line 515 of file mtk_div_1d.cc.

Here is the call graph for this function:



16.3.3.5 bool mtk::Div1D::ComputeStencilBoundaryGrid (void) [private]

Compute mimetic stencil approximating at boundary.

1. Collect lambda values.
2. Compute alpha values.
3. Compute the mimetic boundary approximations.

Definition at line 1241 of file mtk_div_1d.cc.

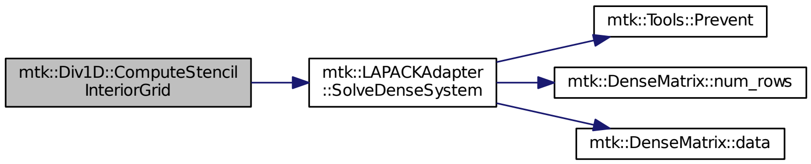
16.3.3.6 bool mtk::Div1D::ComputeStencilInteriorGrid (void) [private]

Compute the stencil approximating the interior of the staggered grid.

1. Create vector for interior spatial coordinates.
2. Create Vandermonde matrix (using interior coordinates as generator).
3. Create order-selector vector.
4. Solve dense Vandermonde system to attain the interior coefficients.

Definition at line 414 of file mtk_div_1d.cc.

Here is the call graph for this function:



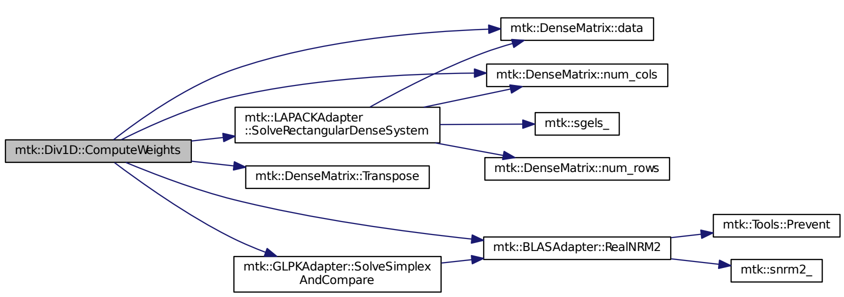
16.3.3.7 bool mtk::Div1D::ComputeWeights (void) [private]

Compute the set of mimetic weights to impose the mimetic condition.

1. Construct the ■ matrix.
2. Use interior stencil to build proper RHS vector $\mathbf{h}$.
3. Get weights (as **CRSA**): ■$\mathbf{q} = \mathbf{h}$.
4. If required order is greater than critical order, start the **CBSA**.
5. Create ■ matrix from ■.
6. Prepare constraint vector as in the CBSA: ■.
7. Brute force search through all the rows of the Φ matrix.
8. Apply solution found from brute force search.

Definition at line 911 of file mtk_div_1d.cc.

Here is the call graph for this function:



16.3.3.8 bool mtk::Div1D::ConstructDiv1D (int *order_accuracy* = kDefaultOrderAccuracy, mtk::Real *mimetic_threshold* = kDefaultMimeticThreshold)

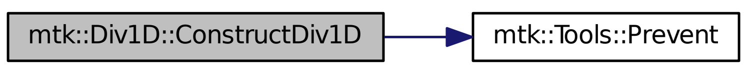
Returns

Success of the construction.

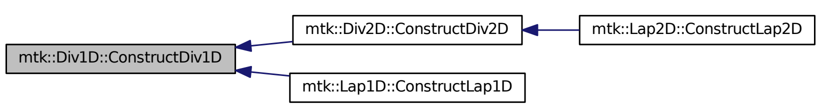
1. Compute stencil for the interior cells.
2. Compute a rational basis for the null-space for the first matrix.
3. Compute preliminary approximation (non-mimetic) on the boundaries.
4. Compute quadrature weights to impose the mimetic conditions.
5. Compute real approximation (mimetic) on the boundaries.
6. Assemble operator.

Definition at line 176 of file mtk_div_1d.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



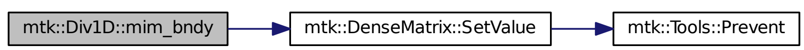
16.3.3.9 mtk::DenseMatrix mtk::Div1D::mim_bndy ( ) const

Returns

Collection of mimetic approximations at the boundary.

Definition at line 335 of file mtk_div_1d.cc.

Here is the call graph for this function:



16.3.3.10 int mtk::Div1D::num_bndy_coeffs ( ) const

Returns

How many coefficients are approximating at the boundary.

Definition at line 315 of file mtk_div_1d.cc.

16.3.3.11 mtk::DenseMatrix mtk::Div1D::ReturnAsDenseMatrix (const UniStgGrid1D & *grid*) const

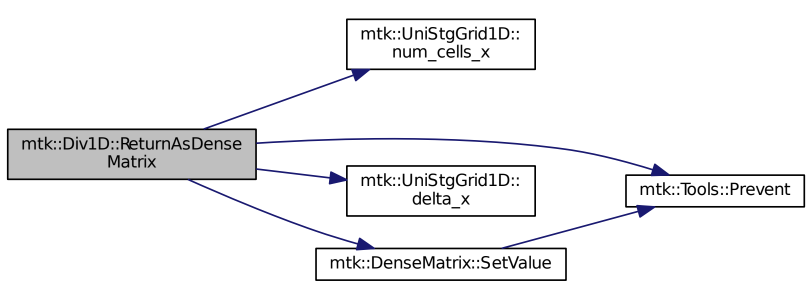
Returns

The operator as a dense matrix.

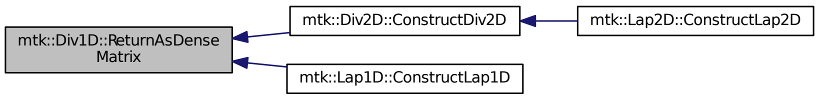
1. Insert mimetic boundary at the west.
2. Insert coefficients for the interior of the grid.
3. Impose center-skew symmetry by permuting the mimetic boundaries.

Definition at line 350 of file mtk_div_1d.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.3.3.12 mtk::Real * mtk::Div1D::weights_cbs (void) const

Returns

Collection of weights as computed by the CBSA.

Definition at line 330 of file mtk_div_1d.cc.

16.3.3.13 mtk::Real * mtk::Div1D::weights_crs (void) const

Returns

Collection of weights as computed by the CRSA.

Definition at line 325 of file mtk_div_1d.cc.

16.3.4 Friends And Related Function Documentation

16.3.4.1 std::ostream& operator<< (std::ostream & *stream*, mtk::Div1D & *in*) [friend]

1. Print order of accuracy.
2. Print approximating coefficients for the interior.
3. Print mimetic weights.
4. Print mimetic approximations at the boundary.

Definition at line 79 of file mtk_div_1d.cc.

16.3.5 Member Data Documentation

16.3.5.1 Real* mtk::Div1D::coeffs_interior_ [private]

Definition at line 202 of file mtk_div_1d.h.

16.3.5.2 int mtk::Div1D::dim_null_ [private]

Definition at line 194 of file mtk_div_1d.h.

16.3.5.3 Real* mtk::Div1D::divergence_ [private]

Definition at line 207 of file mtk_div_1d.h.

16.3.5.4 int mtk::Div1D::divergence_length_ [private]

Definition at line 196 of file mtk_div_1d.h.

16.3.5.5 Real* mtk::Div1D::mim_bndy_ [private]

Definition at line 206 of file mtk_div_1d.h.

16.3.5.6 Real mtk::Div1D::mimetic_threshold_ [private]

Definition at line 209 of file mtk_div_1d.h.

16.3.5.7 int mtk::Div1D::minrow_ [private]

Definition at line 197 of file mtk_div_1d.h.

16.3.5.8 int mtk::Div1D::num_bndy_coeffs_ [private]

Definition at line 195 of file mtk_div_1d.h.

16.3.5.9 int mtk::Div1D::order_accuracy_ [private]

Definition at line 193 of file mtk_div_1d.h.

16.3.5.10 Real* mtk::Div1D::prem_apps_ [private]

Definition at line 203 of file mtk_div_1d.h.

16.3.5.11 DenseMatrix mtk::Div1D::rat_basis_null_space_ [private]

Definition at line 200 of file mtk_div_1d.h.

16.3.5.12 int mtk::Div1D::row_ [private]

Definition at line 198 of file mtk_div_1d.h.

16.3.5.13 Real* mtk::Div1D::weights_cbs_ [private]

Definition at line 205 of file mtk_div_1d.h.

16.3.5.14 Real* mtk::Div1D::weights_crs_ [private]

Definition at line 204 of file mtk_div_1d.h.

The documentation for this class was generated from the following files:

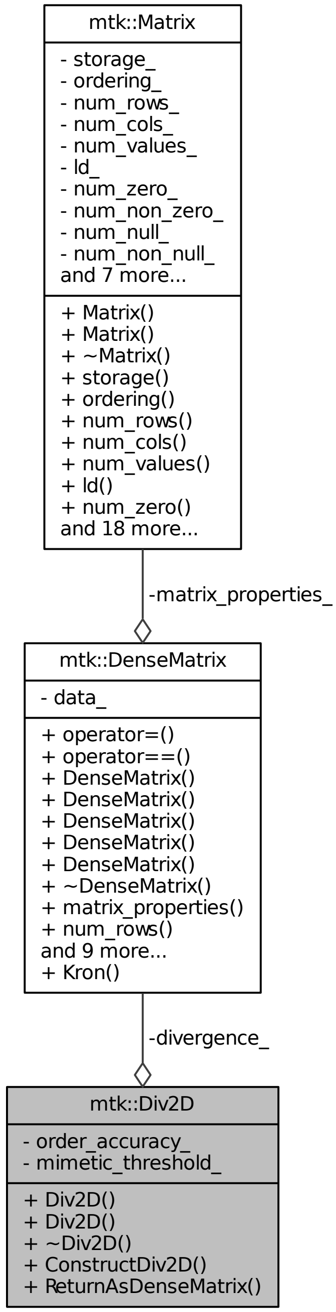
- include/mtk_div_1d.h
- src/mtk_div_1d.cc

16.4 mtk::Div2D Class Reference

Implements a 2D mimetic divergence operator.

`#include <mtk_div_2d.h>`

Collaboration diagram for mtk::Div2D:



Public Member Functions

- Div2D ()

Default constructor.

- Div2D (const Div2D &div)

  Copy constructor.
- ∼Div2D ()

  Destructor.
- bool ConstructDiv2D (const UniStgGrid2D &grid, int order_accuracy=kDefaultOrderAccuracy, Real mimetic_↩ threshold=kDefaultMimeticThreshold)

  Factory method implementing the CBS Algorithm to build operator.
- DenseMatrix ReturnAsDenseMatrix () const

  Return the operator as a dense matrix.

Private Attributes

- DenseMatrix divergence_

  Actual operator.
- int order_accuracy_

  Order of accuracy.
- Real mimetic_threshold_

  Mimetic Threshold.

16.4.1 Detailed Description

This class implements a 2D divergence operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (CBSA).

Definition at line 76 of file mtk_div_2d.h.

16.4.2 Constructor & Destructor Documentation

16.4.2.1 mtk::Div2D::Div2D ( )

Definition at line 69 of file mtk_div_2d.cc.

16.4.2.2 mtk::Div2D::Div2D (const Div2D & *div*)

Parameters

in	*div*	Given divergence.

Definition at line 73 of file mtk_div_2d.cc.

16.4.2.3 mtk::Div2D::∼Div2D ( )

Definition at line 77 of file mtk_div_2d.cc.

16.4.3 Member Function Documentation

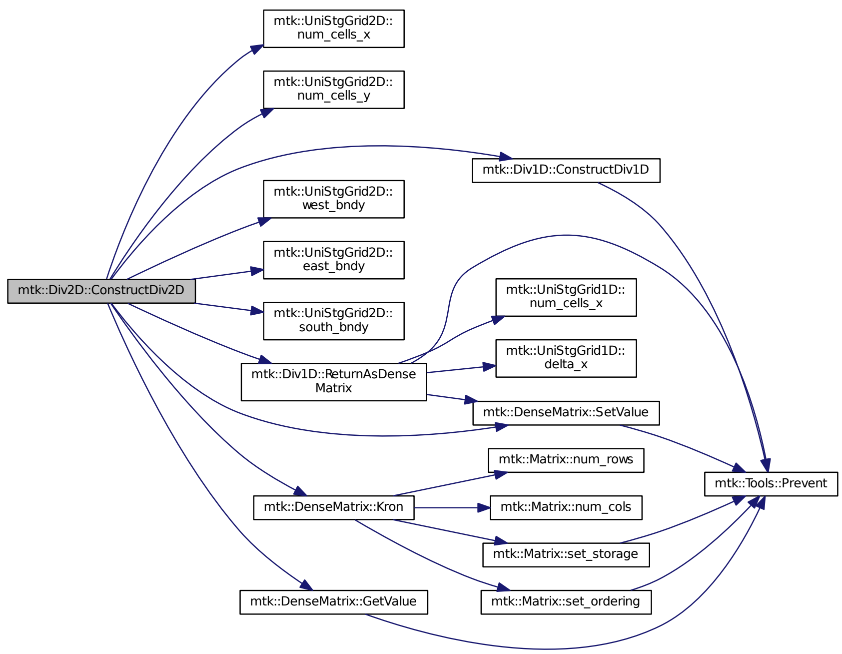
16.4.3.1 bool mtk::Div2D::ConstructDiv2D (const UniStgGrid2D & *grid*, int *order_accuracy* = kDefaultOrderAccuracy, mtk::Real *mimetic_threshold* = kDefaultMimeticThreshold)

Returns

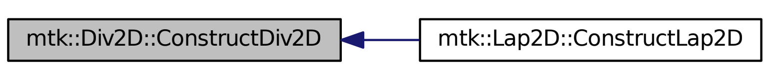
Success of the construction.

Definition at line 79 of file mtk_div_2d.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



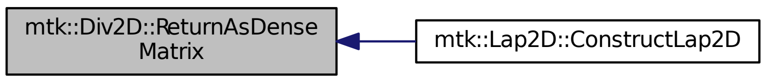
16.4.3.2 mtk::DenseMatrix mtk::Div2D::ReturnAsDenseMatrix ( ) const

Returns

The operator as a dense matrix.

Definition at line 147 of file mtk_div_2d.cc.

Here is the caller graph for this function:



16.4.4 Member Data Documentation

16.4.4.1 DenseMatrix mtk::Div2D::divergence_ [private]

Definition at line 108 of file mtk_div_2d.h.

16.4.4.2 Real mtk::Div2D::mimetic_threshold_ [private]

Definition at line 112 of file mtk_div_2d.h.

16.4.4.3 int mtk::Div2D::order_accuracy_ [private]

Definition at line 110 of file mtk_div_2d.h.

The documentation for this class was generated from the following files:

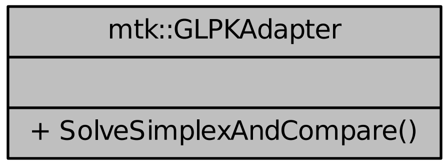
- include/mtk_div_2d.h
- src/mtk_div_2d.cc

16.5 mtk::GLPKAdapter Class Reference

Adapter class for the GLPK API.

`#include <mtk_glpk_adapter.h>`

Collaboration diagram for mtk::GLPKAdapter:



Static Public Member Functions

- static mtk::Real SolveSimplexAndCompare (mtk::Real ∗A, int nrows, int ncols, int kk, mtk::Real ∗hh, mtk::Real ∗qq, int robjective, mtk::Real mimetic_tol, int copy)

  Solves a CLO problem and compares the solution to a reference solution.

16.5.1 Detailed Description

This class contains a collection of static classes, that posses direct access to the underlying structure of the matrices, thus allowing programmers to exploit some of the numerical methods implemented in the GLPK.

The **GLPK (GNU Linear Programming Kit)** package is intended for solving large-scale linear programming (LP), mixed integer programming (MIP), and other related problems. It is a set of routines written in ANSI C and organized in the form of a callable library.

Warning

We use the GLPK temporarily in order to test the CBSA, but it will be removed due to potential licensing issues.

See also

`http://www.gnu.org/software/glpk/`

Todo Rescind from the GLPK as the numerical core for CLO problems.

Definition at line 101 of file mtk_glpk_adapter.h.

16.5.2 Member Function Documentation

16.5.2.1 mtk::Real mtk::GLPKAdapter::SolveSimplexAndCompare (mtk::Real ∗ *A,* int *nrows,* int *ncols,* int *kk,* mtk::Real ∗ *hh,* mtk::Real ∗ *qq,* int *robjective,* mtk::Real *mimetic_tol,* int *copy*) `[static]`

This routine is the pivot of the CBSA. It solves a Constrained Linear Optimization (CLO) problem, and it compares the attained solution to a given reference solution. This comparison is done computing the norm-2 relative error.

Parameters

`in`	*alpha*	First scalar.
`in`	*AA*	Given matrix.
`in`	*xx*	First vector.
`in`	*beta*	Second scalar.
`in`	*beta*	Second scalar.
`in,out`	*yy*	Second vector (output).
`in`	*xx*	First vector.
`in`	*beta*	Second scalar.
`in`	*beta*	Second scalar.

Returns

Relative error computed between attained solution and provided ref.

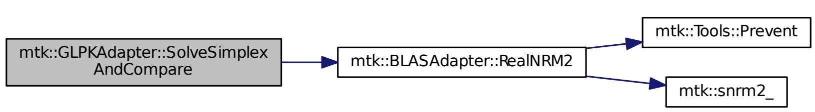
Warning

GLPK indexes in [1,n], so we must get the extra space needed.

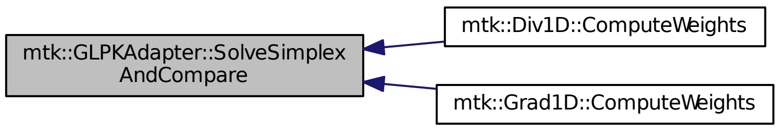
1. Memory allocation.
2. Fill the problem.
3. Copy the row to the vector objective.
4. Forming the RHS.
5. Setting up the objective function.
6. Setting up constraints.
7. Copy the matrix minus the row objective to the glpk problem.
8. Solve problem.

Definition at line 76 of file mtk_glpk_adapter.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



The documentation for this class was generated from the following files:

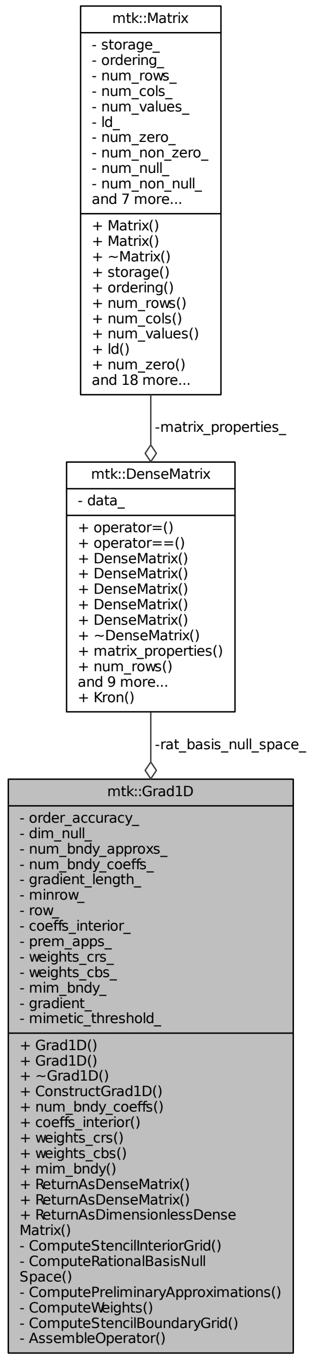
- include/mtk_glpk_adapter.h
- src/mtk_glpk_adapter.cc

16.6 mtk::Grad1D Class Reference

Implements a 1D mimetic gradient operator.

`#include <mtk_grad_1d.h>`

Collaboration diagram for mtk::Grad1D:



Public Member Functions

- Grad1D ()

Default constructor.

- Grad1D (const Grad1D &grad)

  Copy constructor.

- ∼Grad1D ()

  Destructor.

- bool ConstructGrad1D (int order_accuracy=kDefaultOrderAccuracy, Real mimetic_threshold=kDefaultMimetic←Threshold)

  Factory method implementing the CBS Algorithm to build operator.

- int num_bndy_coeffs () const

  Returns how many coefficients are approximating at the boundary.

- Real ∗ coeffs_interior () const

  Returns coefficients for the interior of the grid.

- Real ∗ weights_crs (void) const

  Returns collection of weights as computed by the CRSA.

- Real ∗ weights_cbs (void) const

  Returns collection of weights as computed by the CBSA.

- DenseMatrix mim_bndy () const

  Return collection of mimetic approximations at the boundary.

- DenseMatrix ReturnAsDenseMatrix (Real west, Real east, int num_cells_x) const

  Returns the operator as a dense matrix.

- DenseMatrix ReturnAsDenseMatrix (const UniStgGrid1D &grid) const

  Returns the operator as a dense matrix.

- DenseMatrix ReturnAsDimensionlessDenseMatrix (int num_cells_x) const

  Returns the operator as a dimensionless dense matrix.

Private Member Functions

- bool ComputeStencilInteriorGrid (void)

  Stage 1 of the CBS Algorithm.

- bool ComputeRationalBasisNullSpace (void)

  Stage 2.1 of the CBS Algorithm.

- bool ComputePreliminaryApproximations (void)

  Stage 2.2 of the CBS Algorithm.

- bool ComputeWeights (void)

  Stage 2.3 of the CBS Algorithm.

- bool ComputeStencilBoundaryGrid (void)

  Stage 2.4 of the CBS Algorithm.

- bool AssembleOperator (void)

  Stage 3 of the CBS Algorithm.

Private Attributes

- int order_accuracy_

  Order of numerical accuracy of the operator.

- int dim_null_

  Dim. null-space for boundary approximations.

- int num_bndy_approxs_

Req. approximations at and near the boundary.
- int num_bndy_coeffs_

  Req. coeffs. per bndy pt. uni. order accuracy.
- int gradient_length_

  Length of the output array.
- int minrow_

  Row from the optimizer with the minimum rel. nor.
- int row_

  Row currently processed by the optimizer.
- DenseMatrix rat_basis_null_space_

  Rational b. null-space w. bndy.
- Real ∗ coeffs_interior_

  Interior stencil.
- Real ∗ prem_apps_

  2D array of boundary preliminary approximations.
- Real ∗ weights_crs_

  Array containing weights from CRSA.
- Real ∗ weights_cbs_

  Array containing weights from CBSA.
- Real ∗ mim_bndy_

  Array containing mimetic boundary approximations.
- Real ∗ gradient_

  Output array containing the operator and weights.
- Real mimetic_threshold_

  < Mimetic threshold.

Friends

- std::ostream & operator<< (std::ostream &stream, Grad1D &in)

  Output stream operator for printing.

16.6.1 Detailed Description

This class implements a 1D gradient operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (C↩BSA).

Definition at line 81 of file mtk_grad_1d.h.

16.6.2 Constructor & Destructor Documentation

16.6.2.1 mtk::Grad1D::Grad1D ( )

Definition at line 129 of file mtk_grad_1d.cc.

16.6.2.2 mtk::Grad1D::Grad1D (const Grad1D & *grad*)

Parameters

in	*div*	Given divergence.

Definition at line 145 of file mtk_grad_1d.cc.

16.6.2.3 mtk::Grad1D::∼Grad1D ( )

Definition at line 161 of file mtk_grad_1d.cc.

16.6.3 Member Function Documentation

16.6.3.1 bool mtk::Grad1D::AssembleOperator (void) [private]

Construct the output array with the operator and its weights.

1. The first entry of the array will contain the order of accuracy.
2. The second entry of the array will contain the collection of approximating coefficients for the interior of the grid.
3. The third entry will contain the collection of weights.
4. The next dim_null + 1 entries will contain the collections of approximating coefficients for the west boundary of the grid.

Definition at line 1499 of file mtk_grad_1d.cc.

16.6.3.2 mtk::Real ∗ mtk::Grad1D::coeffs_interior ( ) const

Returns

Coefficients for the interior of the grid.

Definition at line 326 of file mtk_grad_1d.cc.

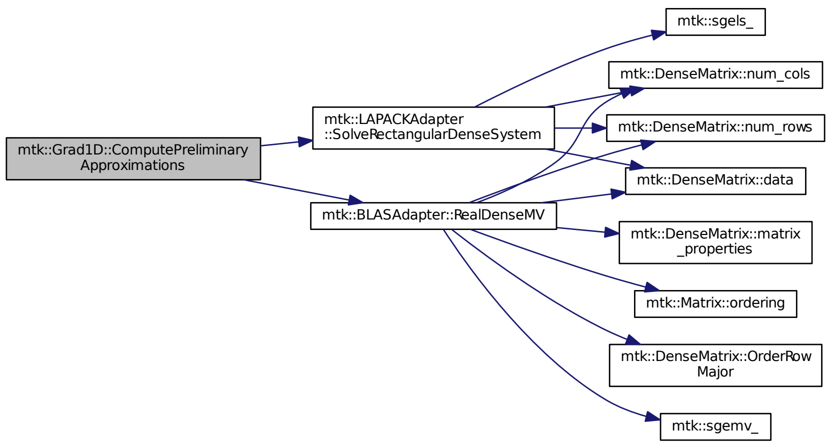
16.6.3.3 bool mtk::Grad1D::ComputePreliminaryApproximations (void) [private]

Compute the set of preliminary approximations on the boundary neighborhood.

1. Create generator vector for the first approximation.
2. Compute the dim_null near-the-boundary columns of the pi matrix.
3. Create the Vandermonde matrix for this iteration.
4. New order-selector vector (gets re-written with LAPACK solutions).
5. Solving TT∗rr = ob yields the columns rr of the kk matrix.
6. Scale the kk matrix to make it a rational basis for null-space.
7. Extract the last dim_null values of the pre-scaled ob.
8. Once we posses the bottom elements, we proceed with the scaling.

Definition at line 831 of file mtk_grad_1d.cc.

Here is the call graph for this function:



16.6.3.4 bool mtk::Grad1D::ComputeRationalBasisNullSpace (void) [private]

Compute a rational basis for the null-space of the Vandermonde matrix approximating at the west boundary.

1. Create generator vector for the first approximation.

2. Create Vandermonde matrix.

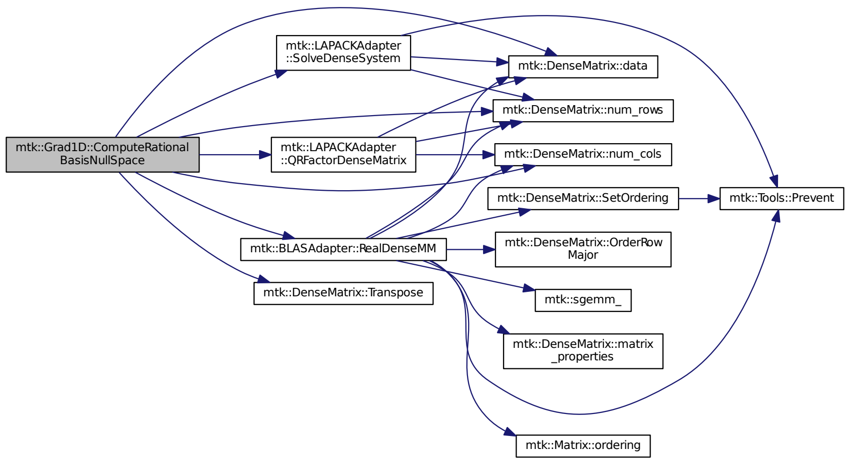
3. QR-factorize the Vandermonde matrix.

4. Extract the basis for the null-space from Q matrix.

5. Scale null-space to make it rational.

Definition at line 648 of file mtk_grad_1d.cc.

Here is the call graph for this function:



16.6.3.5 bool mtk::Grad1D::ComputeStencilBoundaryGrid (void) [private]

Compute mimetic stencil approximating at boundary.

1. Collect lambda values.
2. Compute alpha values.
3. Compute the mimetic boundary approximations.

Definition at line 1393 of file mtk_grad_1d.cc.

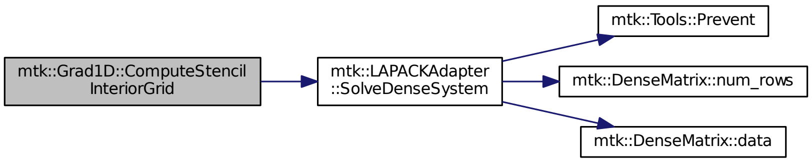
16.6.3.6 bool mtk::Grad1D::ComputeStencilInteriorGrid (void) [private]

Compute the stencil approximating the interior of the staggered grid.

1. Create vector for interior spatial coordinates.
2. Create Vandermonde matrix (using interior coordinates as generator).
3. Create order-selector vector.
4. Solve dense Vandermonde system to attain the interior coefficients.

Definition at line 551 of file mtk_grad_1d.cc.

Here is the call graph for this function:



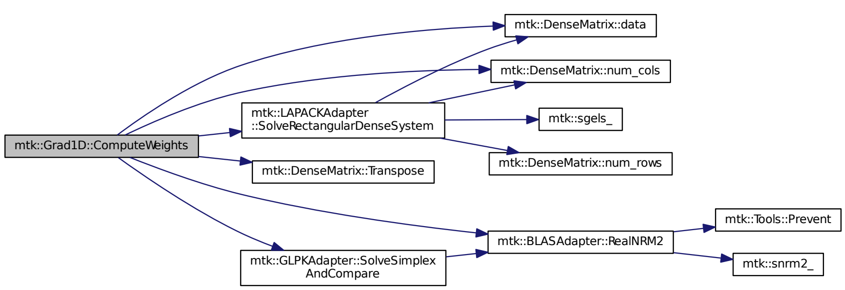
16.6.3.7 bool mtk::Grad1D::ComputeWeights (void) [private]

Compute the set of mimetic weights to impose the mimetic condition.

1. Construct the ■ matrix.
2. Use interior stencil to build proper RHS vector $\mathbf{h}$.
3. Get weights (as **CRSA**): ■$\mathbf{q} = \mathbf{h}$.
4. If required order is greater than critical order, start the **CBSA**.
5. Create ■ matrix from ■.
6. Prepare constraint vector as in the CBSA: ■.
7. Brute force search through all the rows of the Φ matrix.
8. Apply solution found from brute force search.

Definition at line 1052 of file mtk_grad_1d.cc.

Here is the call graph for this function:



16.6.3.8 bool mtk::Grad1D::ConstructGrad1D (int *order_accuracy* = kDefaultOrderAccuracy, Real *mimetic_threshold* = kDefaultMimeticThreshold)

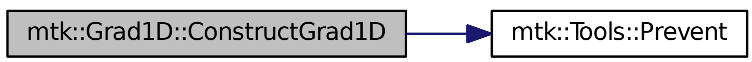
Returns

Success of the solution.

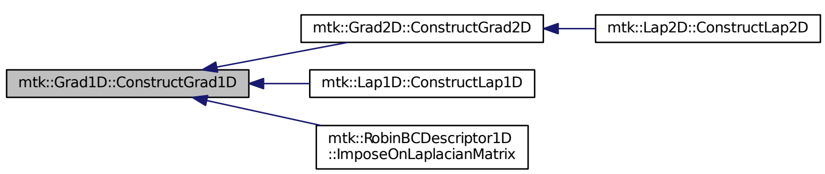
1. Compute stencil for the interior cells.
2. Compute a rational null-space from the first matrix transposed.
3. Compute preliminary approximation (non-mimetic) on the boundaries.
4. Compute quadrature weights to impose the mimetic conditions.
5. Compute real approximation (mimetic) on the boundaries.
6. Assemble operator.

Definition at line 182 of file mtk_grad_1d.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



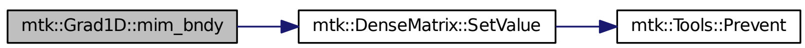
16.6.3.9 mtk::DenseMatrix mtk::Grad1D::mim_bndy ( ) const

Returns

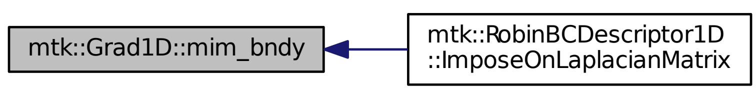
Collection of mimetic approximations at the boundary.

Definition at line 341 of file mtk_grad_1d.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.6.3.10 int mtk::Grad1D::num_bndy_coeffs ( ) const

Returns

How many coefficients are approximating at the boundary.

Definition at line 321 of file mtk_grad_1d.cc.

16.6.3.11 mtk::DenseMatrix mtk::Grad1D::ReturnAsDenseMatrix (mtk::Real *west*, mtk::Real *east*, int *num_cells_x*) const

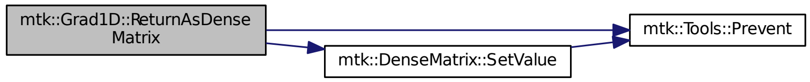
Returns

The operator as a dense matrix.

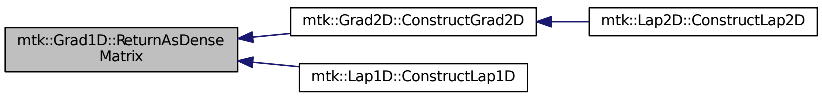
1. Insert mimetic boundary at the west.
2. Insert coefficients for the interior of the grid.
3. Impose center-skew symmetry by permuting the mimetic boundaries.

Definition at line 356 of file mtk_grad_1d.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.6.3.12 mtk::DenseMatrix mtk::Grad1D::ReturnAsDenseMatrix (const UniStgGrid1D & *grid*) const

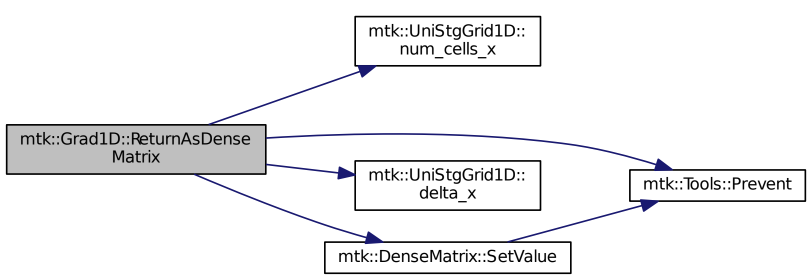
Returns

The operator as a dense matrix.

1. Insert mimetic boundary at the west.
2. Insert coefficients for the interior of the grid.
3. Impose center-skew symmetry by permuting the mimetic boundaries.

Definition at line 425 of file mtk_grad_1d.cc.

Here is the call graph for this function:



16.6.3.13 mtk::DenseMatrix mtk::Grad1D::ReturnAsDimensionlessDenseMatrix (int *num_cells_x*) const

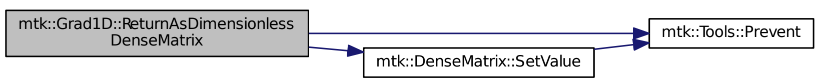
Returns

The operator as a dimensionless dense matrix.

1. Insert mimetic boundary at the west.
2. Insert coefficients for the interior of the grid.
3. Impose center-skew symmetry by permuting the mimetic boundaries.

Definition at line 489 of file mtk_grad_1d.cc.

Here is the call graph for this function:



16.6.3.14 mtk::Real * mtk::Grad1D::weights_cbs (void) const

Returns

Collection of weights as computed by the CBSA.

Definition at line 336 of file mtk_grad_1d.cc.

16.6.3.15 mtk::Real * mtk::Grad1D::weights_crs (void) const

Returns

Success of the solution.

Definition at line 331 of file mtk_grad_1d.cc.

16.6.4 Friends And Related Function Documentation

16.6.4.1 std::ostream& operator<< (std::ostream & *stream*, mtk::Grad1D & *in*) [friend]

1. Print order of accuracy.
2. Print approximating coefficients for the interior.
3. Print mimetic weights.
4. Print mimetic approximations at the boundary.

Definition at line 79 of file mtk_grad_1d.cc.

16.6.5 Member Data Documentation

16.6.5.1 Real* mtk::Grad1D::coeffs_interior_ [private]

Definition at line 217 of file mtk_grad_1d.h.

16.6.5.2 int mtk::Grad1D::dim_null_ [private]

Definition at line 208 of file mtk_grad_1d.h.

16.6.5.3 Real* mtk::Grad1D::gradient_ [private]

Definition at line 222 of file mtk_grad_1d.h.

16.6.5.4 int mtk::Grad1D::gradient_length_ [private]

Definition at line 211 of file mtk_grad_1d.h.

16.6.5.5 Real* mtk::Grad1D::mim_bndy_ [private]

Definition at line 221 of file mtk_grad_1d.h.

16.6.5.6 Real mtk::Grad1D::mimetic_threshold_ [private]

Definition at line 224 of file mtk_grad_1d.h.

16.6.5.7 int mtk::Grad1D::minrow_ [private]

Definition at line 212 of file mtk_grad_1d.h.

16.6.5.8 int mtk::Grad1D::num_bndy_approxs_ [private]

Definition at line 209 of file mtk_grad_1d.h.

16.6.5.9 int mtk::Grad1D::num_bndy_coeffs_ [private]

Definition at line 210 of file mtk_grad_1d.h.

16.6.5.10 int mtk::Grad1D::order_accuracy_ [private]

Definition at line 207 of file mtk_grad_1d.h.

16.6.5.11 Real* mtk::Grad1D::prem_apps_ [private]

Definition at line 218 of file mtk_grad_1d.h.

16.6.5.12 DenseMatrix mtk::Grad1D::rat_basis_null_space_ [private]

Definition at line 215 of file mtk_grad_1d.h.

16.6.5.13 int mtk::Grad1D::row_ [private]

Definition at line 213 of file mtk_grad_1d.h.

16.6.5.14 Real* mtk::Grad1D::weights_cbs_ [private]

Definition at line 220 of file mtk_grad_1d.h.

16.6.5.15 Real* mtk::Grad1D::weights_crs_ [private]

Definition at line 219 of file mtk_grad_1d.h.

The documentation for this class was generated from the following files:

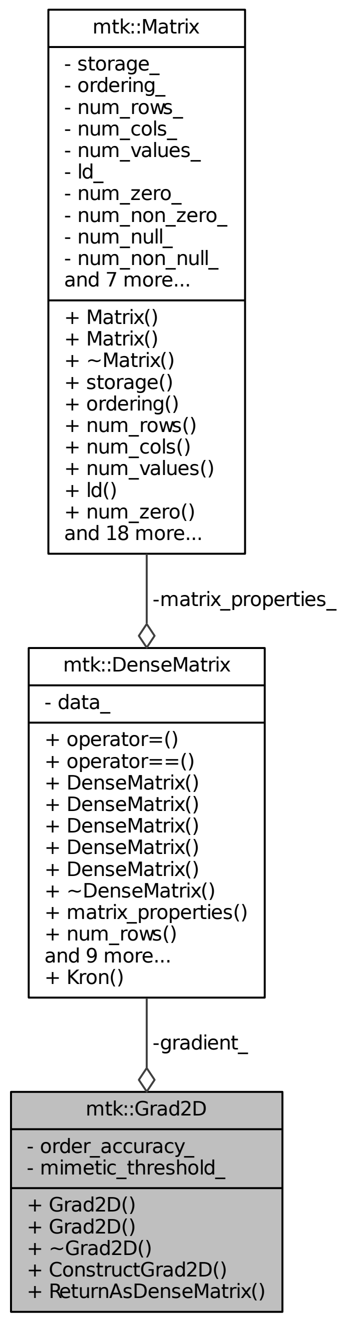
- include/mtk_grad_1d.h
- src/mtk_grad_1d.cc

16.7 mtk::Grad2D Class Reference

Implements a 2D mimetic gradient operator.

`#include <mtk_grad_2d.h>`

Collaboration diagram for mtk::Grad2D:



Public Member Functions

- Grad2D ()

Default constructor.

- Grad2D (const Grad2D &grad)

  Copy constructor.

- ∼Grad2D ()

  Destructor.

- bool ConstructGrad2D (const UniStgGrid2D &grid, int order_accuracy=kDefaultOrderAccuracy, Real mimetic_↩ threshold=kDefaultMimeticThreshold)

  Factory method implementing the CBS Algorithm to build operator.

- DenseMatrix ReturnAsDenseMatrix () const

  Return the operator as a dense matrix.

Private Attributes

- DenseMatrix gradient_

  Actual operator.

- int order_accuracy_

  Order of accuracy.

- Real mimetic_threshold_

  Mimetic Threshold.

16.7.1 Detailed Description

This class implements a 2D gradient operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (C↩ BSA).

Definition at line 76 of file mtk_grad_2d.h.

16.7.2 Constructor & Destructor Documentation

16.7.2.1 mtk::Grad2D::Grad2D ( )

Definition at line 67 of file mtk_grad_2d.cc.

16.7.2.2 mtk::Grad2D::Grad2D (const Grad2D & *grad*)

Parameters

in	*div*	Given divergence.

Definition at line 71 of file mtk_grad_2d.cc.

16.7.2.3 mtk::Grad2D::∼Grad2D ( )

Definition at line 75 of file mtk_grad_2d.cc.

16.7.3 Member Function Documentation

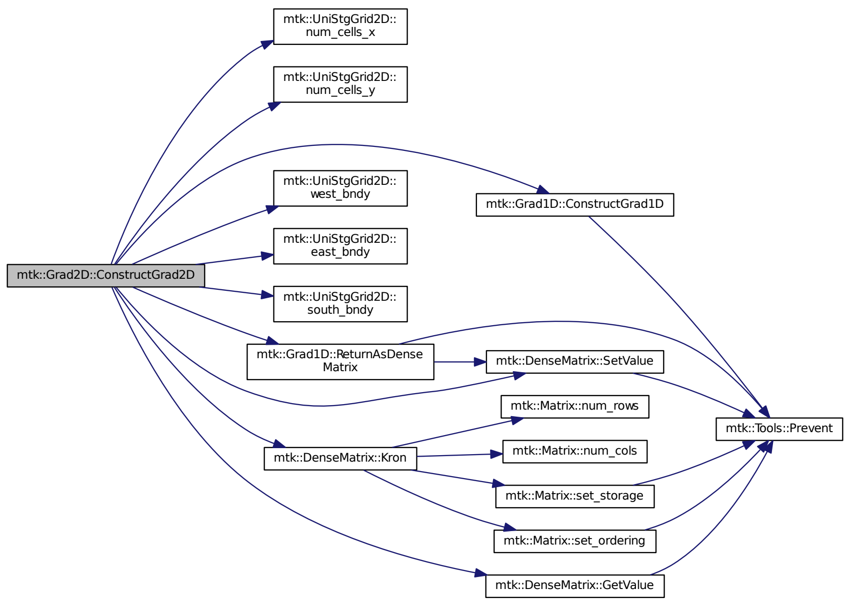
16.7.3.1 bool mtk::Grad2D::ConstructGrad2D (const UniStgGrid2D & *grid*, int *order_accuracy* = kDefaultOrderAccuracy, mtk::Real *mimetic_threshold* = kDefaultMimeticThreshold)

Returns

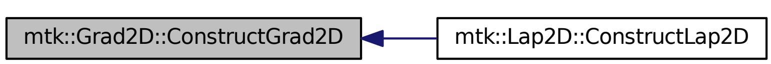
Success of the construction.

Definition at line 77 of file mtk_grad_2d.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



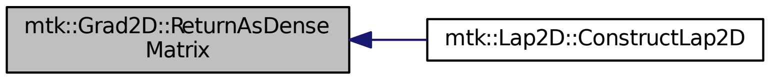
16.7.3.2 mtk::DenseMatrix mtk::Grad2D::ReturnAsDenseMatrix ( ) const

Returns

The operator as a dense matrix.

Definition at line 145 of file mtk_grad_2d.cc.

Here is the caller graph for this function:



16.7.4 Member Data Documentation

16.7.4.1 DenseMatrix mtk::Grad2D::gradient_ [private]

Definition at line 108 of file mtk_grad_2d.h.

16.7.4.2 Real mtk::Grad2D::mimetic_threshold_ [private]

Definition at line 112 of file mtk_grad_2d.h.

16.7.4.3 int mtk::Grad2D::order_accuracy_ [private]

Definition at line 110 of file mtk_grad_2d.h.

The documentation for this class was generated from the following files:

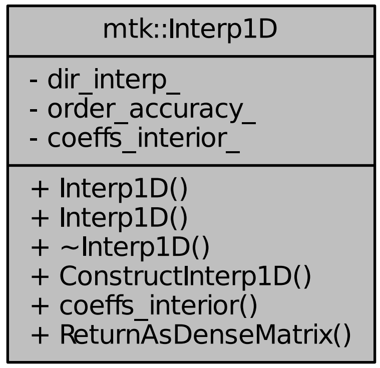
- include/mtk_grad_2d.h
- src/mtk_grad_2d.cc

16.8 mtk::Interp1D Class Reference

Implements a 1D interpolation operator.

`#include <mtk_interp_1d.h>`

Collaboration diagram for mtk::Interp1D:



Public Member Functions

- Interp1D ()

  Default constructor.
- Interp1D (const Interp1D &interp)

  Copy constructor.
- ∼Interp1D ()

  Destructor.
- bool ConstructInterp1D (int order_accuracy=kDefaultOrderAccuracy, mtk::DirInterp dir=SCALAR_TO_VECTOR)

  Factory method to build operator.
- Real ∗ coeffs_interior () const

  Returns coefficients for the interior of the grid.
- DenseMatrix ReturnAsDenseMatrix (const UniStgGrid1D &grid) const

  Returns the operator as a dense matrix.

Private Attributes

- DirInterp dir_interp_

  Direction of interpolation.
- int order_accuracy_

  Order of numerical accuracy of the operator.
- Real ∗ coeffs_interior_

  Interior stencil.

Friends

- std::ostream & operator<< (std::ostream &stream, Interp1D &in)

  Output stream operator for printing.

16.8.1 Detailed Description

This class implements a 1D interpolation operator.

Definition at line 82 of file mtk_interp_1d.h.

16.8.2 Constructor & Destructor Documentation

16.8.2.1 mtk::Interp1D::Interp1D ( )

Definition at line 80 of file mtk_interp_1d.cc.

16.8.2.2 mtk::Interp1D::Interp1D (const **Interp1D** & *interp*)

Parameters

in	*interp*	Given interpolation operator.

Definition at line 85 of file mtk_interp_1d.cc.

16.8.2.3 mtk::Interp1D::∼Interp1D ( )

Definition at line 90 of file mtk_interp_1d.cc.

16.8.3 Member Function Documentation

16.8.3.1 **mtk::Real** ∗ mtk::Interp1D::coeffs_interior ( ) const

Returns

Coefficients for the interior of the grid.

Definition at line 132 of file mtk_interp_1d.cc.

16.8.3.2 bool mtk::Interp1D::ConstructInterp1D (int *order_accuracy* = **kDefaultOrderAccuracy**, **mtk::DirInterp** *dir* = **SCALAR_TO_VECTOR**)

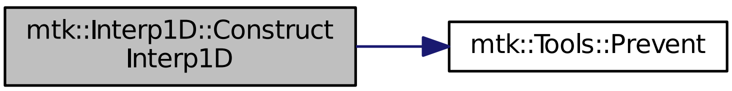
Returns

Success of the solution.

1. Compute stencil for the interior cells.

Definition at line 96 of file mtk_interp_1d.cc.

Here is the call graph for this function:



16.8.3.3 mtk::DenseMatrix mtk::Interp1D::ReturnAsDenseMatrix (const UniStgGrid1D & *grid*) const

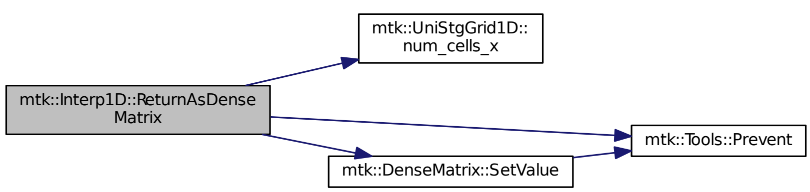
Returns

The operator as a dense matrix.

1. Preserve values at the boundary.
2. Insert coefficients for the interior of the grid.
3. Impose center-skew symmetry by permuting the boundaries.

Definition at line 137 of file mtk_interp_1d.cc.

Here is the call graph for this function:



16.8.4 Friends And Related Function Documentation

16.8.4.1 std::ostream& operator<< (std::ostream & *stream*, mtk::Interp1D & *in*) [friend]

1. Print approximating coefficients for the interior.

Definition at line 66 of file mtk_interp_1d.cc.

16.8.5 Member Data Documentation

16.8.5.1 Real* mtk::Interp1D::coeffs_interior_ [private]

Definition at line 127 of file mtk_interp_1d.h.

16.8.5.2 DirInterp mtk::Interp1D::dir_interp_ [private]

Definition at line 123 of file mtk_interp_1d.h.

16.8.5.3 int mtk::Interp1D::order_accuracy_ [private]

Definition at line 125 of file mtk_interp_1d.h.

The documentation for this class was generated from the following files:

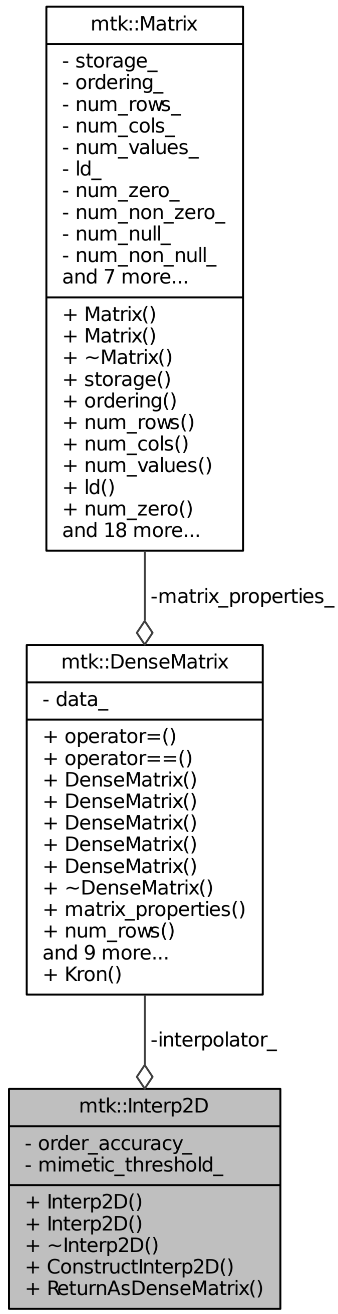
- include/mtk_interp_1d.h
- src/mtk_interp_1d.cc

16.9 mtk::Interp2D Class Reference

Implements a 2D interpolation operator.

`#include <mtk_interp_2d.h>`

Collaboration diagram for mtk::Interp2D:



Public Member Functions

- Interp2D ()

Default constructor.

- Interp2D (const Interp2D &interp)

  Copy constructor.

- ∼Interp2D ()

  Destructor.

- DenseMatrix ConstructInterp2D (const UniStgGrid2D &grid, int order_accuracy=kDefaultOrderAccuracy, Real mimetic_threshold=kDefaultMimeticThreshold)

  Factory method implementing the CBS Algorithm to build operator.

- DenseMatrix ReturnAsDenseMatrix ()

  Return the operator as a dense matrix.

Private Attributes

- DenseMatrix interpolator_

  Actual operator.

- int order_accuracy_

  Order of accuracy.

- Real mimetic_threshold_

  Mimetic Threshold.

16.9.1 Detailed Description

This class implements a 2D interpolation operator.

Definition at line 76 of file mtk_interp_2d.h.

16.9.2 Constructor & Destructor Documentation

16.9.2.1 mtk::Interp2D::Interp2D ( )

16.9.2.2 mtk::Interp2D::Interp2D (const Interp2D & *interp*)

Parameters

in	*lap*	Given Laplacian.

16.9.2.3 mtk::Interp2D::∼Interp2D ( )

16.9.3 Member Function Documentation

16.9.3.1 DenseMatrix mtk::Interp2D::ConstructInterp2D (const UniStgGrid2D & *grid*, int *order_accuracy* = kDefaultOrderAccuracy, Real *mimetic_threshold* = kDefaultMimeticThreshold)

Returns

Success of the construction.

16.9.3.2 DenseMatrix mtk::Interp2D::ReturnAsDenseMatrix ( )

Returns

The operator as a dense matrix.

16.9.4 Member Data Documentation

16.9.4.1 DenseMatrix mtk::Interp2D::interpolator_ [private]

Definition at line 108 of file mtk_interp_2d.h.

16.9.4.2 Real mtk::Interp2D::mimetic_threshold_ [private]

Definition at line 112 of file mtk_interp_2d.h.

16.9.4.3 int mtk::Interp2D::order_accuracy_ [private]

Definition at line 110 of file mtk_interp_2d.h.

The documentation for this class was generated from the following file:

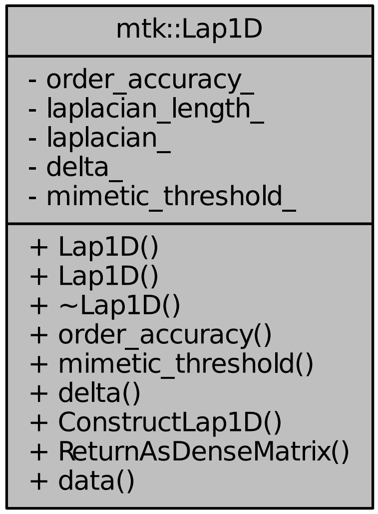
- include/mtk_interp_2d.h

16.10 mtk::Lap1D Class Reference

Implements a 1D mimetic Laplacian operator.

`#include <mtk_lap_1d.h>`

Collaboration diagram for mtk::Lap1D:



Public Member Functions

- Lap1D ()

  Default constructor.
- Lap1D (const Lap1D &lap)

  Copy constructor.
- ∼Lap1D ()

  Destructor.
- int order_accuracy () const

  Order of accuracy of the operator.
- Real mimetic_threshold () const

  Mimetic threshold used in the CBS algorithm to construct this operator.
- Real delta () const

  Value of Δx used be scaled. If 0, then dimensionless.
- bool ConstructLap1D (int order_accuracy=kDefaultOrderAccuracy, Real mimetic_threshold=kDefaultMimeticThreshold)

  Factory method implementing the CBS Algorithm to build operator.
- DenseMatrix ReturnAsDenseMatrix (const UniStgGrid1D &grid) const

  Return the operator as a dense matrix.
- const mtk::Real ∗ data (const UniStgGrid1D &grid) const

  Return the operator as a dense array.

Private Attributes

- int order_accuracy_

  Order of numerical accuracy of the operator.
- int laplacian_length_

  Length of the output array.
- Real * laplacian_

  Output array containing the operator and weights.
- Real delta_

  < If 0.0, then this Laplacian is dimensionless.
- Real mimetic_threshold_

  < Mimetic threshold.

Friends

- std::ostream & operator<< (std::ostream &stream, Lap1D &in)

  Output stream operator for printing.

16.10.1 Detailed Description

This class implements a 1D Laplacian operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (CBSA).

Definition at line 76 of file mtk_lap_1d.h.

16.10.2 Constructor & Destructor Documentation

16.10.2.1 mtk::Lap1D::Lap1D ( )

Definition at line 108 of file mtk_lap_1d.cc.

16.10.2.2 mtk::Lap1D::Lap1D (const Lap1D & *lap*)

Parameters

in	*lap*	Given Laplacian.

16.10.2.3 mtk::Lap1D::∼Lap1D ( )

Definition at line 114 of file mtk_lap_1d.cc.

16.10.3 Member Function Documentation

16.10.3.1 bool mtk::Lap1D::ConstructLap1D (int *order_accuracy* = kDefaultOrderAccuracy, mtk::Real *mimetic_threshold* = kDefaultMimeticThreshold)

Returns

Success of the solution.

1. Create gradient operator using specific values for the Laplacian.
2. Create gradient operator using specific values for the Laplacian.
3. Create both operators as matrices.
4. Multiply both operators: $\breve{\mathbf{L}}^k_x = \breve{\mathbf{D}}^k_x \breve{\mathbf{G}}^k_x$
5. Extract the coefficients from the matrix and store them in the array.

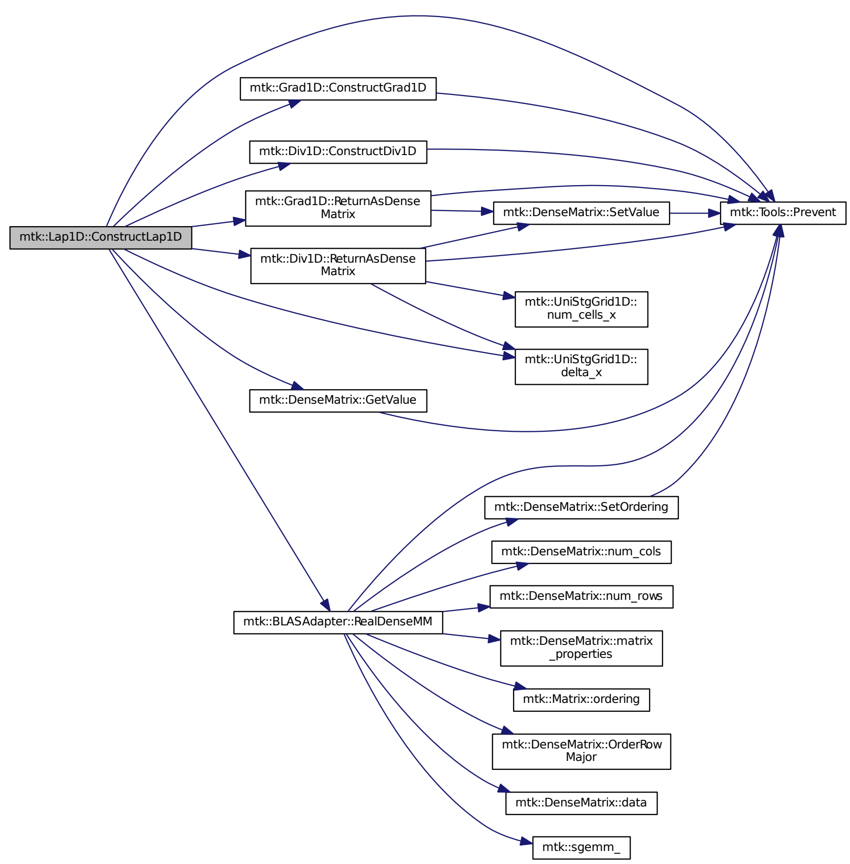
Warning

We do not compute weights for this operator... no need to!

1. The first entry of the array will contain the order of accuracy.
2. The second entry of the array will contain the collection of approximating coefficients for the interior of the grid.
3. We DO NOT have weights in this operator. Copy mimetic bndy coeffs.

Definition at line 135 of file mtk_lap_1d.cc.

Here is the call graph for this function:



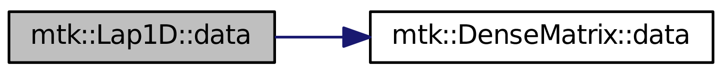
16.10.3.2 const mtk::Real ∗ mtk::Lap1D::data (const UniStgGrid1D & *grid*) const

Returns

The operator as a dense array.

Definition at line 356 of file mtk_lap_1d.cc.

Here is the call graph for this function:



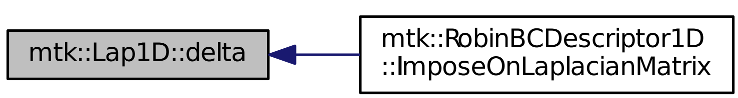
16.10.3.3 mtk::Real mtk::Lap1D::delta ( ) const

Returns

Value of Δx used be scaled. If 0, then dimensionless.

Definition at line 130 of file mtk_lap_1d.cc.

Here is the caller graph for this function:



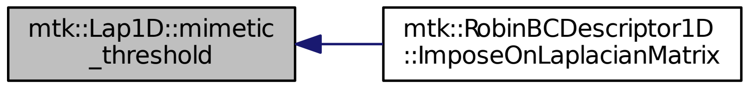
16.10.3.4 mtk::Real mtk::Lap1D::mimetic_threshold ( ) const

Returns

Mimetic threshold used in the CBS algorithm to construct operator.

Definition at line 125 of file mtk_lap_1d.cc.

Here is the caller graph for this function:



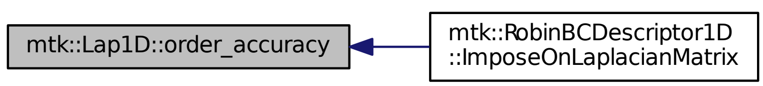
16.10.3.5 int mtk::Lap1D::order_accuracy ( ) const

Returns

Order of accuracy of the operator.

Definition at line 120 of file mtk_lap_1d.cc.

Here is the caller graph for this function:



16.10.3.6 mtk::DenseMatrix mtk::Lap1D::ReturnAsDenseMatrix (const UniStgGrid1D & *grid*) const

Returns

The operator as a dense matrix.

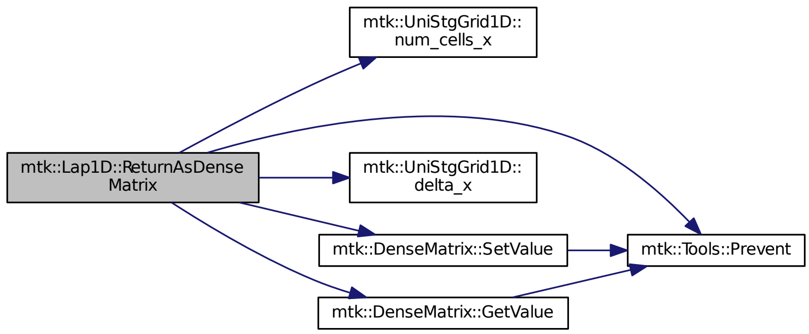
1. Extract mimetic coefficients from the west boundary.
2. Extract interior coefficients.
3. Extract mimetic coefficients from the west boundary to go east.

Note

We could create two matrices of the requested size and multiply them, but that would be inefficient, since we already have the computed coefficients stored. We just have to set them in place, in a matrix of an adequate size, and multiply them times the inverse of the square of the step size, in order for the matrix to actually represent a differential operator.

Definition at line 286 of file mtk_lap_1d.cc.

Here is the call graph for this function:



16.10.4 Friends And Related Function Documentation

16.10.4.1 std::ostream& operator<< (std::ostream & *stream*, mtk::Lap1D & *in*) [friend]

1. Print order of accuracy.
2. Print approximating coefficients for the interior.
3. No weights, thus print the mimetic boundary coefficients.

Definition at line 73 of file mtk_lap_1d.cc.

16.10.5 Member Data Documentation

16.10.5.1 Real mtk::Lap1D::delta_ [mutable], [private]

Definition at line 143 of file mtk_lap_1d.h.

16.10.5.2 Real* mtk::Lap1D::laplacian_ [private]

Definition at line 141 of file mtk_lap_1d.h.

16.10.5.3 int mtk::Lap1D::laplacian_length_ [private]

Definition at line 139 of file mtk_lap_1d.h.

16.10.5.4 Real mtk::Lap1D::mimetic_threshold_ [private]

Definition at line 145 of file mtk_lap_1d.h.

16.10.5.5 int mtk::Lap1D::order_accuracy_ [private]

Definition at line 138 of file mtk_lap_1d.h.

The documentation for this class was generated from the following files:

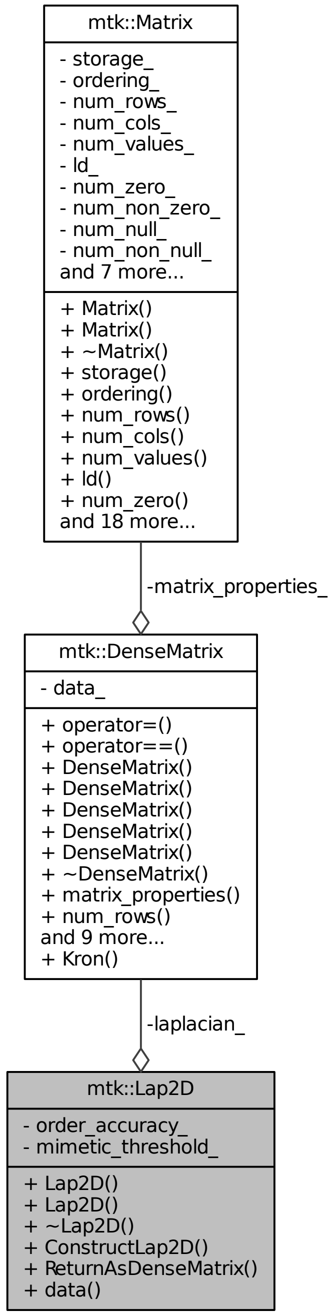
- include/mtk_lap_1d.h
- src/mtk_lap_1d.cc

16.11 mtk::Lap2D Class Reference

Implements a 2D mimetic Laplacian operator.

```
#include <mtk_lap_2d.h>
```

Collaboration diagram for mtk::Lap2D:



Public Member Functions

- Lap2D ()

Default constructor.

- Lap2D (const Lap2D &lap)

  Copy constructor.

- ∼Lap2D ()

  Destructor.

- bool ConstructLap2D (const UniStgGrid2D &grid, int order_accuracy=kDefaultOrderAccuracy, Real mimetic_↩ threshold=kDefaultMimeticThreshold)

  Factory method implementing the CBS Algorithm to build operator.

- DenseMatrix ReturnAsDenseMatrix () const

  Return the operator as a dense matrix.

- Real ∗ data () const

  Return the operator as a dense array.

Private Attributes

- DenseMatrix laplacian_

  Actual operator.

- int order_accuracy_

  Order of accuracy.

- Real mimetic_threshold_

  Mimetic Threshold.

16.11.1 Detailed Description

This class implements a 2D Laplacian operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (CBSA).

Definition at line 76 of file mtk_lap_2d.h.

16.11.2 Constructor & Destructor Documentation

16.11.2.1 mtk::Lap2D::Lap2D ( )

Definition at line 69 of file mtk_lap_2d.cc.

16.11.2.2 mtk::Lap2D::Lap2D (const Lap2D & *lap*)

Parameters

in	*lap*	Given Laplacian.

Definition at line 71 of file mtk_lap_2d.cc.

16.11.2.3 mtk::Lap2D::∼Lap2D ( )

Definition at line 75 of file mtk_lap_2d.cc.

16.11.3 Member Function Documentation

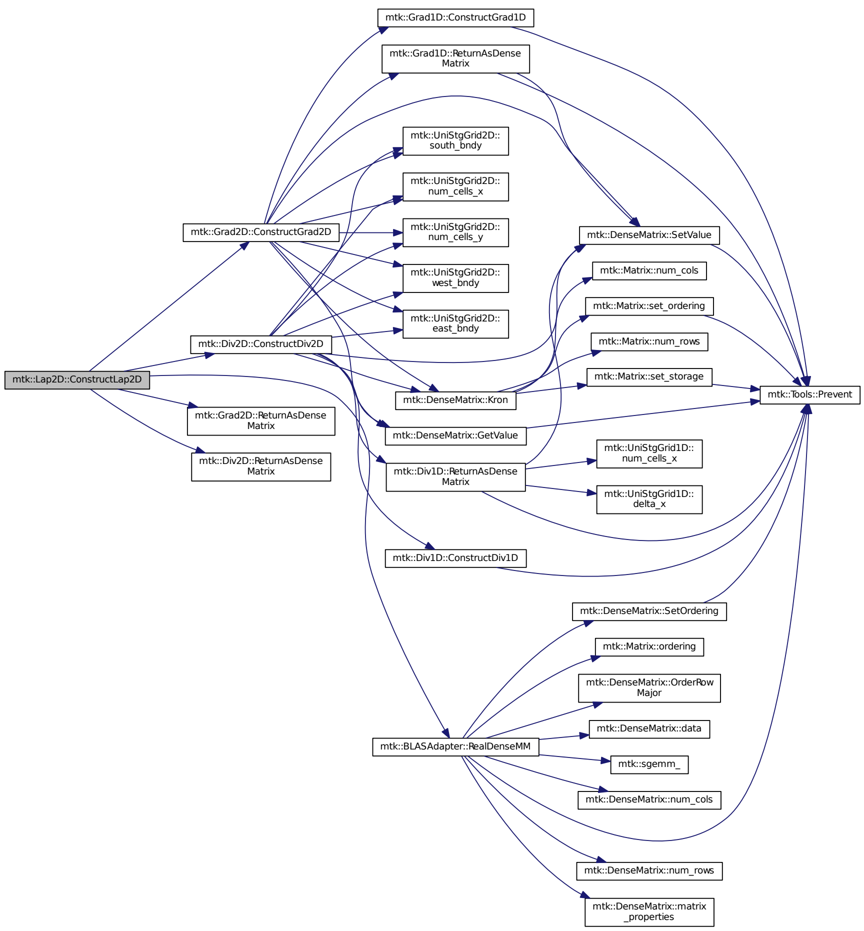
16.11.3.1 bool mtk::Lap2D::ConstructLap2D (const UniStgGrid2D & *grid*, int *order_accuracy* = kDefaultOrderAccuracy, mtk::Real *mimetic_threshold* = kDefaultMimeticThreshold)

Returns

Success of the construction.

Definition at line 77 of file mtk_lap_2d.cc.

Here is the call graph for this function:



16.11.3.2 mtk::Real ∗ mtk::Lap2D::data ( ) const

Returns

The operator as a dense array.

Definition at line 115 of file mtk_lap_2d.cc.

16.11.3.3 mtk::DenseMatrix mtk::Lap2D::ReturnAsDenseMatrix ( ) const

Returns

The operator as a dense matrix.

Definition at line 110 of file mtk_lap_2d.cc.

16.11.4 Member Data Documentation

16.11.4.1 DenseMatrix mtk::Lap2D::laplacian_ `[private]`

Definition at line 115 of file mtk_lap_2d.h.

16.11.4.2 Real mtk::Lap2D::mimetic_threshold_ `[private]`

Definition at line 119 of file mtk_lap_2d.h.

16.11.4.3 int mtk::Lap2D::order_accuracy_ `[private]`

Definition at line 117 of file mtk_lap_2d.h.

The documentation for this class was generated from the following files:

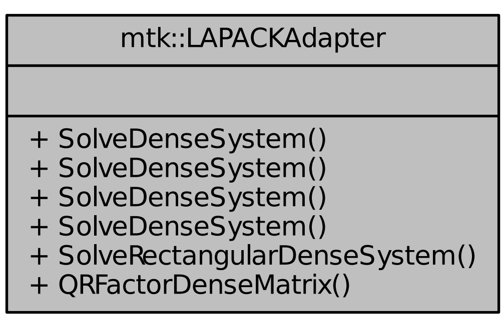
- include/mtk_lap_2d.h
- src/mtk_lap_2d.cc

16.12 mtk::LAPACKAdapter Class Reference

Adapter class for the LAPACK API.

`#include <mtk_lapack_adapter.h>`

Collaboration diagram for mtk::LAPACKAdapter:



Static Public Member Functions

- static int SolveDenseSystem (mtk::DenseMatrix &mm, mtk::Real ∗rhs)

  Solves a dense system of linear equations.
- static int SolveDenseSystem (mtk::DenseMatrix &mm, mtk::DenseMatrix &rr)

  Solves a dense system of linear equations.
- static int SolveDenseSystem (mtk::DenseMatrix &mm, mtk::UniStgGrid1D &rhs)

  Solves a dense system of linear equations.
- static int SolveDenseSystem (mtk::DenseMatrix &mm, mtk::UniStgGrid2D &rhs)

  Solves a dense system of linear equations.
- static int SolveRectangularDenseSystem (const mtk::DenseMatrix &aa, mtk::Real ∗ob_, int ob_ld_)

  Solves overdetermined or underdetermined real linear systems.
- static mtk::DenseMatrix QRFactorDenseMatrix (DenseMatrix &matrix)

  Performs a QR factorization on a dense matrix.

16.12.1 Detailed Description

This class contains a collection of static classes, that posses direct access to the underlying structure of the matrices, thus allowing programmers to exploit the numerical methods implemented in the LAPACK.

The **LAPACK (Linear Algebra PACKage)** is written in Fortran 90 and provides routines for solving systems of simultaneous linear equations, least-squares solutions of linear systems of equations, eigenvalue problems, and singular value problems.

See also

`http://www.netlib.org/lapack/`

Definition at line 93 of file mtk_lapack_adapter.h.

16.12.2 Member Function Documentation

16.12.2.1 mtk::DenseMatrix mtk::LAPACKAdapter::QRFactorDenseMatrix (mtk::DenseMatrix & *aa*) [static]

Adapts the MTK to LAPACK's routine.

Parameters

in,out	*matrix*	Input matrix.

Returns

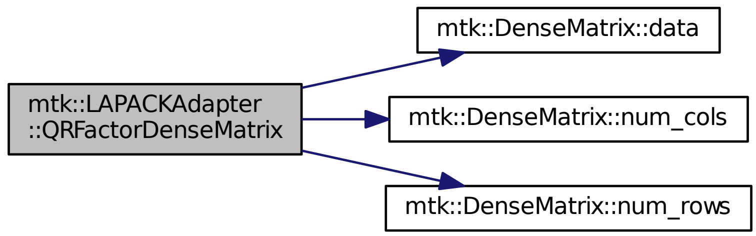
Matrix **Q**.

Exceptions

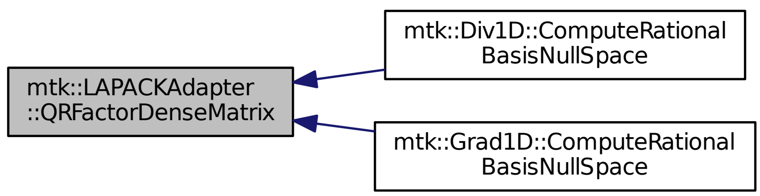
std::bad_alloc	

Definition at line 593 of file mtk_lapack_adapter.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.12.2.2 int mtk::LAPACKAdapter::SolveDenseSystem (**mtk::DenseMatrix** & *mm*, **mtk::Real** ∗ *rhs*) `[static]`

Adapts the MTK to LAPACK's dgesv_ routine.

Parameters

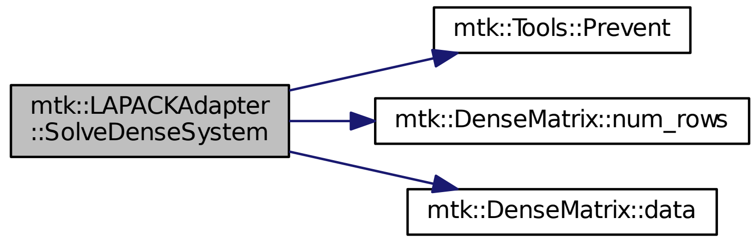
`in`	*matrix*	Input matrix.
`in`	*rhs*	Input right-hand sides vector.

Exceptions

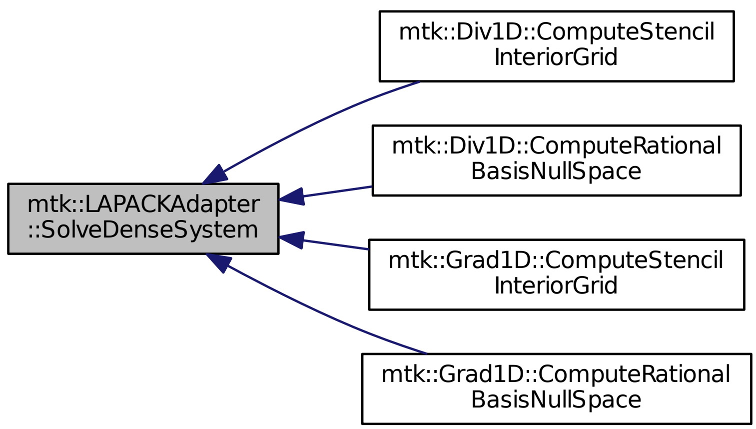
std::bad_alloc	

Definition at line 430 of file mtk_lapack_adapter.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.12.2.3 int mtk::LAPACKAdapter::SolveDenseSystem (**mtk::DenseMatrix** & *mm*, **mtk::DenseMatrix** & *rr*) `[static]`

Adapts the MTK to LAPACK's dgesv_ routine.

Parameters

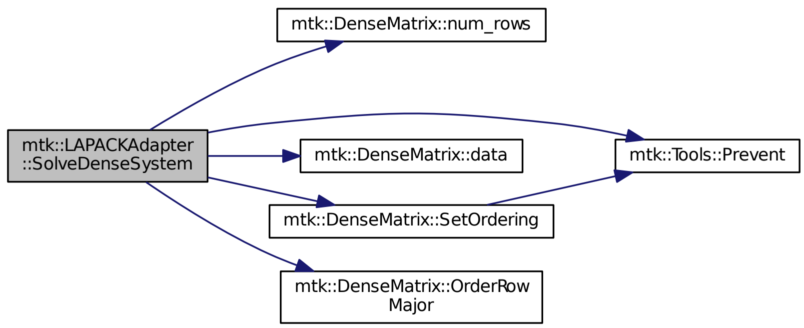
`in`	*matrix*	Input matrix.
`in`	*rr*	Input right-hand sides matrix.

Exceptions

std::bad_alloc	

Definition at line 465 of file mtk_lapack_adapter.cc.

Here is the call graph for this function:



16.12.2.4 int mtk::LAPACKAdapter::SolveDenseSystem (mtk::DenseMatrix & *mm*, mtk::UniStgGrid1D & *rhs*) [static]

Adapts the MTK to LAPACK's dgesv_ routine.

Parameters

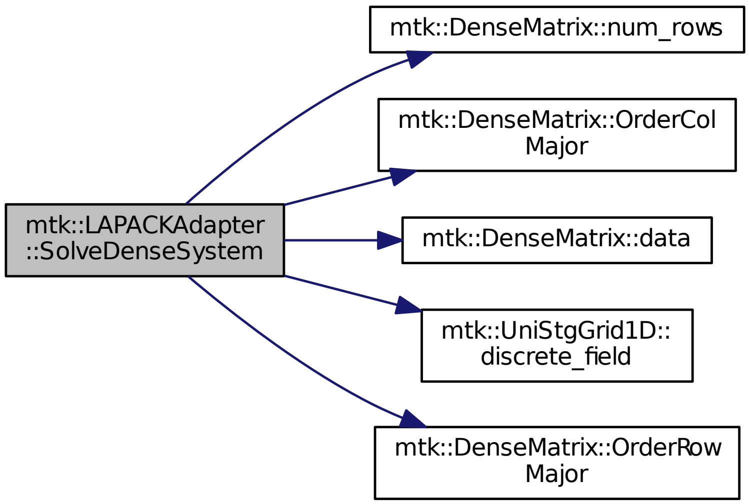
in	*matrix*	Input matrix.
in	*rhs*	Input right-hand side from info on a grid.

Exceptions

std::bad_alloc	

Definition at line 517 of file mtk_lapack_adapter.cc.

Here is the call graph for this function:



16.12.2.5 int mtk::LAPACKAdapter::SolveDenseSystem (mtk::DenseMatrix & *mm*, mtk::UniStgGrid2D & *rhs*) [static]

Adapts the MTK to LAPACK's dgesv_ routine.

Parameters

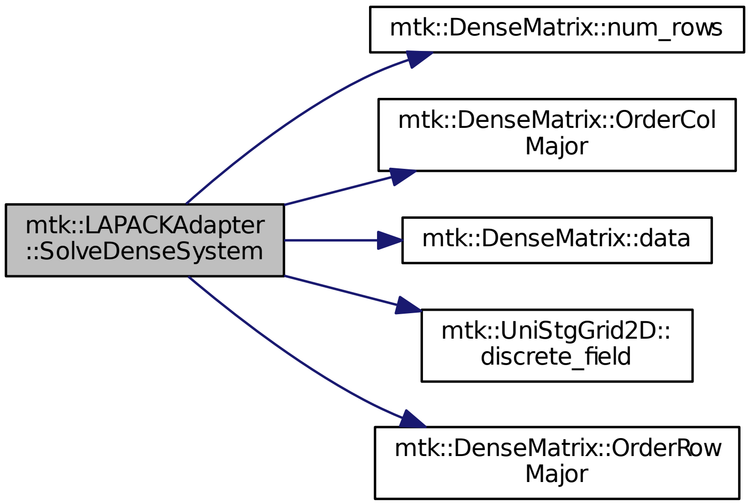
in	*matrix*	Input matrix.
in	*rhs*	Input right-hand side from info on a grid.

Exceptions

std::bad_alloc	

Definition at line 555 of file mtk_lapack_adapter.cc.

Here is the call graph for this function:



16.12.2.6 int mtk::LAPACKAdapter::SolveRectangularDenseSystem (const mtk::DenseMatrix & *aa*, mtk::Real ∗ *ob_*, int *ob_ld_*) [static]

Adapts the MTK to LAPACK's routine.

Parameters

in,out	*matrix*	Input matrix.

Returns

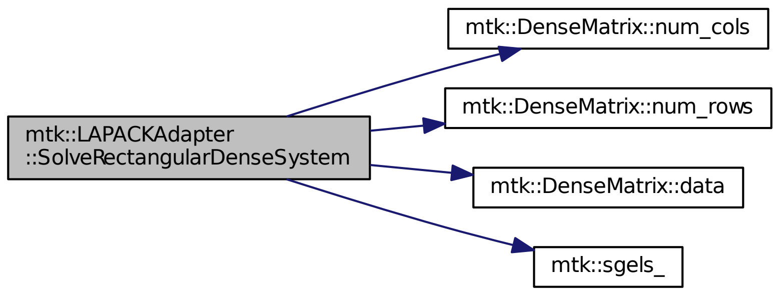
Success of the solution.

Exceptions

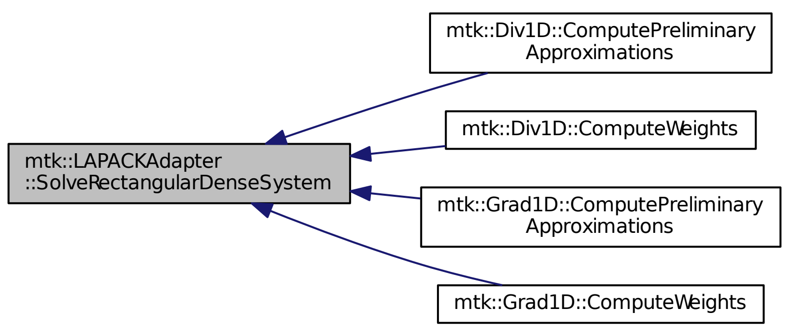
std::bad_alloc	

Definition at line 790 of file mtk_lapack_adapter.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



The documentation for this class was generated from the following files:

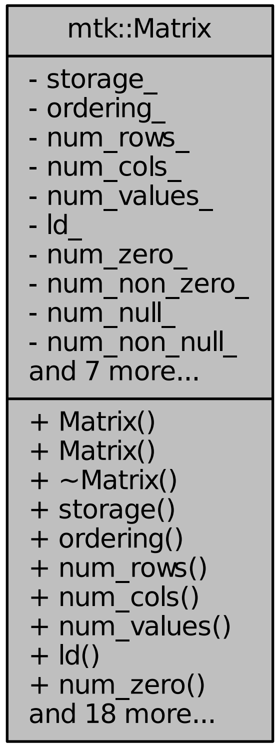
- include/mtk_lapack_adapter.h
- src/mtk_lapack_adapter.cc

16.13 mtk::Matrix Class Reference

Definition of the representation of a matrix in the MTK.

```
#include <mtk_matrix.h>
```

Collaboration diagram for mtk::Matrix:



Public Member Functions

- Matrix ()

    Default constructor.
- Matrix (const Matrix &in)

    Copy constructor.
- ∼Matrix () noexcept

    Destructor.
- MatrixStorage storage () const noexcept

    Gets the type of storage of this matrix.
- MatrixOrdering ordering () const noexcept

    Gets the type of ordering of this matrix.
- int num_rows () const noexcept

    Gets the number of rows.
- int num_cols () const noexcept

    Gets the number of rows.

- int num_values () const noexcept

  Gets the number of values.
- int ld () const noexcept

  Gets the matrix' leading dimension.
- int num_zero () const noexcept

  Gets the number of zeros.
- int num_non_zero () const noexcept

  Gets the number of non-zero values.
- int num_null () const noexcept

  Gets the number of null values.
- int num_non_null () const noexcept

  Gets the number of non-null values.
- int kl () const noexcept

  Gets the number of lower diagonals.
- int ku () const noexcept

  Gets the number of upper diagonals.
- int bandwidth () const noexcept

  Gets the bandwidth.
- Real abs_density () const noexcept

  Gets the absolute density.
- Real rel_density () const noexcept

  Gets the relative density.
- Real abs_sparsity () const noexcept

  Gets the Absolute sparsity.
- Real rel_sparsity () const noexcept

  Gets the Relative sparsity.
- void set_storage (const MatrixStorage &tt) noexcept

  Sets the storage type of the matrix.
- void set_ordering (const MatrixOrdering &oo) noexcept

  Sets the ordering of the matrix.
- void set_num_rows (const int &num_rows) noexcept

  Sets the number of rows of the matrix.
- void set_num_cols (const int &num_cols) noexcept

  Sets the number of columns of the matrix.
- void set_num_zero (const int &in) noexcept

  Sets the number of zero values of the matrix that matter.
- void set_num_null (const int &in) noexcept

  Sets the number of zero values of the matrix that DO NOT matter.
- void IncreaseNumZero () noexcept

  Increases the number of values that equal zero but with meaning.
- void IncreaseNumNull () noexcept

  Increases the number of values that equal zero but with no meaning.

Private Attributes

- MatrixStorage storage_

  What type of matrix is this?
- MatrixOrdering ordering_

  What kind of ordering is it following?
- int num_rows_

  Number of rows.
- int num_cols_

  Number of columns.
- int num_values_

  Number of total values in matrix.
- int ld_

  Elements between successive rows when row-major.
- int num_zero_

  Number of zeros.
- int num_non_zero_

  Number of non-zero values.
- int num_null_

  Number of null (insignificant) values.
- int num_non_null_

  Number of null (significant) values.
- int kl_

  Number of lower diagonals on a banded matrix.
- int ku_

  Number of upper diagonals on a banded matrix.
- int bandwidth_

  Bandwidth of the matrix.
- Real abs_density_

  Absolute density of matrix.
- Real rel_density_

  Relative density of matrix.
- Real abs_sparsity_

  Absolute sparsity of matrix.
- Real rel_sparsity_

  Relative sparsity of matrix.

16.13.1 Detailed Description

Definition of the representation for the matrices implemented in the MTK.

Definition at line 75 of file mtk_matrix.h.

16.13.2 Constructor & Destructor Documentation

16.13.2.1 mtk::Matrix::Matrix ( )

Definition at line 67 of file mtk_matrix.cc.

16.13.2.2 mtk::Matrix::Matrix (const Matrix & *in*)

Parameters

in	*in*	Given matrix.

Definition at line 86 of file mtk_matrix.cc.

16.13.2.3 mtk::Matrix::∼Matrix ( ) [noexcept]

Definition at line 105 of file mtk_matrix.cc.

16.13.3 Member Function Documentation

16.13.3.1 Real mtk::Matrix::abs_density ( ) const [noexcept]

See also

http://www.csrc.sdsu.edu/research_reports/CSRCR2013-01.pdf

Returns

Absolute density of the matrix.

16.13.3.2 mtk::Real mtk::Matrix::abs_sparsity ( ) const [noexcept]

See also

http://www.csrc.sdsu.edu/research_reports/CSRCR2013-01.pdf

Returns

Absolute sparsity of the matrix.

Definition at line 177 of file mtk_matrix.cc.

16.13.3.3 int mtk::Matrix::bandwidth ( ) const [noexcept]

Returns

Bandwidth of the matrix.

Definition at line 167 of file mtk_matrix.cc.

16.13.3.4 void mtk::Matrix::IncreaseNumNull ( ) [noexcept]

Todo Review the definition of sparse matrices properties.

Definition at line 274 of file mtk_matrix.cc.

16.13.3.5 void mtk::Matrix::IncreaseNumZero ( ) [noexcept]

Todo Review the definition of sparse matrices properties.

Definition at line 264 of file mtk_matrix.cc.

16.13.3.6 int mtk::Matrix::kl ( ) const [noexcept]

Returns

Number of lower diagonals.

Definition at line 157 of file mtk_matrix.cc.

16.13.3.7 int mtk::Matrix::ku ( ) const [noexcept]

Returns

Number of upper diagonals.

Definition at line 162 of file mtk_matrix.cc.

16.13.3.8 int mtk::Matrix::ld ( ) const [noexcept]

Leading dimension of the data array is the number of elements between successive rows (for row major storage) in memory. Most of the cases, the leading dimension is the same as the number of columns.

Returns

Leading dimension of the matrix.

Definition at line 132 of file mtk_matrix.cc.

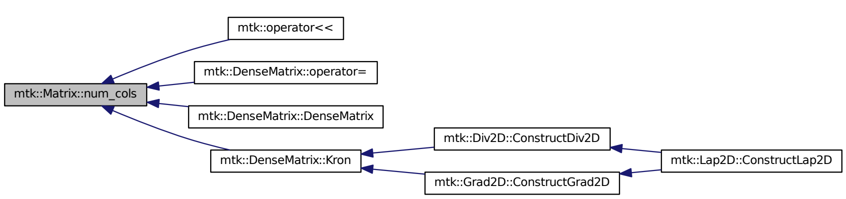
16.13.3.9 int mtk::Matrix::num_cols ( ) const [noexcept]

Returns

Number of rows of the matrix.

Definition at line 122 of file mtk_matrix.cc.

Here is the caller graph for this function:



16.13.3.10 int mtk::Matrix::num_non_null ( ) const [noexcept]

See also

http://www.csrc.sdsu.edu/research_reports/CSRCR2013-01.pdf

Returns

Number of non-null values of the matrix.

Definition at line 152 of file mtk_matrix.cc.

16.13.3.11 int mtk::Matrix::num_non_zero ( ) const [noexcept]

Returns

Number of non-zero values of the matrix.

Definition at line 142 of file mtk_matrix.cc.

16.13.3.12 int mtk::Matrix::num_null ( ) const [noexcept]

See also

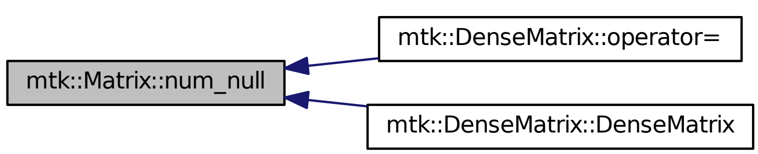
http://www.csrc.sdsu.edu/research_reports/CSRCR2013-01.pdf

Returns

Number of null values of the matrix.

Definition at line 147 of file mtk_matrix.cc.

Here is the caller graph for this function:



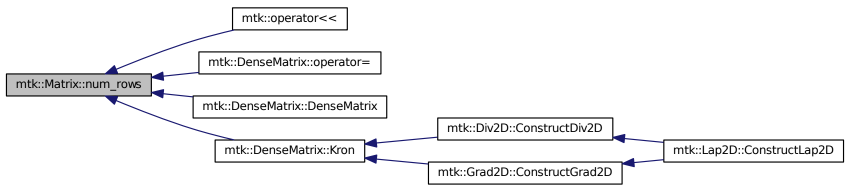
16.13.3.13 int mtk::Matrix::num_rows ( ) const [noexcept]

Returns

Number of rows of the matrix.

Definition at line 117 of file mtk_matrix.cc.

Here is the caller graph for this function:



16.13.3.14 int mtk::Matrix::num_values ( ) const [noexcept]

Returns

Number of values of the matrix.

Definition at line 127 of file mtk_matrix.cc.

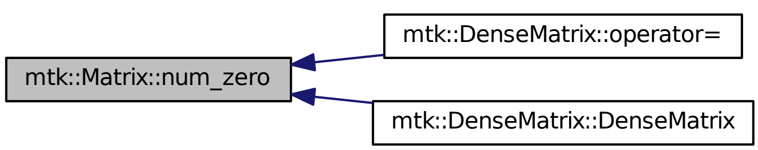
16.13.3.15 int mtk::Matrix::num_zero ( ) const [noexcept]

Returns

Number of zeros of the matrix.

Definition at line 137 of file mtk_matrix.cc.

Here is the caller graph for this function:



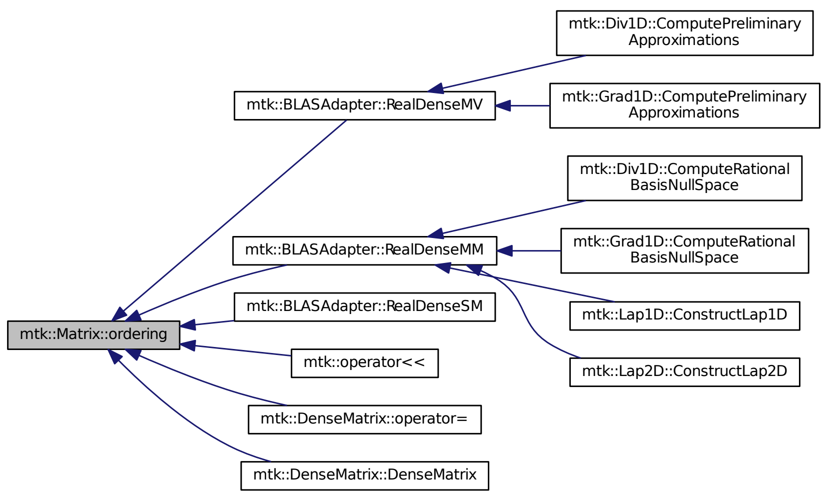
16.13.3.16 mtk::MatrixOrdering mtk::Matrix::ordering ( ) const [noexcept]

Returns

Type of ordering of this matrix.

Definition at line 112 of file mtk_matrix.cc.

Here is the caller graph for this function:



16.13.3.17 mtk::Real mtk::Matrix::rel_density ( ) const [noexcept]

See also

http://www.csrc.sdsu.edu/research_reports/CSRCR2013-01.pdf

Returns

Relative density of the matrix.

Definition at line 172 of file mtk_matrix.cc.

16.13.3.18 mtk::Real mtk::Matrix::rel_sparsity ( ) const [noexcept]

See also

http://www.csrc.sdsu.edu/research_reports/CSRCR2013-01.pdf

Returns

Relative sparsity of the matrix.

Definition at line 182 of file mtk_matrix.cc.

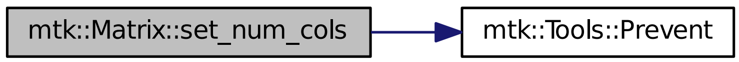
16.13.3.19 void mtk::Matrix::set_num_cols (const int & *num_cols*) [noexcept]

Parameters

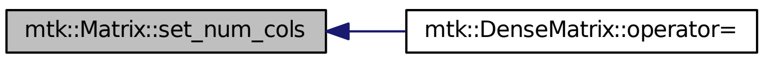
in	*num_cols*	Number of columns.

Definition at line 224 of file mtk_matrix.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.13.3.20 void mtk::Matrix::set_num_null (const int & *in*) [noexcept]

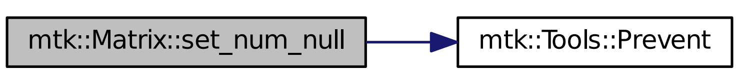
Parameters

in	*in*	Number of zero values.

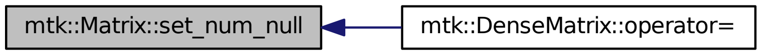
Bug -nan assigned on construction time due to num_values_ being 0.

Definition at line 250 of file mtk_matrix.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



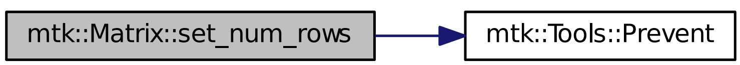
16.13.3.21 void mtk::Matrix::set_num_rows (const int & *num_rows*) [noexcept]

Parameters

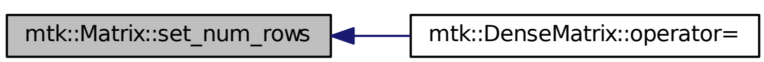
in	*num_rows*	Number of rows.

Definition at line 212 of file mtk_matrix.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.13.3.22 void mtk::Matrix::set_num_zero (const int & *in*) [noexcept]

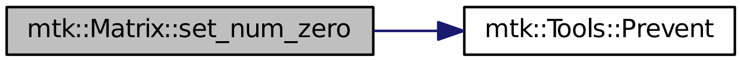
Parameters

in	*in*	Number of zero values.

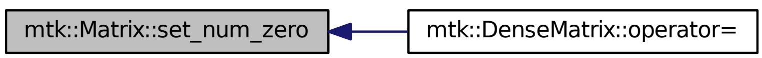
Bug -nan assigned on construction time due to num_values_ being 0.

Definition at line 236 of file mtk_matrix.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.13.3.23 void mtk::Matrix::set_ordering (const MatrixOrdering & *oo*) [noexcept]

See also

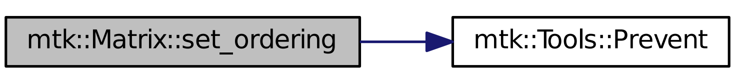
MatrixOrdering

Parameters

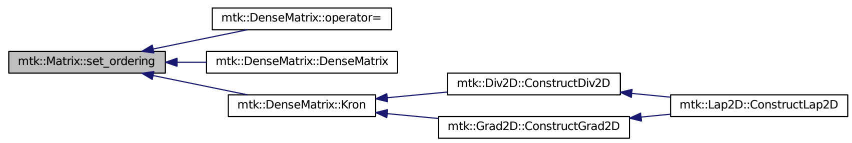
in	*oo*	Ordering of the matrix.

Definition at line 199 of file mtk_matrix.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



16.13.3.24 void mtk::Matrix::set_storage (const MatrixStorage & *tt*) [noexcept]

See also

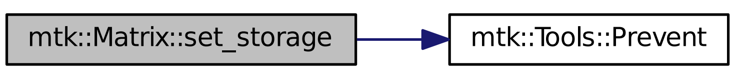
MatrixStorage

Parameters

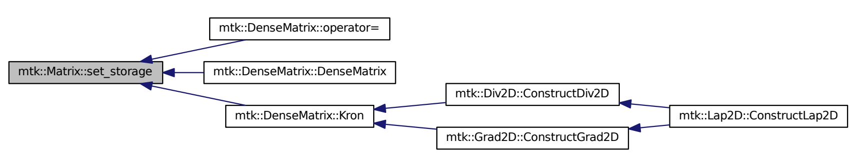
in	*tt*	Type of the matrix storage.

Definition at line 187 of file mtk_matrix.cc.

Here is the call graph for this function:



Here is the caller graph for this function:



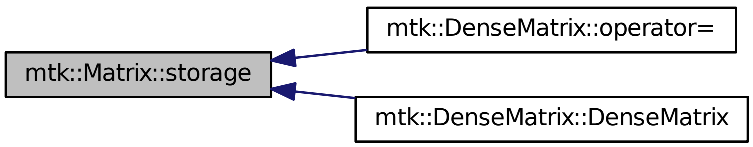
16.13.3.25 mtk::MatrixStorage mtk::Matrix::storage ( ) const [noexcept]

Returns

Type of storage of this matrix.

Definition at line 107 of file mtk_matrix.cc.

Here is the caller graph for this function:



16.13.4 Member Data Documentation

16.13.4.1 Real mtk::Matrix::abs_density_ [private]

Definition at line 296 of file mtk_matrix.h.

16.13.4.2 Real mtk::Matrix::abs_sparsity_ [private]

Definition at line 298 of file mtk_matrix.h.

16.13.4.3 int mtk::Matrix::bandwidth_ [private]

Definition at line 294 of file mtk_matrix.h.

16.13.4.4 int mtk::Matrix::kl_ [private]

Definition at line 292 of file mtk_matrix.h.

16.13.4.5 int mtk::Matrix::ku_ [private]

Definition at line 293 of file mtk_matrix.h.

16.13.4.6 int mtk::Matrix::ld_ [private]

Definition at line 285 of file mtk_matrix.h.

16.13.4.7 int mtk::Matrix::num_cols_ [private]

Definition at line 283 of file mtk_matrix.h.

16.13.4.8 int mtk::Matrix::num_non_null_ [private]

Definition at line 290 of file mtk_matrix.h.

16.13.4.9 int mtk::Matrix::num_non_zero_ [private]

Definition at line 288 of file mtk_matrix.h.

16.13.4.10 int mtk::Matrix::num_null_ [private]

Definition at line 289 of file mtk_matrix.h.

16.13.4.11 int mtk::Matrix::num_rows_ [private]

Definition at line 282 of file mtk_matrix.h.

16.13.4.12 int mtk::Matrix::num_values_ [private]

Definition at line 284 of file mtk_matrix.h.

16.13.4.13 int mtk::Matrix::num_zero_ [private]

Definition at line 287 of file mtk_matrix.h.

16.13.4.14 MatrixOrdering mtk::Matrix::ordering_ [private]

Definition at line 280 of file mtk_matrix.h.

16.13.4.15 Real mtk::Matrix::rel_density_ [private]

Definition at line 297 of file mtk_matrix.h.

16.13.4.16 Real mtk::Matrix::rel_sparsity_ [private]

Definition at line 299 of file mtk_matrix.h.

16.13.4.17 MatrixStorage mtk::Matrix::storage_ [private]

Definition at line 278 of file mtk_matrix.h.

The documentation for this class was generated from the following files:

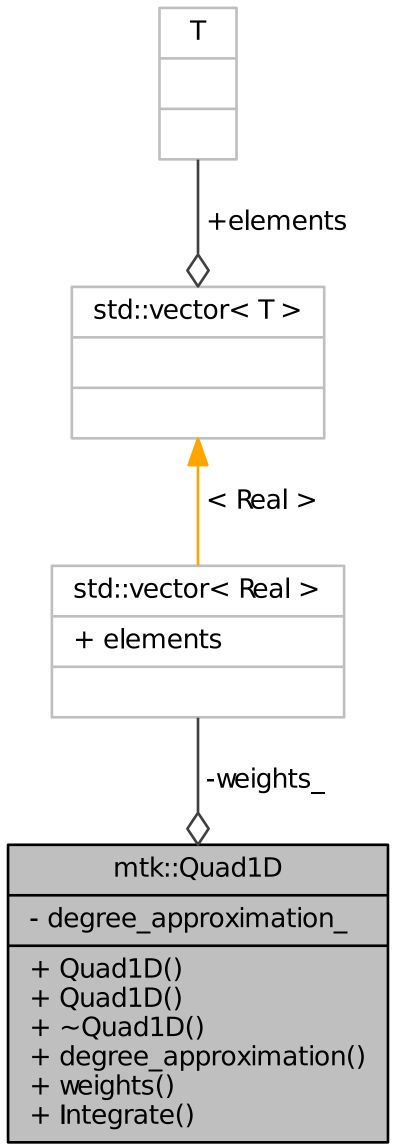
- include/mtk_matrix.h
- src/mtk_matrix.cc

16.14 mtk::Quad1D Class Reference

Implements a 1D mimetic quadrature.

`#include <mtk_quad_1d.h>`

Collaboration diagram for mtk::Quad1D:



Public Member Functions

- Quad1D ()

  Default constructor.
- Quad1D (const Quad1D &quad)

  Copy constructor.
- ∼Quad1D ()

  Destructor.
- int degree_approximation () const

  Get the degree of interpolating polynomial per sub-interval of domain.
- Real ∗ weights () const

  Return collection of weights.
- Real Integrate (Real(∗Integrand)(Real xx), UniStgGrid1D grid) const

  Mimetic integration routine.

Private Attributes

- int degree_approximation_

  Degree of the interpolating polynomial.
- std::vector< Real > weights_

  Collection of weights.

Friends

- std::ostream & operator<< (std::ostream &stream, Quad1D &in)

  Output stream operator for printing.

16.14.1 Detailed Description

This class implements a 1D quadrature solver based on the mimetic discretization of the gradient operator.

Definition at line 81 of file mtk_quad_1d.h.

16.14.2 Constructor & Destructor Documentation

16.14.2.1 mtk::Quad1D::Quad1D ( )

16.14.2.2 mtk::Quad1D::Quad1D (const Quad1D & *quad*)

Parameters

in	*div*	Given quadrature.

16.14.2.3 mtk::Quad1D::∼Quad1D ( )

16.14.3 Member Function Documentation

16.14.3.1 int mtk::Quad1D::degree_approximation ( ) const

Returns

Degree of the interpolating polynomial per sub-interval of the domain.

16.14.3.2 Real mtk::Quad1D::Integrate (Real(∗)(Real xx) *Integrand,* UniStgGrid1D *grid*) const

Parameters

in	*Integrand*	Real-valued function to integrate.
in	*grid*	Given integration domain.

Returns

Result of the integration.

16.14.3.3 Real∗ mtk::Quad1D::weights ( ) const

Returns

Collection of weights.

16.14.4 Friends And Related Function Documentation

16.14.4.1 std::ostream& operator<< (std::ostream & *stream,* Quad1D & *in*) [friend]

16.14.5 Member Data Documentation

16.14.5.1 int mtk::Quad1D::degree_approximation_ [private]

Definition at line 124 of file mtk_quad_1d.h.

16.14.5.2 std::vector<Real> mtk::Quad1D::weights_ [private]

Definition at line 126 of file mtk_quad_1d.h.

The documentation for this class was generated from the following file:

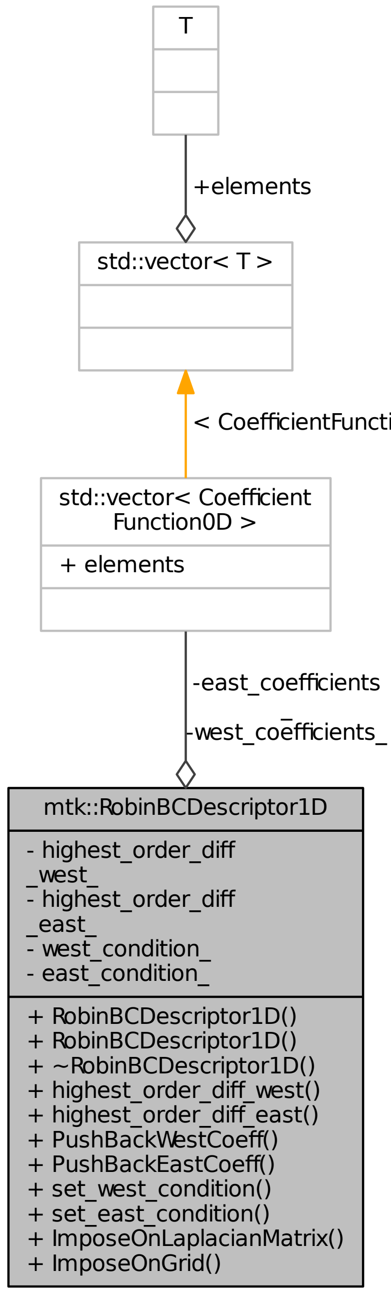
- include/mtk_quad_1d.h

16.15 mtk::RobinBCDescriptor1D Class Reference

Impose Robin boundary conditions on the operators and on the grids.

`#include <mtk_robin_bc_descriptor_1d.h>`

Collaboration diagram for mtk::RobinBCDescriptor1D:



Public Member Functions

- RobinBCDescriptor1D ()

Default constructor.
- RobinBCDescriptor1D (const RobinBCDescriptor1D &desc)

  Copy constructor.
- ∼RobinBCDescriptor1D () noexcept

  Destructor.
- int highest_order_diff_west () const noexcept

  Getter for the highest order of differentiation in the west boundary.
- int highest_order_diff_east () const noexcept

  Getter for the highest order of differentiation in the east boundary.
- void PushBackWestCoeff (CoefficientFunction0D cw)

  Push back coefficient function at west of lowest order diff. available.
- void PushBackEastCoeff (CoefficientFunction0D ce)

  Push back coefficient function at east of lowest order diff. available.
- void set_west_condition (Real(∗west_condition)(const Real &tt)) noexcept

  Set boundary condition at west.
- void set_east_condition (Real(∗east_condition)(const Real &tt)) noexcept

  Set boundary condition at east.
- bool ImposeOnLaplacianMatrix (const Lap1D &lap, DenseMatrix &matrix, const Real &time=mtk::kZero) const

  Imposes the condition on the operator represented as matrix.
- void ImposeOnGrid (UniStgGrid1D &grid, const Real &time=mtk::kZero) const

  Imposes the condition on the grid.

Private Attributes

- int highest_order_diff_west_

  Highest order of differentiation for west.
- int highest_order_diff_east_

  Highest order of differentiation for east.
- std::vector
  < CoefficientFunction0D > west_coefficients_

  Coeffs. west.
- std::vector
  < CoefficientFunction0D > east_coefficients_

  Coeffs. east.
- Real(∗ west_condition_)(const Real &tt)

  Condition for west.
- Real(∗ east_condition_)(const Real &tt)

  Condition for east.

16.15.1 Detailed Description

This class presents an interface for the user to specify Robin boundary conditions on 1D mimetic operators and the grids they are acting on.

Def. Let $u(\mathbf{x},t) : \Omega \times [t_0,t_n] \mapsto \mathbb{R}$ be the solution to an ordinary or partial differential equation of interest. We say that u satisfies a **Robin boundary condition on** $\partial\Omega$ if and only if there exists $\beta(\mathbf{x},t) : \Omega \times [t_0,t_n] \mapsto \mathbb{R}$ so that:

$$\forall t \in [t_0,t_n]\ \forall \mathbf{x} \in \partial\Omega : \delta(\mathbf{x},t)u(\mathbf{x},t) + \eta(\mathbf{x},t)(\hat{\mathbf{n}} \cdot \nabla u) = \beta(\mathbf{x},t).$$

Intuitively, a **Robin boundary condition** is a constraint that must be satisfied by any linear combination of any scalar field u and its first normal derivative, in order for u to represent a unique solution to a given ordinary or partial differential equation of interest.

In a 1D context ($\partial\Omega = \{a,b\} \subset \mathbb{R}$), this condition can be written as follows:

$$\delta_a(a,t)u(a,t) - \eta_a(a,t)u'(a,t) = \beta_a(a,t),$$
$$\delta_b(b,t)u(b,t) + \eta_b(b,t)u'(b,t) = \beta_b(b,t).$$

Instances of this class receive information about the coefficient functions and each condition for any subset of the boundary (west and east, in 1D). These instances then handle the complexity of placing the coefficients in the differentiation matrices and the conditions in the grids.

See also

http://mathworld.wolfram.com/NormalVector.html

Definition at line 155 of file mtk_robin_bc_descriptor_1d.h.

16.15.2 Constructor & Destructor Documentation

16.15.2.1 mtk::RobinBCDescriptor1D::RobinBCDescriptor1D ( )

Definition at line 93 of file mtk_robin_bc_descriptor_1d.cc.

16.15.2.2 mtk::RobinBCDescriptor1D::RobinBCDescriptor1D (const RobinBCDescriptor1D & *desc*)

Parameters

in	*desc*	Given 1D descriptor.

Definition at line 99 of file mtk_robin_bc_descriptor_1d.cc.

16.15.2.3 mtk::RobinBCDescriptor1D::∼RobinBCDescriptor1D ( ) [noexcept]

Definition at line 106 of file mtk_robin_bc_descriptor_1d.cc.

16.15.3 Member Function Documentation

16.15.3.1 int mtk::RobinBCDescriptor1D::highest_order_diff_east ( ) const [noexcept]

Returns

Integer highest order of differentiation in the east boundary.

Definition at line 113 of file mtk_robin_bc_descriptor_1d.cc.

16.15.3.2 int mtk::RobinBCDescriptor1D::highest_order_diff_west ( ) const [noexcept]

Returns

Integer highest order of differentiation in the west boundary.

Definition at line 108 of file mtk_robin_bc_descriptor_1d.cc.

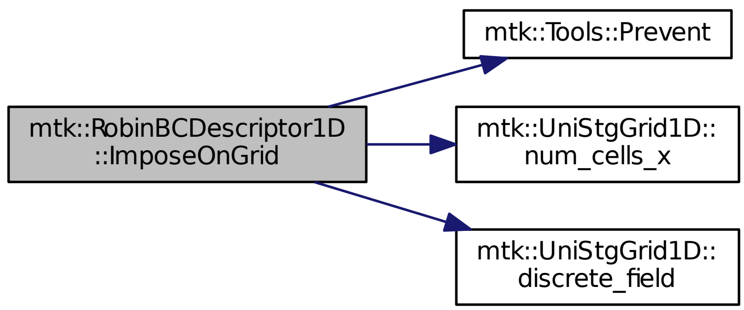
16.15.3.3 void mtk::RobinBCDescriptor1D::ImposeOnGrid (UniStgGrid1D & *grid,* const Real & *time =* mtk::kZero) const

Parameters

in,out	*grid*	Grid upon which impose the desired boundary condition.
in	*time*	Current time snapshot. Default is kZero.

Definition at line 246 of file mtk_robin_bc_descriptor_1d.cc.

Here is the call graph for this function:



16.15.3.4 bool mtk::RobinBCDescriptor1D::ImposeOnLaplacianMatrix (const Lap1D & *lap,* mtk::DenseMatrix & *matrix,* const Real & *time =* mtk::kZero) const

Parameters

in	*lap*	Operator in the Matrix.
in,out	*matrix*	Input Laplacian operator.
in	*time*	Current time snapshot. Default is kZero.

Returns

Success of the imposition.

1. Impose Dirichlet coefficients. 1.1. Impose Dirichlet condition at the west.

1.2. Impose Dirichlet condition at the east.

1. Impose Neumann coefficients.

2.1. Create a mimetic gradient to approximate the first derivative.

2.2. Extract the coefficients approximating the boundary.

Warning

Coefficients returned by the mim_bndy getter are dimensionless! Therefore we must scale them by delta_x (from the grid), before adding to the matrix! But this information is in the given lap!

2.3. Impose Neumann condition at the west.

2.3.1. Get gradient coefficient and scale it.

2.3.2. Multiply times the coefficient for this boundary, times the unit normal for this boundary.

2.3.3. Set the final value summing it with what is on the matrix.

2.4. Impose Neumann condition at the east.

Warning

The Coefficients returned by the mim_bndy getter are those intended for the west boundary. We must enforce the center-skew-symmetry of the resulting operator by permuting their location in the matrix, and changing their sign.

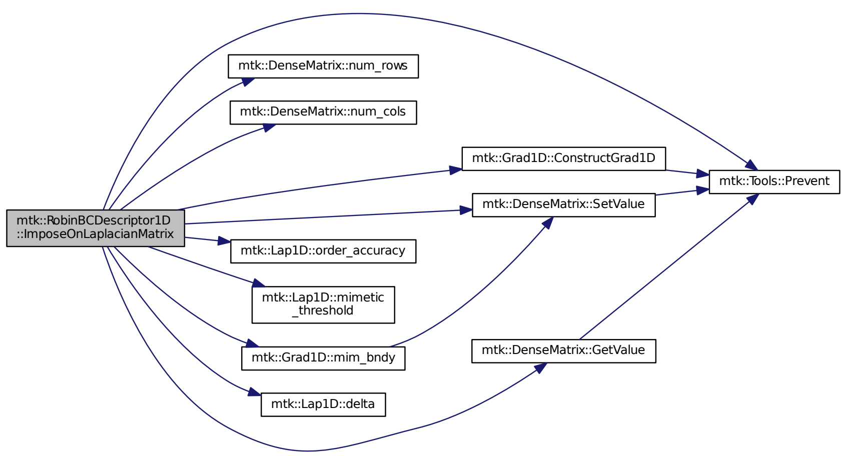
2.4.1. Get gradient coefficient and scale it.

2.4.2. Multiply times the coefficient for this boundary, times the unit normal for this boundary, and change the sign to enforce center-skew-symmetry.

2.4.3. Set the final value summing it with what is on the matrix.

Definition at line 166 of file mtk_robin_bc_descriptor_1d.cc.

Here is the call graph for this function:



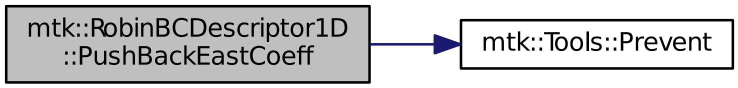
16.15.3.5 void mtk::RobinBCDescriptor1D::PushBackEastCoeff (mtk::CoefficientFunction0D *ce*)

Parameters

in	*ce*	Function $c_e(x,y) : \Omega \mapsto \mathbb{R}$.

Definition at line 132 of file mtk_robin_bc_descriptor_1d.cc.

Here is the call graph for this function:



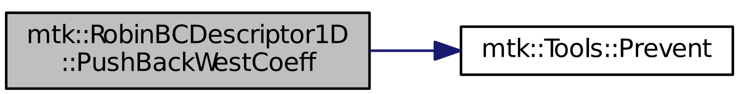
16.15.3.6 void mtk::RobinBCDescriptor1D::PushBackWestCoeff (mtk::CoefficientFunction0D *cw*)

Parameters

in	*cw*	Function $c_w(x,y) : \Omega \mapsto \mathbb{R}$.

Definition at line 118 of file mtk_robin_bc_descriptor_1d.cc.

Here is the call graph for this function:



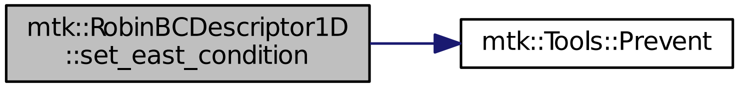
16.15.3.7 void mtk::RobinBCDescriptor1D::set_east_condition (Real(*)(const Real &tt) *east_condition*) [noexcept]

Parameters

in	*east_condition*	$\beta_e(y,t) : \Omega \mapsto \mathbb{R}$.

Definition at line 156 of file mtk_robin_bc_descriptor_1d.cc.

Here is the call graph for this function:



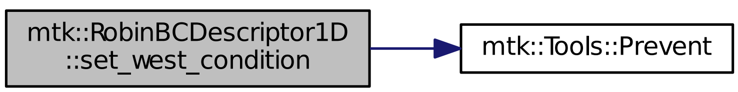
16.15.3.8 void mtk::RobinBCDescriptor1D::set_west_condition (Real(∗)(const Real &tt) *west_condition*) [noexcept]

Parameters

in	*west_condition*	$\beta_w(y,t) : \Omega \mapsto \mathbb{R}$.

Definition at line 146 of file mtk_robin_bc_descriptor_1d.cc.

Here is the call graph for this function:



16.15.4 Member Data Documentation

16.15.4.1 std::vector<CoefficientFunction0D> mtk::RobinBCDescriptor1D::east_coefficients_ [private]

Definition at line 237 of file mtk_robin_bc_descriptor_1d.h.

16.15.4.2 Real(∗ mtk::RobinBCDescriptor1D::east_condition_)(const Real &tt) [private]

Definition at line 240 of file mtk_robin_bc_descriptor_1d.h.

16.15.4.3 int mtk::RobinBCDescriptor1D::highest_order_diff_east_ [private]

Definition at line 234 of file mtk_robin_bc_descriptor_1d.h.

16.15.4.4 int mtk::RobinBCDescriptor1D::highest_order_diff_west_ [private]

Definition at line 233 of file mtk_robin_bc_descriptor_1d.h.

16.15.4.5 std::vector<CoefficientFunction0D> mtk::RobinBCDescriptor1D::west_coefficients_ [private]

Definition at line 236 of file mtk_robin_bc_descriptor_1d.h.

16.15.4.6 Real(* mtk::RobinBCDescriptor1D::west_condition_)(const Real &tt) [private]

Definition at line 239 of file mtk_robin_bc_descriptor_1d.h.

The documentation for this class was generated from the following files:

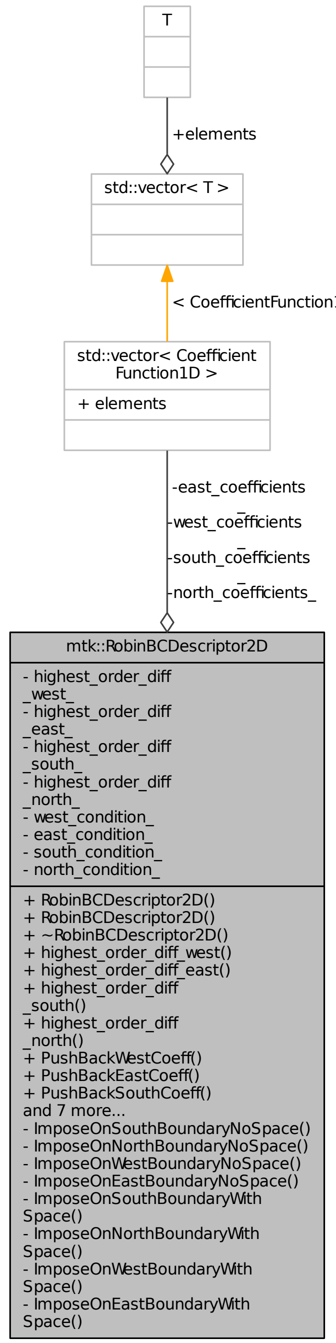
- include/mtk_robin_bc_descriptor_1d.h
- src/mtk_robin_bc_descriptor_1d.cc

16.16 mtk::RobinBCDescriptor2D Class Reference

Impose Robin boundary conditions on the operators and on the grids.

`#include <mtk_robin_bc_descriptor_2d.h>`

Collaboration diagram for mtk::RobinBCDescriptor2D:



Public Member Functions

- RobinBCDescriptor2D ()

Default constructor.
- RobinBCDescriptor2D (const RobinBCDescriptor2D &desc)

  Copy constructor.
- ∼RobinBCDescriptor2D () noexcept

  Destructor.
- int highest_order_diff_west () const noexcept

  Getter for the highest order of differentiation in the west boundary.
- int highest_order_diff_east () const noexcept

  Getter for the highest order of differentiation in the east boundary.
- int highest_order_diff_south () const noexcept

  Getter for the highest order of differentiation in the south boundary.
- int highest_order_diff_north () const noexcept

  Getter for the highest order of differentiation in the north boundary.
- void PushBackWestCoeff (CoefficientFunction1D cw)

  Push back coefficient function at west of lowest order diff. available.
- void PushBackEastCoeff (CoefficientFunction1D ce)

  Push back coefficient function at east of lowest order diff. available.
- void PushBackSouthCoeff (CoefficientFunction1D cs)

  Push back coefficient function south of lowest order diff. available.
- void PushBackNorthCoeff (CoefficientFunction1D cn)

  Push back coefficient function north of lowest order diff. available.
- void set_west_condition (Real(∗west_condition)(const Real &yy, const Real &tt)) noexcept

  Set boundary condition at west.
- void set_east_condition (Real(∗east_condition)(const Real &yy, const Real &tt)) noexcept

  Set boundary condition at east.
- void set_south_condition (Real(∗south_condition)(const Real &xx, const Real &tt)) noexcept

  Set boundary condition at south.
- void set_north_condition (Real(∗north_condition)(const Real &xx, const Real &tt)) noexcept

  Set boundary condition at north.
- bool ImposeOnLaplacianMatrix (const Lap2D &lap, const UniStgGrid2D &grid, DenseMatrix &matrix, const Real &time=kZero) const

  Imposes the condition on the operator represented as matrix.
- void ImposeOnGrid (UniStgGrid2D &grid, const Real &time=kZero) const

  Imposes the condition on the grid.

Private Member Functions

- bool ImposeOnSouthBoundaryNoSpace (const Lap2D &lap, const UniStgGrid2D &grid, DenseMatrix &matrix, const Real &time=kZero) const

  Imposes the condition on the south boundary.
- bool ImposeOnNorthBoundaryNoSpace (const Lap2D &lap, const UniStgGrid2D &grid, DenseMatrix &matrix, const Real &time=kZero) const

  Imposes the condition on the north boundary.
- bool ImposeOnWestBoundaryNoSpace (const Lap2D &lap, const UniStgGrid2D &grid, DenseMatrix &matrix, const Real &time=kZero) const

  Imposes the condition on the west boundary.
- bool ImposeOnEastBoundaryNoSpace (const Lap2D &lap, const UniStgGrid2D &grid, DenseMatrix &matrix, const Real &time=kZero) const

Imposes the condition on the east boundary.

- bool ImposeOnSouthBoundaryWithSpace (const Lap2D &lap, const UniStgGrid2D &grid, DenseMatrix &matrix, const Real &time=kZero) const

  Imposes the condition on the south boundary.
- bool ImposeOnNorthBoundaryWithSpace (const Lap2D &lap, const UniStgGrid2D &grid, DenseMatrix &matrix, const Real &time=kZero) const

  Imposes the condition on the north boundary.
- bool ImposeOnWestBoundaryWithSpace (const Lap2D &lap, const UniStgGrid2D &grid, DenseMatrix &matrix, const Real &time=kZero) const

  Imposes the condition on the west boundary.
- bool ImposeOnEastBoundaryWithSpace (const Lap2D &lap, const UniStgGrid2D &grid, DenseMatrix &matrix, const Real &time=kZero) const

  Imposes the condition on the east boundary.

Private Attributes

- int highest_order_diff_west_

  Highest order of differentiation west.
- int highest_order_diff_east_

  Highest order of differentiation east.
- int highest_order_diff_south_

  Highest order differentiation for south.
- int highest_order_diff_north_

  Highest order differentiation for north.
- std::vector
  < CoefficientFunction1D > west_coefficients_

  Coeffs. west.
- std::vector
  < CoefficientFunction1D > east_coefficients_

  Coeffs. east.
- std::vector
  < CoefficientFunction1D > south_coefficients_

  Coeffs. south.
- std::vector
  < CoefficientFunction1D > north_coefficients_

  Coeffs. south.
- Real(∗ west_condition_)(const Real &xx, const Real &tt)

  Condition west.
- Real(∗ east_condition_)(const Real &xx, const Real &tt)

  Condition east.
- Real(∗ south_condition_)(const Real &yy, const Real &tt)

  Cond. south.
- Real(∗ north_condition_)(const Real &yy, const Real &tt)

  Cond. north.

16.16.1 Detailed Description

This class presents an interface for the user to specify Robin boundary conditions on 2D mimetic operators and the grids they are acting on.

Def. Let $u(\mathbf{x},t) : \Omega \times [t_0,t_n] \mapsto \mathbb{R}$ be the solution to an ordinary or partial differential equation of interest. We say that u satisfies a **Robin boundary condition on** $\partial\Omega$ if and only if there exists $\beta(\mathbf{x},t) : \Omega \times [t_0,t_n] \mapsto \mathbb{R}$ so that:

$$\forall t \in [t_0,t_n] \; \forall \mathbf{x} \in \partial\Omega : \delta(\mathbf{x},t)u(\mathbf{x},t) + \eta(\mathbf{x},t)(\hat{\mathbf{n}} \cdot \nabla u) = \beta(\mathbf{x},t).$$

Intuitively, a **Robin boundary condition** is a constraint that must be satisfied by any linear combination of any scalar field u and its first normal derivative, in order for u to represent a unique solution to a given ordinary or partial differential equation of interest.

Instances of this class receive information about the coefficient functions and each condition for any subset of the boundary (west, east, south and north in 2D). These instances then handle the complexity of placing the coefficients in the differentiation matrices and the conditions in the grids.

See also

`http://mathworld.wolfram.com/NormalVector.html`

Definition at line 132 of file mtk_robin_bc_descriptor_2d.h.

16.16.2 Constructor & Destructor Documentation

16.16.2.1 mtk::RobinBCDescriptor2D::RobinBCDescriptor2D ( )

Definition at line 84 of file mtk_robin_bc_descriptor_2d.cc.

16.16.2.2 mtk::RobinBCDescriptor2D::RobinBCDescriptor2D (const RobinBCDescriptor2D & *desc*)

Parameters

in	*desc*	Given 2D descriptor.

Definition at line 94 of file mtk_robin_bc_descriptor_2d.cc.

16.16.2.3 mtk::RobinBCDescriptor2D::~RobinBCDescriptor2D ( ) [noexcept]

Definition at line 105 of file mtk_robin_bc_descriptor_2d.cc.

16.16.3 Member Function Documentation

16.16.3.1 int mtk::RobinBCDescriptor2D::highest_order_diff_east ( ) const [noexcept]

Returns

Integer highest order of differentiation in the east boundary.

Definition at line 112 of file mtk_robin_bc_descriptor_2d.cc.

16.16.3.2 int mtk::RobinBCDescriptor2D::highest_order_diff_north ( ) const [noexcept]

Returns

Integer highest order of differentiation in the north boundary.

Definition at line 122 of file mtk_robin_bc_descriptor_2d.cc.

16.16.3.3 int mtk::RobinBCDescriptor2D::highest_order_diff_south ( ) const [noexcept]

Returns

Integer highest order of differentiation in the south boundary.

Definition at line 117 of file mtk_robin_bc_descriptor_2d.cc.

16.16.3.4 int mtk::RobinBCDescriptor2D::highest_order_diff_west ( ) const [noexcept]

Returns

Integer highest order of differentiation in the west boundary.

Definition at line 107 of file mtk_robin_bc_descriptor_2d.cc.

16.16.3.5 bool mtk::RobinBCDescriptor2D::ImposeOnEastBoundaryNoSpace (const Lap2D & *lap*, const UniStgGrid2D & *grid*, mtk::DenseMatrix & *matrix*, const Real & *time* = kZero) const [private]

Parameters

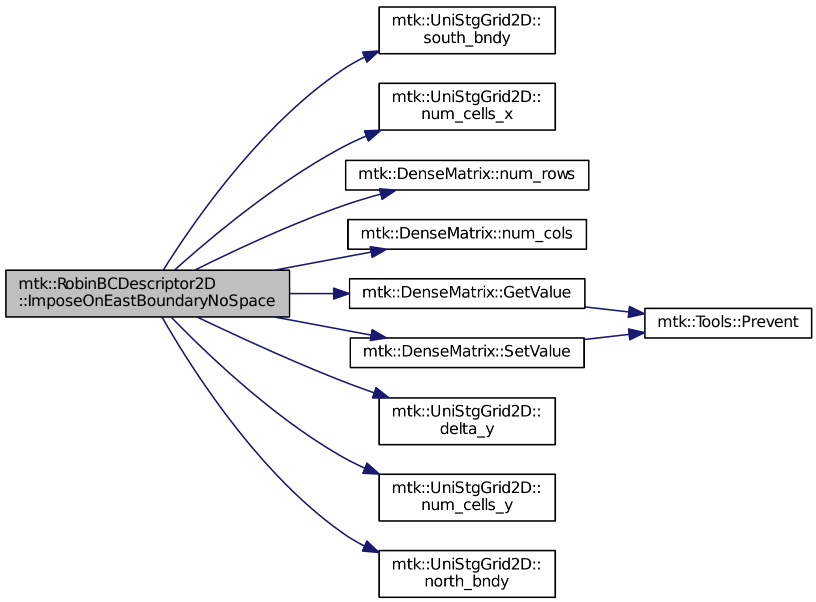
in	*lap*	Laplacian operator on the matrix.
in	*grid*	Grid upon which impose the desired boundary condition.
in,out	*matrix*	Input matrix with the Laplacian operator.
in	*time*	Current time snapshot. Default is kZero.

1. Impose the Dirichlet condition first.

2. Impose the Neumann condition.

Definition at line 495 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



16.16.3.6 bool mtk::RobinBCDescriptor2D::ImposeOnEastBoundaryWithSpace (const **Lap2D** & *lap,* const **UniStgGrid2D** & *grid,* **mtk::DenseMatrix** & *matrix,* const **Real** & *time* = **kZero**) const [private]

Parameters

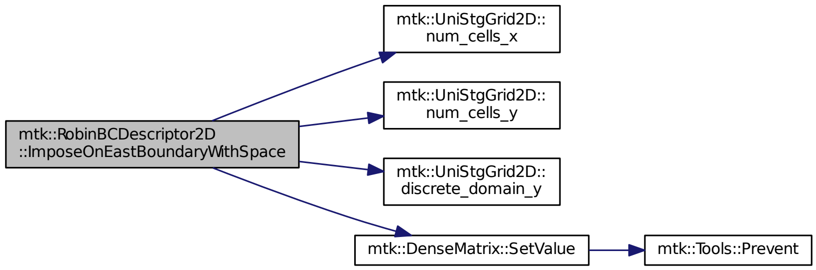
in	*lap*	Laplacian operator on the matrix.
in	*grid*	Grid upon which impose the desired boundary condition.
in,out	*matrix*	Input matrix with the Laplacian operator.
in	*time*	Current time snapshot. Default is kZero.

1. Impose the Dirichlet condition first.

2. Impose the Neumann condition.

Definition at line 564 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



16.16.3.7 void mtk::RobinBCDescriptor2D::ImposeOnGrid (mtk::UniStgGrid2D & *grid*, const Real & *time* = kZero) const

Parameters

in,out	*grid*	Grid upon which impose the desired boundary condition.
in	*time*	Current time snapshot. Default is kZero.

1. Impose assuming an scalar grid.

1.1. Impose south condition.

1.1.1. Impose south-west corner.

1.1.2. Impose south border.

1.1.3. Impose south-east corner.

1.2. Impose north condition.

1.2.1. Impose north-west corner.

1.2.2. Impose north border.

1.2.3. Impose north-east corner.

1.3. Impose west condition.

1.3.1. Impose south-west corner.

Note

As per discussion with Otilio, we will take the **arithmetic mean** of the values of the BCs at the corners.

1.3.2. Impose west border.

1.3.3. Impose north-west corner.

1.4. Impose east condition.

1.4.1. Impose south-east corner.

1.4.2. Impose east border.

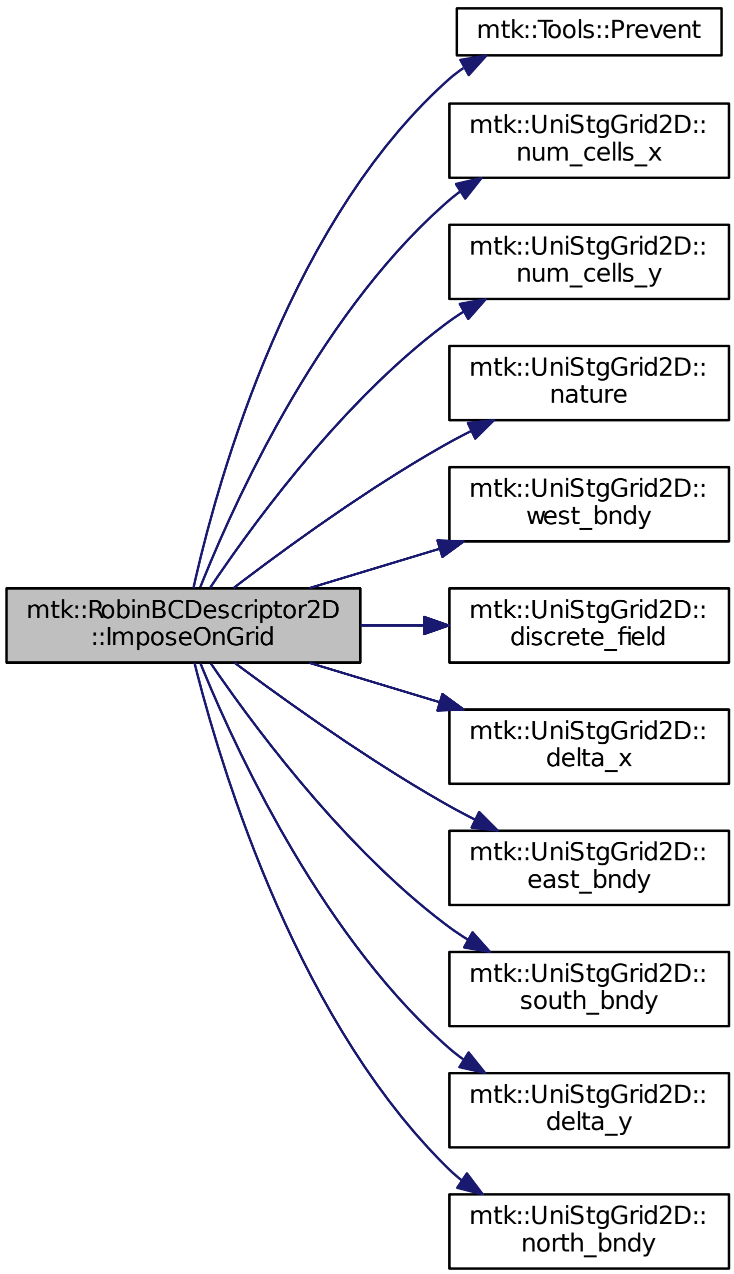
1.4.3. Impose north-east corner.

1. Impose assuming a vector grid.

Todo Implement imposition for vector-valued grids. Need research here!

Definition at line 674 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



16.16.3.8 bool mtk::RobinBCDescriptor2D::ImposeOnLaplacianMatrix (const **Lap2D** & *lap*, const **UniStgGrid2D** & *grid*, **mtk::DenseMatrix** & *matrix*, const **Real** & *time* = **kZero**) const

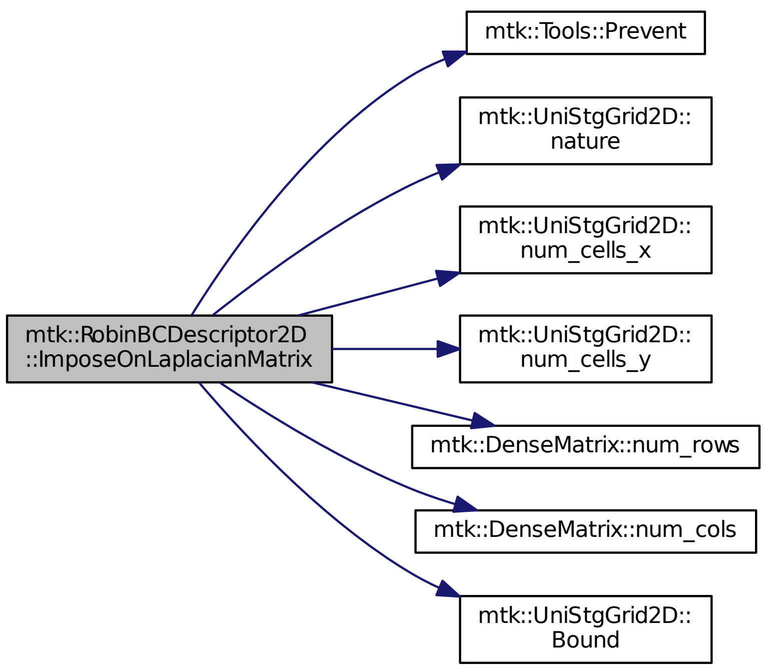
Parameters

`in`	*lap*	Laplacian operator on the matrix.
`in`	*grid*	Grid upon which impose the desired boundary condition.
`in,out`	*matrix*	Input matrix with the Laplacian operator.
`in`	*time*	Current time snapshot. Default is kZero.

If we have not bound anything to the grid, then we have to generate our collection of spatial coordinates, as we evaluate the coefficients.

Definition at line 591 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



16.16.3.9 bool mtk::RobinBCDescriptor2D::ImposeOnNorthBoundaryNoSpace (const **Lap2D** & *lap*, const **UniStgGrid2D** & *grid*, **mtk::DenseMatrix** & *matrix*, const **Real** & *time* = **kZero**) const `[private]`

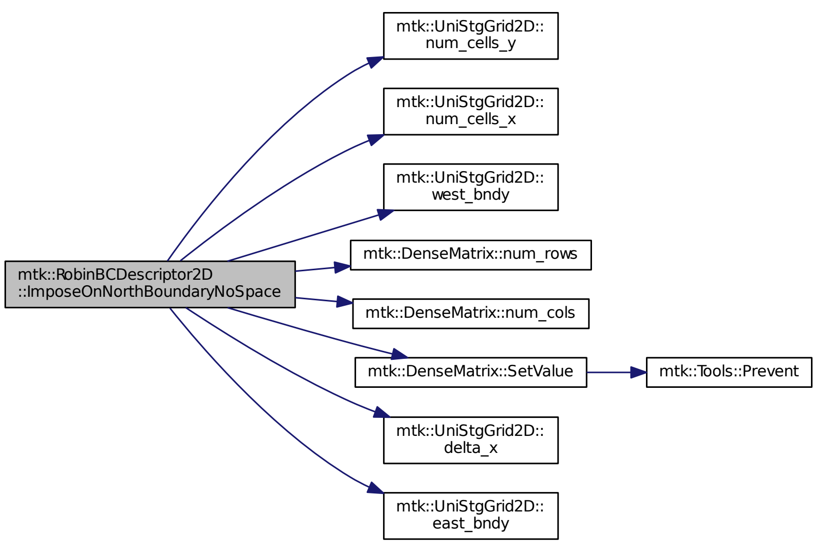
Parameters

in	*lap*	Laplacian operator on the matrix.
in	*grid*	Grid upon which impose the desired boundary condition.
in,out	*matrix*	Input matrix with the Laplacian operator.
in	*time*	Current time snapshot. Default is kZero.

1. Impose the Dirichlet condition first.
2. Impose the Neumann condition.

Definition at line 312 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



16.16.3.10 bool mtk::RobinBCDescriptor2D::ImposeOnNorthBoundaryWithSpace (const Lap2D & *lap*, const UniStgGrid2D & *grid*, mtk::DenseMatrix & *matrix*, const Real & *time* = kZero) const [private]

Parameters

in	*lap*	Laplacian operator on the matrix.
in	*grid*	Grid upon which impose the desired boundary condition.
in,out	*matrix*	Input matrix with the Laplacian operator.
in	*time*	Current time snapshot. Default is kZero.

1. Impose Dirichlet condition.

For each entry on the diagonal:

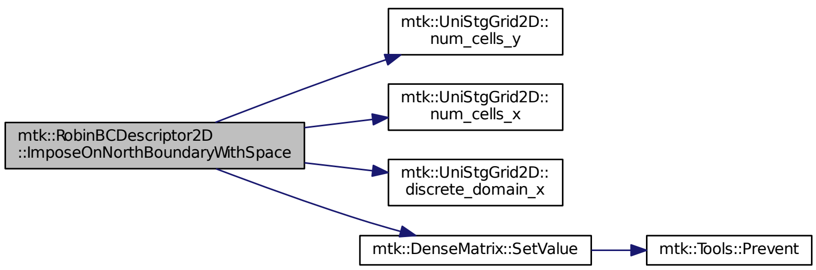
Evaluate next set spatial coordinates to evaluate the coefficient.

Evaluate and assign the Dirichlet coefficient.

1. Impose the Neumann condition.

Definition at line 372 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



16.16.3.11 bool mtk::RobinBCDescriptor2D::ImposeOnSouthBoundaryNoSpace (const Lap2D & *lap*, const UniStgGrid2D & *grid*, mtk::DenseMatrix & *matrix*, const Real & *time* = kZero) const [private]

Parameters

in	*lap*	Laplacian operator on the matrix.
in	*grid*	Grid upon which impose the desired boundary condition.
in,out	*matrix*	Input matrix with the Laplacian operator.
in	*time*	Current time snapshot. Default is kZero.

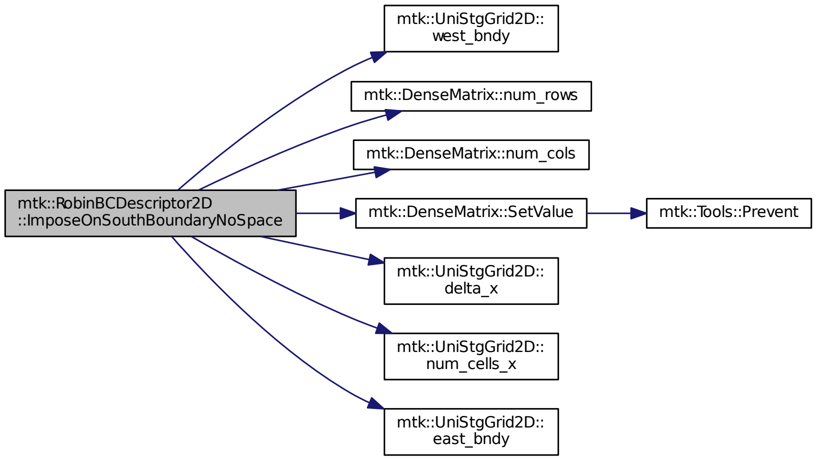
1. Impose the Dirichlet condition first.

2. Impose the Neumann condition.

Todo Impose the Neumann conditions on every pole, for every scenario.

Definition at line 229 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



16.16.3.12 bool mtk::RobinBCDescriptor2D::ImposeOnSouthBoundaryWithSpace (const Lap2D & *lap*, const UniStgGrid2D & *grid*, mtk::DenseMatrix & *matrix*, const Real & *time* = kZero) const [private]

Parameters

in	*lap*	Laplacian operator on the matrix.
in	*grid*	Grid upon which impose the desired boundary condition.
in,out	*matrix*	Input matrix with the Laplacian operator.
in	*time*	Current time snapshot. Default is kZero.

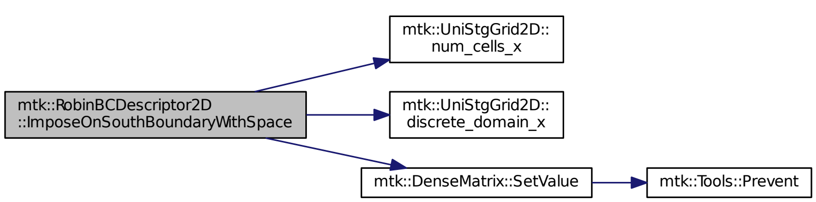
1. Impose the Dirichlet condition first.

Todo Impose Harmonic mean on the corners for the case when the generated space is available, for all poles.

1. Impose the Neumann condition.

Definition at line 284 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



16.16.3.13 bool mtk::RobinBCDescriptor2D::ImposeOnWestBoundaryNoSpace (const Lap2D & *lap*, const UniStgGrid2D & *grid*, mtk::DenseMatrix & *matrix*, const Real & *time* = kZero) const [private]

Parameters

in	*lap*	Laplacian operator on the matrix.
in	*grid*	Grid upon which impose the desired boundary condition.
in,out	*matrix*	Input matrix with the Laplacian operator.
in	*time*	Current time snapshot. Default is kZero.

1. Impose the Dirichlet condition first.

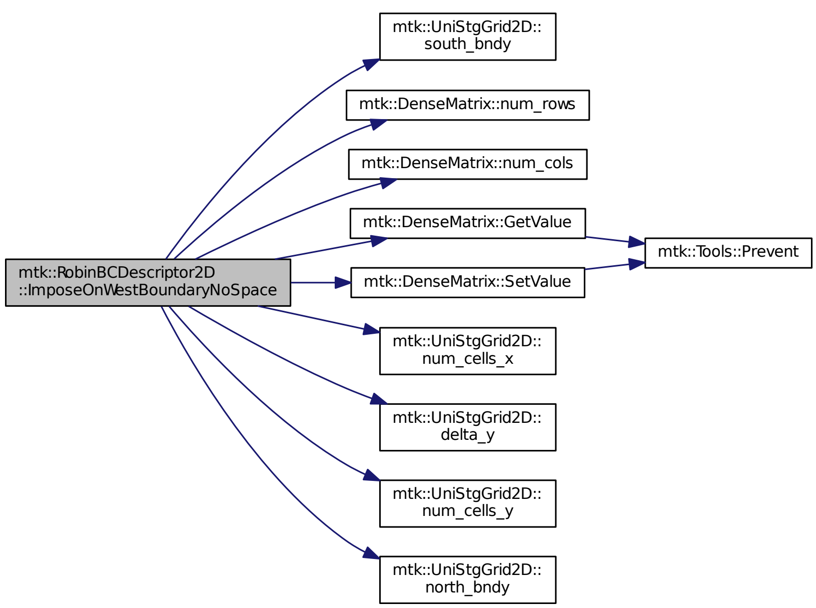
Note

As it can be seen, we must adopt a convention about how to treat the corners. Based on a reasoning with Otilio, we will take the **harmonic mean**.

1. Impose the Neumann condition.

Definition at line 399 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



16.16.3.14 bool mtk::RobinBCDescriptor2D::ImposeOnWestBoundaryWithSpace (const Lap2D & *lap*, const UniStgGrid2D & *grid*, mtk::DenseMatrix & *matrix*, const Real & *time* = kZero) const [private]

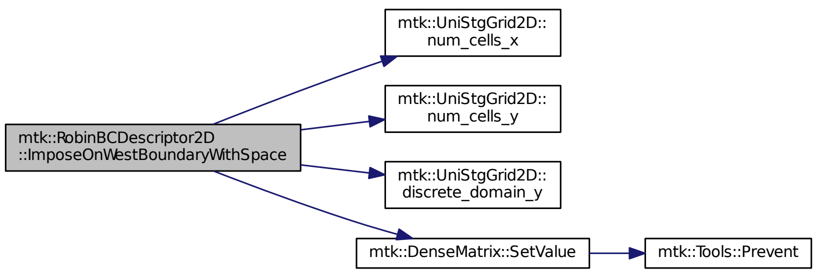
Parameters

in	*lap*	Laplacian operator on the matrix.
in	*grid*	Grid upon which impose the desired boundary condition.
in,out	*matrix*	Input matrix with the Laplacian operator.
in	*time*	Current time snapshot. Default is kZero.

1. Impose the Dirichlet condition first.
2. Impose the Neumann condition.

Definition at line 468 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



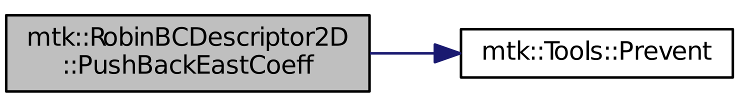
16.16.3.15 void mtk::RobinBCDescriptor2D::PushBackEastCoeff (mtk::CoefficientFunction1D *ce*)

Parameters

in	*cw*	Coeff. $c_e(y,t) : \partial\Omega \times [t_0,t_n] \mapsto \mathbb{R}$.

Definition at line 141 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



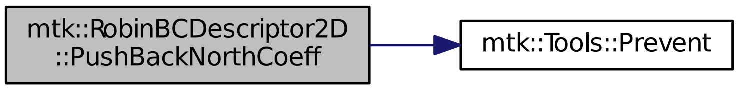
16.16.3.16 void mtk::RobinBCDescriptor2D::PushBackNorthCoeff (mtk::CoefficientFunction1D *cn*)

Parameters

in	*cw*	Coeff. $c_n(x,t) : \partial\Omega \times [t_0, t_n] \mapsto \mathbb{R}$.

Definition at line 169 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



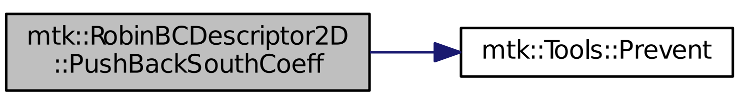
16.16.3.17 void mtk::RobinBCDescriptor2D::PushBackSouthCoeff (mtk::CoefficientFunction1D *cs*)

Parameters

in	*cw*	Coeff. $c_s(x,t) : \partial\Omega \times [t_0, t_n] \mapsto \mathbb{R}$.

Definition at line 155 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



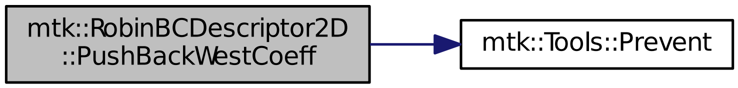
16.16.3.18 void mtk::RobinBCDescriptor2D::PushBackWestCoeff (mtk::CoefficientFunction1D *cw*)

Parameters

in	*cw*	Coeff. $c_w(y,t) : \partial\Omega \times [t_0, t_n] \mapsto \mathbb{R}$.

Definition at line 127 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



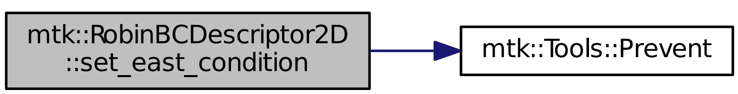
16.16.3.19 void mtk::RobinBCDescriptor2D::set_east_condition (Real(∗)(const Real &yy, const Real &tt) *east_condition*) [noexcept]

Parameters

in	*east_condition*	$\beta_e(y,t) : \partial\Omega \times [t_0, t_n] \mapsto \mathbb{R}$.

Definition at line 194 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



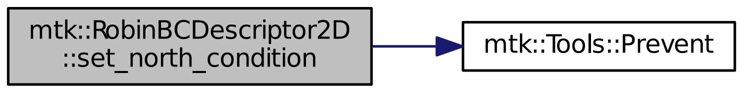
16.16.3.20 void mtk::RobinBCDescriptor2D::set_north_condition (Real(∗)(const Real &xx, const Real &tt) *north_condition*) [noexcept]

Parameters

in	*north_condition*	$\beta_n(x,t) : \partial\Omega \times [t_0, t_n] \mapsto \mathbb{R}$.

Definition at line 217 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



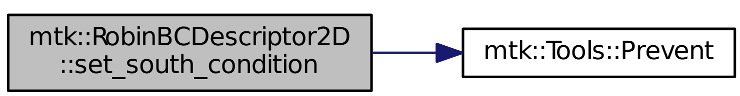
16.16.3.21 void mtk::RobinBCDescriptor2D::set_south_condition (Real(∗)(const Real &xx, const Real &tt) *south_condition*) [noexcept]

Parameters

in	*south_condition*	$\beta_s(x,t) : \partial\Omega \times [t_0, t_n] \mapsto \mathbb{R}$.

Definition at line 205 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



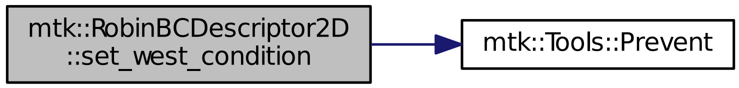
16.16.3.22 void mtk::RobinBCDescriptor2D::set_west_condition (Real(∗)(const Real &yy, const Real &tt) *west_condition*) [noexcept]

Parameters

in	*west_condition*	$\beta_w(y,t) : \partial\Omega \times [t_0, t_n] \mapsto \mathbb{R}$.

Definition at line 183 of file mtk_robin_bc_descriptor_2d.cc.

Here is the call graph for this function:



16.16.4 Member Data Documentation

16.16.4.1 std::vector<CoefficientFunction1D> mtk::RobinBCDescriptor2D::east_coefficients_ [private]

Definition at line 367 of file mtk_robin_bc_descriptor_2d.h.

16.16.4.2 Real(* mtk::RobinBCDescriptor2D::east_condition_)(const Real &xx, const Real &tt) [private]

Definition at line 372 of file mtk_robin_bc_descriptor_2d.h.

16.16.4.3 int mtk::RobinBCDescriptor2D::highest_order_diff_east_ [private]

Definition at line 362 of file mtk_robin_bc_descriptor_2d.h.

16.16.4.4 int mtk::RobinBCDescriptor2D::highest_order_diff_north_ [private]

Definition at line 364 of file mtk_robin_bc_descriptor_2d.h.

16.16.4.5 int mtk::RobinBCDescriptor2D::highest_order_diff_south_ [private]

Definition at line 363 of file mtk_robin_bc_descriptor_2d.h.

16.16.4.6 int mtk::RobinBCDescriptor2D::highest_order_diff_west_ [private]

Definition at line 361 of file mtk_robin_bc_descriptor_2d.h.

16.16.4.7 std::vector<CoefficientFunction1D> mtk::RobinBCDescriptor2D::north_coefficients_ [private]

Definition at line 369 of file mtk_robin_bc_descriptor_2d.h.

16.16.4.8 Real(* mtk::RobinBCDescriptor2D::north_condition_)(const Real &yy, const Real &tt) [private]

Definition at line 374 of file mtk_robin_bc_descriptor_2d.h.

16.16.4.9 std::vector<CoefficientFunction1D> mtk::RobinBCDescriptor2D::south_coefficients_ [private]

Definition at line 368 of file mtk_robin_bc_descriptor_2d.h.

16.16.4.10 Real(∗ mtk::RobinBCDescriptor2D::south_condition_)(const Real &yy, const Real &tt) [private]

Definition at line 373 of file mtk_robin_bc_descriptor_2d.h.

16.16.4.11 std::vector<CoefficientFunction1D> mtk::RobinBCDescriptor2D::west_coefficients_ [private]

Definition at line 366 of file mtk_robin_bc_descriptor_2d.h.

16.16.4.12 Real(∗ mtk::RobinBCDescriptor2D::west_condition_)(const Real &xx, const Real &tt) [private]

Definition at line 371 of file mtk_robin_bc_descriptor_2d.h.

The documentation for this class was generated from the following files:

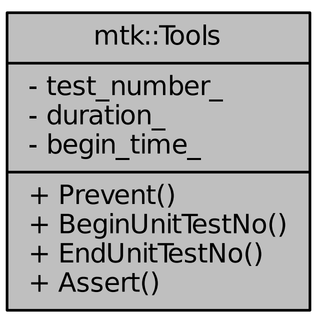
- include/mtk_robin_bc_descriptor_2d.h
- src/mtk_robin_bc_descriptor_2d.cc

16.17 mtk::Tools Class Reference

Tool manager class.

`#include <mtk_tools.h>`

Collaboration diagram for mtk::Tools:



Static Public Member Functions

- static void Prevent (const bool complement, const char ∗const fname, int lineno, const char ∗const fxname) noexcept

Enforces preconditions by preventing their complements from occur.

- static void BeginUnitTestNo (const int &nn) noexcept

  Begins the execution of a unit test. Starts a timer.
- static void EndUnitTestNo (const int &nn) noexcept

  Ends the execution of a unit test. Stops and reports wall-clock time.
- static void Assert (const bool &condition) noexcept

  Asserts if the condition required to pass the unit test occurs.

Static Private Attributes

- static int test_number_

  Current test being executed.
- static Real duration_

  Duration of the current test.
- static clock_t begin_time_

  Elapsed time on current test.

16.17.1 Detailed Description

Basic tools to ensure execution correctness.

Definition at line 78 of file mtk_tools.h.

16.17.2 Member Function Documentation

16.17.2.1 void mtk::Tools::Assert (const bool & *condition*) [static], [noexcept]

Parameters

in	*condition*	Condition to be asserted.

Definition at line 109 of file mtk_tools.cc.

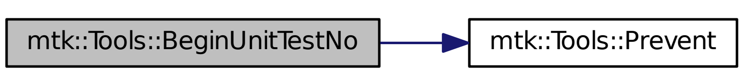
16.17.2.2 void mtk::Tools::BeginUnitTestNo (const int & *nn*) [static], [noexcept]

Parameters

in	*nn*	Number of the test.

Definition at line 88 of file mtk_tools.cc.

Here is the call graph for this function:



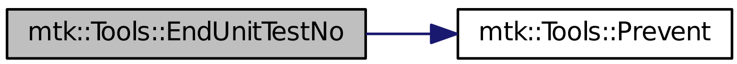
16.17.2.3 void mtk::Tools::EndUnitTestNo (const int & *nn*) [static], [noexcept]

Parameters

in	*nn*	Number of the test.

Definition at line 100 of file mtk_tools.cc.

Here is the call graph for this function:



16.17.2.4 void mtk::Tools::Prevent (const bool *complement*, const char ∗const *fname*, int *lineno*, const char ∗const *fxname*) [static], [noexcept]

See also

http://stackoverflow.com/questions/8884335/print-the-file-name-line-number-and-function

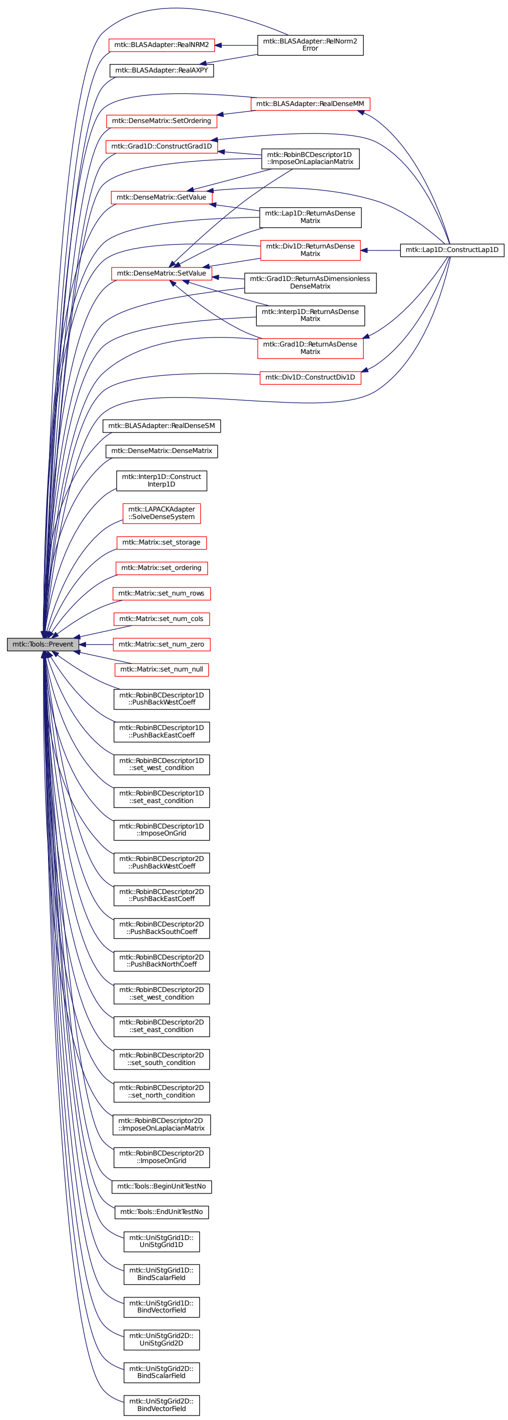
Parameters

in	*complement*	Complement of desired pre-condition.
in	*fname*	Name of the file being checked.
in	*lineno*	Number of the line where the check is executed.
in	*fxname*	Name of the module containing the check.

Todo Check if this is the best way of stalling execution.

Definition at line 61 of file mtk_tools.cc.

Here is the caller graph for this function:



16.17.3 Member Data Documentation

16.17.3.1 clock_t mtk::Tools::begin_time_ [static], [private]

Definition at line 121 of file mtk_tools.h.

16.17.3.2 mtk::Real mtk::Tools::duration_ [static], [private]

Definition at line 119 of file mtk_tools.h.

16.17.3.3 int mtk::Tools::test_number_ [static], [private]

Todo Check usage of static methods and private members.

Definition at line 117 of file mtk_tools.h.

The documentation for this class was generated from the following files:

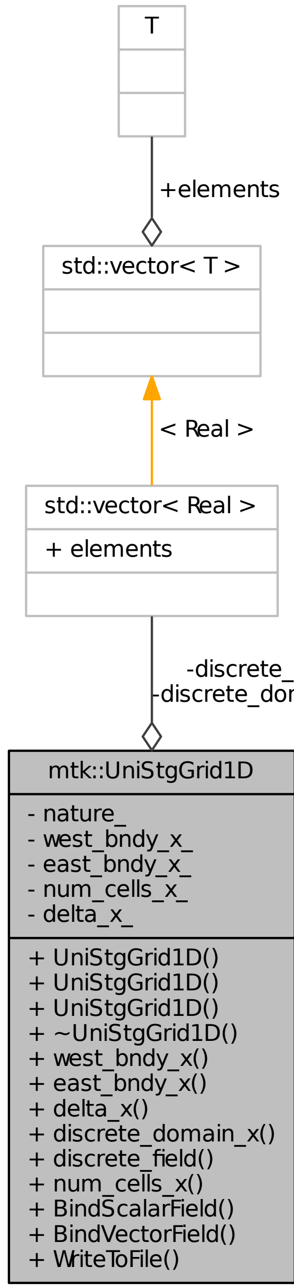
- include/mtk_tools.h
- src/mtk_tools.cc

16.18 mtk::UniStgGrid1D Class Reference

Uniform 1D Staggered Grid.

`#include <mtk_uni_stg_grid_1d.h>`

Collaboration diagram for mtk::UniStgGrid1D:



Public Member Functions

- UniStgGrid1D ()

Default constructor.

- UniStgGrid1D (const UniStgGrid1D &grid)

    Copy constructor.

- UniStgGrid1D (const Real &west_bndy_x, const Real &east_bndy_x, const int &num_cells_x, const mtk::Field←Nature &nature=mtk::SCALAR)

    Construct a grid based on spatial discretization parameters.

- ∼UniStgGrid1D ()

    Destructor.

- Real west_bndy_x () const

    Provides access to west boundary spatial coordinate.

- Real east_bndy_x () const

    Provides access to east boundary spatial coordinate.

- Real delta_x () const

    Provides access to the computed $ x $.

- const Real ∗ discrete_domain_x () const

    Provides access to the grid spatial data.

- Real ∗ discrete_field ()

    Provides access to the grid field data.

- int num_cells_x () const

    Provides access to the number of cells of the grid.

- void BindScalarField (Real(∗ScalarField)(const Real &xx))

    Binds a given scalar field to the grid.

- void BindVectorField (Real(∗VectorField)(Real xx))

    Binds a given vector field to the grid.

- bool WriteToFile (std::string filename, std::string space_name, std::string field_name) const

    Writes grid to a file compatible with gnuplot 4.6.

Private Attributes

- FieldNature nature_

    Nature of the discrete field.

- std::vector< Real > discrete_domain_x_

    Array of spatial data.

- std::vector< Real > discrete_field_

    Array of field's data.

- Real west_bndy_x_

    West boundary spatial coordinate.

- Real east_bndy_x_

    East boundary spatial coordinate.

- Real num_cells_x_

    Number of cells discretizing the domain.

- Real delta_x_

    Produced Δx.

Friends

- std::ostream & operator<< (std::ostream &stream, UniStgGrid1D &in)

    Prints the grid as a tuple of arrays.

16.18.1 Detailed Description

Uniform 1D Staggered Grid.

Definition at line 77 of file mtk_uni_stg_grid_1d.h.

16.18.2 Constructor & Destructor Documentation

16.18.2.1 mtk::UniStgGrid1D::UniStgGrid1D ( )

Definition at line 99 of file mtk_uni_stg_grid_1d.cc.

16.18.2.2 mtk::UniStgGrid1D::UniStgGrid1D (const UniStgGrid1D & *grid*)

Parameters

in	*grid*	Given grid.

Definition at line 108 of file mtk_uni_stg_grid_1d.cc.

16.18.2.3 mtk::UniStgGrid1D::UniStgGrid1D (const Real & *west_bndy_x*, const Real & *east_bndy_x*, const int & *num_cells_x*, const mtk::FieldNature & *nature* = mtk::SCALAR)

Parameters

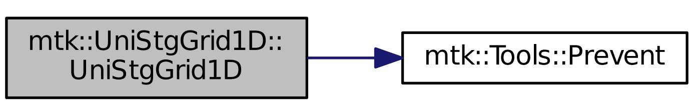
in	*west_bndy_x*	Coordinate for the west boundary.
in	*east_bndy_x*	Coordinate for the east boundary.
in	*num_cells_x*	Number of cells of the required grid.
in	*nature*	Nature of the discrete field to hold.

See also

mtk::FieldNature

Definition at line 124 of file mtk_uni_stg_grid_1d.cc.

Here is the call graph for this function:



16.18.2.4 mtk::UniStgGrid1D::∼UniStgGrid1D ( )

Definition at line 144 of file mtk_uni_stg_grid_1d.cc.

16.18.3 Member Function Documentation

16.18.3.1 void mtk::UniStgGrid1D::BindScalarField (Real(∗)(const Real &xx) *ScalarField*)

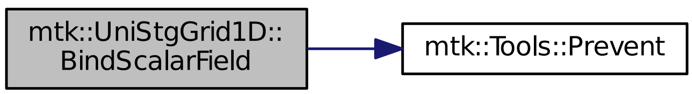
Parameters

in	*ScalarField*	Pointer to the function implementing the scalar field.

1. Create collection of spatial coordinates.
2. Create collection of field samples.

Definition at line 176 of file mtk_uni_stg_grid_1d.cc.

Here is the call graph for this function:



16.18.3.2 void mtk::UniStgGrid1D::BindVectorField (Real(∗)(Real xx) *VectorField*)

We assume the field to be of the form:

$$\mathbf{v}(x) = v(x)\hat{\mathbf{i}}$$

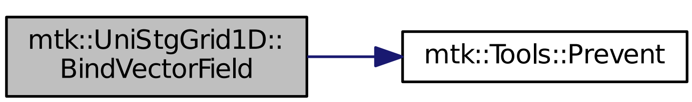
Parameters

in	*VectorField*	Pointer to the function implementing the vector field.

1. Create collection of spatial coordinates.
2. Create collection of field samples.

Definition at line 212 of file mtk_uni_stg_grid_1d.cc.

Here is the call graph for this function:



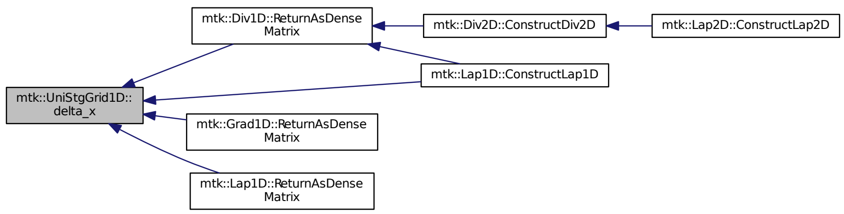
16.18.3.3 mtk::Real mtk::UniStgGrid1D::delta_x ( ) const

Returns

Computed $ x $.

Definition at line 156 of file mtk_uni_stg_grid_1d.cc.

Here is the caller graph for this function:



16.18.3.4 const mtk::Real * mtk::UniStgGrid1D::discrete_domain_x ( ) const

Returns

Pointer to the spatial data.

Todo Review const-correctness of the pointer we return.

Definition at line 161 of file mtk_uni_stg_grid_1d.cc.

16.18.3.5 mtk::Real * mtk::UniStgGrid1D::discrete_field ( )

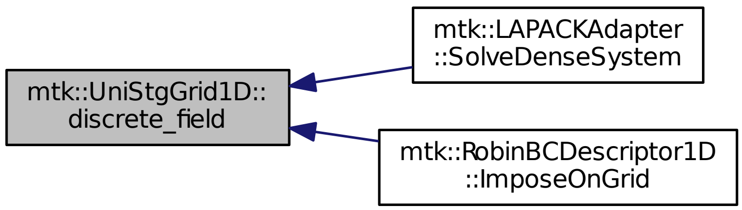
Returns

Pointer to the field data.

Todo Review const-correctness of the pointer we return. Look at the STL!

Definition at line 166 of file mtk_uni_stg_grid_1d.cc.

Here is the caller graph for this function:



16.18.3.6 mtk::Real mtk::UniStgGrid1D::east_bndy_x ( ) const

Returns

East boundary spatial coordinate.

Definition at line 151 of file mtk_uni_stg_grid_1d.cc.

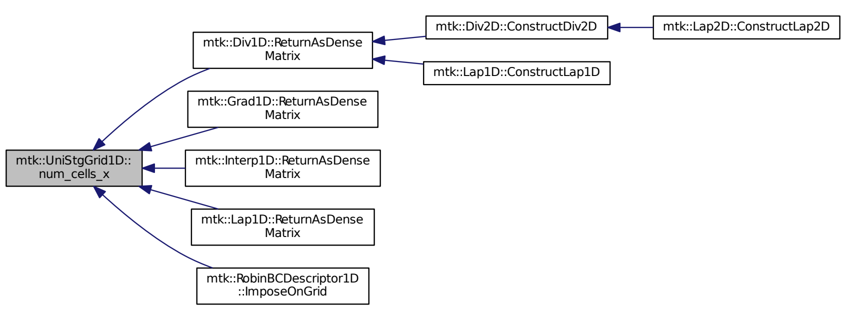
16.18.3.7 int mtk::UniStgGrid1D::num_cells_x ( ) const

Returns

Number of cells of the grid.

Definition at line 171 of file mtk_uni_stg_grid_1d.cc.

Here is the caller graph for this function:



16.18.3.8 mtk::Real mtk::UniStgGrid1D::west_bndy_x ( ) const

Returns

West boundary spatial coordinate.

Definition at line 146 of file mtk_uni_stg_grid_1d.cc.

16.18.3.9 bool mtk::UniStgGrid1D::WriteToFile (std::string *filename*, std::string *space_name*, std::string *field_name*) const

Parameters

in	*filename*	Name of the output file.
in	*space_name*	Name for the first column of the data.
in	*field_name*	Name for the second column of the data.

Returns

Success of the file writing process.

See also

http://www.gnuplot.info/

Definition at line 240 of file mtk_uni_stg_grid_1d.cc.

16.18.4 Friends And Related Function Documentation

16.18.4.1 std::ostream& operator<< (std::ostream & *stream*, mtk::UniStgGrid1D & *in*) [friend]

1. Print spatial coordinates.
2. Print scalar field.

Definition at line 68 of file mtk_uni_stg_grid_1d.cc.

16.18.5 Member Data Documentation

16.18.5.1 Real mtk::UniStgGrid1D::delta_x_ [private]

Definition at line 200 of file mtk_uni_stg_grid_1d.h.

16.18.5.2 std::vector<Real> mtk::UniStgGrid1D::discrete_domain_x_ [private]

Definition at line 194 of file mtk_uni_stg_grid_1d.h.

16.18.5.3 std::vector<Real> mtk::UniStgGrid1D::discrete_field_ [private]

Definition at line 195 of file mtk_uni_stg_grid_1d.h.

16.18.5.4 Real mtk::UniStgGrid1D::east_bndy_x_ [private]

Definition at line 198 of file mtk_uni_stg_grid_1d.h.

16.18.5.5 FieldNature mtk::UniStgGrid1D::nature_ [private]

Definition at line 192 of file mtk_uni_stg_grid_1d.h.

16.18.5.6 Real mtk::UniStgGrid1D::num_cells_x_ [private]

Definition at line 199 of file mtk_uni_stg_grid_1d.h.

16.18.5.7 Real mtk::UniStgGrid1D::west_bndy_x_ [private]

Definition at line 197 of file mtk_uni_stg_grid_1d.h.

The documentation for this class was generated from the following files:

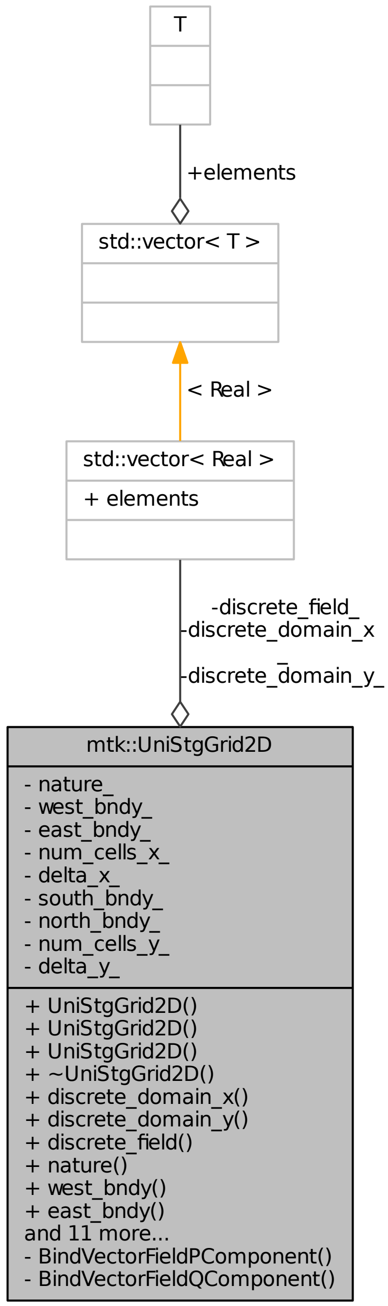
- include/mtk_uni_stg_grid_1d.h
- src/mtk_uni_stg_grid_1d.cc

16.19 mtk::UniStgGrid2D Class Reference

Uniform 2D Staggered Grid.

`#include <mtk_uni_stg_grid_2d.h>`

Collaboration diagram for mtk::UniStgGrid2D:



Public Member Functions

- UniStgGrid2D ()

Default constructor.

- UniStgGrid2D (const UniStgGrid2D &grid)

  Copy constructor.

- UniStgGrid2D (const Real &west_bndy_x, const Real &east_bndy_x, const int &num_cells_x, const Real &south_bndy_y, const Real &north_bndy_y, const int &num_cells_y, const mtk::FieldNature &nature=mtk::S↩ CALAR)

  Construct a grid based on spatial discretization parameters.

- ∼UniStgGrid2D ()

  Destructor.

- const Real ∗ discrete_domain_x () const

  Provides access to the grid spatial data.

- const Real ∗ discrete_domain_y () const

  Provides access to the grid spatial data.

- Real ∗ discrete_field ()

  Provides access to the grid field data.

- FieldNature nature () const

  Physical nature of the data bound to the grid.

- Real west_bndy () const

  Provides access to west boundary spatial coordinate.

- Real east_bndy () const

  Provides access to east boundary spatial coordinate.

- int num_cells_x () const

  Provides access to the number of cells of the grid.

- Real delta_x () const

  Provides access to the computed $ x $.

- Real south_bndy () const

  Provides access to south boundary spatial coordinate.

- Real north_bndy () const

  Provides access to north boundary spatial coordinate.

- int num_cells_y () const

  Provides access to the number of cells of the grid.

- Real delta_y () const

  Provides access to the computed $ y $.

- bool Bound () const

  Have any field been bound to the grid?

- int Size () const

  Total number of samples in the grid.

- void BindScalarField (Real(∗ScalarField)(const Real &xx, const Real &yy))

  Binds a given scalar field to the grid.

- void BindVectorField (Real(∗VectorFieldPComponent)(const Real &xx, const Real &yy), Real(∗VectorFieldQ↩ Component)(const Real &xx, const Real &yy))

  Binds a given vector field to the grid.

- bool WriteToFile (std::string filename, std::string space_name_x, std::string space_name_y, std::string field_↩ name) const

  Writes grid to a file compatible with Gnuplot 4.6.

Private Member Functions

- void BindVectorFieldPComponent (Real(∗VectorFieldPComponent)(const Real &xx, const Real &yy))

  Binds a given component of a vector field to the grid.
- void BindVectorFieldQComponent (Real(∗VectorFieldQComponent)(const Real &xx, const Real &yy))

  Binds a given component of a vector field to the grid.

Private Attributes

- std::vector< Real > discrete_domain_x_

  Array of spatial data.
- std::vector< Real > discrete_domain_y_

  Array of spatial data.
- std::vector< Real > discrete_field_

  Array of field's data.
- FieldNature nature_

  Nature of the discrete field.
- Real west_bndy_

  West boundary spatial coordinate.
- Real east_bndy_

  East boundary spatial coordinate.
- int num_cells_x_

  Number of cells discretizing the domain.
- Real delta_x_

  Computed Δx.
- Real south_bndy_

  West boundary spatial coordinate.
- Real north_bndy_

  East boundary spatial coordinate.
- int num_cells_y_

  Number of cells discretizing the domain.
- Real delta_y_

  Computed Δy.

Friends

- std::ostream & operator<< (std::ostream &stream, UniStgGrid2D &in)

  Prints the grid as a tuple of arrays.

16.19.1 Detailed Description

Uniform 2D Staggered Grid.

Definition at line 79 of file mtk_uni_stg_grid_2d.h.

16.19.2 Constructor & Destructor Documentation

16.19.2.1 mtk::UniStgGrid2D::UniStgGrid2D ( )

Definition at line 131 of file mtk_uni_stg_grid_2d.cc.

16.19.2.2 mtk::UniStgGrid2D::UniStgGrid2D (const **UniStgGrid2D** & *grid*)

Parameters

in	*grid*	Given grid.

Definition at line 145 of file mtk_uni_stg_grid_2d.cc.

16.19.2.3 mtk::UniStgGrid2D::UniStgGrid2D (const **Real** & *west_bndy_x,* const **Real** & *east_bndy_x,* const int & *num_cells_x,* const **Real** & *south_bndy_y,* const **Real** & *north_bndy_y,* const int & *num_cells_y,* const **mtk::FieldNature** & *nature* = **mtk::SCALAR**)

Parameters

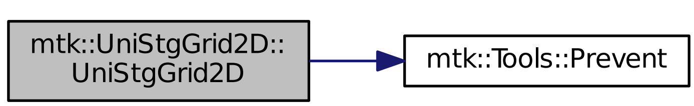
in	*west_bndy_x*	Coordinate for the west boundary.
in	*east_bndy_x*	Coordinate for the east boundary.
in	*num_cells_x*	Number of cells of the required grid.
in	*south_bndy_y*	Coordinate for the west boundary.
in	*north_bndy_y*	Coordinate for the east boundary.
in	*num_cells_y*	Number of cells of the required grid.
in	*nature*	Nature of the discrete field to hold.

See also

mtk::FieldNature

Definition at line 169 of file mtk_uni_stg_grid_2d.cc.

Here is the call graph for this function:



16.19.2.4 mtk::UniStgGrid2D::∼UniStgGrid2D ( )

Definition at line 203 of file mtk_uni_stg_grid_2d.cc.

16.19.3 Member Function Documentation

16.19.3.1 void mtk::UniStgGrid2D::BindScalarField (Real(∗)(const Real &xx, const Real &yy) *ScalarField*)

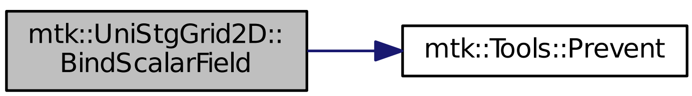
Parameters

in	*ScalarField*	Pointer to the function implementing the scalar field.

1. Create collection of spatial coordinates for x.
2. Create collection of spatial coordinates for y.
3. Create collection of field samples.

Definition at line 275 of file mtk_uni_stg_grid_2d.cc.

Here is the call graph for this function:



16.19.3.2 void mtk::UniStgGrid2D::BindVectorField (Real(∗)(const Real &xx, const Real &yy) *VectorFieldPComponent,* Real(∗)(const Real &xx, const Real &yy) *VectorFieldQComponent*)

We assume the field to be of the form:

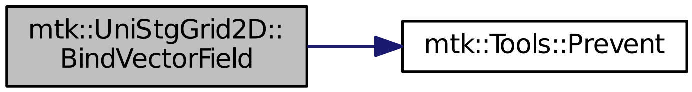
$$\mathbf{v}(x) = p(x,y)\hat{\mathbf{i}} + q(x,y)\hat{\mathbf{j}}$$

Parameters

in	*VectorFieldP↩ Component*	Pointer to the function implementing the $ p $ component of the vector field.
in	*VectorFieldP↩ Component*	Pointer to the function implementing the $ q $ component of the vector field.

Definition at line 423 of file mtk_uni_stg_grid_2d.cc.

Here is the call graph for this function:



16.19.3.3 void mtk::UniStgGrid2D::BindVectorFieldPComponent (Real(∗)(const Real &xx, const Real &yy) *VectorFieldPComponent*) [private]

We assume the field to be of the form:

$$\mathbf{v}(x) = p(x,y)\hat{\mathbf{i}} + q(x,y)\hat{\mathbf{j}}$$

Parameters

in	*BindVectorField←PComponent*	Pointer to the function implementing the $ p $ component of the vector field.

1. Create collection of spatial coordinates for x.
2. Create collection of spatial coordinates for y.
3. Allocate space for discrete vector field and bind $ p $ component.

Definition at line 330 of file mtk_uni_stg_grid_2d.cc.

16.19.3.4 void mtk::UniStgGrid2D::BindVectorFieldQComponent (Real(∗)(const Real &xx, const Real &yy) *VectorFieldQComponent*) [private]

We assume the field to be of the form:

$$\mathbf{v}(x) = p(x,y)\hat{\mathbf{i}} + q(x,y)\hat{\mathbf{j}}$$

Parameters

in	*BindVectorField←QComponent*	Pointer to the function implementing the $ q $ component of the vector field.

1. Bind $ q $ component, since $ p $ component has already been bound.

Definition at line 395 of file mtk_uni_stg_grid_2d.cc.

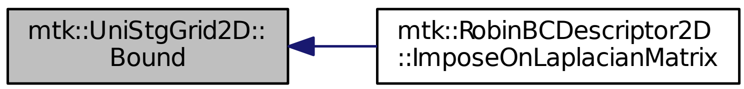
16.19.3.5 bool mtk::UniStgGrid2D::Bound ( ) const

Returns

True is a field has been bound.

Definition at line 255 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



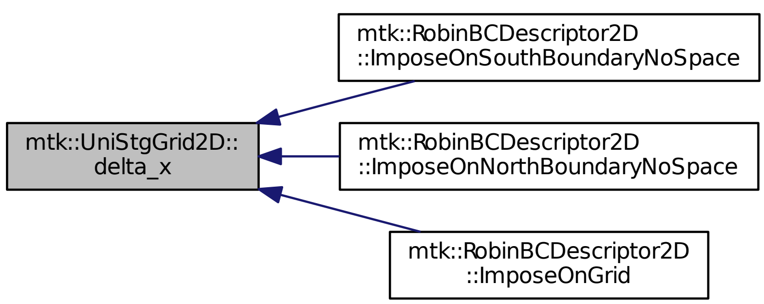
16.19.3.6 mtk::Real mtk::UniStgGrid2D::delta_x ( ) const

Returns

Computed $ x $.

Definition at line 225 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



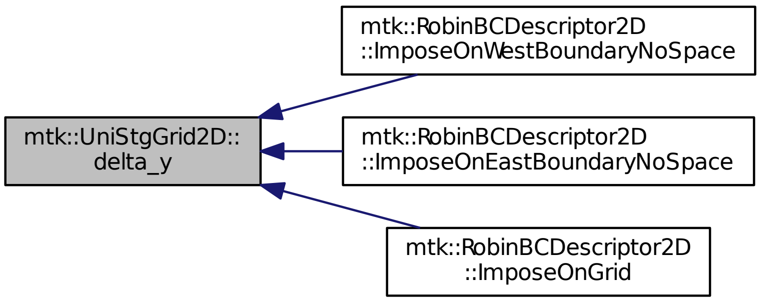
16.19.3.7 mtk::Real mtk::UniStgGrid2D::delta_y ( ) const

Returns

Computed $ y $.

Definition at line 250 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



16.19.3.8 const mtk::Real * mtk::UniStgGrid2D::discrete_domain_x ( ) const

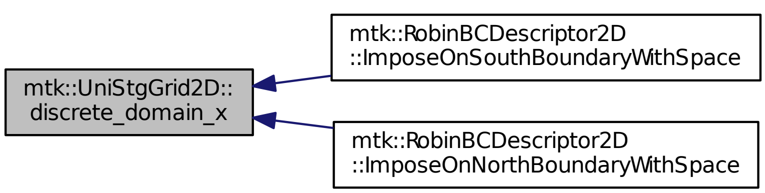
Returns

Pointer to the spatial data.

Todo Review const-correctness of the pointer we return.

Definition at line 230 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



16.19.3.9 const mtk::Real * mtk::UniStgGrid2D::discrete_domain_y ( ) const

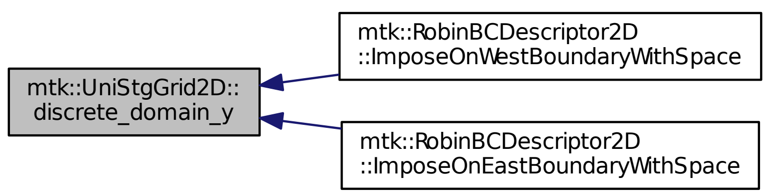
Returns

Pointer to the spatial data.

Todo Review const-correctness of the pointer we return.

Definition at line 260 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



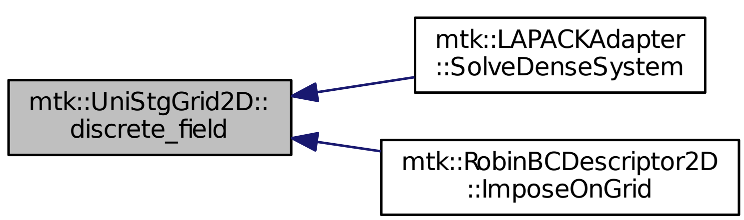
16.19.3.10 mtk::Real ∗ mtk::UniStgGrid2D::discrete_field ( )

Returns

Pointer to the field data.

Definition at line 265 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



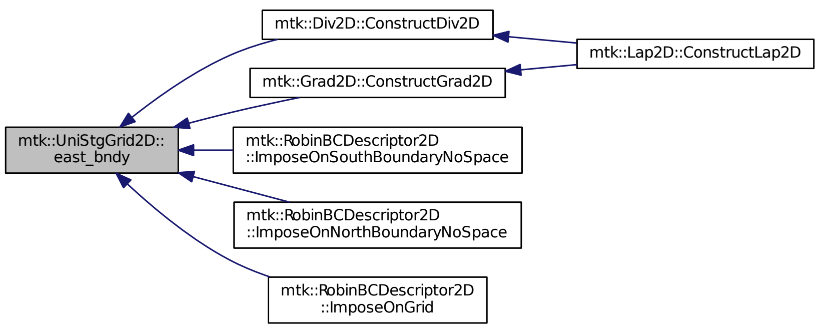
16.19.3.11 mtk::Real mtk::UniStgGrid2D::east_bndy ( ) const

Returns

East boundary spatial coordinate.

Definition at line 215 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



16.19.3.12 mtk::FieldNature mtk::UniStgGrid2D::nature ( ) const

Returns

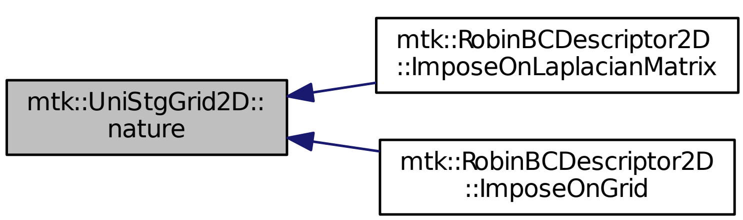
Value of an enumeration.

See also

mtk::FieldNature

Definition at line 205 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



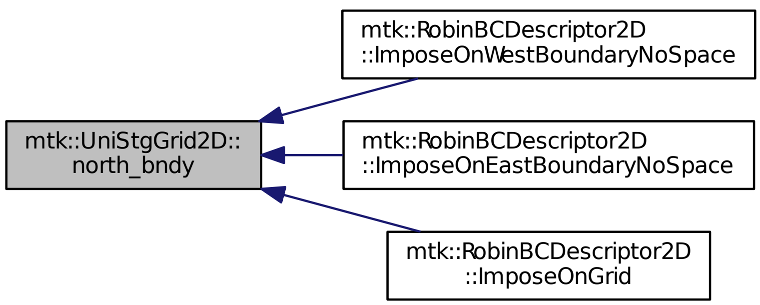
16.19.3.13 mtk::Real mtk::UniStgGrid2D::north_bndy ( ) const

Returns

North boundary spatial coordinate.

Definition at line 240 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



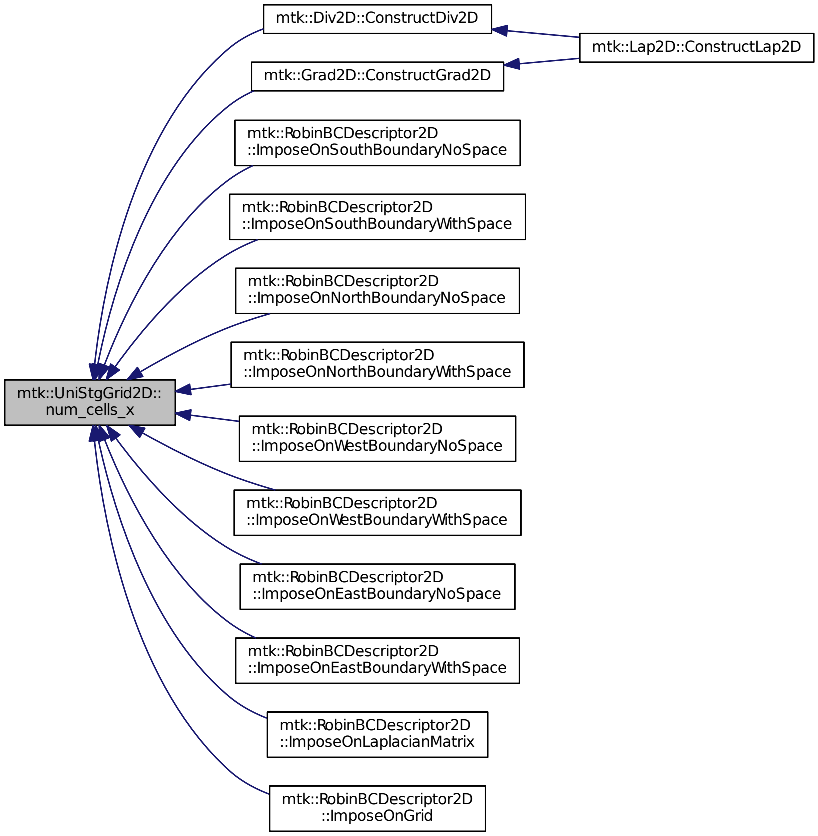
16.19.3.14 int mtk::UniStgGrid2D::num_cells_x ( ) const

Returns

Number of cells of the grid.

Definition at line 220 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



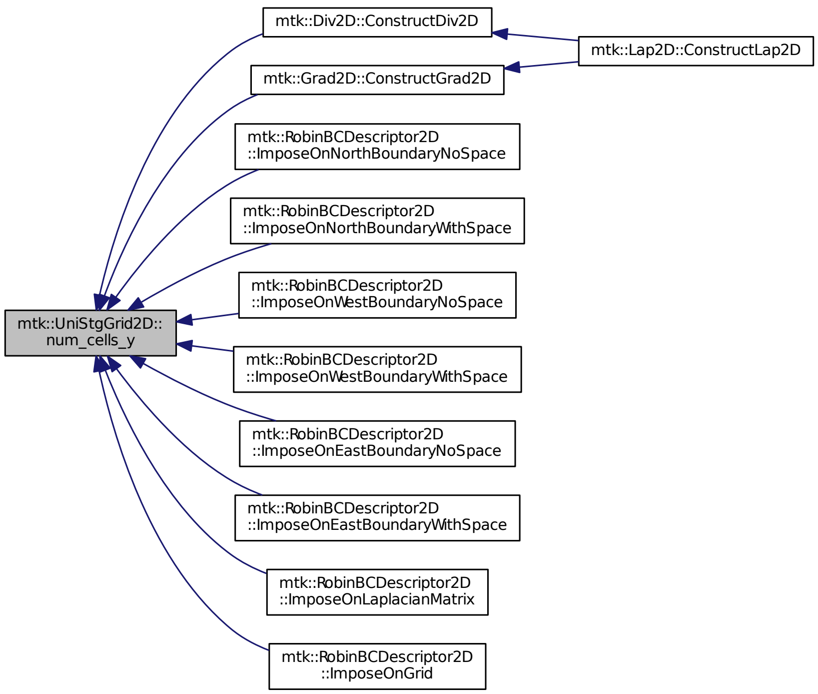
16.19.3.15 int mtk::UniStgGrid2D::num_cells_y ( ) const

Returns

Number of cells of the grid.

Definition at line 245 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



16.19.3.16 int mtk::UniStgGrid2D::Size ( ) const

Returns

Total number of samples in the grid.

Definition at line 270 of file mtk_uni_stg_grid_2d.cc.

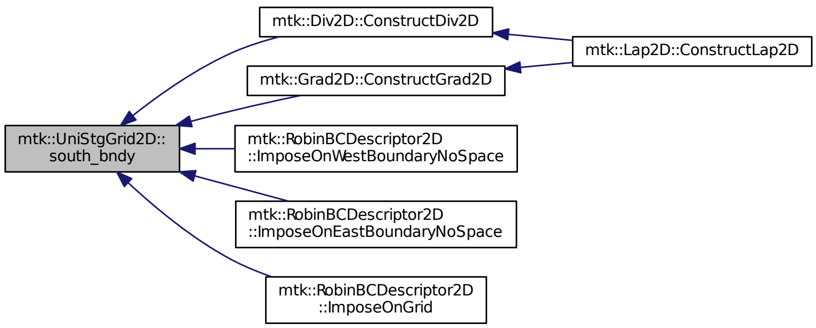
16.19.3.17 mtk::Real mtk::UniStgGrid2D::south_bndy ( ) const

Returns

South boundary spatial coordinate.

Definition at line 235 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



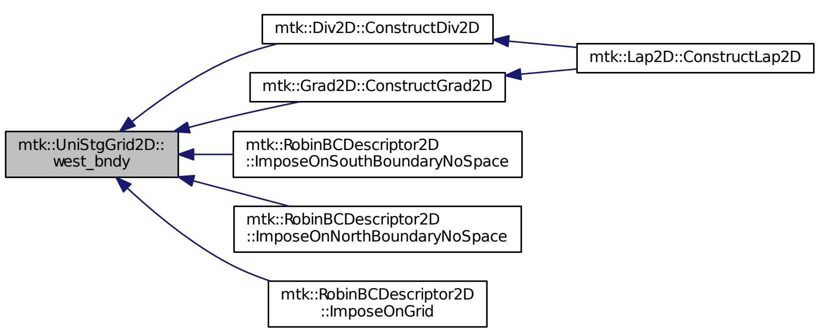
16.19.3.18 mtk::Real mtk::UniStgGrid2D::west_bndy ( ) const

Returns

West boundary spatial coordinate.

Definition at line 210 of file mtk_uni_stg_grid_2d.cc.

Here is the caller graph for this function:



16.19.3.19 bool mtk::UniStgGrid2D::WriteToFile (std::string *filename*, std::string *space_name_x*, std::string *space_name_y*, std::string *field_name*) const

Parameters

in	*filename*	Name of the output file.
in	*space_name_x*	Name for the first column of the (spatial) data.
in	*space_name_y*	Name for the second column of the (spatial) data.
in	*field_name*	Name for the second column of the (physical field) data.

Returns

Success of the file writing process.

See also

http://www.gnuplot.info/

Write the values of the p component, with a null q component.

Write the values of the q component, with a null p component.

Definition at line 435 of file mtk_uni_stg_grid_2d.cc.

16.19.4 Friends And Related Function Documentation

16.19.4.1 std::ostream& operator<< (std::ostream & *stream,* mtk::UniStgGrid2D & *in*) [friend]

1. Print spatial coordinates.
2. Print scalar field.

Definition at line 67 of file mtk_uni_stg_grid_2d.cc.

16.19.5 Member Data Documentation

16.19.5.1 Real mtk::UniStgGrid2D::delta_x_ [private]

Definition at line 305 of file mtk_uni_stg_grid_2d.h.

16.19.5.2 Real mtk::UniStgGrid2D::delta_y_ [private]

Definition at line 310 of file mtk_uni_stg_grid_2d.h.

16.19.5.3 std::vector<Real> mtk::UniStgGrid2D::discrete_domain_x_ [private]

Definition at line 296 of file mtk_uni_stg_grid_2d.h.

16.19.5.4 std::vector<Real> mtk::UniStgGrid2D::discrete_domain_y_ [private]

Definition at line 297 of file mtk_uni_stg_grid_2d.h.

16.19.5.5 std::vector< Real > mtk::UniStgGrid2D::discrete_field_ [private]

Definition at line 298 of file mtk_uni_stg_grid_2d.h.

16.19.5.6 Real mtk::UniStgGrid2D::east_bndy_ [private]

Definition at line 303 of file mtk_uni_stg_grid_2d.h.

16.19.5.7 FieldNature mtk::UniStgGrid2D::nature_ [private]

Definition at line 300 of file mtk_uni_stg_grid_2d.h.

16.19.5.8 Real mtk::UniStgGrid2D::north_bndy_ [private]

Definition at line 308 of file mtk_uni_stg_grid_2d.h.

16.19.5.9 int mtk::UniStgGrid2D::num_cells_x_ [private]

Definition at line 304 of file mtk_uni_stg_grid_2d.h.

16.19.5.10 int mtk::UniStgGrid2D::num_cells_y_ [private]

Definition at line 309 of file mtk_uni_stg_grid_2d.h.

16.19.5.11 Real mtk::UniStgGrid2D::south_bndy_ [private]

Definition at line 307 of file mtk_uni_stg_grid_2d.h.

16.19.5.12 Real mtk::UniStgGrid2D::west_bndy_ [private]

Definition at line 302 of file mtk_uni_stg_grid_2d.h.

The documentation for this class was generated from the following files:

- include/mtk_uni_stg_grid_2d.h
- src/mtk_uni_stg_grid_2d.cc

Chapter 17

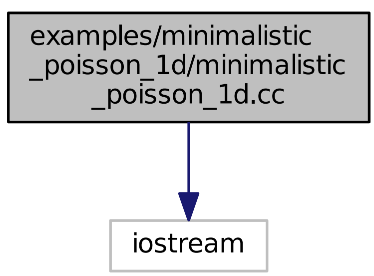
File Documentation

17.1 examples/minimalistic_poisson_1d/minimalistic_poisson_1d.cc File Reference

Poisson Equation on a 1D Uniform Staggered Grid with Robin BCs.

`#include <iostream>`

Include dependency graph for minimalistic_poisson_1d.cc:



Functions

- int main ()

17.1.1 Detailed Description

We solve:

$$-\nabla^2 p(x) = s(x),$$

for $x \in \Omega = [a,b] = [0,1]$.

The source term function is defined as:

$$s(x) = -\frac{\lambda^2 \exp(\lambda x)}{\exp(\lambda) - 1},$$

where $\lambda = -1$ is a real-valued parameter.

We consider Robin's boundary conditions of the form:

$$\alpha p(a) - \beta p'(a) = \omega,$$

$$\alpha p(b) + \beta p'(b) = \varepsilon,$$

where $\alpha = -\exp(\lambda)$, $\beta = (\exp(\lambda) - 1.0)/\lambda$, $\omega = -1$, and $\varepsilon = 0$.

The analytical solution for this problem is given by:

$$p(x) = \frac{\exp(\lambda x) - 1}{\exp(\lambda) - 1}.$$

The mimetic counterpart of this equation is:

$$-\breve{\mathbf{L}}_x^k \tilde{p} = \tilde{s}.$$

Finally, we will solve this problem considering $k = 2$.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file minimalistic_poisson_1d.cc.

17.1.2 Function Documentation

17.1.2.1 int main ( )

Definition at line 164 of file minimalistic_poisson_1d.cc.

17.2 minimalistic_poisson_1d.cc

```
00001
00043 /*
00044 Copyright (C) 2015, Computational Science Research Center, San Diego State
00045 University. All rights reserved.
00046
00047 Redistribution and use in source and binary forms, with or without modification,
00048 are permitted provided that the following conditions are met:
00049
00050 1. Modifications to source code should be reported to: esanchez@mail.sdsu.edu
00051 and a copy of the modified files should be reported once modifications are
00052 completed, unless these modifications are made through the project's GitHub
00053 page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
00054 should be developed and included in any deliverable.
00055
00056 2. Redistributions of source code must be done through direct
00057 downloads from the project's GitHub page: http://www.csrc.sdsu.edu/mtk
00058
00059 3. Redistributions in binary form must reproduce the above copyright notice,
00060 this list of conditions and the following disclaimer in the documentation and/or
00061 other materials provided with the distribution.
00062
00063 4. Usage of the binary form on proprietary applications shall require explicit
00064 prior written permission from the the copyright holders, and due credit should
00065 be given to the copyright holders.
00066
00067 5. Neither the name of the copyright holder nor the names of its contributors
00068 may be used to endorse or promote products derived from this software without
00069 specific prior written permission.
00070
00071 The copyright holders provide no reassurances that the source code provided does
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WARRANTIES OF MERCHANTABILITY AND FITNESS FOR A PARTICULAR PURPOSE ARE
DISCLAIMED. IN NO EVENT SHALL THE COPYRIGHT HOLDER OR CONTRIBUTORS BE LIABLE FOR
ANY DIRECT, INDIRECT, INCIDENTAL, SPECIAL, EXEMPLARY, OR CONSEQUENTIAL DAMAGES
(INCLUDING, BUT NOT LIMITED TO, PROCUREMENT OF SUBSTITUTE GOODS OR SERVICES;
LOSS OF USE, DATA, OR PROFITS; OR BUSINESS INTERRUPTION) HOWEVER CAUSED AND ON
ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT
(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#if __cplusplus == 201103L

#include <iostream>
#include <fstream>
#include <cmath>
#include <vector>

#include "mtk.h"

mtk::Real Alpha(const mtk::Real &tt) {
  mtk::Real lambda = -1.0;
  return -exp(lambda);
}

mtk::Real Beta(const mtk::Real &tt) {
  mtk::Real lambda = -1.0;
  return (exp(lambda) - 1.0)/lambda;
};

mtk::Real Omega(const mtk::Real &tt) { return -1.0; };

mtk::Real Epsilon(const mtk::Real &tt) { return 0.0; };

mtk::Real Source(const mtk::Real &xx) {
  mtk::Real lambda = -1.0;
  return lambda*lambda*exp(lambda*xx)/(exp(lambda) - 1.0);
}

mtk::Real KnownSolution(const mtk::Real &xx) {
  mtk::Real lambda = -1.0;
  return (exp(lambda*xx) - 1.0)/(exp(lambda) - 1.0);
}

int main () {

  mtk::Real west_bndy_x{};
  mtk::Real east_bndy_x{1.0};
  int num_cells_x{5};
  mtk::Lap1D lap;
  if (!lap.ConstructLap1D()) {
    return EXIT_FAILURE;
  }
  mtk::UniStgGrid1D source(west_bndy_x, east_bndy_x, num_cells_x);
  mtk::UniStgGrid1D comp_sol(west_bndy_x, east_bndy_x, num_cells_x);
  mtk::UniStgGrid1D known_sol(west_bndy_x, east_bndy_x, num_cells_x);
  mtk::DenseMatrix lapm(lap.ReturnAsDenseMatrix(comp_sol));
  source.BindScalarField(Source);
  mtk::RobinBCDescriptor1D bcs;
  bcs.PushBackWestCoeff(Alpha);
  bcs.PushBackWestCoeff(Beta);
  bcs.PushBackEastCoeff(Alpha);
  bcs.PushBackEastCoeff(Beta);
  bcs.set_west_condition(Omega);
  bcs.set_east_condition(Epsilon);
  if (!bcs.ImposeOnLaplacianMatrix(lap, lapm)) {
    return EXIT_FAILURE;
  }
  bcs.ImposeOnGrid(source);
  int info{mtk::LAPACKAdapter::SolveDenseSystem(lapm, source)};
  if (info != 0) {
    return EXIT_FAILURE;
  }
  source.WriteToFile("minimalistic_poisson_1d_comp_sol.dat", "x", "~u(x)");
  known_sol.BindScalarField(KnownSolution);
```

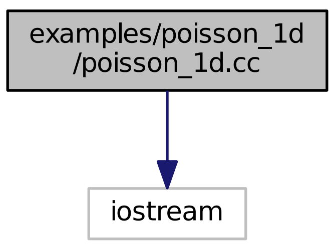
```
  known_sol.WriteToFile("minimalistic_poisson_1d_known_sol.dat", "x", "u(x)");
  mtk::Real relative_norm_2_error =
    mtk::BLASAdapter::RelNorm2Error(source.discrete_field(),
                                    known_sol.discrete_field(),
                                    known_sol.num_cells_x());
  std::cout << relative_norm_2_error << std::endl;
}
#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
  return EXIT_SUCCESS;
}
#endif
```

17.3 examples/poisson_1d/poisson_1d.cc File Reference

Poisson Equation on a 1D Uniform Staggered Grid with Robin BCs.

`#include <iostream>`

Include dependency graph for poisson_1d.cc:



Functions

- int main ()

17.3.1 Detailed Description

We solve:

$$-\nabla^2 p(x) = s(x),$$

for $x \in \Omega = [a,b] = [0,1]$.

The source term function is defined as:

$$s(x) = -\frac{\lambda^2 \exp(\lambda x)}{\exp(\lambda) - 1},$$

where $\lambda = -1$ is a real-valued parameter.

We consider Robin's boundary conditions of the form:

$$\alpha p(a) - \beta p'(a) = \omega,$$

$$\alpha p(b) + \beta p'(b) = \varepsilon,$$

where $\alpha = -\exp(\lambda)$, $\beta = (\exp(\lambda) - 1.0)/\lambda$, $\omega = -1$, and $\varepsilon = 0$.

The analytical solution for this problem is given by:

$$p(x) = \frac{\exp(\lambda x) - 1}{\exp(\lambda) - 1}.$$

The mimetic counterpart of this equation is:

$$-\breve{\mathbf{L}}_x^k \tilde{p} = \tilde{s}.$$

Finally, we will solve this problem considering $k = 2$.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file poisson_1d.cc.

17.3.2 Function Documentation

17.3.2.1 int main ( )

Definition at line 263 of file poisson_1d.cc.

17.4 poisson_1d.cc

```

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*/

#if __cplusplus == 201103L

#include <iostream>
#include <fstream>
#include <cmath>

#include <vector>

#include "mtk.h"

mtk::Real Alpha(const mtk::Real &tt) {

  mtk::Real lambda{-1.0};

  return -exp(lambda);
}

mtk::Real Beta(const mtk::Real &tt) {

  mtk::Real lambda{-1.0};

  return (exp(lambda) - 1.0)/lambda;
};

mtk::Real Omega(const mtk::Real &tt) {

  return -1.0;
};

mtk::Real Epsilon(const mtk::Real &tt) {

  return 0.0;
};

mtk::Real Source(const mtk::Real &xx) {

  mtk::Real lambda{-1.0};

  return -lambda*lambda*exp(lambda*xx)/(exp(lambda) - 1.0);
}

mtk::Real KnownSolution(const mtk::Real &xx) {

  mtk::Real lambda{-1.0};

  return (exp(lambda*xx) - 1.0)/(exp(lambda) - 1.0);
}

int main () {

  std::cout << "Example: Poisson Equation with Robin BCs on a";
  std::cout << "1D Uniform Staggered Grid." << std::endl;

  mtk::Real west_bndy_x{0.0};
  mtk::Real east_bndy_x{1.0};
  int num_cells_x{5};

  mtk::UniStgGrid1D comp_sol(west_bndy_x, east_bndy_x, num_cells_x);

  mtk::Lap1D lap;

  if (!lap.ConstructLap1D()) {
    std::cerr << "Mimetic Laplacian could not be built." << std::endl;
    return EXIT_FAILURE;
  }

```

```
std::cout << "lap=" << std::endl;
std::cout << lap << std::endl;

mtk::DenseMatrix lapm(lap.ReturnAsDenseMatrix(comp_sol));

std::cout << "lapm =" << std::endl;
std::cout << lapm << std::endl;


lapm = mtk::BLASAdapter::RealDenseSM(-1.0, lapm);

std::cout << "-lapm =" << std::endl;
std::cout << lapm << std::endl;

mtk::UniStgGrid1D source(west_bndy_x, east_bndy_x, num_cells_x);

source.BindScalarField(Source);

std::cout << "source =" << std::endl;
std::cout << source << std::endl;

mtk::RobinBCDescriptor1D robin_bc_desc_1d;

robin_bc_desc_1d.PushBackWestCoeff(Alpha);
robin_bc_desc_1d.PushBackWestCoeff(Beta);

robin_bc_desc_1d.PushBackEastCoeff(Alpha);
robin_bc_desc_1d.PushBackEastCoeff(Beta);

robin_bc_desc_1d.set_west_condition(Omega);
robin_bc_desc_1d.set_east_condition(Epsilon);

if (!robin_bc_desc_1d.ImposeOnLaplacianMatrix(lap, lapm)) {
  std::cerr << "BCs  could not be bound to the matrix." << std::endl;
  return EXIT_FAILURE;
}

std::cout << "Mimetic Laplacian operator with imposed BCs:" << std::endl;
std::cout << lapm << std::endl;

if (!lapm.WriteToFile("poisson_1d_lapm.dat")) {
  std::cerr << "Laplacian matrix could not be written to disk." << std::endl;
  return EXIT_FAILURE;
}

robin_bc_desc_1d.ImposeOnGrid(source);

std::cout << "source =" << std::endl;
std::cout << source << std::endl;

if (!source.WriteToFile("poisson_1d_source.dat", "x", "s(x)")) {
  std::cerr << "Source term could not be written to disk." << std::endl;
  return EXIT_FAILURE;
}

int info{mtk::LAPACKAdapter::SolveDenseSystem(lapm, source)};

if (!info) {
  std::cout << "System solved." << std::endl;
  std::cout << std::endl;
} else {
  std::cerr << "Something wrong solving system! info = " << info << std::endl;
  std::cerr << "Exiting..." << std::endl;
  return EXIT_FAILURE;
}

std::cout << "Computed solution:" << std::endl;
std::cout << source << std::endl;

if (!source.WriteToFile("poisson_1d_comp_sol.dat", "x", "~u(x)")) {
  std::cerr << "Solution could not be written to file." << std::endl;
  return EXIT_FAILURE;
}

mtk::UniStgGrid1D known_sol(west_bndy_x, east_bndy_x, num_cells_x);

known_sol.BindScalarField(KnownSolution);

std::cout << "known_sol =" << std::endl;
std::cout << known_sol << std::endl;

```

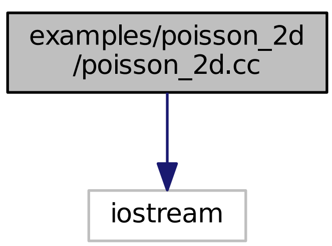
```
  if (!known_sol.WriteToFile("poisson_1d_known_sol.dat", "x", "u(x)")) {
    std::cerr << "Known solution could not be written to file." << std::endl;
    return EXIT_FAILURE;
  }

  mtk::Real relative_norm_2_error{};

  relative_norm_2_error =
    mtk::BLASAdapter::RelNorm2Error(source.discrete_field(),
                                    known_sol.discrete_field(),
                                    known_sol.num_cells_x());

  std::cout << "relative_norm_2_error = ";
  std::cout << relative_norm_2_error << std::endl;
}
#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
  return EXIT_SUCCESS;
}
#endif
```

17.5 examples/poisson_2d/poisson_2d.cc File Reference

Poisson Equation on a 2D Uniform Staggered Grid with Robin BCs.

`#include <iostream>`

Include dependency graph for poisson_2d.cc:



Functions

- int main ()

17.5.1 Detailed Description

We solve:

$$\nabla^2 u(\mathbf{x}) = s(\mathbf{x}),$$

for $\mathbf{x} \in \Omega = [0,1]^2$.

The source term function is defined as

$$s(x,y) = xye^{-0.5(x^2+y^2)}(x^2+y^2-6).$$

Let $\Omega = S \cup N \cup W \cup E$. We consider Dirichlet boundary conditions of the following form:

$$\forall \mathbf{x} \in W : u(\mathbf{x}) = 0.$$

$$\forall \mathbf{x} \in E : u(1,y) = -e^{-0.5(1-y^2)}(1-y^2).$$

$$\forall \mathbf{x} \in S : u(\mathbf{x}) = 0.$$

$$\forall \mathbf{x} \in N : u(x,1) = -e^{-0.5(x^2-1)}(x^2-1).$$

The analytical solution for this problem is given by

$$u(x,y) = xye^{-0.5(x^2+y^2)}.$$

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file poisson_2d.cc.

17.5.2 Function Documentation

17.5.2.1 int main ( )

Definition at line 241 of file poisson_2d.cc.

17.6 poisson_2d.cc

```
00001
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00047 and a copy of the modified files should be reported once modifications are
00048 completed, unless these modifications are made through the project's GitHub
00049 page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
00050 should be developed and included in any deliverable.
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SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#if __cplusplus == 201103L

#include <iostream>
#include <fstream>
#include <cmath>

#include <vector>

#include "mtk.h"

mtk::Real Source(const mtk::Real &xx, const mtk::Real &yy) {

  mtk::Real x_squared{xx*xx};
  mtk::Real y_squared{yy*yy};
  mtk::Real aux{-0.5*(x_squared + y_squared)};

  return xx*yy*exp(aux)*(x_squared + y_squared - 6.0);
}

mtk::Real BCCoeff(const mtk::Real &xx, const mtk::Real &yy) {

  return mtk::kOne;
}

mtk::Real WestBC(const mtk::Real &xx, const mtk::Real &tt) {

  return mtk::kZero;
}

mtk::Real EastBC(const mtk::Real &yy, const mtk::Real &tt) {

  return yy*exp(-0.5*(mtk::kOne + yy*yy));
}

mtk::Real SouthBC(const mtk::Real &xx, const mtk::Real &tt) {

  return mtk::kZero;
}

mtk::Real NorthBC(const mtk::Real &xx, const mtk::Real &tt) {

  return xx*exp(-0.5*(xx*xx + mtk::kOne));
}

mtk::Real KnownSolution(const mtk::Real &xx, const mtk::Real &yy) {

  mtk::Real x_squared{xx*xx};
  mtk::Real y_squared{yy*yy};
  mtk::Real aux{-0.5*(x_squared + y_squared)};

  return xx*yy*exp(aux);
}

int main () {

  std::cout << "Example: Poisson Equation on a 2D Uniform Staggered Grid ";
  std::cout << "with Dirichlet and Neumann BCs." << std::endl;

  mtk::Real west_bndy_x{0.0};
  mtk::Real east_bndy_x{1.0};
  mtk::Real south_bndy_y{0.0};
  mtk::Real north_bndy_y{1.0};
  int num_cells_x{5};
  int num_cells_y{5};
```

```
  mtk::UniStgGrid2D comp_sol(west_bndy_x, east_bndy_x, num_cells_x,
                             south_bndy_y, north_bndy_y, num_cells_y);

  mtk::Lap2D lap;

  if (!lap.ConstructLap2D(comp_sol)) {
    std::cerr << "Mimetic Laplacian could not be built." << std::endl;
    return EXIT_FAILURE;
  }

  mtk::DenseMatrix lapm(lap.ReturnAsDenseMatrix());

  mtk::UniStgGrid2D source(west_bndy_x, east_bndy_x, num_cells_x,
                           south_bndy_y, north_bndy_y, num_cells_y);

  source.BindScalarField(Source);

  mtk::RobinBCDescriptor2D bcd;

  bcd.PushBackWestCoeff(BCCoeff);
  bcd.PushBackEastCoeff(BCCoeff);
  bcd.PushBackSouthCoeff(BCCoeff);
  bcd.PushBackNorthCoeff(BCCoeff);

  bcd.ImposeOnLaplacianMatrix(lap, comp_sol, lapm);

  if (!lapm.WriteToFile("poisson_2d_lapm.dat")) {
    std::cerr << "Laplacian matrix could not be written to disk." << std::endl;
    return EXIT_FAILURE;
  }

  bcd.set_west_condition(WestBC);
  bcd.set_east_condition(EastBC);
  bcd.set_south_condition(SouthBC);
  bcd.set_north_condition(NorthBC);

  bcd.ImposeOnGrid(source);

  if(!source.WriteToFile("poisson_2d_source.dat", "x", "y", "s(x,y)")) {
    std::cerr << "Source term could not be written to disk." << std::endl;
    return EXIT_FAILURE;
  }

  int info{mtk::LAPACKAdapter::SolveDenseSystem(lapm, source)};

  if (!info) {
    std::cout << "System solved." << std::endl;
    std::cout << std::endl;
  } else {
    std::cerr << "Something wrong solving system! info = " << info << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return EXIT_FAILURE;
  }

  if (!source.WriteToFile("poisson_2d_comp_sol.dat", "x", "y", "~u(x,y)")) {
    std::cerr << "Solution could not be written to file." << std::endl;
    return EXIT_FAILURE;
  }

  mtk::UniStgGrid2D known_sol(west_bndy_x, east_bndy_x, num_cells_x,
                              south_bndy_y, north_bndy_y, num_cells_y);

  known_sol.BindScalarField(KnownSolution);

  if (!known_sol.WriteToFile("poisson_2d_known_sol.dat", "x", "y", "u(x,y)")) {
    std::cerr << "Known solution could not be written to file." << std::endl;
    return EXIT_FAILURE;
  }

  mtk::Real relative_norm_2_error{};

  relative_norm_2_error =
    mtk::BLASAdapter::RelNorm2Error(source.discrete_field(),
                                    known_sol.discrete_field(),
                                    known_sol.Size());

  std::cout << "relative_norm_2_error = ";
  std::cout << relative_norm_2_error << std::endl;
}
```

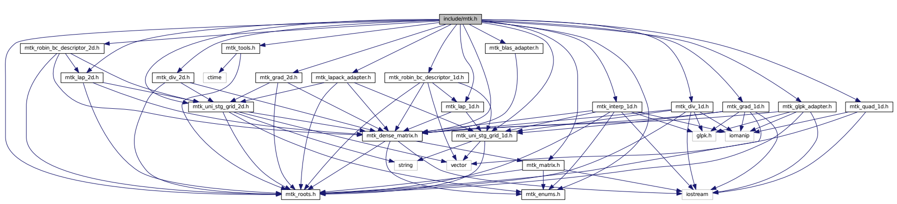
```
#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
  return EXIT_SUCCESS;
}
#endif
```

17.7 include/mtk.h File Reference

Includes the entire API.

```
#include "mtk_roots.h"
#include "mtk_enums.h"
#include "mtk_tools.h"
#include "mtk_matrix.h"
#include "mtk_dense_matrix.h"
#include "mtk_blas_adapter.h"
#include "mtk_lapack_adapter.h"
#include "mtk_glpk_adapter.h"
#include "mtk_uni_stg_grid_1d.h"
#include "mtk_uni_stg_grid_2d.h"
#include "mtk_grad_1d.h"
#include "mtk_div_1d.h"
#include "mtk_lap_1d.h"
#include "mtk_robin_bc_descriptor_1d.h"
#include "mtk_quad_1d.h"
#include "mtk_interp_1d.h"
#include "mtk_grad_2d.h"
#include "mtk_div_2d.h"
#include "mtk_lap_2d.h"
#include "mtk_robin_bc_descriptor_2d.h"
```

Include dependency graph for mtk.h:



17.7.1 Detailed Description

This file contains every required header file, thus containing the entire API. In this way, client codes only have to instruct #include "mtk.h".

Warning

IT IS EXTREMELY IMPORTANT THAT THE HEADERS ARE ADDED TO THIS FILE IN A SPECIFIC ORDER; THAT IS, CONSIDERING THE DEPENDENCE BETWEEN THE CLASSES THESE CONTAIN!

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk.h.

17.8 mtk.h

```
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page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
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ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT
(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/
#ifndef MTK_INCLUDE_MTK_H_
#define MTK_INCLUDE_MTK_H_

#include "mtk_roots.h"

#include "mtk_enums.h"

#include "mtk_tools.h"

#include "mtk_matrix.h"
#include "mtk_dense_matrix.h"

#include "mtk_blas_adapter.h"
#include "mtk_lapack_adapter.h"
#include "mtk_glpk_adapter.h"

#include "mtk_uni_stg_grid_1d.h"
#include "mtk_uni_stg_grid_2d.h"

#include "mtk_grad_1d.h"
#include "mtk_div_1d.h"
#include "mtk_lap_1d.h"
```
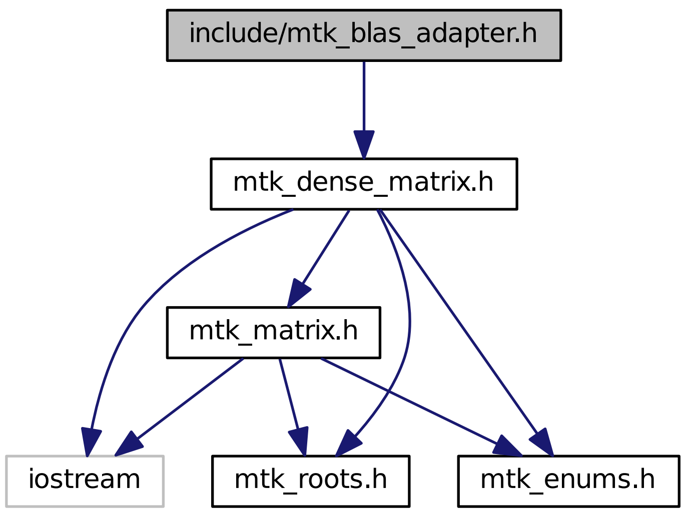

```
#include "mtk_robin_bc_descriptor_1d.h"
#include "mtk_quad_1d.h"
#include "mtk_interp_1d.h"

#include "mtk_grad_2d.h"
#include "mtk_div_2d.h"
#include "mtk_lap_2d.h"
#include "mtk_robin_bc_descriptor_2d.h"

#endif // End of: MTK_INCLUDE_MTK_H_
```

17.9 include/mtk_blas_adapter.h File Reference

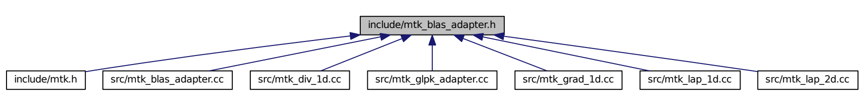
Adapter class for the BLAS API.

`#include "mtk_dense_matrix.h"`

Include dependency graph for mtk_blas_adapter.h:



This graph shows which files directly or indirectly include this file:



Classes

- class mtk::BLASAdapter

    Adapter class for the BLAS API.

Namespaces

- mtk

    Mimetic Methods Toolkit namespace.

17.9.1 Detailed Description

This class contains a collection of static classes, that posses direct access to the underlying structure of the matrices, thus allowing programmers to exploit some of the numerical methods implemented in the BLAS.

The **BLAS (Basic Linear Algebra Subprograms)** are routines that provide standard building blocks for performing basic vector and matrix operations. The Level 1 BLAS perform scalar, vector and vector-vector operations, the Level 2 BLAS perform matrix-vector operations, and the Level 3 BLAS perform matrix-matrix operations.

The BLAS can be installed from links given in the See Also section of this page.

See also

http://www.netlib.org/blas/
https://software.intel.com/en-us/non-commercial-software-development

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_blas_adapter.h.

17.10 mtk_blas_adapter.h

```
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*/

#ifndef MTK_INCLUDE_BLAS_ADAPTER_H_
#define MTK_INCLUDE_BLAS_ADAPTER_H_

#include "mtk_dense_matrix.h"

namespace mtk {

class BLASAdapter {
 public:
  static Real RealNRM2(Real *in, int &in_length);

  static void RealAXPY(Real alpha, Real *xx, Real *yy, int &in_length);

  static Real RelNorm2Error(Real *computed, Real *known, int length);

  static void RealDenseMV(Real &alpha,
                          DenseMatrix &aa,
                          Real *xx,
                          Real &beta,
                          Real *yy);

  static DenseMatrix RealDenseMM(DenseMatrix &aa,
DenseMatrix &bb);

  static DenseMatrix RealDenseSM(Real alpha,
DenseMatrix &aa);
};
}
#endif  // End of: MTK_INCLUDE_BLAS_ADAPTER_H_
```
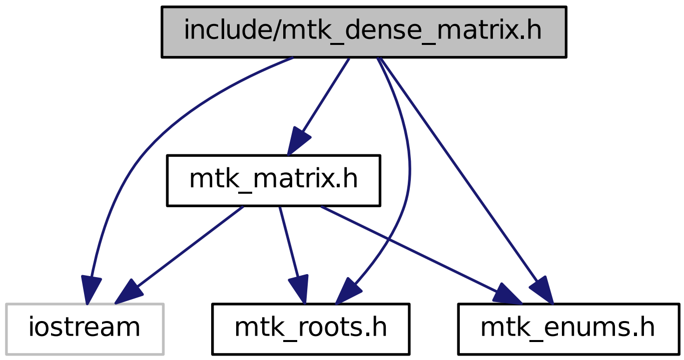

17.11 include/mtk_dense_matrix.h File Reference

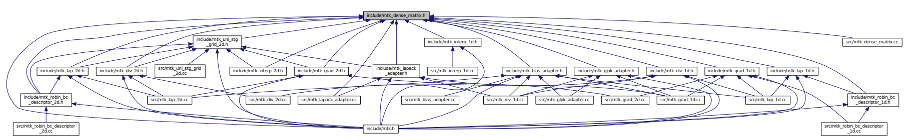
Defines a common dense matrix, using a 1D array.

```
#include <iostream>
#include "mtk_roots.h"
#include "mtk_enums.h"
#include "mtk_matrix.h"
```

Include dependency graph for mtk_dense_matrix.h:



This graph shows which files directly or indirectly include this file:



Classes

- class mtk::DenseMatrix

  Defines a common dense matrix, using a 1D array.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

17.11.1 Detailed Description

For developing purposes, it is better to have a not-so-intrincated data structure implementing matrices. This is the purpose of this class: to be used for prototypes of new code for small test cases. In every other instance, this should be replaced by the most appropriate sparse matrix.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Note

We prefer composition to inheritance [Reedy, 2011]. The main reason for this preference is that inheritance produces a more tightly coupled design. When a class inherits from another type be it public, protected, or private inheritance the subclass gains access to all public and protected members of the base class, whereas with composition, the class is only coupled to the public members of the other class. Furthermore, if you only hold a pointer to the other object, then your interface can use a forward declaration of the class rather than #include its full definition. This results in greater compile-time insulation and improves the time it takes to compile your code.

Definition in file mtk_dense_matrix.h.

17.12 mtk_dense_matrix.h

```

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*/

#ifndef MTK_INCLUDE_DENSE_MATRIX_H_
#define MTK_INCLUDE_DENSE_MATRIX_H_

#include <iostream>

#include "mtk_roots.h"
#include "mtk_enums.h"
#include "mtk_matrix.h"

namespace mtk {

class DenseMatrix {
 public:
```
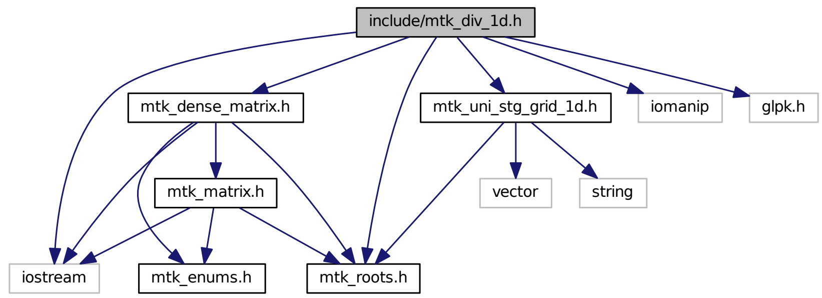

```
  friend std::ostream& operator <<(std::ostream &stream, DenseMatrix &in);

  DenseMatrix& operator =(const DenseMatrix &in);

  bool operator ==(const DenseMatrix &in);

  DenseMatrix();

  DenseMatrix(const DenseMatrix &in);

  DenseMatrix(const int &num_rows, const int &num_cols);

  DenseMatrix(const int &rank, const bool &padded, const bool &transpose);

  DenseMatrix(const Real *const gen,
              const int &gen_length,
              const int &pro_length,
              const bool &transpose);

  ~DenseMatrix();

  Matrix matrix_properties() const noexcept;

  int num_rows() const noexcept;

  int num_cols() const noexcept;

  Real* data() const noexcept;

  void SetOrdering(mtk::MatrixOrdering oo) noexcept;

  Real GetValue(const int &row_coord, const int &col_coord) const noexcept;

  void SetValue(const int &row_coord,
                const int &col_coord,
                const Real &val) noexcept;

  void Transpose();

  void OrderRowMajor();

  void OrderColMajor();

  static DenseMatrix Kron(const DenseMatrix &aa,
                          const DenseMatrix &bb);

  bool WriteToFile(const std::string &filename) const;

 private:
  Matrix matrix_properties_;

  Real *data_;
};
}
#endif  // End of: MTK_INCLUDE_MTK_DENSE_MATRIX_H_
```

17.13 include/mtk_div_1d.h File Reference

Includes the definition of the class Div1D.

```
#include <iostream>
#include <iomanip>
#include "glpk.h"
#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_1d.h"
```

Include dependency graph for mtk_div_1d.h:



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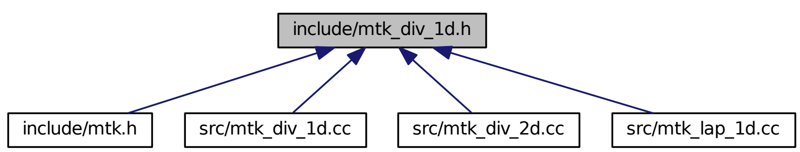

Classes

- class mtk::Div1D

  Implements a 1D mimetic divergence operator.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

17.13.1 Detailed Description

This class implements a 1D divergence operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (CBSA).

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_div_1d.h.

17.14 mtk_div_1d.h

```
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*/

#ifndef MTK_INCLUDE_DIV_1D_H_
#define MTK_INCLUDE_DIV_1D_H_

#include <iostream>
#include <iomanip>

#include "glpk.h"

#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_1d.h"

namespace mtk {

class Div1D {
 public:
  friend std::ostream& operator <<(std::ostream& stream, Div1D &in);

  Div1D();

  Div1D(const Div1D &div);

  ~Div1D();

  bool ConstructDiv1D(int order_accuracy = kDefaultOrderAccuracy,
                      Real mimetic_threshold = kDefaultMimeticThreshold);

  int num_bndy_coeffs() const;

  Real *coeffs_interior() const;

```
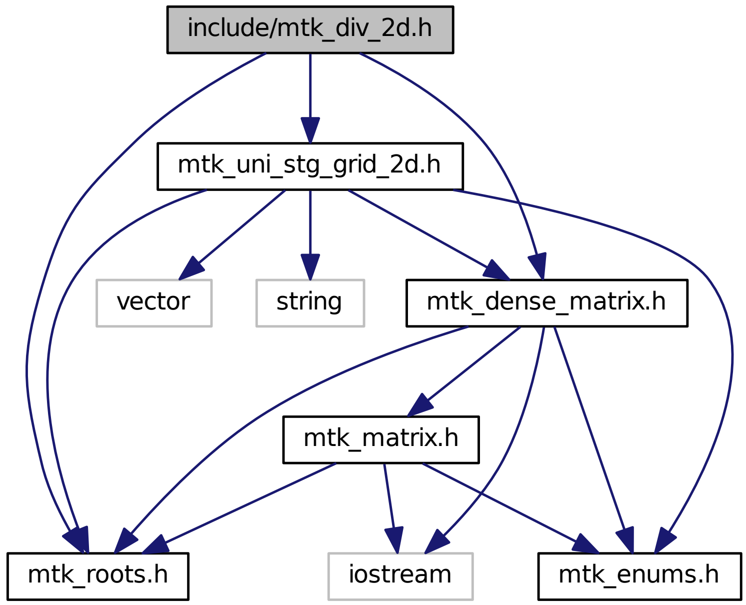

```
  Real *weights_crs(void) const;

  Real *weights_cbs(void) const;

  DenseMatrix mim_bndy() const;

  DenseMatrix ReturnAsDenseMatrix(const UniStgGrid1D &grid) const;

 private:
  bool ComputeStencilInteriorGrid(void);

  bool ComputeRationalBasisNullSpace(void);

  bool ComputePreliminaryApproximations(void);

  bool ComputeWeights(void);

  bool ComputeStencilBoundaryGrid(void);

  bool AssembleOperator(void);

  int order_accuracy_;
  int dim_null_;
  int num_bndy_coeffs_;
  int divergence_length_;
  int minrow_;
  int row_;

  DenseMatrix rat_basis_null_space_;

  Real *coeffs_interior_;
  Real *prem_apps_;
  Real *weights_crs_;
  Real *weights_cbs_;
  Real *mim_bndy_;
  Real *divergence_;

  Real mimetic_threshold_;
};
}
#endif  // End of: MTK_INCLUDE_DIV_1D_H_
```

17.15 include/mtk_div_2d.h File Reference

Includes the definition of the class Div2D.

```
#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_2d.h"
```

Include dependency graph for mtk_div_2d.h:



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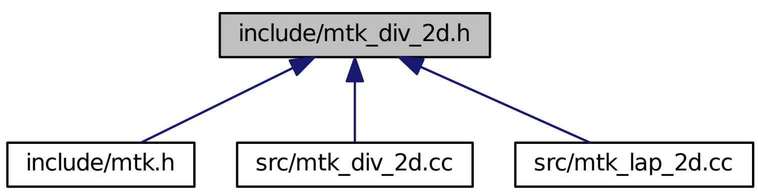

Classes

- class mtk::Div2D

    Implements a 2D mimetic divergence operator.

Namespaces

- mtk

Mimetic Methods Toolkit namespace.

17.15.1 Detailed Description

This class implements a 2D divergence operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (CBSA).

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_div_2d.h.

17.16 mtk_div_2d.h

```

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*/

#ifndef MTK_INCLUDE_MTK_DIV_2D_H_
#define MTK_INCLUDE_MTK_DIV_2D_H_

#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_2d.h"

namespace mtk{
```

```
class Div2D {
 public:
  Div2D();

  Div2D(const Div2D &div);

  ~Div2D();

  bool ConstructDiv2D(const UniStgGrid2D &grid,
                      int order_accuracy = kDefaultOrderAccuracy,
                      Real mimetic_threshold = kDefaultMimeticThreshold);

  DenseMatrix ReturnAsDenseMatrix() const;

 private:
  DenseMatrix divergence_;

  int order_accuracy_;

  Real mimetic_threshold_;
};
}
#endif  // End of: MTK_INCLUDE_MTK_DIV_2D_H_
```

17.17 include/mtk_enums.h File Reference

Considered enumeration types in the MTK.

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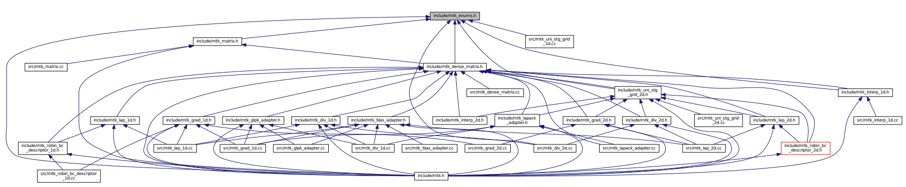

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

Enumerations

- enum mtk::MatrixStorage { mtk::DENSE, mtk::BANDED, mtk::CRS }

  Considered matrix storage schemes to implement sparse matrices.
- enum mtk::MatrixOrdering { mtk::ROW_MAJOR, mtk::COL_MAJOR }

  Considered matrix ordering (for Fortran purposes).
- enum mtk::FieldNature { mtk::SCALAR, mtk::VECTOR }

  Nature of the field discretized in a given grid.
- enum mtk::DirInterp { mtk::SCALAR_TO_VECTOR, mtk::VECTOR_TO_SCALAR }

  Interpolation operator.

17.17.1 Detailed Description

Enumeration types are used throughout the MTK to differentiate instances of derived classes, as well as for mnemonic purposes. In this file, the enumeration types are listed alphabetically.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_enums.h.

17.18 mtk_enums.h

```

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*/

#ifndef MTK_INCLUDE_ENUMS_H_
#define MTK_INCLUDE_ENUMS_H_

namespace mtk {

enum MatrixStorage {
  DENSE,
  BANDED,
  CRS
};

enum MatrixOrdering {
  ROW_MAJOR,
```

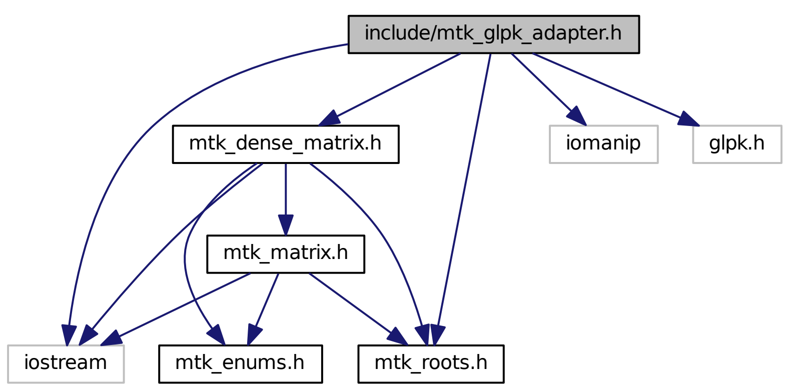
```
00097   COL_MAJOR
00098 };
00099
00113 enum FieldNature {
00114   SCALAR,
00115   VECTOR
00116 };
00117
00127 enum DirInterp {
00128   SCALAR_TO_VECTOR,
00129   VECTOR_TO_SCALAR
00130 };
00131 }
00132 #endif  // End of: MTK_INCLUDE_ENUMS_H_
```

17.19 include/mtk_glpk_adapter.h File Reference

Adapter class for the GLPK API.

```
#include <iostream>
#include <iomanip>
#include "glpk.h"
#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
```

Include dependency graph for mtk_glpk_adapter.h:



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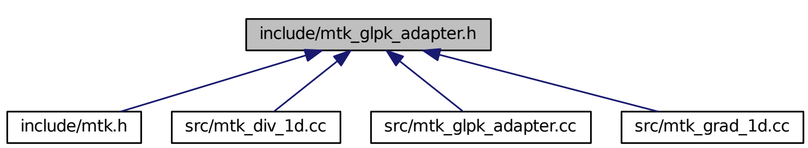

Classes

- class mtk::GLPKAdapter

  Adapter class for the GLPK API.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

17.19.1 Detailed Description

This class contains a collection of static classes, that posses direct access to the underlying structure of the matrices, thus allowing programmers to exploit some of the numerical methods implemented in the GLPK.

The **GLPK (GNU Linear Programming Kit)** package is intended for solving large-scale linear programming (LP), mixed integer programming (MIP), and other related problems. It is a set of routines written in ANSI C and organized in the form of a callable library.

See also

http://www.gnu.org/software/glpk/

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_glpk_adapter.h.

17.20 mtk_glpk_adapter.h

```

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*/

#ifndef MTK_INCLUDE_GLPK_ADAPTER_H_
#define MTK_INCLUDE_GLPK_ADAPTER_H_

#include <iostream>
#include <iomanip>

#include "glpk.h"

#include "mtk_roots.h"
#include "mtk_dense_matrix.h"

namespace mtk {

class GLPKAdapter {
 public:
  static mtk::Real SolveSimplexAndCompare(
mtk::Real *A,
                                         int nrows,
                                         int ncols,
                                         int kk,
                                         mtk::Real *hh,
                                         mtk::Real *qq,
                                         int robjective,
                                         mtk::Real mimetic_tol,
                                         int copy);
};
}
#endif  // End of: MTK_INCLUDE_MTK_GLPK_ADAPTER_H_
```
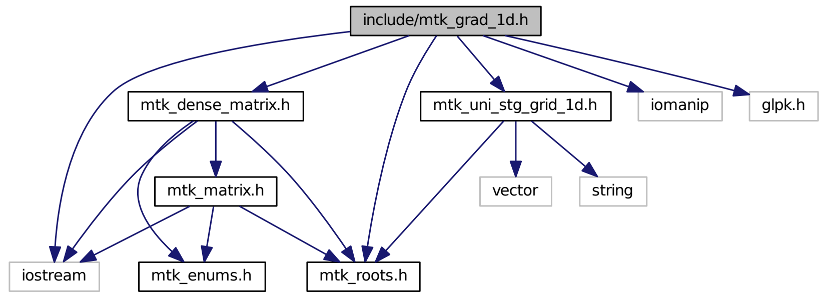

17.21 include/mtk_grad_1d.h File Reference

Includes the definition of the class Grad1D.

```
#include <iostream>
#include <iomanip>
#include "glpk.h"
#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_1d.h"
```

Include dependency graph for mtk_grad_1d.h:



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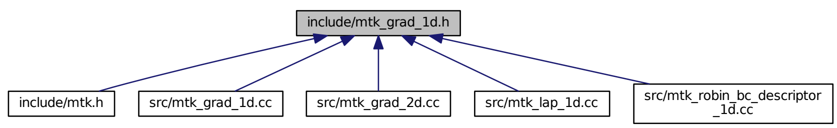

Classes

- class mtk::Grad1D

    Implements a 1D mimetic gradient operator.

Namespaces

- mtk

    Mimetic Methods Toolkit namespace.

17.21.1 Detailed Description

This class implements a 1D gradient operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (C←BSA).

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_grad_1d.h.

17.22 mtk_grad_1d.h

```
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*/

#ifndef MTK_INCLUDE_GRAD_1D_H_
#define MTK_INCLUDE_GRAD_1D_H_

#include <iostream>
#include <iomanip>

#include "glpk.h"

#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_1d.h"

namespace mtk {

class Grad1D {
 public:
  friend std::ostream& operator <<(std::ostream& stream, Grad1D &in);

  Grad1D();

  Grad1D(const Grad1D &grad);

  ~Grad1D();

  bool ConstructGrad1D(int order_accuracy = kDefaultOrderAccuracy,
                       Real mimetic_threshold = kDefaultMimeticThreshold);

  int num_bndy_coeffs() const;

  Real *coeffs_interior() const;

```
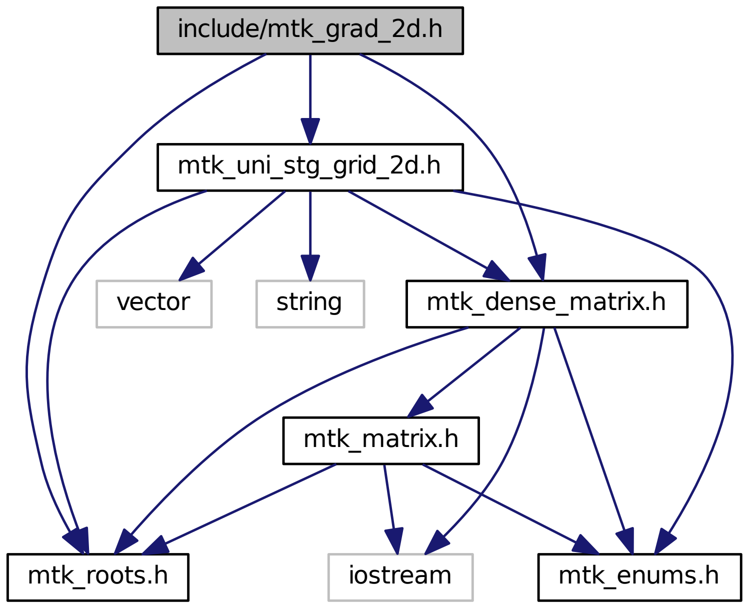

```
  Real *weights_crs(void) const;

  Real *weights_cbs(void) const;

  DenseMatrix mim_bndy() const;

  DenseMatrix ReturnAsDenseMatrix(Real west, Real east, int num_cells_x) const;

  DenseMatrix ReturnAsDenseMatrix(const UniStgGrid1D &grid) const;

  DenseMatrix ReturnAsDimensionlessDenseMatrix(int num_cells_x) const;

 private:
  bool ComputeStencilInteriorGrid(void);

  bool ComputeRationalBasisNullSpace(void);

  bool ComputePreliminaryApproximations(void);

  bool ComputeWeights(void);

  bool ComputeStencilBoundaryGrid(void);

  bool AssembleOperator(void);

  int order_accuracy_;
  int dim_null_;
  int num_bndy_approxs_;
  int num_bndy_coeffs_;
  int gradient_length_;
  int minrow_;
  int row_;

  DenseMatrix rat_basis_null_space_;

  Real *coeffs_interior_;
  Real *prem_apps_;
  Real *weights_crs_;
  Real *weights_cbs_;
  Real *mim_bndy_;
  Real *gradient_;

  Real mimetic_threshold_;
};
}
#endif  // End of: MTK_INCLUDE_GRAD_1D_H_
```

17.23 include/mtk_grad_2d.h File Reference

Includes the definition of the class Grad2D.

```
#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_2d.h"
```

Include dependency graph for mtk_grad_2d.h:



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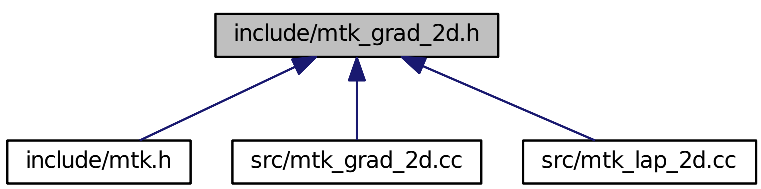

Classes

- class mtk::Grad2D

  Implements a 2D mimetic gradient operator.

Namespaces

- mtk

Mimetic Methods Toolkit namespace.

17.23.1 Detailed Description

This class implements a 2D gradient operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (C←BSA).

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_grad_2d.h.

17.24 mtk_grad_2d.h

```

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*/

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#define MTK_INCLUDE_MTK_GRAD_2D_H_

#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_2d.h"

namespace mtk{
```
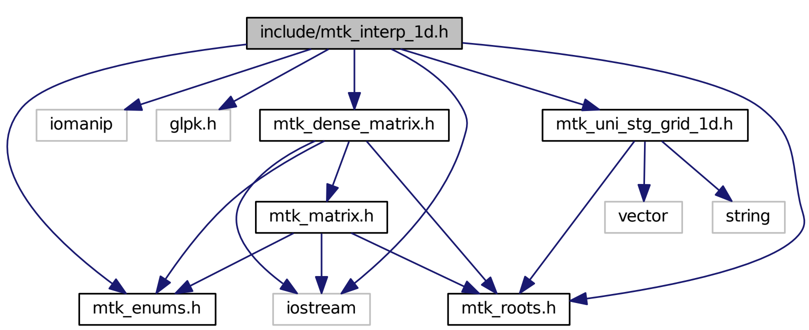

```cpp

class Grad2D {
 public:
  Grad2D();

  Grad2D(const Grad2D &grad);

  ~Grad2D();

  bool ConstructGrad2D(const UniStgGrid2D &grid,
                       int order_accuracy = kDefaultOrderAccuracy,
                       Real mimetic_threshold = kDefaultMimeticThreshold);

  DenseMatrix ReturnAsDenseMatrix() const;

 private:
  DenseMatrix gradient_;

  int order_accuracy_;

  Real mimetic_threshold_;
};
}
#endif  // End of: MTK_INCLUDE_MTK_GRAD_2D_H_
```

17.25 include/mtk_interp_1d.h File Reference

Includes the definition of the class Interp1D.

```cpp
#include <iostream>
#include <iomanip>
#include "glpk.h"
#include "mtk_roots.h"
#include "mtk_enums.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_1d.h"
```

Include dependency graph for mtk_interp_1d.h:



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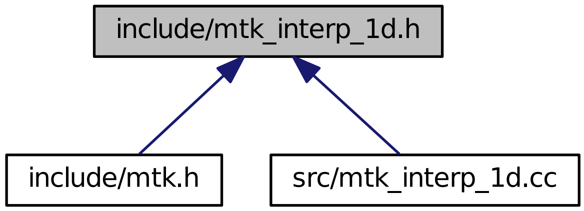

Classes

- class mtk::Interp1D

  Implements a 1D interpolation operator.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

17.25.1 Detailed Description

This class implements a 1D interpolation operator.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu
: Johnny Corbino - jcorbino at mail dot sdsu dot edu

Definition in file mtk_interp_1d.h.

17.26 mtk_interp_1d.h

```

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```

```
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*/

#ifndef MTK_INCLUDE_INTERP_1D_H_
#define MTK_INCLUDE_INTERP_1D_H_

#include <iostream>
#include <iomanip>

#include "glpk.h"

#include "mtk_roots.h"
#include "mtk_enums.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_1d.h"

namespace mtk {

class Interp1D {
 public:
  friend std::ostream& operator <<(std::ostream& stream, Interp1D &in);

  Interp1D();

  Interp1D(const Interp1D &interp);

  ~Interp1D();

  bool ConstructInterp1D(int order_accuracy =
kDefaultOrderAccuracy,
                         mtk::DirInterp dir = SCALAR_TO_VECTOR);

  Real *coeffs_interior() const;

  DenseMatrix ReturnAsDenseMatrix(const
UniStgGrid1D &grid) const;

 private:
  DirInterp dir_interp_;

  int order_accuracy_;

  Real *coeffs_interior_;
};
}
#endif  // End of: MTK_INCLUDE_INTERP_1D_H_
```
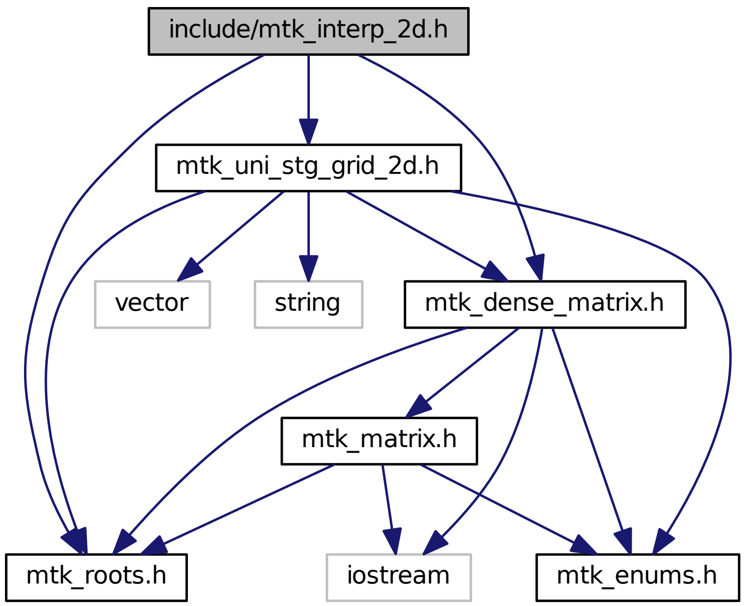

17.27 include/mtk_interp_2d.h File Reference

Includes the definition of the class Interp2D.

```
#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_2d.h"
```

Include dependency graph for mtk_interp_2d.h:



Classes

- class mtk::Interp2D

  Implements a 2D interpolation operator.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

17.27.1 Detailed Description

This class implements a 2D interpolation operator.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

: Johnny Corbino - jcorbino at mail dot sdsu dot edu

Definition in file mtk_interp_2d.h.

17.28 mtk_interp_2d.h

```
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*/

#ifndef MTK_INCLUDE_MTK_INTERP_2D_H_
#define MTK_INCLUDE_MTK_INTERP_2D_H_

#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_2d.h"

namespace mtk{

class Interp2D {
 public:
  Interp2D();

  Interp2D(const Interp2D &interp);

  ~Interp2D();

  DenseMatrix ConstructInterp2D(const UniStgGrid2D &grid,
                                int order_accuracy = kDefaultOrderAccuracy,
```
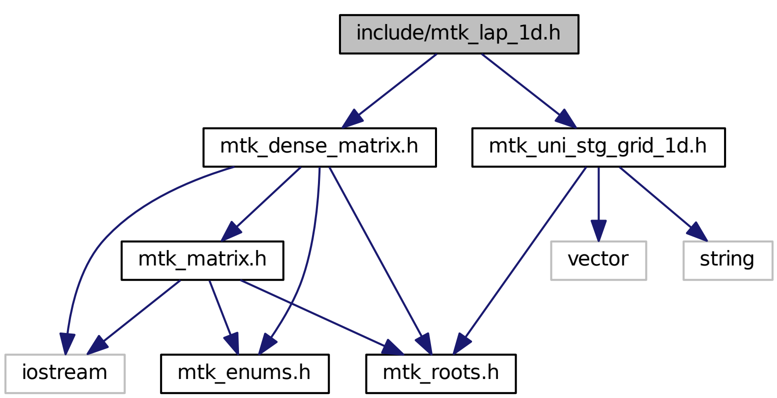

```
                               Real mimetic_threshold =
      kDefaultMimeticThreshold);

  DenseMatrix ReturnAsDenseMatrix();

 private:
  DenseMatrix interpolator_;

  int order_accuracy_;

  Real mimetic_threshold_;
};
}
#endif  // End of: MTK_INCLUDE_MTK_INTERP_2D_H_
```

17.29 include/mtk_lap_1d.h File Reference

Includes the definition of the class Lap1D.

```
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_1d.h"
```

Include dependency graph for mtk_lap_1d.h:



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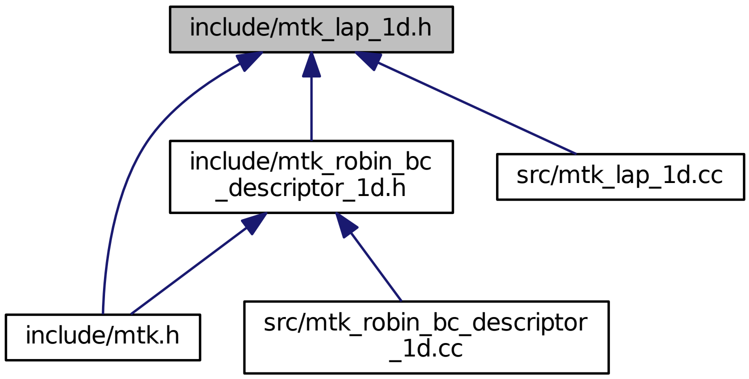

Classes

- class mtk::Lap1D

  Implements a 1D mimetic Laplacian operator.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

17.29.1 Detailed Description

This class implements a 1D Laplacian operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (CBSA).

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_lap_1d.h.

17.30 mtk_lap_1d.h

```

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*/

#ifndef MTK_INCLUDE_LAP_1D_H_
#define MTK_INCLUDE_LAP_1D_H_

#include "mtk_dense_matrix.h"

#include "mtk_uni_stg_grid_1d.h"

namespace mtk {

class Lap1D {
 public:
  friend std::ostream& operator <<(std::ostream& stream, Lap1D &in);

  Lap1D();

  Lap1D(const Lap1D &lap);

  ~Lap1D();

  int order_accuracy() const;

  Real mimetic_threshold() const;

  Real delta() const;

  bool ConstructLap1D(int order_accuracy = kDefaultOrderAccuracy,
                      Real mimetic_threshold = kDefaultMimeticThreshold);

  DenseMatrix ReturnAsDenseMatrix(const
UniStgGrid1D &grid) const;

  const mtk::Real* data(const UniStgGrid1D &grid) const;

 private:
  int order_accuracy_;
  int laplacian_length_;

  Real *laplacian_;

  mutable Real delta_;

  Real mimetic_threshold_;
```

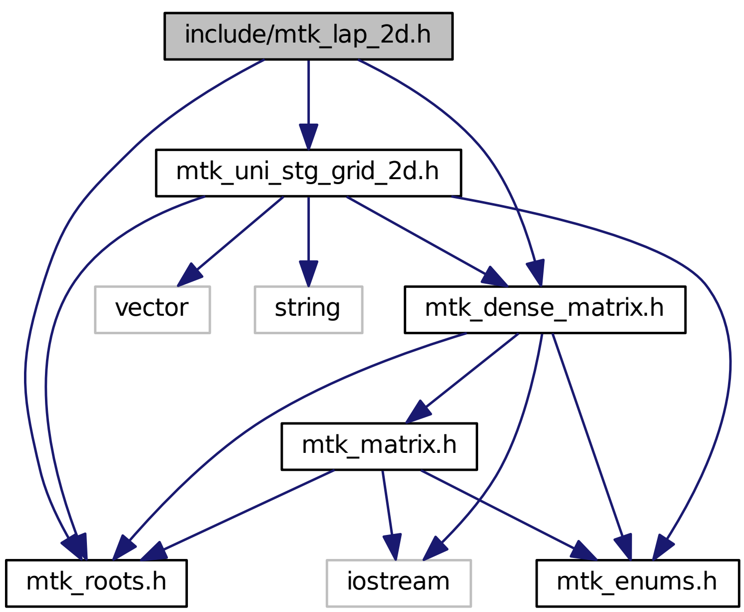
```
00146 };
00147 }
00148 #endif  // End of: MTK_INCLUDE_LAP_1D_H_
```

17.31 include/mtk_lap_2d.h File Reference

Includes the implementation of the class Lap2D.

```
#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_2d.h"
```

Include dependency graph for mtk_lap_2d.h:



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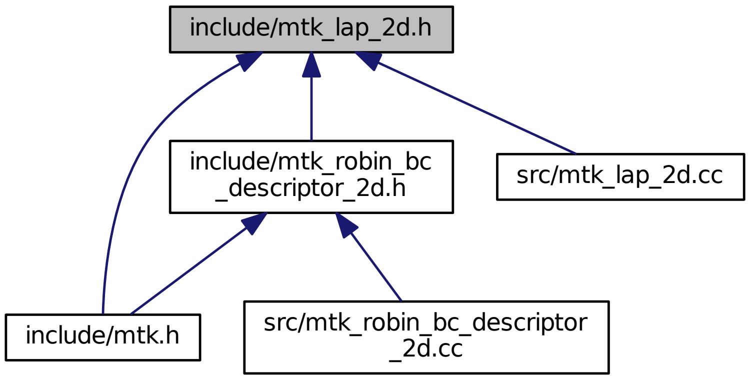

Classes

- class mtk::Lap2D

  Implements a 2D mimetic Laplacian operator.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

17.31.1 Detailed Description

This class implements a 2D Laplacian operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (CBSA).

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_lap_2d.h.

17.32 mtk_lap_2d.h

```

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#define MTK_INCLUDE_MTK_LAP_2D_H_

#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_2d.h"

namespace mtk{

class Lap2D {
 public:
  Lap2D();

  Lap2D(const Lap2D &lap);

  ~Lap2D();

  bool ConstructLap2D(const UniStgGrid2D &grid,
                      int order_accuracy = kDefaultOrderAccuracy,
                      Real mimetic_threshold = kDefaultMimeticThreshold);

  DenseMatrix ReturnAsDenseMatrix() const;

  Real *data() const;

 private:
  DenseMatrix laplacian_;

  int order_accuracy_;

  Real mimetic_threshold_;
};
}
#endif  // End of: MTK_INCLUDE_MTK_LAP_2D_H_
```
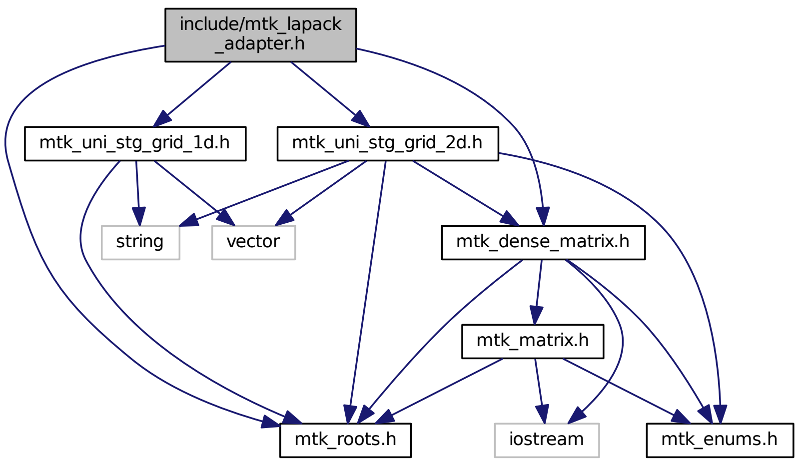

17.33 include/mtk_lapack_adapter.h File Reference

Adapter class for the LAPACK API.

```
#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_1d.h"
#include "mtk_uni_stg_grid_2d.h"
```

Include dependency graph for mtk_lapack_adapter.h:



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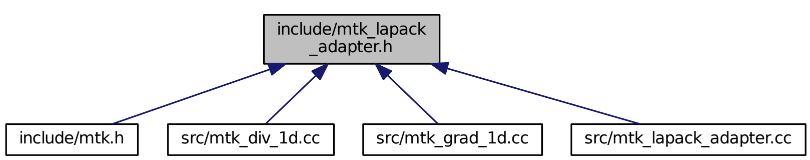

Classes

- class mtk::LAPACKAdapter

    Adapter class for the LAPACK API.

Namespaces

- mtk

    Mimetic Methods Toolkit namespace.

17.33.1 Detailed Description

This class contains a collection of static classes, that posses direct access to the underlying structure of the matrices, thus allowing programmers to exploit some of the numerical methods implemented in the LAPACK.

The **LAPACK (Linear Algebra PACKage)** is written in Fortran 90 and provides routines for solving systems of simultaneous linear equations, least-squares solutions of linear systems of equations, eigenvalue problems, and singular value problems.

See also

http://www.netlib.org/lapack/

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_lapack_adapter.h.

17.34 mtk_lapack_adapter.h

```

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*/

#ifndef MTK_INCLUDE_LAPACK_ADAPTER_H_
```
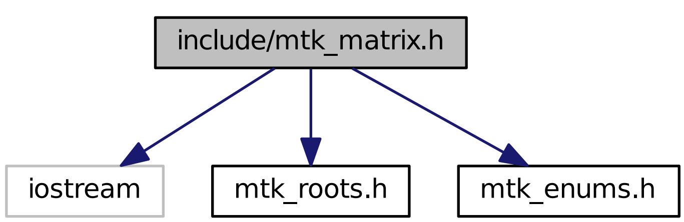

```
#define MTK_INCLUDE_LAPACK_ADAPTER_H_

#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_1d.h"
#include "mtk_uni_stg_grid_2d.h"

namespace mtk {

class LAPACKAdapter {
 public:
  static int SolveDenseSystem(mtk::DenseMatrix &mm,
                              mtk::Real *rhs);

  static int SolveDenseSystem(mtk::DenseMatrix &mm,
                              mtk::DenseMatrix &rr);

  static int SolveDenseSystem(mtk::DenseMatrix &mm,
                              mtk::UniStgGrid1D &rhs);


  static int SolveDenseSystem(mtk::DenseMatrix &mm,
                              mtk::UniStgGrid2D &rhs);

  static int SolveRectangularDenseSystem(const mtk::DenseMatrix &aa,
                                         mtk::Real *ob_,
                                         int ob_ld_);

  static mtk::DenseMatrix QRFactorDenseMatrix(DenseMatrix &matrix);
};
}
#endif  // End of: MTK_INCLUDE_LAPACK_ADAPTER_H_
```

17.35 include/mtk_matrix.h File Reference

Definition of the representation of a matrix in the MTK.

```
#include <iostream>
#include "mtk_roots.h"
#include "mtk_enums.h"
```

Include dependency graph for mtk_matrix.h:



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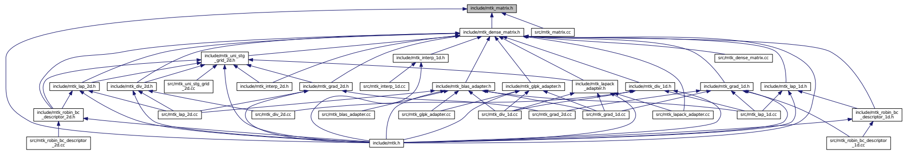

Classes

- class mtk::Matrix

  Definition of the representation of a matrix in the MTK.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

17.35.1 Detailed Description

Definition of the representation for the matrices implemented in the MTK.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_matrix.h.

17.36 mtk_matrix.h

```

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#ifndef MTK_INCLUDE_MATRIX_H_
#define MTK_INCLUDE_MATRIX_H_

#include <iostream>

#include "mtk_roots.h"
#include "mtk_enums.h"

namespace mtk {

class Matrix {
 public:
  Matrix();

  Matrix(const Matrix &in);

  ~Matrix() noexcept ;

  MatrixStorage storage() const noexcept;

  MatrixOrdering ordering() const noexcept;

  int num_rows() const noexcept;

  int num_cols() const noexcept;

  int num_values() const noexcept;

  int ld() const noexcept;

  int num_zero() const noexcept;

  int num_non_zero() const noexcept;

  int num_null() const noexcept;

  int num_non_null() const noexcept;

  int kl() const noexcept;

  int ku() const noexcept;

  int bandwidth() const noexcept;

  Real abs_density() const noexcept;

  Real rel_density() const noexcept;

  Real abs_sparsity() const noexcept;

  Real rel_sparsity() const noexcept;

  void set_storage(const MatrixStorage &tt) noexcept;

  void set_ordering(const MatrixOrdering &oo) noexcept;

  void set_num_rows(const int &num_rows) noexcept;

  void set_num_cols(const int &num_cols) noexcept;

  void set_num_zero(const int &in) noexcept;
```
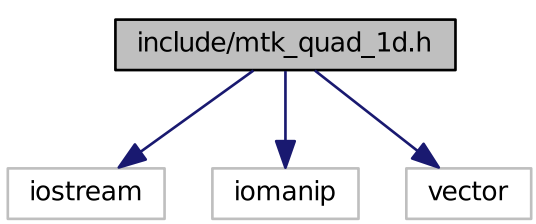

```

  void set_num_null(const int &in) noexcept;

  void IncreaseNumZero() noexcept;

  void IncreaseNumNull() noexcept;

 private:
  MatrixStorage storage_;

  MatrixOrdering ordering_;

  int num_rows_;
  int num_cols_;
  int num_values_;
  int ld_;

  int num_zero_;
  int num_non_zero_;
  int num_null_;
  int num_non_null_;

  int kl_;
  int ku_;
  int bandwidth_;

  Real abs_density_;
  Real rel_density_;
  Real abs_sparsity_;
  Real rel_sparsity_;
};
}
#endif  // End of: MTK_INCLUDE_MATRIX_H_
```

17.37 include/mtk_quad_1d.h File Reference

Includes the definition of the class Quad1D.

```
#include <iostream>
#include <iomanip>
#include <vector>
```

Include dependency graph for mtk_quad_1d.h:



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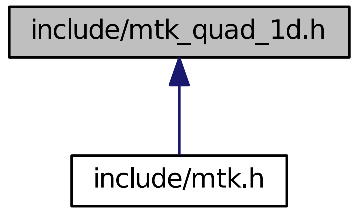

Classes

- class mtk::Quad1D

    Implements a 1D mimetic quadrature.

Namespaces

- mtk

    Mimetic Methods Toolkit namespace.

17.37.1 Detailed Description

This class implements a 1D quadrature solver based on the mimetic discretization of the gradient operator.

See also

mtk::Grad1D

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Todo Implement this class.

Definition in file mtk_quad_1d.h.

17.38 mtk_quad_1d.h

```

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*/

#ifndef MTK_INCLUDE_QUAD_1D_H_
#define MTK_INCLUDE_QUAD_1D_H_

#include <iostream>
#include <iomanip>

#include <vector>

namespace mtk {

class Quad1D {
 public:
  friend std::ostream& operator <<(std::ostream& stream, Quad1D &in);

  Quad1D();

  Quad1D(const Quad1D &quad);

  ~Quad1D();

  int degree_approximation() const;

  Real *weights() const;

  Real Integrate(Real (*Integrand)(Real xx), UniStgGrid1D grid) const;

 private:
  int degree_approximation_;

  std::vector<Real> weights_;
};
}
#endif  // End of: MTK_INCLUDE_QUAD_1D_H_
```
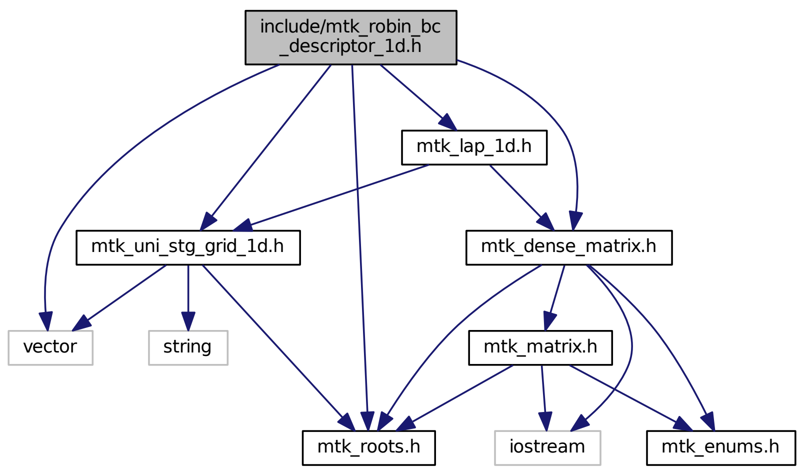

17.39 include/mtk_robin_bc_descriptor_1d.h File Reference

Impose Robin boundary conditions on the operators and on the grids.

```
#include <vector>
#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_1d.h"
#include "mtk_lap_1d.h"
```

Include dependency graph for mtk_robin_bc_descriptor_1d.h:



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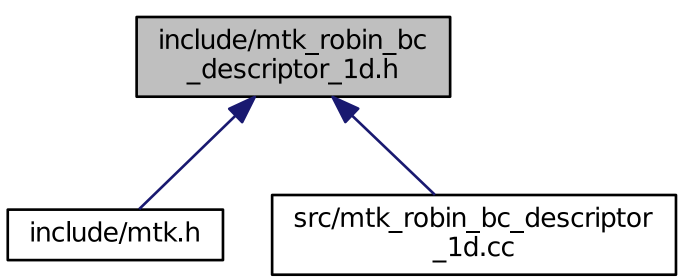

Classes

- class mtk::RobinBCDescriptor1D

Impose Robin boundary conditions on the operators and on the grids.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

Typedefs

- typedef Real($*$ mtk::CoefficientFunction0D)(const Real &tt)

  A function of a BC coefficient evaluated on a 0D domain and time.

17.39.1 Detailed Description

This class presents an interface for the user to specify Robin boundary conditions on 1D mimetic operators and the grids they are acting on.

Def. Let $u(\mathbf{x},t) : \Omega \times [t_0,t_n] \mapsto \mathbb{R}$ be the solution to an ordinary or partial differential equation of interest. We say that u satisfies a **Robin boundary condition on** $\partial\Omega$ if and only if there exists $\beta(\mathbf{x},t) : \Omega \times [t_0,t_n] \mapsto \mathbb{R}$ so that:

$$\forall t \in [t_0,t_n] \; \forall \mathbf{x} \in \partial\Omega : \delta(\mathbf{x},t)u(\mathbf{x},t) + \eta(\mathbf{x},t)(\hat{\mathbf{n}} \cdot \nabla u) = \beta(\mathbf{x},t).$$

Intuitively, a **Robin boundary condition** is a constraint that must be satisfied by any linear combination of any scalar field u and its first normal derivative, in order for u to represent a unique solution to a given ordinary or partial differential equation of interest.

In a 1D context ($\partial\Omega = \{a,b\} \subset \mathbb{R}$), this condition can be written as follows:

$$\delta_a(a,t)u(a,t) - \eta_a(a,t)u'(a,t) = \beta_a(a,t),$$

$$\delta_b(b,t)u(b,t) + \eta_b(b,t)u'(b,t) = \beta_b(b,t).$$

Instances of this class receive information about the coefficient functions and each condition for any subset of the boundary (west and east, in 1D). These instances then handle the complexity of placing the coefficients in the differentiation matrices and the condition in the grids.

See also

`http://mathworld.wolfram.com/NormalVector.html`

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_robin_bc_descriptor_1d.h.

17.40 mtk_robin_bc_descriptor_1d.h

```
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```

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*/

#include <vector>

#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_uni_stg_grid_1d.h"
#include "mtk_lap_1d.h"

#ifndef MTK_INCLUDE_ROBIN_BC_DESCRIPTOR_1D_H_
#define MTK_INCLUDE_ROBIN_BC_DESCRIPTOR_1D_H_

namespace mtk {
typedef Real (*CoefficientFunction0D)(const Real &tt);

class RobinBCDescriptor1D {
 public:
  RobinBCDescriptor1D();

  RobinBCDescriptor1D(const RobinBCDescriptor1D &desc);

  ~RobinBCDescriptor1D() noexcept;

  int highest_order_diff_west() const noexcept;

  int highest_order_diff_east() const noexcept;

  void PushBackWestCoeff(CoefficientFunction0D cw);

  void PushBackEastCoeff(CoefficientFunction0D ce);

  void set_west_condition(Real (*west_condition)(const
Real &tt)) noexcept;

  void set_east_condition(Real (*east_condition)(const
Real &tt)) noexcept;

  bool ImposeOnLaplacianMatrix(const Lap1D &lap,
                               DenseMatrix &matrix,
                               const Real &time = mtk::kZero) const;
  void ImposeOnGrid(UniStgGrid1D &grid, const Real &time =
```

```
      mtk::kZero) const;

 private:
  int highest_order_diff_west_;
  int highest_order_diff_east_;

  std::vector<CoefficientFunction0D> west_coefficients_;
  std::vector<CoefficientFunction0D> east_coefficients_;

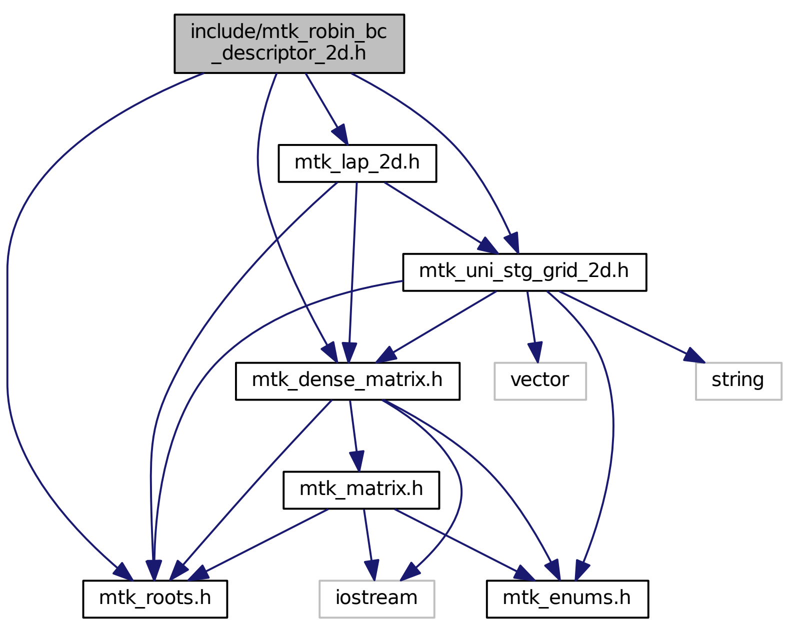
  Real (*west_condition_)(const Real &tt);
  Real (*east_condition_)(const Real &tt);
};
}
#endif  // End of: MTK_INCLUDE_ROBIN_BC_DESCRIPTOR_1D_H_
```

17.41 include/mtk_robin_bc_descriptor_2d.h File Reference

Impose Robin boundary conditions on the operators and on the grids.

```
#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_lap_2d.h"
#include "mtk_uni_stg_grid_2d.h"
```

Include dependency graph for mtk_robin_bc_descriptor_2d.h:



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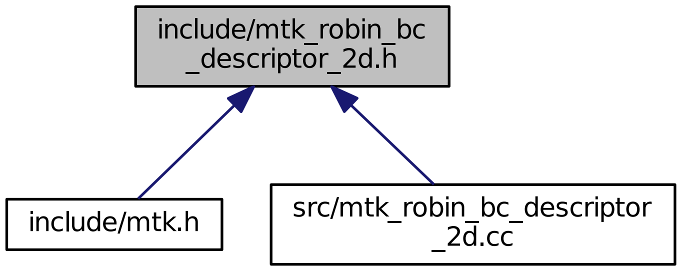

Classes

- class mtk::RobinBCDescriptor2D

  Impose Robin boundary conditions on the operators and on the grids.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

Typedefs

- typedef Real($*$ mtk::CoefficientFunction1D)(const Real &xx, const Real &tt)

  A function of a BC coefficient evaluated on a 1D domain and time.

17.41.1 Detailed Description

This class presents an interface for the user to specify Robin boundary conditions on 2D mimetic operators and the grids they are acting on.

Def. Let $u(\mathbf{x},t) : \Omega \times [t_0, t_n] \mapsto \mathbb{R}$ be the solution to an ordinary or partial differential equation of interest. We say that u satisfies a **Robin boundary condition on** $\partial\Omega$ if and only if there exists $\beta(\mathbf{x},t) : \Omega \times [t_0, t_n] \mapsto \mathbb{R}$ so that:

$$\forall t \in [t_0, t_n]\ \forall \mathbf{x} \in \partial\Omega : \delta(\mathbf{x},t)u(\mathbf{x},t) + \eta(\mathbf{x},t)(\hat{\mathbf{n}} \cdot \nabla u) = \beta(\mathbf{x},t).$$

Intuitively, a **Robin boundary condition** is a constraint that must be satisfied by any linear combination of any scalar field u and its first normal derivative, in order for u to represent a unique solution to a given ordinary or partial differential equation of interest.

Instances of this class receive information about the coefficient functions and each condition for any subset of the boundary (west, east, south and north in 2D). These instances then handle the complexity of placing the coefficients in the differentiation matrices and the conditions in the grids.

See also

http://mathworld.wolfram.com/NormalVector.html

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_robin_bc_descriptor_2d.h.

17.42 mtk_robin_bc_descriptor_2d.h

```
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#define MTK_INCLUDE_BC_DESCRIPTOR_2D_H_

#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_lap_2d.h"
#include "mtk_uni_stg_grid_2d.h"

namespace mtk{

typedef Real (*CoefficientFunction1D)(const Real &xx, const Real &tt);

class RobinBCDescriptor2D {
```

```
 public:
  RobinBCDescriptor2D();

  RobinBCDescriptor2D(const RobinBCDescriptor2D &desc);

  ~RobinBCDescriptor2D() noexcept;

  int highest_order_diff_west() const noexcept;

  int highest_order_diff_east() const noexcept;

  int highest_order_diff_south() const noexcept;

  int highest_order_diff_north() const noexcept;

  void PushBackWestCoeff(CoefficientFunction1D cw);

  void PushBackEastCoeff(CoefficientFunction1D ce);

  void PushBackSouthCoeff(CoefficientFunction1D cs);

  void PushBackNorthCoeff(CoefficientFunction1D cn);

  void set_west_condition(Real (*west_condition)(const Real &yy,
                                                 const Real &tt)) noexcept;

  void set_east_condition(Real (*east_condition)(const Real &yy,
                                                 const Real &tt)) noexcept;

  void set_south_condition(Real (*south_condition)(const Real &xx,
                                                   const Real &tt)) noexcept;

  void set_north_condition(Real (*north_condition)(const Real &xx,
                                                   const Real &tt)) noexcept;

  bool ImposeOnLaplacianMatrix(const Lap2D &lap,
                               const UniStgGrid2D &grid,
                               DenseMatrix &matrix,
                               const Real &time = kZero) const;
  void ImposeOnGrid(UniStgGrid2D &grid, const Real &time = kZero) const;

 private:
  bool ImposeOnSouthBoundaryNoSpace(const Lap2D &lap,
                                    const UniStgGrid2D &grid,
                                    DenseMatrix &matrix,
                                    const Real &time = kZero) const;
  bool ImposeOnNorthBoundaryNoSpace(const Lap2D &lap,
                                    const UniStgGrid2D &grid,
                                    DenseMatrix &matrix,
                                    const Real &time = kZero) const;
  bool ImposeOnWestBoundaryNoSpace(const Lap2D &lap,
                                   const UniStgGrid2D &grid,
                                   DenseMatrix &matrix,
                                   const Real &time = kZero) const;
  bool ImposeOnEastBoundaryNoSpace(const Lap2D &lap,
                                   const UniStgGrid2D &grid,
                                   DenseMatrix &matrix,
                                   const Real &time = kZero) const;
  bool ImposeOnSouthBoundaryWithSpace(const Lap2D &lap,
                                      const UniStgGrid2D &grid,
                                      DenseMatrix &matrix,
                                      const Real &time = kZero) const;
  bool ImposeOnNorthBoundaryWithSpace(const Lap2D &lap,
                                      const UniStgGrid2D &grid,
                                      DenseMatrix &matrix,
                                      const Real &time = kZero) const;
  bool ImposeOnWestBoundaryWithSpace(const Lap2D &lap,
                                     const UniStgGrid2D &grid,
                                     DenseMatrix &matrix,
                                     const Real &time = kZero) const;
  bool ImposeOnEastBoundaryWithSpace(const Lap2D &lap,
                                     const UniStgGrid2D &grid,
                                     DenseMatrix &matrix,
                                     const Real &time = kZero) const;

  int highest_order_diff_west_;
```

```
  int highest_order_diff_east_;
  int highest_order_diff_south_;
  int highest_order_diff_north_;

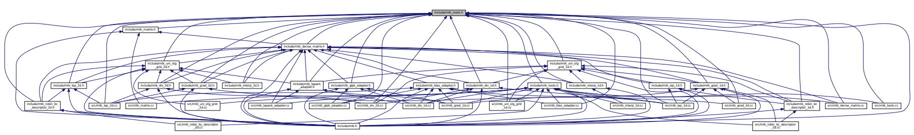
  std::vector<CoefficientFunction1D> west_coefficients_;
  std::vector<CoefficientFunction1D> east_coefficients_;
  std::vector<CoefficientFunction1D> south_coefficients_;
  std::vector<CoefficientFunction1D> north_coefficients_;

  Real (*west_condition_)(const Real &xx, const Real &tt);
  Real (*east_condition_)(const Real &xx, const Real &tt);
  Real (*south_condition_)(const Real &yy, const Real &tt);
  Real (*north_condition_)(const Real &yy, const Real &tt);
};
}
#endif  // End of: MTK_INCLUDE_BC_DESCRIPTOR_2D_H_
```

17.43 include/mtk_roots.h File Reference

Fundamental definitions to be used across all classes of the MTK.

This graph shows which files directly or indirectly include this file:



Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

Typedefs

- typedef float mtk::Real

  Users can simply change this to build a double- or single-precision MTK.

Variables

- const float mtk::kZero {0.0f}

  MTK's zero defined according to selective compilation.
- const float mtk::kOne {1.0f}

  MTK's one defined according to selective compilation.
- const float mtk::kTwo {2.0f}

  MTK's two defined according to selective compilation.
- const float mtk::kDefaultTolerance {1e-7f}

  Considered tolerance for comparisons in numerical methods.
- const int mtk::kDefaultOrderAccuracy {2}

  Default order of accuracy for mimetic operators.
- const float mtk::kDefaultMimeticThreshold {1e-6f}

  Default tolerance for higher-order mimetic operators.

- const int mtk::kCriticalOrderAccuracyDiv {8}

    At this order (and higher) we must use the CBSA to construct.

- const int mtk::kCriticalOrderAccuracyGrad {10}

    At this order (and higher) we must use the CBSA to construct.

17.43.1 Detailed Description

This file contains the fundamental definitions that classes of the MTK rely on to be implemented. Examples of these definitions are the definition of fundamental data types, and global variables affecting the construction of mimetic operators, among others.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at sciences dot sdsu dot edu

Todo Documentation should (better?) capture effects from selective compilation.

Todo Test selective precision mechanisms.

Definition in file mtk_roots.h.

17.44 mtk_roots.h

```

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```

```
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*/

#ifndef MTK_INCLUDE_ROOTS_H_
#define MTK_INCLUDE_ROOTS_H_

namespace mtk {

#ifdef MTK_PRECISION_DOUBLE
typedef double Real;
#else
typedef float Real;
#endif

#ifdef MTK_PRECISION_DOUBLE
const double kZero{0.0};
const double kOne{1.0};
const double kTwo{2.0};
#else
const float kZero{0.0f};
const float kOne{1.0f};
const float kTwo{2.0f};
#endif

#ifdef MTK_PRECISION_DOUBLE
const double kDefaultTolerance{1e-7};
#else
const float kDefaultTolerance{1e-7f};
#endif

const int kDefaultOrderAccuracy{2};

#ifdef MTK_PRECISION_DOUBLE
const double kDefaultMimeticThreshold{1e-6};
#else
const float kDefaultMimeticThreshold{1e-6f};
#endif

const int kCriticalOrderAccuracyDiv{8};

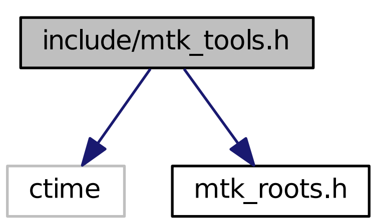
const int kCriticalOrderAccuracyGrad{10};
}
#endif  // End of: MTK_INCLUDE_ROOTS_H_
```

17.45 include/mtk_tools.h File Reference

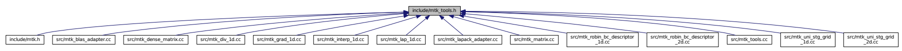
Tool manager class.

```
#include <ctime>
#include "mtk_roots.h"
```

Include dependency graph for mtk_tools.h:



This graph shows which files directly or indirectly include this file:



Classes

- class mtk::Tools

  Tool manager class.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

17.45.1 Detailed Description

Basic utilities.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Note

Performance Tip 8.1. If they do not need to be modified by the called function, pass large objects using pointers to constant data or references to constant data, to obtain the performance benefits of pass-by-reference.

Definition in file mtk_tools.h.

17.46 mtk_tools.h

```

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```

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*/

#ifndef MTK_INCLUDE_TOOLS_H_
#define MTK_INCLUDE_TOOLS_H_

#include <ctime>

#include "mtk_roots.h"

namespace mtk {

class Tools {
 public:
  static void Prevent(const bool complement,
                      const char *const fname,
                      int lineno,
                      const char *const fxname) noexcept;

  static void BeginUnitTestNo(const int &nn) noexcept;

  static void EndUnitTestNo(const int &nn) noexcept;

  static void Assert(const bool &condition) noexcept;

 private:
  static int test_number_;

  static Real duration_;

  static clock_t begin_time_;
};
}
#endif  // End of: MTK_INCLUDE_TOOLS_H_
```
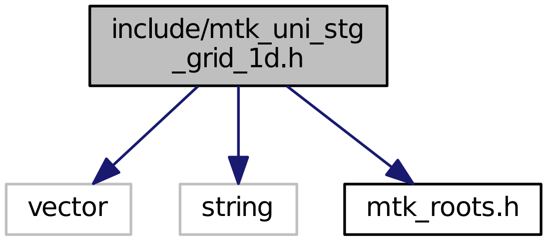

17.47 include/mtk_uni_stg_grid_1d.h File Reference

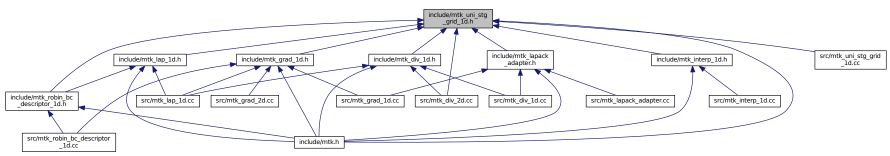
Definition of an 1D uniform staggered grid.

```
#include <vector>
#include <string>
#include "mtk_roots.h"
```

Include dependency graph for mtk_uni_stg_grid_1d.h:



This graph shows which files directly or indirectly include this file:



Classes

- class mtk::UniStgGrid1D

  Uniform 1D Staggered Grid.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

17.47.1 Detailed Description

Definition of an 1D uniform staggered grid.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Todo Create overloaded binding routines that read data from files.

Definition in file mtk_uni_stg_grid_1d.h.

17.48 mtk_uni_stg_grid_1d.h

```
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ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT
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*/

#ifndef MTK_INCLUDE_UNI_STG_GRID_1D_H_
#define MTK_INCLUDE_UNI_STG_GRID_1D_H_

#include <vector>
#include <string>

#include "mtk_roots.h"

namespace mtk {

class UniStgGrid1D {
 public:
  friend std::ostream& operator <<(std::ostream& stream, UniStgGrid1D &in);

  UniStgGrid1D();

  UniStgGrid1D(const UniStgGrid1D &grid);

  UniStgGrid1D(const Real &west_bndy_x,
               const Real &east_bndy_x,
               const int &num_cells_x,
               const mtk::FieldNature &nature = mtk::SCALAR);

  ~UniStgGrid1D();

  Real west_bndy_x() const;

  Real east_bndy_x() const;

  Real delta_x() const;

```
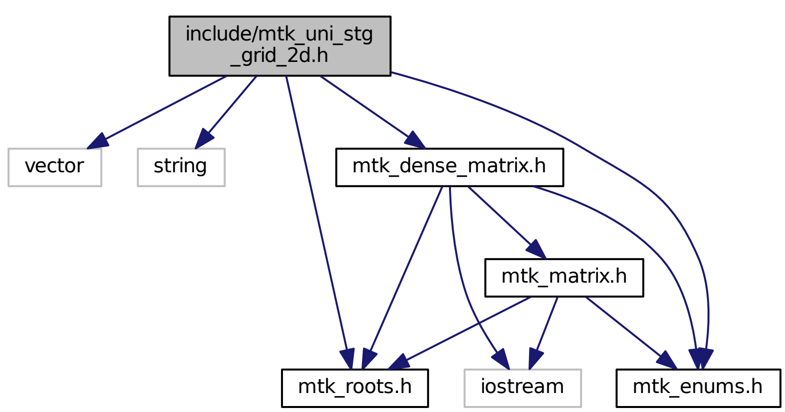

```
  const Real *discrete_domain_x() const;

  Real *discrete_field();

  int num_cells_x() const;

  void BindScalarField(Real (*ScalarField)(const Real &xx));

  void BindVectorField(Real (*VectorField)(Real xx));

  bool WriteToFile(std::string filename,
                   std::string space_name,
                   std::string field_name) const;

 private:
  FieldNature nature_;

  std::vector<Real> discrete_domain_x_;
  std::vector<Real> discrete_field_;

  Real west_bndy_x_;
  Real east_bndy_x_;
  Real num_cells_x_;
  Real delta_x_;
};
}
#endif  // End of: MTK_INCLUDE_UNI_STG_GRID_1D_H_
```

17.49 include/mtk_uni_stg_grid_2d.h File Reference

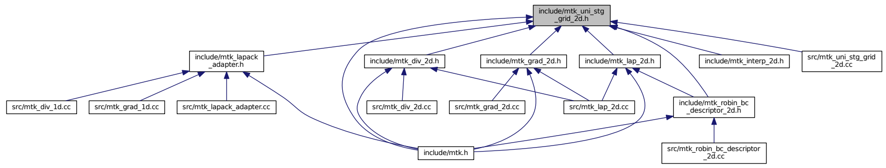
Definition of an 2D uniform staggered grid.

```
#include <vector>
#include <string>
#include "mtk_roots.h"
#include "mtk_enums.h"
#include "mtk_dense_matrix.h"
```

Include dependency graph for mtk_uni_stg_grid_2d.h:



This graph shows which files directly or indirectly include this file:



Classes

- class mtk::UniStgGrid2D

  Uniform 2D Staggered Grid.

Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

17.49.1 Detailed Description

Definition of an 2D uniform staggered grid.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Todo Create overloaded binding routines that read data from files.

Definition in file mtk_uni_stg_grid_2d.h.

17.50 mtk_uni_stg_grid_2d.h

```
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*/

#ifndef MTK_INCLUDE_UNI_STG_GRID_2D_H_
#define MTK_INCLUDE_UNI_STG_GRID_2D_H_

#include <vector>
#include <string>

#include "mtk_roots.h"
#include "mtk_enums.h"
#include "mtk_dense_matrix.h"

namespace mtk {

class UniStgGrid2D {
 public:
  friend std::ostream& operator <<(std::ostream& stream, UniStgGrid2D &in);

  UniStgGrid2D();

  UniStgGrid2D(const UniStgGrid2D &grid);

  UniStgGrid2D(const Real &west_bndy_x,
               const Real &east_bndy_x,
               const int &num_cells_x,
               const Real &south_bndy_y,
               const Real &north_bndy_y,
               const int &num_cells_y,
               const mtk::FieldNature &nature =
mtk::SCALAR);

  ~UniStgGrid2D();

  const Real *discrete_domain_x() const;

  const Real *discrete_domain_y() const;

  Real *discrete_field();

  FieldNature nature() const;

  Real west_bndy() const;

  Real east_bndy() const;

  int num_cells_x() const;

  Real delta_x() const;

  Real south_bndy() const;

  Real north_bndy() const;

  int num_cells_y() const;

  Real delta_y() const;

  bool Bound() const;
```

```
  int Size() const;

  void BindScalarField(Real (*ScalarField)(const Real &xx, const Real &yy));

  void BindVectorField(Real (*VectorFieldPComponent)(const Real &xx,
                                                     const Real &yy),
                       Real (*VectorFieldQComponent)(const Real &xx,
                                                     const Real &yy));

  bool WriteToFile(std::string filename,
                   std::string space_name_x,
                   std::string space_name_y,
                   std::string field_name) const;

 private:
  void BindVectorFieldPComponent(
    Real (*VectorFieldPComponent)(const Real &xx, const Real &yy));

  void BindVectorFieldQComponent(
    Real (*VectorFieldQComponent)(const Real &xx, const Real &yy));

  std::vector<Real> discrete_domain_x_;
  std::vector<Real> discrete_domain_y_;
  std::vector<Real> discrete_field_;

  FieldNature nature_;

  Real west_bndy_;
  Real east_bndy_;
  int num_cells_x_;
  Real delta_x_;

  Real south_bndy_;
  Real north_bndy_;
  int num_cells_y_;
  Real delta_y_;
};
}
#endif  // End of: MTK_INCLUDE_UNI_STG_GRID_2D_H_
```

17.51 Makefile.inc File Reference

17.52 Makefile.inc

```
# Makefile setup file for the MTK.

SHELL := /bin/bash

# Please set the following variables up:

#   1. Absolute path to base directory of the MTK.
#   __________________________________________________________________

BASE = /home/esanchez/Dropbox/MTK

#   2. The machine (platform) identifier and required machine precision.
#   __________________________________________________________________

# Options are:
# - LINUX: A LINUX box installation.
# - OSX: Uses OS X optimized solvers.

PLAT = LINUX

# Options are:
# - SINGLE: Use 4 B floating point numbers.
# - DOUBLE: Use 8 B floating point numbers.

PRECISION = DOUBLE

#   3. Optimized solvers and operations by means of ATLAS in Linux?
#   __________________________________________________________________
```

```
# If you have selected OSX in step 1, then you don't need to worry about this.

# Options are ON xor OFF:

ATL_OPT = OFF

#   4. Paths to dependencies (header files for compiling).
#   __________________________________________________________________

# GLPK include path (soon to go):

GLPK_INC = $(HOME)/Libraries/glpk-4.35/include

# Linux: If ATLAS optimization is ON, users should only provide the path to
# ATLAS:

ATLAS_INC = $(HOME)/Libraries/ATLAS_3.8.4-CORE/include

# OS X: Do nothing.

#   5. Paths to dependencies (archive files for (static) linking).
#   __________________________________________________________________

# GLPK linking path (soon to go):

GLPK_LIB = $(HOME)/Libraries/glpk-4.35/lib/lib64/libglpk.a

# If optimization is OFF, then provide the paths for:

BLAS_LIB = $(HOME)/Libraries/BLAS-3.5.0/libblas.a
LAPACK_LIB = $(HOME)/Libraries/lapack-3.5.0/liblapack.a

# WARNING: Vendor libraries should be used whenever they are available.

# However, if optimization is ON, please provide the path the ATLAS' archive:

ATLAS_LIB   = $(HOME)/Libraries/ATLAS_3.8.4-CORE/ATLAS_3.8.4-BUILD-Citadel/lib

#   6. Compiler and its flags.
#   __________________________________________________________________

CC = g++

# Selective Verbose Execution for Quick Debugging. Options are defined per
# concern, and per data hierarchy on each concern.

# 0: NO verbose at all.

# 1: Enable verbose down to the 7th concern: messages.
# 2: Enable verbose down to the 7th concern: messages + scalar results.
# 3: Enable verbose down to the 7th concern. 1.1. + array results.
# 4: Enable verbose down to the 7th concern. 1.2. + matrix results.

# 5: Enable verbose down to the 6th concern: messages.
# 6: Enable verbose down to the 6th concern: messages + scalar results.
# 7: Enable verbose down to the 6th concern. 2.1. + array results.
# 8: Enable verbose down to the 6th concern. 2.2. + matrix results.

# 9: Enable verbose down to the 5th concern: messages.
# 10: Enable verbose down to the 5th concern: messages + scalar results.
# 11: Enable verbose down to the 5th concern. 3.1. + array results.
# 12: Enable verbose down to the 5th concern. 3.2. + matrix results.

# 13: Enable verbose down to the 4th concern: messages.
# 14: Enable verbose down to the 4th concern: messages + scalar results.
# 15: Enable verbose down to the 4th concern. 4.1. + array results.
# 16: Enable verbose down to the 4th concern. 4.2. + matrix results.

VERBOSE_LEVEL = 16

# Enable preventions. In the MTK, methods first validate their required
# pre-conditions in run-time. Similarly, in many points throughout the MTK
# codebase, different sanity checks are performed, as well. If this symbol is
# defined to be 0, the MTK will # perform no validations to enhance execution
# performance. Options are:
# - YES.
# - NO.

PERFORM_PREVENTIONS = YES
```

```
# Flags recommended for release code:

CCFLAGS = -Wall -Werror -O3

# Flags recommended for debugging code:

CCFLAGS = -Wall -Werror -g

#   7. Archiver, its flags, and ranlib:
#   __________________________________________________________________

ARCH      = ar
ARCHFLAGS = cr

# If your system does not have "ranlib" then set: "RANLIB = echo":

RANLIB = echo

# But, if possible:

RANLIB = ranlib

#   8. Valgrind's memcheck options (optional):
#   __________________________________________________________________

MEMCHECK_OPTS = -v --tool=memcheck --leak-check=full --show-leak-kinds=all \
  --track-origins=yes --freelist-vol=20000000

# Done! User, please, do not mess with the definitions from this point on.

#   __________________________________________________________________
#   __________________________________________________________________
#   __________________________________________________________________

#   MTK-related.
#   __________________________________________________________________

SRC        = $(BASE)/src
INCLUDE    = $(BASE)/include
LIB        = $(BASE)/lib
MTK_LIB    = $(LIB)/libmtk.a
TESTS      = $(BASE)/tests
EXAMPLES   = $(BASE)/examples

#   Compiling-related.
#   __________________________________________________________________

CCFLAGS += -std=c++11 -fPIC \
  -DMTK_VERBOSE_LEVEL=$(VERBOSE_LEVEL) -I$(INCLUDE) -c

ifeq ($(PRECISION),DOUBLE)
  CCFLAGS += -DMTK_PRECISION_DOUBLE
else
  CCFLAGS += -DMTK_PRECISION_SINGLE
endif

ifeq ($(PERFORM_PREVENTIONS),YES)
  CCFLAGS += -DMTK_PERFORM_PREVENTIONS
endif

# Only the GLPK is included because the other dependencies are coded in Fortran.

ifeq ($(ATL_OPT),ON)
  CCFLAGS  += -I$(GLPK_INC) $(ATLAS_INC)
else
  CCFLAGS  += -I$(GLPK_INC)
endif

#   Linking-related.
#   __________________________________________________________________

NOOPT_LIBS  = $(LAPACK_LIB) $(BLAS_LIB) -lm $(GLPK_LIB) -lstdc++

OPT_LIBS    = -L$(ATLAS_LIB) -latlas -llapack -lblas -lm -latlas -lstdc++

ifeq ($(PLAT),OSX)
  LINKER  = g++
  LINKER  += -framework Accelerate $(GLPK_LIB) $(MTK_LIB)
else
  ifeq ($(ATL_OPT),ON)
    LINKER  = g++
```

```
    LIBS = $(MTK_LIB)
    LIBS += $(OPT_LIBS)
  else
    LINKER  = gfortran
    LIBS = $(MTK_LIB)
    LIBS += $(NOOPT_LIBS)
  endif
endif

#   Documentation-related.
#   __________________________________________________________________

DOCGEN      = doxygen
DOCFILENAME = doc_config.dxcf
DOC         = $(BASE)/doc
DOCFILE     = $(BASE)/$(DOCFILENAME)
```

17.53 README.md File Reference

17.54 README.md

```
# The Mimetic Methods Toolkit (MTK)

By: **Eduardo J. Sanchez, Ph.D. - esanchez at mail dot sdsu dot edu**
    __________________________________________________________________

## 1. Description

We define numerical methods that are based on discretizations preserving the
properties of their continuum counterparts to be **mimetic**.

The **Mimetic Methods Toolkit (MTK)** is a C++ library for mimetic numerical
methods. It is arranged as a set of classes for **mimetic quadratures**,
**mimetic interpolation**, and **mimetic finite differences** methods for the
numerical solution of ordinary and partial differential equations.

An older version of this library is available outside of GitHub... just email me
about it, and you can have it... it is ugly, yet it is functional and more
complete.
    __________________________________________________________________

## 2. Dependencies

This README assumes all of these dependencies are installed in the following
folder:

```
$(HOME)/Libraries/
```

In this version, the MTK optionally uses ATLAS-optimized BLAS and LAPACK
routines for the internal computation on some of the layers. However, ATLAS
requires both BLAS and LAPACK in order to create their optimized distributions.
Therefore, the following dependencies tree arises:

For Linux:

1. LAPACK - Available from: http://www.netlib.org/lapack/
  1. BLAS - Available from: http://www.netlib.org/blas/

2. GLPK - Available from: https://www.gnu.org/software/glpk/

3. (Optional) ATLAS - Available from: http://math-atlas.sourceforge.net/
  1. LAPACK - Available from: http://www.netlib.org/lapack/
    1. BLAS - Available from: http://www.netlib.org/blas

4. (Optional) Valgrind - Available from: http://valgrind.org/

5. (Optional) Doxygen - Available from http://www.stack.nl/~dimitri/doxygen/

For OS X:

1. GLPK - Available from: https://www.gnu.org/software/glpk/
    ____

```

```
3. Installation

PART 1. CONFIGURATION OF THE MAKEFILE.

The following steps are required to build and test the MTK. Please use the
accompanying 'Makefile.inc' file, which should provide a solid template to
start with. The following command provides help on the options for make:

```
$ make help
-----
Makefile for the MTK.

Options are:
- all: builds the library, the tests, and examples.
- mtklib: builds the library.
- test: builds the test files.
- example: builds the examples.

- testall: runs all the tests.

- gendoc: generates the documentation for the library.

- clean: cleans all the generated files.
- cleanlib: cleans the generated archive and object files.
- cleantest: cleans the generated tests executables.
- cleanexample: cleans the generated examples executables.
-----
```

PART 2. BUILD THE LIBRARY.

```
$ make
```

If successful you'll read (before building the tests and examples):

```
----- Library created! Check in /home/ejspeiro/Dropbox/MTK/lib
```

Examples and tests will also be built.
    ____

4. Frequently Asked Questions

Q: Why haven't you guys implemented GBS to build the library?
A: I'm on it as we speak! ;)

Q: Is there any main reference when it comes to the theory on Mimetic Methods?
A: Yes! Check: http://www.csrc.sdsu.edu/mimetic-book

Q: Do I need to generate the documentation myself?
A: You can if you want to... but if you DO NOT want to, just go to our website.
    ____

5. Contact, Support, and Credits

The MTK is developed by researchers and adjuncts to the
[Computational Science Research Center (CSRC)](http://www.csrc.sdsu.edu/)
at [San Diego State University (SDSU)](http://www.sdsu.edu/).

Developers are members of:

1. Mimetic Numerical Methods Research and Development Group.
2. Computational Geoscience Research and Development Group.
3. Ocean Modeling Research and Development Group.

Currently the developers are:

- **Eduardo J. Sanchez, Ph.D. - esanchez at mail dot sdsu dot edu** - @ejspeiro
- Jose E. Castillo, Ph.D. - jcastillo at mail dot sdsu dot edu
- Guillermo F. Miranda, Ph.D. - unigrav at hotmail dot com
- Christopher P. Paolini, Ph.D. - paolini at engineering dot sdsu dot edu
- Angel Boada.
- Johnny Corbino.
- Raul Vargas-Navarro.

Finally, please feel free to contact me with suggestions or corrections:

```

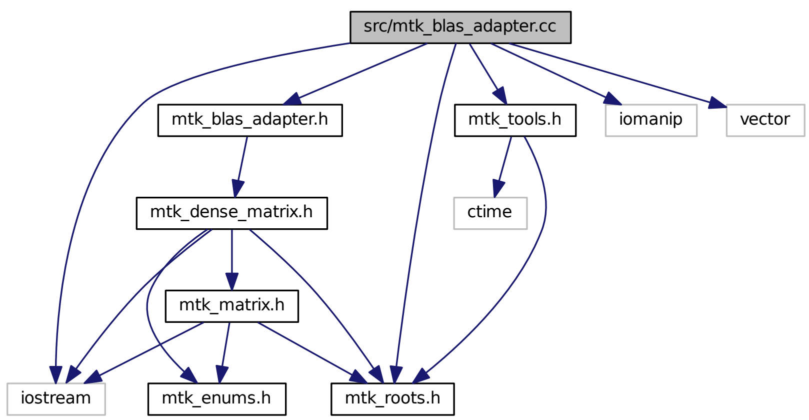
```
00136 **Eduardo J. Sanchez, Ph.D. - esanchez at mail dot sdsu dot edu** - @ejspeiro
00137
00138 Thanks and happy coding!
```

17.55 src/mtk_blas_adapter.cc File Reference

Adapter class for the BLAS API.

```
#include <iostream>
#include <iomanip>
#include <vector>
#include "mtk_roots.h"
#include "mtk_tools.h"
#include "mtk_blas_adapter.h"
```

Include dependency graph for mtk_blas_adapter.cc:



Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

Functions

- float mtk::snrm2_ (int ∗n, float ∗x, int ∗incx)
- void mtk::saxpy_ (int ∗n, float ∗sa, float ∗sx, int ∗incx, float ∗sy, int ∗incy)
- void mtk::sgemv_ (char ∗trans, int ∗m, int ∗n, float ∗alpha, float ∗a, int ∗lda, float ∗x, int ∗incx, float ∗beta, float ∗y, int ∗incy)
- void mtk::sgemm_ (char ∗transa, char ∗transb, int ∗m, int ∗n, int ∗k, double ∗alpha, double ∗a, int ∗lda, double ∗b, aamm int ∗ldb, double ∗beta, double ∗c, int ∗ldc)

17.55.1 Detailed Description

This class contains a collection of static classes, that posses direct access to the underlying structure of the matrices, thus allowing programmers to exploit some of the numerical methods implemented in the BLAS.

The **BLAS (Basic Linear Algebra Subprograms)** are routines that provide standard building blocks for performing basic vector and matrix operations. The Level 1 BLAS perform scalar, vector and vector-vector operations, the Level 2 BLAS perform matrix-vector operations, and the Level 3 BLAS perform matrix-matrix operations.

The BLAS can be installed from links given in the See Also section of this page.

See also

http://www.netlib.org/blas/
https://software.intel.com/en-us/non-commercial-software-development

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_blas_adapter.cc.

17.56 mtk_blas_adapter.cc

```

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page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
should be developed and included in any deliverable.

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(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
```

```
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#include <iostream>
#include <iomanip>

#include <vector>

#include "mtk_roots.h"
#include "mtk_tools.h"
#include "mtk_blas_adapter.h"

namespace mtk {

extern "C" {

#ifdef MTK_PRECISION_DOUBLE

double dnrm2_(int *n, double *x, int *incx);
#else

float snrm2_(int *n, float *x, int *incx);
#endif

#ifdef MTK_PRECISION_DOUBLE

void daxpy_(int *n, double *da, double *dx, int *incx, double *dy, int *incy);
#else

void saxpy_(int *n, float *sa, float *sx, int *incx, float *sy, int *incy);
#endif

#ifdef MTK_PRECISION_DOUBLE

void dgemv_(char *trans,
            int *m,
            int *n,
            double *alpha,
            double *a,
            int *lda,
            double *x,
            int *incx,
            double *beta,
            double *y,
            int *incy);
#else

void sgemv_(char *trans,
            int *m,
            int *n,
            float *alpha,
            float *a,
            int *lda,
            float *x,
            int *incx,
            float *beta,
            float *y,
            int *incy);
#endif

#ifdef MTK_PRECISION_DOUBLE

void dgemm_(char *transa,
            char* transb,
            int *m,
            int *n,
            int *k,
            double *alpha,
            double *a,
            int *lda,
            double *b,
            int *ldb,
            double *beta,
            double *c,
            int *ldc);
}
#else

void sgemm_(char *transa,
            char* transb,
            int *m,
```

```
            int *n,
            int *k,
            double *alpha,
            double *a,
            int *lda,
            double *b,aamm
            int *ldb,
            double *beta,
            double *c,
            int *ldc);
}
#endif
}

mtk::Real mtk::BLASAdapter::RealNRM2(Real *in, int &in_length) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(in_length <= 0, __FILE__, __LINE__, __func__);
  #endif

  int incx{1};  // Increment for the elements of xx. ix >= 0.

  #ifdef MTK_PRECISION_DOUBLE
  return dnrm2_(&in_length, in, &incx);
  #else
  return snrm2_(&in_length, in, &incx);
  #endif
}

void mtk::BLASAdapter::RealAXPY(mtk::Real alpha,
                                mtk::Real *xx,
                                mtk::Real *yy,
                                int &in_length) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(xx == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(yy == nullptr, __FILE__, __LINE__, __func__);
  #endif

  int incx{1};  // Increment for the elements of xx. ix >= 0.

  #ifdef MTK_PRECISION_DOUBLE
  daxpy_(&in_length, &alpha, xx, &incx, yy, &incx);
  #else
  saxpy_(&in_length, &alpha, xx, &incx, yy, &incx);
  #endif
}

mtk::Real mtk::BLASAdapter::RelNorm2Error(mtk::Real *computed,
                                          mtk::Real *known,
                                          int length) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(computed == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(known == nullptr, __FILE__, __LINE__, __func__);
  #endif

  mtk::Real norm_2_computed{mtk::BLASAdapter::RealNRM2(known, length)};

  mtk::Real alpha{-mtk::kOne};

  mtk::BLASAdapter::RealAXPY(alpha, known, computed, length);

  mtk::Real norm_2_difference{mtk::BLASAdapter::RealNRM2(computed, length)};

  return norm_2_difference/norm_2_computed;
}

void mtk::BLASAdapter::RealDenseMV(mtk::Real &alpha,
                                   mtk::DenseMatrix &aa,
                                   mtk::Real *xx,
                                   mtk::Real &beta,
                                   mtk::Real *yy) {

  // Make sure input matrices are row-major ordered.

  if (aa.matrix_properties().ordering() == mtk::COL_MAJOR) {
    aa.OrderRowMajor();
```

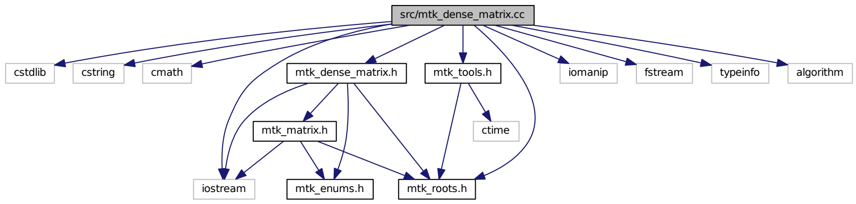
```
  }

  char transa{'T'}; // State that now, the input WILL be in row-major ordering.

  int mm{aa.num_rows()};                   // Rows of aa.
  int nn{aa.num_cols()};                   // Columns of aa.
  int lda{(aa.matrix_properties()).ld()}; // Leading dimension.
  int incx{1};                             // Increment of values in x.
  int incy{1};                             // Increment of values in y.

  std::swap(mm,nn);
  #ifdef MTK_PRECISION_DOUBLE
  dgemv_(&transa, &mm, &nn, &alpha, aa.data(), &lda,
         xx, &incx, &beta, yy, &incy);
  #else
  sgemv_(&transa, &mm, &nn, &alpha, aa.data(), &lda,
        xx, &incx, &beta, yy, &incy);
  #endif
  std::swap(mm,nn);
}

mtk::DenseMatrix mtk::BLASAdapter::RealDenseMM(
mtk::DenseMatrix &aa,
                                               mtk::DenseMatrix &bb) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(aa.num_cols() != bb.num_rows(),
                      __FILE__, __LINE__, __func__);
  #endif

  if (aa.matrix_properties().ordering() ==
mtk::COL_MAJOR) {
    aa.OrderRowMajor();
  }
  if (bb.matrix_properties().ordering() ==
mtk::COL_MAJOR) {
    bb.OrderRowMajor();
  }

  char ta{'T'}; // State that input matrix aa is in row-wise ordering.
  char tb{'T'}; // State that input matrix bb is in row-wise ordering.

  int mm{aa.num_rows()};  // Rows of aa and rows of cc.
  int nn{bb.num_cols()};  // Cols of bb and cols of cc.
  int kk{aa.num_cols()};  // Cols of aa and rows of bb.

  int cc_num_rows{mm};  // Rows of cc.
  int cc_num_cols{nn};  // Columns of cc.

  int lda{std::max(1,kk)};  // Leading dimension of the aa matrix.
  int ldb{std::max(1,nn)};  // Leading dimension of the bb matrix.
  int ldc{std::max(1,mm)};  // Leading dimension of the cc matrix.

  mtk::Real alpha{mtk::kOne}; // First scalar coefficient.
  mtk::Real beta{mtk::kZero}; // Second scalar coefficient.

  mtk::DenseMatrix cc_col_maj_ord(cc_num_rows,cc_num_cols); // Output matrix.

  cc_col_maj_ord.SetOrdering(mtk::COL_MAJOR);

  #ifdef MTK_PRECISION_DOUBLE
  dgemm_(&ta, &tb, &mm, &nn, &kk, &alpha, aa.data(), &lda,
         bb.data(), &ldb, &beta, cc_col_maj_ord.data(), &ldc);
  #else
  sgemm_(&ta, &tb, &mm, &nn, &kk, &alpha, aa.data(), &lda,
         bb.data(), &ldb, &beta, cc_col_maj_ord.data(), &ldc);
  #endif

  #if MTK_VERBOSE_LEVEL > 12
  std::cout << "cc_col_maj_ord =" << std::endl;
  std::cout << cc_col_maj_ord << std::endl;
  #endif

  cc_col_maj_ord.OrderRowMajor();

  return cc_col_maj_ord;
}

mtk::DenseMatrix mtk::BLASAdapter::RealDenseSM(
mtk::Real alpha,
                                               mtk::DenseMatrix &aa) {
```

```
  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(aa.num_rows() == 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(aa.num_cols() == 0, __FILE__, __LINE__, __func__);
  #endif

  if (aa.matrix_properties().ordering() == mtk::COL_MAJOR) {
    aa.OrderRowMajor();
  }

  char ta{'T'}; // State that input matrix aa is in row-wise ordering.
  char tb{'T'}; // State that input matrix bb is in row-wise ordering.

  int mm{aa.num_rows()};  // Rows of aa and rows of cc.
  int nn{aa.num_cols()};  // Cols of bb and cols of cc.
  int kk{aa.num_cols()};  // Cols of aa and rows of bb.

  int lda{std::max(1,kk)};  // Leading dimension of the aa matrix.
  int ldb{std::max(1,nn)};  // Leading dimension of the bb matrix.
  int ldc{std::max(1,mm)};  // Leading dimension of the cc matrix.

  mtk::Real beta{alpha}; // Second scalar coefficient.

  alpha = mtk::kZero;

  mtk::DenseMatrix alpha_aa(aa); // Output matrix.

  #ifdef MTK_PRECISION_DOUBLE
  dgemm_(&ta, &tb, &mm, &nn, &kk, &alpha, aa.data(), &lda,
         aa.data(), &ldb, &beta, alpha_aa.data(), &ldc);
  #else
  sgemm_(&ta, &tb, &mm, &nn, &kk, &alpha, aa.data(), &lda,
         aa.data(), &ldb, &beta, alpha_aa.data(), &ldc);
  #endif

  #if MTK_VERBOSE_LEVEL > 12
  std::cout << "alpha_aa =" << std::endl;
  std::cout << alpha_aa << std::endl;
  #endif

  return alpha_aa;
}
```

17.57 src/mtk_dense_matrix.cc File Reference

```
#include <cstdlib>
#include <cstring>
#include <cmath>
#include <iostream>
#include <iomanip>
#include <fstream>
#include <typeinfo>
#include <algorithm>
#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_tools.h"
```

Include dependency graph for mtk_dense_matrix.cc:



Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

Functions

- std::ostream & mtk::operator<< (std::ostream &stream, mtk::DenseMatrix &in)

17.58 mtk_dense_matrix.cc

```

/*
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page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
should be developed and included in any deliverable.

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```
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SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#include <cstdlib>
#include <cstring>
#include <cmath>

#include <iostream>
#include <iomanip>
#include <fstream>

#include <typeinfo>

#include <algorithm>

#include "mtk_roots.h"
#include "mtk_dense_matrix.h"
#include "mtk_tools.h"

namespace mtk {

std::ostream& operator <<(std::ostream &stream, mtk::DenseMatrix &in) {

  int mm{in.matrix_properties_.num_rows()};  // Auxiliary.
  int nn{in.matrix_properties_.num_cols()};  // Auxiliary.

  if (in.matrix_properties_.ordering() ==
mtk::COL_MAJOR) {
    std::swap(mm, nn);
  }
  for (int ii = 0; ii < mm; ii++) {
    int offset{ii*nn};
    for (int jj = 0; jj < nn; jj++) {
      mtk::Real value = in.data_[offset + jj];
      stream << std::setw(9) << value;
    }
    stream << std::endl;
  }
  if (in.matrix_properties_.ordering() ==
mtk::COL_MAJOR) {
    std::swap(mm, nn);
  }
  return stream;
}
}

mtk::DenseMatrix& mtk::DenseMatrix::operator =(const
mtk::DenseMatrix &in) {

  if(this == &in) {
    return *this;
  }

  matrix_properties_.set_storage(in.
matrix_properties_.storage());

  matrix_properties_.set_ordering(in.
matrix_properties_.ordering());

  auto aux = in.matrix_properties_.num_rows();
  matrix_properties_.set_num_rows(aux);

  aux = in.matrix_properties().num_cols();
  matrix_properties_.set_num_cols(aux);

  aux = in.matrix_properties().num_zero();
  matrix_properties_.set_num_zero(aux);

  aux = in.matrix_properties().num_null();
  matrix_properties_.set_num_null(aux);

  auto num_rows = matrix_properties_.num_rows();
  auto num_cols = matrix_properties_.num_cols();

  delete [] data_;

  try {
```

```
    data_ = new mtk::Real[num_rows*num_cols];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(data_, mtk::kZero, sizeof(data_[0])*num_rows*num_cols);

  std::copy(in.data_, in.data_ + num_rows*num_cols, data_);

  return *this;
}

bool mtk::DenseMatrix::operator ==(const DenseMatrix &in) {

  bool ans{true};

  auto mm = in.num_rows();
  auto nn = in.num_cols();

  if (mm != matrix_properties_.num_rows() ||
      nn != matrix_properties_.num_cols()) {
    return false;
  }

  for (int ii = 0; ii < mm && ans; ++ii) {
    for (int jj = 0; jj < nn && ans; ++jj) {
      ans = ans &&
        abs(data_[ii*nn + jj] - in.data()[ii*nn + jj]) < mtk::kDefaultTolerance;
    }
  }
  return ans;
}

mtk::DenseMatrix::DenseMatrix(): data_(nullptr) {

  matrix_properties_.set_storage(mtk::DENSE);
  matrix_properties_.set_ordering(mtk::ROW_MAJOR);
}

mtk::DenseMatrix::DenseMatrix(const mtk::DenseMatrix &in) {

  matrix_properties_.set_storage(in.matrix_properties_.storage());

  matrix_properties_.set_ordering(in.matrix_properties_.ordering());

  auto aux = in.matrix_properties_.num_rows();
  matrix_properties_.set_num_rows(aux);

  aux = in.matrix_properties().num_cols();
  matrix_properties_.set_num_cols(aux);

  aux = in.matrix_properties().num_zero();
  matrix_properties_.set_num_zero(aux);

  aux = in.matrix_properties().num_null();
  matrix_properties_.set_num_null(aux);

  auto num_rows = in.matrix_properties_.num_rows();
  auto num_cols = in.matrix_properties_.num_cols();

  try {
    data_ = new mtk::Real[num_rows*num_cols];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(data_, mtk::kZero, sizeof(data_[0])*num_rows*num_cols);

  std::copy(in.data_,in.data_ + num_rows*num_cols,data_);
}

mtk::DenseMatrix::DenseMatrix(const int &num_rows, const int &num_cols) {

  #ifdef MTK_PERFORM_PREVENTIONS
```

```
  mtk::Tools::Prevent(num_rows < 1, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(num_cols < 1, __FILE__, __LINE__, __func__);
  #endif

  matrix_properties_.set_storage(mtk::DENSE);
  matrix_properties_.set_ordering(mtk::ROW_MAJOR);
  matrix_properties_.set_num_rows(num_rows);
  matrix_properties_.set_num_cols(num_cols);

  try {
    data_ = new mtk::Real[num_rows*num_cols];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(data_, mtk::kZero, sizeof(data_[0])*num_rows*num_cols);
}

mtk::DenseMatrix::DenseMatrix(const int &rank,
                              const bool &padded,
                              const bool &transpose) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(rank < 1, __FILE__, __LINE__, __func__);
  #endif

  int aux{};  // Used to control the padding.

  if (padded) {
    aux = 1;
  }

  matrix_properties_.set_storage(mtk::DENSE);
  matrix_properties_.set_ordering(mtk::ROW_MAJOR);
  matrix_properties_.set_num_rows(aux + rank + aux);
  matrix_properties_.set_num_cols(rank);

  try {
    data_ = new mtk::Real[matrix_properties_.num_values()];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(data_,
         mtk::kZero,
         sizeof(data_[0])*(matrix_properties_.num_values()));

  for (auto ii =0 ; ii < matrix_properties_.num_rows(); ++ii) {
    for (auto jj = 0; jj < matrix_properties_.num_cols(); ++jj) {
      data_[ii*matrix_properties_.num_cols() + jj] =
        (ii == jj + aux)? mtk::kOne: mtk::kZero;
    }
  }
  if (transpose) {
    Transpose();
  }
}

mtk::DenseMatrix::DenseMatrix(const mtk::Real *const gen,
                              const int &gen_length,
                              const int &pro_length,
                              const bool &transpose) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(gen == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(gen_length < 1, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(pro_length < 1, __FILE__, __LINE__, __func__);
  #endif

  matrix_properties_.set_storage(mtk::DENSE);
  matrix_properties_.set_ordering(mtk::ROW_MAJOR);
  if (!transpose) {
    matrix_properties_.set_num_rows(gen_length);
    matrix_properties_.set_num_cols(pro_length);
  } else {
    matrix_properties_.set_num_rows(pro_length);
    matrix_properties_.set_num_cols(gen_length);
  }

```

```
  int mm = matrix_properties_.num_rows(); // Used to construct this matrix.
  int nn = matrix_properties_.num_cols(); // Used to construct this matrix.

  try {
    data_ = new mtk::Real[mm*nn];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(data_, mtk::kZero, sizeof(data_[0])*mm*nn);

  if (!transpose) {
    for (auto ii = 0; ii < mm; ii++) {
      for (auto jj = 0; jj < nn; jj++) {
        data_[ii*nn + jj] = pow(gen[ii], (double) jj);
      }
    }
  } else {
    for (auto ii = 0; ii < mm; ii++) {
      for (auto jj = 0; jj < nn; jj++) {
        data_[ii*nn + jj] = pow(gen[jj], (double) ii);
      }
    }
  }
}

mtk::DenseMatrix::~DenseMatrix() {

  delete [] data_;
  data_ = nullptr;
}

mtk::Matrix mtk::DenseMatrix::matrix_properties() const
noexcept {

  return matrix_properties_;
}

void mtk::DenseMatrix::SetOrdering(
mtk::MatrixOrdering oo) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(!(oo == mtk::ROW_MAJOR || oo ==
mtk::COL_MAJOR),
                      __FILE__, __LINE__, __func__);
  #endif

  matrix_properties_.set_ordering(oo);
}

int mtk::DenseMatrix::num_rows() const noexcept {

  return matrix_properties_.num_rows();
}

int mtk::DenseMatrix::num_cols() const noexcept {

  return matrix_properties_.num_cols();
}

mtk::Real* mtk::DenseMatrix::data() const noexcept {

  return data_;
}

mtk::Real mtk::DenseMatrix::GetValue(
    const int &mm,
    const int &nn) const noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(mm < 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(nn < 0, __FILE__, __LINE__, __func__);
  #endif

  return data_[mm*matrix_properties_.num_cols() + nn];
}

void  mtk::DenseMatrix::SetValue(
    const int &mm,
    const int &nn,
```

```
    const mtk::Real &val) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(mm < 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(nn < 0, __FILE__, __LINE__, __func__);
  #endif

  data_[mm*matrix_properties_.num_cols() + nn] = val;
}

void mtk::DenseMatrix::Transpose() {


  mtk::Real *data_transposed{}; // Buffer.

  int mm = matrix_properties_.num_rows(); // Used to construct this matrix.
  int nn = matrix_properties_.num_cols(); // Used to construct this matrix.

  try {
    data_transposed = new mtk::Real[mm*nn];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(data_transposed,
         mtk::kZero,
         sizeof(data_transposed[0])*mm*nn);

  // Assign the values to their transposed position.
  for (auto ii = 0; ii < mm; ++ii) {
    for (auto jj = 0; jj < nn; ++jj) {
      data_transposed[jj*mm + ii] = data_[ii*nn + jj];
    }
  }

  // Swap pointers.
  auto tmp = data_; // Temporal holder.
  data_ = data_transposed;
  delete [] tmp;
  tmp = nullptr;

  matrix_properties_.set_num_rows(nn);
  matrix_properties_.set_num_cols(mm);
}

void mtk::DenseMatrix::OrderRowMajor() {

  if (matrix_properties_.ordering() == mtk::COL_MAJOR) {


    mtk::Real *data_transposed{}; // Buffer.

    int mm = matrix_properties_.num_rows(); // Used to construct this matrix.
    int nn = matrix_properties_.num_cols(); // Used to construct this matrix.

    try {
      data_transposed = new mtk::Real[mm*nn];
    } catch (std::bad_alloc &memory_allocation_exception) {
      std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
        std::endl;
      std::cerr << memory_allocation_exception.what() << std::endl;
    }
    memset(data_transposed,
           mtk::kZero,
           sizeof(data_transposed[0])*mm*nn);

    // Assign the values to their transposed position.
    std::swap(mm, nn);
    for (auto ii = 0; ii < mm; ++ii) {
      for (auto jj = 0; jj < nn; ++jj) {
        data_transposed[jj*mm + ii] = data_[ii*nn + jj];
      }
    }
    std::swap(mm, nn);

    // Swap pointers.
    auto tmp = data_; // Temporal holder.
    data_ = data_transposed;
    delete [] tmp;
    tmp = nullptr;
```

```

    matrix_properties_.set_ordering(mtk::ROW_MAJOR);
  }
}

void mtk::DenseMatrix::OrderColMajor() {

  if (matrix_properties_.ordering() == ROW_MAJOR) {


    mtk::Real *data_transposed{}; // Buffer.

    int mm = matrix_properties_.num_rows(); // Used to construct this matrix.
    int nn = matrix_properties_.num_cols(); // Used to construct this matrix.

    try {
      data_transposed = new mtk::Real[mm*nn];
    } catch (std::bad_alloc &memory_allocation_exception) {
      std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
        std::endl;
      std::cerr << memory_allocation_exception.what() << std::endl;
    }
    memset(data_transposed,
          mtk::kZero,
          sizeof(data_transposed[0])*mm*nn);

    // Assign the values to their transposed position.
    for (auto ii = 0; ii < mm; ++ii) {
      for (auto jj = 0; jj < nn; ++jj) {
        data_transposed[jj*mm + ii] = data_[ii*nn + jj];
      }
    }

    // Swap pointers.
    auto tmp = data_; // Temporal holder.
    data_ = data_transposed;
    delete [] tmp;
    tmp = nullptr;

    matrix_properties_.set_ordering(mtk::COL_MAJOR);
  }
}

mtk::DenseMatrix mtk::DenseMatrix::Kron(const mtk::DenseMatrix &aa,
                                        const mtk::DenseMatrix &bb) {

  int row_offset{}; // Offset for rows.
  int col_offset{}; // Offset for rows.

  mtk::Real aa_factor{}; // Used in computation.

  // Auxiliary variables:
  auto aux1 = aa.matrix_properties_.num_rows()*bb.matrix_properties_.num_rows();
  auto aux2 = aa.matrix_properties_.num_cols()*bb.matrix_properties_.num_cols();

  mtk::DenseMatrix output(aux1,aux2); // Output matrix.

  int kk_num_cols{output.matrix_properties_.num_cols()}; // Aux.

  auto mm = aa.matrix_properties_.num_rows(); // Rows of aa.
  auto nn = aa.matrix_properties_.num_cols(); // Cols of aa.
  auto pp = bb.matrix_properties_.num_rows(); // Rows of bb.
  auto qq = bb.matrix_properties_.num_cols(); // Cols of bb.

  for (auto ii = 0; ii < mm; ++ii) {
    row_offset = ii*pp;
    for (auto jj = 0; jj < nn; ++jj) {
      col_offset = jj*qq;
      aa_factor = aa.data_[ii*nn + jj];
      for (auto ll = 0; ll < pp; ++ll) {
        for (auto oo = 0; oo < qq; ++oo) {
          auto index = (ll + row_offset)*kk_num_cols + (oo + col_offset);
          output.data_[index] = aa_factor*bb.data_[ll*qq + oo];
        }
      }
    }
  }

```

```
  output.matrix_properties_.set_storage(mtk::DENSE);
  output.matrix_properties_.set_ordering(mtk::ROW_MAJOR);

  return output;
}

bool mtk::DenseMatrix::WriteToFile(const std::string &filename) const {

  std::ofstream output_dat_file;  // Output file.

  output_dat_file.open(filename);

  if (!output_dat_file.is_open()) {
    return false;
  }

  int mm{matrix_properties_.num_rows()};
  int nn{matrix_properties_.num_cols()};

  for (int ii = 0; ii < mm; ++ii) {
    int offset{ii*nn};
    for (int jj = 0; jj < nn; ++jj) {
      output_dat_file << ii << ' ' << jj << ' ' << data_[offset + jj] <<
        std::endl;
    }
  }

  output_dat_file.close();

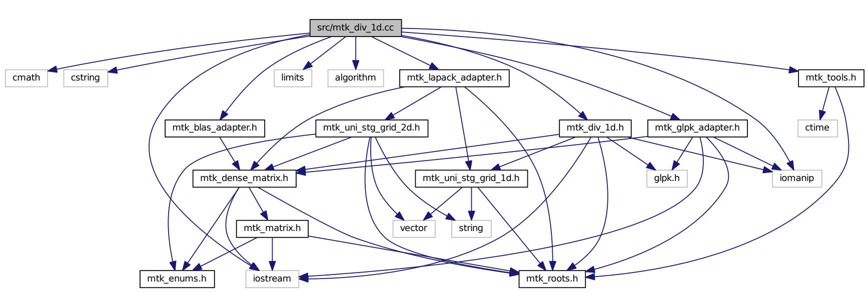
  return true;
}
```

17.59 src/mtk_div_1d.cc File Reference

Implements the class Div1D.

```
#include <cmath>
#include <cstring>
#include <iostream>
#include <iomanip>
#include <limits>
#include <algorithm>
#include "mtk_tools.h"
#include "mtk_blas_adapter.h"
#include "mtk_lapack_adapter.h"
#include "mtk_glpk_adapter.h"
#include "mtk_div_1d.h"
```

Include dependency graph for mtk_div_1d.cc:



Namespaces

- mtk

    Mimetic Methods Toolkit namespace.

Functions

- std::ostream & mtk::operator<< (std::ostream &stream, mtk::Div1D &in)

17.59.1 Detailed Description

This class implements a 1D divergence matrix operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Todo Overload ostream operator as in mtk::Lap1D.

Todo Implement creation of ■ w. mtk::BLASAdapter.

Definition in file mtk_div_1d.cc.

17.60 mtk_div_1d.cc

```

/*
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*/

#include <cmath>
#include <cstring>

#include <iostream>
#include <iomanip>
#include <limits>
#include <algorithm>

#include "mtk_tools.h"

#include "mtk_blas_adapter.h"
#include "mtk_lapack_adapter.h"
#include "mtk_glpk_adapter.h"

#include "mtk_div_1d.h"

namespace mtk {

std::ostream& operator <<(std::ostream &stream, mtk::Div1D &in) {


  stream << "divergence_[0] = " << std::setw(9) << in.divergence_[0] <<
    std::endl;


  stream << "divergence_[1:" << in.order_accuracy_ << "] = ";
  for (auto ii = 1; ii <= in.order_accuracy_; ++ii) {
    stream << std::setw(9) << in.divergence_[ii] << " ";
  }
  stream << std::endl;

  if (in.order_accuracy_ > 2) {


    stream << "divergence_[" << in.order_accuracy_ + 1 << ":" <<
      2*in.order_accuracy_ << "] = ";
    for (auto ii = in.order_accuracy_ + 1; ii <= 2*in.order_accuracy_; ++ii) {
      stream << std::setw(9) << in.divergence_[ii] << " ";
    }
    stream << std::endl;


    auto offset = (2*in.order_accuracy_ + 1);
    int mm{};
    for (auto ii = 0; ii < in.dim_null_; ++ii) {
      stream << "divergence_[" << offset + mm << ":" <<
        offset + mm + in.num_bndy_coeffs_ - 1 << "] = ";
      for (auto jj = 0; jj < in.num_bndy_coeffs_; ++jj) {
        auto value = in.divergence_[offset + mm];
        stream << std::setw(9) << value << " ";
        ++mm;
      }
      stream << std::endl;
    }
  }

  return stream;
}
}

mtk::Div1D::Div1D():
  order_accuracy_(mtk::kDefaultOrderAccuracy),
  dim_null_(),
  num_bndy_coeffs_(),
  divergence_length_(),
  minrow_(),
  row_(),
  coeffs_interior_(),
  prem_apps_(),
  weights_crs_(),
```

```
  weights_cbs_(),
  mim_bndy_(),
  divergence_(),
  mimetic_threshold_(mtk::kDefaultMimeticThreshold) {}

mtk::Div1D::Div1D(const Div1D &div):
  order_accuracy_(div.order_accuracy_),
  dim_null_(div.dim_null_),
  num_bndy_coeffs_(div.num_bndy_coeffs_),
  divergence_length_(div.divergence_length_),
  minrow_(div.minrow_),
  row_(div.row_),
  coeffs_interior_(div.coeffs_interior_),
  prem_apps_(div.prem_apps_),
  weights_crs_(div.weights_crs_),
  weights_cbs_(div.weights_cbs_),
  mim_bndy_(div.mim_bndy_),
  divergence_(div.divergence_),
  mimetic_threshold_(div.mimetic_threshold_) {}

mtk::Div1D::~Div1D() {

  delete[] coeffs_interior_;
  coeffs_interior_ = nullptr;

  delete[] prem_apps_;
  prem_apps_ = nullptr;

  delete[] weights_crs_;
  weights_crs_ = nullptr;

  delete[] weights_cbs_;
  weights_cbs_ = nullptr;

  delete[] mim_bndy_;
  mim_bndy_ = nullptr;

  delete[] divergence_;
  divergence_ = nullptr;
}

bool mtk::Div1D::ConstructDiv1D(int order_accuracy,
                                mtk::Real mimetic_threshold) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(order_accuracy < 2, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent((order_accuracy%2) != 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(mimetic_threshold <= mtk::kZero,
                      __FILE__, __LINE__, __func__);

  if (order_accuracy >= mtk::kCriticalOrderAccuracyDiv) {
    std::cout << "WARNING: Numerical accuracy is critical." << std::endl;
  }

  std::cout << "order_accuracy_ = " << order_accuracy << std::endl;
  std::cout << "mimetic_threshold_ = " << mimetic_threshold << std::endl;
  #endif

  order_accuracy_ = order_accuracy;
  mimetic_threshold_ = mimetic_threshold;


  bool abort_construction = ComputeStencilInteriorGrid();

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!abort_construction) {
    std::cerr << "Could NOT complete stage 1." << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif

  // At this point, we already have the values for the interior stencil stored
  // in the coeffs_interior_ array.

  // It is noteworthy, that the 2nd-order-accurate divergence operator has NO
  // approximation at the boundary, thus it has no weights. For this case, the
  // dimension of the null-space of the Vandermonde matrices used to compute the
  // approximating coefficients at the boundary is 0. Ergo, we compute this
  // number first and then decide if we must compute anything at the boundary.

```

```
dim_null_ = order_accuracy_/2 - 1;

if (dim_null_ > 0) {

  #ifdef MTK_PRECISION_DOUBLE
  num_bndy_coeffs_ = (int) (3.0*((mtk::Real) order_accuracy_)/2.0);
  #else
  num_bndy_coeffs_ = (int) (3.0f*((mtk::Real) order_accuracy_)/2.0f);
  #endif


  // For this we will follow recommendations given in:
  //
  // http://icl.cs.utk.edu/lapack-forum/viewtopic.php?f=5&t=4506
  //
  // We will compute the QR Factorization of the transpose, as in the
  // following (MATLAB) pseudo-code:
  //
  // [Q,R] = qr(V'); % Full QR as defined in
  // % http://www.stanford.edu/class/ee263/notes/qr_matlab.pdf
  //
  // null-space = Q(:, last (order_accuracy_/2 - 1) columns of Q );
  //
  // However, given the nature of the Vandermonde matrices we've just
  // computed, they all posses the same null-space. Therefore, we impose the
  // convention of computing the null-space of the first Vandermonde matrix
  // (west boundary).

  abort_construction = ComputeRationalBasisNullSpace();

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!abort_construction) {
    std::cerr << "Could NOT complete stage 2.1." << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif


  abort_construction = ComputePreliminaryApproximations();

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!abort_construction) {
    std::cerr << "Could NOT complete stage 2.2." << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif


  abort_construction = ComputeWeights();

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!abort_construction) {
    std::cerr << "Could NOT complete stage 2.3." << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif


  abort_construction = ComputeStencilBoundaryGrid();

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!abort_construction) {
    std::cerr << "Could NOT complete stage 2.4." << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif

} // End of: if (dim_null_ > 0);


// Once we have the following three collections of data:
//   (a) the coefficients for the interior,
//   (b) the coefficients for the boundary (if it applies),
//   (c) and the weights (if it applies),
// we will store everything in the output array:

abort_construction = AssembleOperator();
```

```
  #ifdef MTK_PERFORM_PREVENTIONS
  if (!abort_construction) {
    std::cerr << "Could NOT complete stage 3." << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif

  return true;
}

int mtk::Div1D::num_bndy_coeffs() const {

  return num_bndy_coeffs_;
}

mtk::Real *mtk::Div1D::coeffs_interior() const {

  return coeffs_interior_;
}

mtk::Real *mtk::Div1D::weights_crs() const {

  return weights_crs_;
}

mtk::Real *mtk::Div1D::weights_cbs() const {

  return weights_cbs_;
}

mtk::DenseMatrix mtk::Div1D::mim_bndy() const {

  mtk::DenseMatrix xx(dim_null_, 3*order_accuracy_/2);

  auto counter = 0;
  for (auto ii = 0; ii < dim_null_; ++ii) {
    for(auto jj = 0; jj < 3*order_accuracy_/2; ++jj) {
      xx.SetValue(ii,jj, divergence_[2*order_accuracy_ + 1 + counter]);
      counter++;
    }
  }

  return xx;
}

mtk::DenseMatrix mtk::Div1D::ReturnAsDenseMatrix(
  const UniStgGrid1D &grid) const {

  int nn{grid.num_cells_x()}; // Number of cells on the grid.

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(nn <= 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(nn < 3*order_accuracy_ - 1, __FILE__, __LINE__, __func__);
  #endif

  mtk::Real inv_delta_x{mtk::kOne/grid.delta_x()};

  int dd_num_rows = nn + 2;
  int dd_num_cols = nn + 1;
  int elements_per_row = num_bndy_coeffs_;
  int num_extra_rows = dim_null_;

  // Output matrix featuring sizes for divergence operators.
  mtk::DenseMatrix out(dd_num_rows, dd_num_cols);


  auto ee_index = 0;
  for (auto ii = 1; ii < num_extra_rows + 1; ii++) {
    auto cc = 0;
    for(auto jj = 0 ; jj < dd_num_rows; jj++) {
      if( cc >= elements_per_row) {
        out.SetValue(ii, jj, mtk::kZero);
      } else {
        out.SetValue(ii,jj, mim_bndy_[ee_index++]*inv_delta_x);
        cc++;
      }
    }
  }

```

```

  for (auto ii = num_extra_rows + 1;
       ii < dd_num_rows - num_extra_rows - 1; ii++) {
    auto jj = ii - num_extra_rows - 1;
    for (auto cc = 0; cc < order_accuracy_; cc++, jj++) {
      out.SetValue(ii, jj, coeffs_interior_[cc]*inv_delta_x);
    }
  }


  ee_index = 0;
  for (auto ii = dd_num_rows - 2; ii >= dd_num_rows - num_extra_rows - 1; ii--)
{
    auto cc = 0;
    for (auto jj = dd_num_cols - 1; jj >= 0; jj--) {
      if( cc >= elements_per_row) {
        out.SetValue(ii,jj,0.0);
      } else {
        out.SetValue(ii,jj,-mim_bndy_[ee_index++]*inv_delta_x);
        cc++;
      }
     }
  }

  return out;
}

bool mtk::Div1D::ComputeStencilInteriorGrid() {


  mtk::Real* pp{}; // Spatial coordinates to create interior stencil.

  try {
    pp = new mtk::Real[order_accuracy_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(pp, mtk::kZero, sizeof(pp[0])*order_accuracy_);

  #ifdef MTK_PRECISION_DOUBLE
  pp[0] = 1.0/2.0 - ((mtk::Real) order_accuracy_)/2.0;
  #else
  pp[0] = 1.0f/2.0f - ((mtk::Real) order_accuracy_)/2.0f;
  #endif

  for (auto ii = 1; ii < order_accuracy_; ++ii) {
    pp[ii] = pp[ii - 1] + mtk::kOne;
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "pp =" << std::endl;
  for (auto ii = 0; ii < order_accuracy_; ++ii) {
    std::cout << std::setw(12) << pp[ii];
  }
  std::cout << std::endl << std::endl;
  #endif


  bool transpose{false};

  mtk::DenseMatrix vander_matrix(pp,
                                 order_accuracy_,
                                 order_accuracy_,
                                 transpose);

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "vander_matrix = " << std::endl;
  std::cout << vander_matrix << std::endl;
  #endif


  try {
    coeffs_interior_ = new mtk::Real[order_accuracy_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(coeffs_interior_,
```

```
        mtk::kZero,
        sizeof(coeffs_interior_[0])*order_accuracy_);

  coeffs_interior_[1] = mtk::kOne;

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "oo =" << std::endl;
  for (auto ii = 0; ii < order_accuracy_; ++ii) {
    std::cout << std::setw(12) << coeffs_interior_[ii] << std::endl;
  }
  std::cout << std::endl;
  #endif


  int info{mtk::LAPACKAdapter::SolveDenseSystem(vander_matrix,
                                                coeffs_interior_)};

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!info) {
    std::cout << "System solved! Interior stencil attained!" << std::endl;
    std::cout << std::endl;
  }
  else {
    std::cerr << "Something wrong solving system! info = " << info << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "coeffs_interior_ =" << std::endl;
  for (auto ii = 0; ii < order_accuracy_; ++ii) {
    std::cout << std::setw(12) << coeffs_interior_[ii];
  }
  std::cout << std::endl << std::endl;
  #endif

  delete [] pp;
  pp = nullptr;

  return true;
}

bool mtk::Div1D::ComputeRationalBasisNullSpace(void) {

  mtk::Real* gg{}; // Generator vector for the first Vandermonde matrix.


  try {
    gg = new mtk::Real[num_bndy_coeffs_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(gg, mtk::kZero, sizeof(gg[0])*num_bndy_coeffs_);

  #ifdef MTK_PRECISION_DOUBLE
  gg[0] = -1.0/2.0;
  #else
  gg[0] = -1.0f/2.0f;
  #endif
  for (auto ii = 1; ii < num_bndy_coeffs_; ++ii) {
    gg[ii] = gg[ii - 1] + mtk::kOne;
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "gg =" << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    std::cout << std::setw(12) << gg[ii];
  }
  std::cout << std::endl << std::endl;
  #endif


  bool tran{true}; // Should I transpose the Vandermonde matrix.

  mtk::DenseMatrix vv_west_t(gg, num_bndy_coeffs_, order_accuracy_ + 1, tran);

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "vv_west_t =" << std::endl;
```

```
  std::cout << vv_west_t << std::endl;
  #endif


  mtk::DenseMatrix qq_t(mtk::LAPACKAdapter::QRFactorDenseMatrix
(vv_west_t));

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "QQ^T = " << std::endl;
  std::cout << qq_t << std::endl;
  #endif


  int KK_num_rows_{num_bndy_coeffs_};
  int KK_num_cols_{dim_null_};

  mtk::DenseMatrix KK(KK_num_rows_, KK_num_cols_);

  for (auto ii = num_bndy_coeffs_ - dim_null_; ii < num_bndy_coeffs_; ++ii) {
    for (auto jj = 0; jj < num_bndy_coeffs_; ++jj) {
      KK.data()[jj*dim_null_ + (ii - (num_bndy_coeffs_ - dim_null_))] =
          qq_t.data()[ii*num_bndy_coeffs_ + jj];
    }
  }

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "KK =" << std::endl;
  std::cout << KK << std::endl;
  std::cout << "KK.num_rows() = " << KK.num_rows() << std::endl;
  std::cout << "KK.num_cols() = " << KK.num_cols() << std::endl;
  std::cout << std::endl;
  #endif


  // Scale thus requesting that the last entries of the attained basis for the
  // null-space, adopt the pattern we require.
  // Essentially we will implement the following MATLAB pseudo-code:
  //  scalers = KK(num_bndy_approxs - (dim_null - 1):num_bndy_approxs,:)\B
  //  SK = KK*scalers
  // where SK is the scaled null-space.

  // In this point, we almost have all the data we need correctly allocated
  // in memory. We will create the matrix II_, and elements we wish to scale in
  // the KK array. Using the concept of the leading dimension, we could just
  // use KK, with the correct leading dimension and that is it. BUT I DO NOT
  // GET how does it work. So I will just create a matrix with the content of
  // this array that we need, solve for the scalers and then scale the
  // whole KK:

  // We will then create memory for that sub-matrix of KK (SUBK).

  mtk::DenseMatrix SUBK(dim_null_,dim_null_);

  for (auto ii = num_bndy_coeffs_ - dim_null_; ii < num_bndy_coeffs_; ++ii) {
    for (auto jj = 0; jj < dim_null_; ++jj) {
      SUBK.data()[(ii - (num_bndy_coeffs_ - dim_null_))*dim_null_ + jj] =
          KK.data()[ii*dim_null_ + jj];
    }
  }

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "SUBK =" << std::endl;
  std::cout << SUBK << std::endl;
  #endif

  SUBK.Transpose();

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "SUBK^T =" << std::endl;
  std::cout << SUBK << std::endl;
  #endif

  bool padded{false};
  tran = false;

  mtk::DenseMatrix II(dim_null_, padded, tran);

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "II =" << std::endl;
  std::cout << II << std::endl;
  #endif
```

```
  // Solve the system to compute the scalers.
  // An example of the system to solve, for k = 8, is:
  //
  // SUBK*scalers = II_ or
  //
  // |  0.386018  -0.0339244   -0.129478 |            | 1 0 0 |
  // | -0.119774   0.0199423   0.0558632 |*scalers = | 0 1 0 |
  // | 0.0155708 -0.00349546 -0.00853182 |            | 0 0 1 |
  //
  // Notice this is a nrhs = 3 system.
  // Noteworthy: we do NOT ACTUALLY ALLOCATE space for the scalers... they
  // will be stored in the created identity matrix.
  // Let us first transpose SUBK (because of LAPACK):

  int info{mtk::LAPACKAdapter::SolveDenseSystem(SUBK, II)};

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!info) {
    std::cout << "System successfully solved!" <<
      std::endl;
  } else {
    std::cerr << "Something went wrong solving system! info = " << info <<
      std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  std::cout << std::endl;
  #endif

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "Computed scalers:" << std::endl;
  std::cout << II << std::endl;
  #endif

  // Multiply the two matrices to attain a scaled basis for null-space.

  rat_basis_null_space_ = mtk::BLASAdapter::RealDenseMM(KK, II);

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "Rational basis for the null-space:" << std::endl;
  std::cout << rat_basis_null_space_ << std::endl;
  #endif

  // At this point, we have a rational basis for the null-space, with the
  // pattern we need! :)

  delete [] gg;
  gg = nullptr;

  return true;
}

bool mtk::Div1D::ComputePreliminaryApproximations(void) {


  mtk::Real *gg{}; // Generator vector for the first approximation.

  try {
    gg = new mtk::Real[num_bndy_coeffs_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(gg, mtk::kZero, sizeof(gg[0])*num_bndy_coeffs_);

  #ifdef MTK_PRECISION_DOUBLE
  gg[0] = -1.0/2.0;
  #else
  gg[0] = -1.0f/2.0f;
  #endif
  for (auto ii = 1; ii < num_bndy_coeffs_; ++ii) {
    gg[ii] = gg[ii - 1] + mtk::kOne;
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "gg0 =" << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    std::cout << std::setw(12) << gg[ii];
  }
```

```
  std::cout << std::endl << std::endl;
  #endif

  // Allocate 2D array to store the collection of preliminary approximations.
  try {
    prem_apps_ = new mtk::Real[num_bndy_coeffs_*dim_null_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(prem_apps_,
         mtk::kZero,
         sizeof(prem_apps_[0])*num_bndy_coeffs_*dim_null_);


  for (auto ll = 0; ll < dim_null_; ++ll) {

    // Re-check new generator vector for every iteration except for the first.
    #if MTK_VERBOSE_LEVEL > 3
    if (ll > 0) {
      std::cout << "gg" << ll << " =" << std::endl;
      for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
        std::cout << std::setw(12) << gg[ii];
      }
      std::cout << std::endl << std::endl;
    }
    #endif


    bool transpose{false};

    mtk::DenseMatrix AA_(gg,
                         num_bndy_coeffs_, order_accuracy_ + 1,
                         transpose);

    #if MTK_VERBOSE_LEVEL > 4
    std::cout << "AA_" << ll << " =" << std::endl;
    std::cout << AA_ << std::endl;
    #endif


    mtk::Real *ob{};

    auto ob_ld = num_bndy_coeffs_;

    try {
      ob = new mtk::Real[ob_ld];
    } catch (std::bad_alloc &memory_allocation_exception) {
      std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
        std::endl;
      std::cerr << memory_allocation_exception.what() << std::endl;
    }
    memset(ob, mtk::kZero, sizeof(ob[0])*ob_ld);

    ob[1] = mtk::kOne;

    #if MTK_VERBOSE_LEVEL > 4
    std::cout << "ob = " << std::endl << std::endl;
    for (auto ii = 0; ii < ob_ld; ++ii) {
      std::cout << std::setw(12) << ob[ii] << std::endl;
    }
    std::cout << std::endl;
    #endif


    // However, this is an under-determined system of equations. So we can not
    // use the same LAPACK routine (dgesv_). We will instead use dgels_, through
    // our LAPACKAdapter class.

    int info_{
      mtk::LAPACKAdapter::SolveRectangularDenseSystem(AA_,
ob, ob_ld)};

    #ifdef MTK_PERFORM_PREVENTIONS
    if (!info_) {
      std::cout << "System successfully solved!" << std::endl << std::endl;
    } else {
      std::cerr << "Error solving system! info = " << info_ << std::endl;
    }
    #endif
```

```
#if MTK_VERBOSE_LEVEL > 3
std::cout << "ob =" << std::endl;
for (auto ii = 0; ii < ob_ld; ++ii) {
  std::cout << std::setw(12) << ob[ii] << std::endl;
}
std::cout << std::endl;
#endif


// This implies a DAXPY operation. However, we must construct the arguments
// for this operation.

// Save them into the ob_bottom array:

Real *ob_bottom{}; // Bottom part of the attained kernel used to scale it.

try {
  ob_bottom = new mtk::Real[dim_null_];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(ob_bottom, mtk::kZero, sizeof(ob_bottom[0])*dim_null_);

for (auto ii = 0; ii < dim_null_; ++ii) {
  ob_bottom[(dim_null_ - 1) - ii] = ob[num_bndy_coeffs_ - ii - 1];
}

#if MTK_VERBOSE_LEVEL > 3
std::cout << "ob_bottom =" << std::endl;
for (auto ii = 0; ii < dim_null_; ++ii) {
  std::cout << std::setw(12) << ob_bottom[ii] << std::endl;
}
std::cout << std::endl;
#endif


// We must computed an scaled ob, sob, using the scaled null-space in
// rat_basis_null_space_.
// Such operation is: sob = ob - rat_basis_null_space_*ob_bottom
// or:                 ob = -1.0*rat_basis_null_space_*ob_bottom + 1.0*ob
// thus:                Y =    a*A    *x         +   b*Y (DAXPY).

#if MTK_VERBOSE_LEVEL > 3
std::cout << "Rational basis for the null-space:" << std::endl;
std::cout << rat_basis_null_space_ << std::endl;
#endif

mtk::Real alpha{-mtk::kOne};
mtk::Real beta{mtk::kOne};

mtk::BLASAdapter::RealDenseMV(alpha, rat_basis_null_space_,
                              ob_bottom, beta, ob);

#if MTK_VERBOSE_LEVEL > 3
std::cout << "scaled ob:" << std::endl;
for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
  std::cout << std::setw(12) << ob[ii] << std::endl;
}
std::cout << std::endl;
#endif

// We save the recently scaled solution, into an array containing these.
// We can NOT start building the pi matrix, simply because I want that part
// to be separated since its construction depends on the algorithm we want
// to implement.

for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
  prem_apps_[ii*dim_null_ + ll] = ob[ii];
}

// After the first iteration, simply shift the entries of the last
// generator vector used:
for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
  gg[ii]--;
}

// Garbage collection for this loop:
delete[] ob;
```

```
    ob = nullptr;

    delete[] ob_bottom;
    ob_bottom = nullptr;
  } // End of: for (ll = 0; ll < dim_null; ll++);

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "Matrix post-scaled preliminary apps: " << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    for (auto jj = 0; jj < dim_null_; ++jj) {
      std::cout << std::setw(12) << prem_apps_[ii*dim_null_ + jj];
    }
    std::cout << std::endl;
  }
  std::cout << std::endl;
  #endif

  delete[] gg;
  gg = nullptr;

  return true;
}

bool mtk::Div1D::ComputeWeights(void) {

  // Matrix to copmpute the weights as in the CRSA.
  mtk::DenseMatrix pi(num_bndy_coeffs_, num_bndy_coeffs_ - 1);


  // Assemble the pi matrix using:
  // 1. The collection of scaled preliminary approximations.
  // 2. The collection of coefficients approximating at the interior.
  // 3. The scaled basis for the null-space.

  // 1.1. Process array of scaled preliminary approximations.

  // These are queued in scaled_solutions. Each one of these, will be a column
  // of the pi matrix:
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    for (auto jj = 0; jj < dim_null_; ++jj) {
      pi.data()[ii*(2*dim_null_ + (order_accuracy_/2 + 1)) + jj] =
        prem_apps_[ii*dim_null_ + jj];
    }
  }

  // 1.2. Add columns from known stencil approximating at the interior.

  // However, these must be padded by zeros, according to their position in the
  // final pi matrix:
  auto mm = 0;
  for (auto jj = dim_null_; jj < order_accuracy_; ++jj) {
    for (auto ii = 0; ii < order_accuracy_; ++ii) {
      pi.data()[(ii + mm)*(2*dim_null_ + (order_accuracy_/2 + 1)) + jj] =
        coeffs_interior_[ii];
    }
    ++mm;
  }

  rat_basis_null_space_.OrderColMajor();

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "Rational basis for the null-space (col. major):" << std::endl;
  std::cout << rat_basis_null_space_ << std::endl;
  #endif

  // 1.3. Add final set of columns: rational basis for null-space.
  for (auto jj = dim_null_ + (order_accuracy_/2 + 1);
       jj < num_bndy_coeffs_ - 1;
       ++jj) {
    for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
      auto og =
        (jj - (dim_null_ + (order_accuracy_/2 + 1)))*num_bndy_coeffs_ + ii;
      auto de = ii*(2*dim_null_ + (order_accuracy_/2 + 1)) + jj;
      pi.data()[de] = rat_basis_null_space_.data()[og];
    }
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "coeffs_interior_ =" << std::endl;
  for (auto ii = 0; ii < order_accuracy_; ++ii) {
    std::cout << std::setw(12) << coeffs_interior_[ii];
```

```
  }
  std::cout << std::endl << std::endl;
  #endif

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "Constructed pi matrix for CRS Algorithm: " << std::endl;
  std::cout << pi << std::endl;
  #endif


  // This imposes the mimetic condition.

  mtk::Real *hh{};  // Right-hand side to compute weights in the C{R,B}SA.

  try {
    hh = new mtk::Real[num_bndy_coeffs_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(hh, mtk::kZero, sizeof(hh[0])*num_bndy_coeffs_);

  hh[0] = -mtk::kOne;
  for (auto ii = (order_accuracy_/2 + 2 - 1); ii < num_bndy_coeffs_; ++ii) {
    auto aux_xx = mtk::kZero;
    for (auto jj = 0; jj < ((ii - (order_accuracy_/2 - 1)) - 1); ++jj) {
      aux_xx += coeffs_interior_[jj];
    }
    hh[ii] = -mtk::kOne*aux_xx;
  }


  // That is, we construct a system, to solve for the weights.

  // Once again we face the challenge of solving with LAPACK. However, for the
  // CRSA, this matrix PI is over-determined, since it has more rows than
  // unknowns. However, according to the theory, the solution to this system is
  // unique. We will use dgels_.

  try {
    weights_cbs_ = new mtk::Real[num_bndy_coeffs_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(weights_cbs_, mtk::kZero, sizeof(weights_cbs_[0])*num_bndy_coeffs_);

  int weights_ld{pi.num_cols() + 1};

  // Preserve hh.
  std::copy(hh, hh + weights_ld, weights_cbs_);

  pi.Transpose();

  int info{mtk::LAPACKAdapter::SolveRectangularDenseSystem(
pi,
                                                            weights_cbs_,
                                                            weights_ld)};

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!info) {
    std::cout << "System successfully solved!" << std::endl << std::endl;
  } else {
    std::cerr << "Error solving system! info = " << info << std::endl;
  }
  #endif

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "hh =" << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    std::cout << std::setw(11) << hh[ii] << std::endl;
  }
  std::cout << std::endl;
  #endif

  // Preserve the original weights for research.

  try {
    weights_crs_ = new mtk::Real[num_bndy_coeffs_];
```

```
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(weights_crs_, mtk::kZero, sizeof(weights_crs_[0])*num_bndy_coeffs_);

  std::copy(weights_cbs_, weights_cbs_ + (weights_ld - 1), weights_crs_);

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "weights_CRSA + lambda =" << std::endl;
  for (auto ii = 0; ii < weights_ld - 1; ++ii) {
    std::cout << std::setw(12) << weights_crs_[ii] << std::endl;
  }
  std::cout << std::endl;
  #endif


  if (order_accuracy_ >= mtk::kCriticalOrderAccuracyDiv) {

    int minrow_{std::numeric_limits<int>::infinity()};

    mtk::Real norm_{mtk::BLASAdapter::RealNRM2(weights_cbs_,
order_accuracy_)};
    mtk::Real minnorm_{std::numeric_limits<mtk::Real>::infinity()};


    mtk::DenseMatrix phi(order_accuracy_ + 1, order_accuracy_);

    for (auto ii = 0; ii < order_accuracy_ + 1; ++ii) {
      for (auto jj = 0; jj < dim_null_; ++jj) {
        phi.data()[ii*(order_accuracy_) + jj] = prem_apps_[ii*dim_null_ + jj];
      }
    }

    int aux{};  // Auxiliary variable.
    for (auto jj = dim_null_; jj < dim_null_ + 2; ++jj) {
      for (auto ii = 0; ii < order_accuracy_; ++ii) {
        phi.data()[(ii + aux)*order_accuracy_ + jj] = coeffs_interior_[ii];
      }
      ++aux;
    }

    for(auto jj=order_accuracy_ - 1; jj >=order_accuracy_ - dim_null_; jj--) {
      for(auto ii=0; ii<order_accuracy_ + 1; ++ii) {
        phi.data()[ii*order_accuracy_+jj] = mtk::kZero;
      }
    }

    for (auto jj = 0; jj < order_accuracy_ + 1; ++jj) {
      for (auto ii = 0; ii < dim_null_; ++ii) {
        phi.data()[(ii + order_accuracy_ - dim_null_ + jj*order_accuracy_)] =
          -prem_apps_[(dim_null_ - ii - 1 + jj*dim_null_)];
      }
    }

    for(auto ii = 0; ii < order_accuracy_/2; ++ii) {
      for (auto jj = dim_null_ + 2; jj < order_accuracy_; ++jj) {
        auto swap = phi.data()[ii*order_accuracy_+jj];
        phi.data()[ii*order_accuracy_ + jj] =
          phi.data()[(order_accuracy_-ii)*order_accuracy_+jj];
        phi.data()[(order_accuracy_-ii)*order_accuracy_+jj] = swap;
      }
    }

    #if MTK_VERBOSE_LEVEL > 4
    std::cout << "Constructed PHI matrix for CBS Algorithm: " << std::endl;
    std::cout << phi << std::endl;
    #endif


    mtk::Real *lamed{};  // Used to build big lambda.

    try {
      lamed = new mtk::Real[dim_null_];
    } catch (std::bad_alloc &memory_allocation_exception) {
      std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
        std::endl;
      std::cerr << memory_allocation_exception.what() << std::endl;
    }
    memset(lamed, mtk::kZero, sizeof(lamed[0])*dim_null_);
```

```
    for (auto ii = 0; ii < dim_null_; ++ii) {
      lamed[ii] = hh[ii + order_accuracy_ + 1] ;
    }

    #if MTK_VERBOSE_LEVEL > 3
    std::cout << "lamed =" << std::endl;
    for (auto ii = 0; ii < dim_null_; ++ii) {
      std::cout << std::setw(12) << lamed[ii] << std::endl;
    }
    std::cout << std::endl;
    #endif

    for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
      mtk::Real temp = mtk::kZero;
      for(auto jj = 0; jj < dim_null_; ++jj) {
        temp = temp +
          lamed[jj]*rat_basis_null_space_.data()[jj*num_bndy_coeffs_ + ii];
      }
      hh[ii] = hh[ii] - temp;
    }

    #if MTK_VERBOSE_LEVEL > 3
    std::cout << "big_lambda =" << std::endl;
    for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
      std::cout << std::setw(12) << hh[ii] << std::endl;
    }
    std::cout << std::endl;
    #endif

    int copy_result{};

    mtk::Real normerr_; // Norm of the error for the solution on each row.


    for(auto row_= 0; row_ < order_accuracy_ + 1; ++row_) {
      normerr_ = mtk::GLPKAdapter::SolveSimplexAndCompare(phi.data(),
                                                          order_accuracy_ + 1,
                                                          order_accuracy_,
                                                          order_accuracy_,
                                                          hh,
                                                          weights_cbs_,
                                                          row_,
                                                          mimetic_threshold_,
                                                          copy_result);
      mtk::Real aux{normerr_/norm_};

      #if MTK_VERBOSE_LEVEL > 2
      std::cout << "Relative norm: " << aux << " " << std::endl;
      std::cout << std::endl;
      #endif

      if (aux < minnorm_) {
        minnorm_ = aux;
        minrow_= row_;
      }
    }

    #if MTK_VERBOSE_LEVEL > 3
    std::cout << "weights_CBSA + lambda (after brute force search):" <<
      std::endl;
    for (auto ii = 0; ii < num_bndy_coeffs_ - 1; ++ii) {
      std::cout << std::setw(12) << weights_cbs_[ii] << std::endl;
    }
    std::cout << std::endl;
    #endif


    // After we know which row yields the smallest relative norm that row is
    // chosen to be the objective function and the result of the optimizer is
    // chosen to be the new weights_.

    #if MTK_VERBOSE_LEVEL > 2
    std::cout << "Minimum Relative Norm " << minnorm_ << " found at row " <<
      minrow_ + 1 << std::endl;
    std::cout << std::endl;
    #endif

    copy_result = 1;
    normerr_ = mtk::GLPKAdapter::SolveSimplexAndCompare(phi.
```

```
data(),
                                                        order_accuracy_ + 1,
                                                        order_accuracy_,
                                                        order_accuracy_,
                                                        hh,
                                                        weights_cbs_,
                                                        minrow_,
                                                        mimetic_threshold_,
                                                        copy_result);
    mtk::Real aux_{normerr_/norm_};
    #if MTK_VERBOSE_LEVEL > 2
    std::cout << "Relative norm: " << aux_ << std::endl;
    std::cout << std::endl;
    #endif

    delete [] lamed;
    lamed = nullptr;
  }

  delete [] hh;
  hh = nullptr;

  return true;
}

bool mtk::Div1D::ComputeStencilBoundaryGrid(void) {

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "weights_CBSA + lambda =" << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_ - 1; ++ii) {
    std::cout << std::setw(12) << weights_cbs_[ii] << std::endl;
  }
  std::cout << std::endl;
  #endif


  mtk::Real *lambda{}; // Collection of bottom values from weights_.

  try {
    lambda = new mtk::Real[dim_null_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(lambda, mtk::kZero, sizeof(lambda[0])*dim_null_);

  for (auto ii = 0; ii < dim_null_; ++ii) {
    lambda[ii] = weights_cbs_[order_accuracy_ + ii];
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "lambda =" << std::endl;
  for (auto ii = 0; ii < dim_null_; ++ii) {
    std::cout << std::setw(12) << lambda[ii] << std::endl;
  }
  std::cout << std::endl;
  #endif


  mtk::Real *alpha{}; // Collection of alpha values.

  try {
    alpha = new mtk::Real[dim_null_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(alpha, mtk::kZero, sizeof(alpha[0])*dim_null_);

  for (auto ii = 0; ii < dim_null_; ++ii) {
    alpha[ii] = lambda[ii]/weights_cbs_[ii] ;
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "alpha =" << std::endl;
  for (auto ii = 0; ii < dim_null_; ++ii) {
    std::cout << std::setw(12) << alpha[ii] << std::endl;
  }
  std::cout << std::endl;
```

```
  #endif


  try {
    mim_bndy_ = new mtk::Real[num_bndy_coeffs_*dim_null_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(mim_bndy_,
         mtk::kZero,
         sizeof(mim_bndy_[0])*num_bndy_coeffs_*dim_null_);

  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    for (auto jj = 0; jj < dim_null_; ++jj) {
      mim_bndy_[ii*dim_null_ + jj] =
        prem_apps_[ii*dim_null_ + jj] +
        alpha[jj]*rat_basis_null_space_.data()[jj*num_bndy_coeffs_ + ii];
    }
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "Collection of mimetic approximations:" << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    for (auto jj = 0; jj < dim_null_; ++jj) {
      std::cout << std::setw(13) << mim_bndy_[ii*dim_null_ + jj];
    }
    std::cout << std::endl;
  }
  std::cout << std::endl;
  #endif

  delete[] lambda;
  lambda = nullptr;

  delete[] alpha;
  alpha = nullptr;

  return true;
}

bool mtk::Div1D::AssembleOperator(void) {

  // The output array will have this form:
  // 1. The first entry of the array will contain used order order_accuracy_.
  // 2. The second entry of the array will contain the collection of
  // approximating coefficients for the interior of the grid.
  // 3. IF order_accuracy_ > 2, then the third entry will contain a collection
  // of weights.
  // 4. IF order_accuracy_ > 2, the next dim_null_ entries will contain the
  // collections of approximating coefficients for the west boundary of the
  // grid.

  if (order_accuracy_ > mtk::kDefaultOrderAccuracy) {
    divergence_length_ =
      1 + order_accuracy_ + order_accuracy_ + dim_null_*num_bndy_coeffs_;
  } else {
    divergence_length_ = 1 + order_accuracy_;
  }

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "divergence_length_ = " << divergence_length_ << std::endl;
  #endif

  try {
    divergence_ = new double[divergence_length_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(divergence_, mtk::kZero, sizeof(divergence_[0])*divergence_length_);


  divergence_[0] = order_accuracy_;


  for (auto ii = 0; ii < order_accuracy_; ++ii) {
  divergence_[ii + 1] = coeffs_interior_[ii];
  }
```

```
  if (order_accuracy_ > 2) {
    for (auto ii = 0; ii < order_accuracy_; ++ii) {
      divergence_[(1 + order_accuracy_) + ii] = weights_cbs_[ii];
    }
  }


  if (order_accuracy_ > 2) {
    auto offset = (2*order_accuracy_ + 1);
    int mm{};
    for (auto ii = 0; ii < dim_null_; ++ii) {
      for (auto jj = 0; jj < num_bndy_coeffs_; ++jj) {
        divergence_[offset + (mm)] = mim_bndy_[jj*dim_null_ + ii];
        ++mm;
      }
    }
  }

  #if MTK_VERBOSE_LEVEL > 1
  std::cout << "1D " << order_accuracy_ << "-order div built!" << std::endl;
  std::cout << std::endl;
  #endif

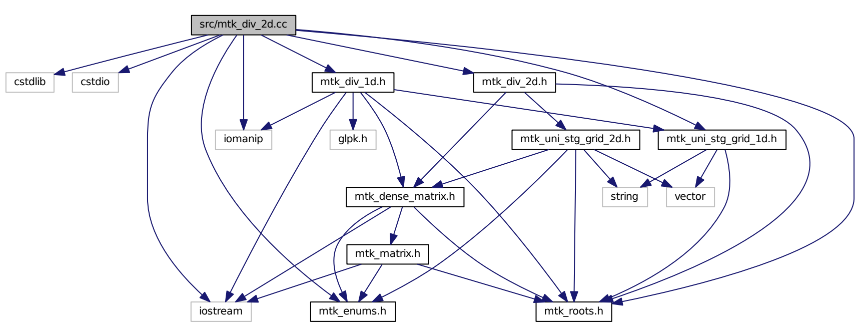
  return true;
}
```

17.61 src/mtk_div_2d.cc File Reference

Implements the class Div2D.

```
#include <cstdlib>
#include <cstdio>
#include <iostream>
#include <iomanip>
#include "mtk_roots.h"
#include "mtk_enums.h"
#include "mtk_uni_stg_grid_1d.h"
#include "mtk_div_1d.h"
#include "mtk_div_2d.h"
```

Include dependency graph for mtk_div_2d.cc:



17.61.1 Detailed Description

This class implements a 2D divergence matrix operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_div_2d.cc.

17.62 mtk_div_2d.cc

```

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*/

#include <cstdlib>
#include <cstdio>

#include <iostream>
#include <iomanip>

#include "mtk_roots.h"
#include "mtk_enums.h"
#include "mtk_uni_stg_grid_1d.h"
#include "mtk_div_1d.h"
#include "mtk_div_2d.h"

mtk::Div2D::Div2D():
  order_accuracy_(),
  mimetic_threshold_() {}

mtk::Div2D::Div2D(const Div2D &div):
  order_accuracy_(div.order_accuracy_),
  mimetic_threshold_(div.mimetic_threshold_) {}

mtk::Div2D::~Div2D() {}
```

```
bool mtk::Div2D::ConstructDiv2D(const
mtk::UniStgGrid2D &grid,
                                int order_accuracy,
                                mtk::Real mimetic_threshold) {

  int num_cells_x = grid.num_cells_x();
  int num_cells_y = grid.num_cells_y();

  int mx = num_cells_x + 2;  // Dx vertical dimension.
  int nx = num_cells_x + 1;  // Dx horizontal dimension.
  int my = num_cells_y + 2;  // Dy vertical dimension.
  int ny = num_cells_y + 1;  // Dy horizontal dimension.

  mtk::Div1D div;

  bool info = div.ConstructDiv1D(order_accuracy, mimetic_threshold);

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!info) {
    std::cerr << "Mimetic div could not be built." << std::endl;
    return info;
  }
  #endif

  auto west = grid.west_bndy();
  auto east = grid.east_bndy();
  auto south = grid.south_bndy();
  auto north = grid.east_bndy();

  mtk::UniStgGrid1D grid_x(west, east, num_cells_x);
  mtk::UniStgGrid1D grid_y(south, north, num_cells_y);

  mtk::DenseMatrix dx(div.ReturnAsDenseMatrix(grid_x));
  mtk::DenseMatrix dy(div.ReturnAsDenseMatrix(grid_y));

  bool padded{true};
  bool transpose{false};

  mtk::DenseMatrix ix(num_cells_x, padded, transpose);
  mtk::DenseMatrix iy(num_cells_y, padded, transpose);

  mtk::DenseMatrix dxy(mtk::DenseMatrix::Kron(iy, dx));
  mtk::DenseMatrix dyx(mtk::DenseMatrix::Kron(dy, ix));

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "Dx: " << mx << " by " << nx << std::endl;
  std::cout << "Iy : " << num_cells_y<< " by " << ny  << std::endl;
  std::cout << "Dy: " << my << " by " << ny << std::endl;
  std::cout << "Ix : " << num_cells_x<< " by " << nx  << std::endl;
  std::cout << "Div 2D: " << mx*num_cells_y + my*num_cells_x << " by " <<
    nx*ny <<std::endl;
  #endif

  mtk::DenseMatrix d2d(mx*my, nx*num_cells_y + ny*num_cells_x);

  for (auto ii = 0; ii < mx*my; ii++) {
    for (auto jj = 0; jj < nx*num_cells_y; jj++) {
      d2d.SetValue(ii, jj, dxy.GetValue(ii,jj));
    }
    for(auto kk=0; kk<ny*num_cells_x; kk++) {
      d2d.SetValue(ii, kk + nx*num_cells_y, dyx.GetValue(ii, kk));
    }
  }

  divergence_ = d2d;

  return info;
}

mtk::DenseMatrix mtk::Div2D::ReturnAsDenseMatrix() const {

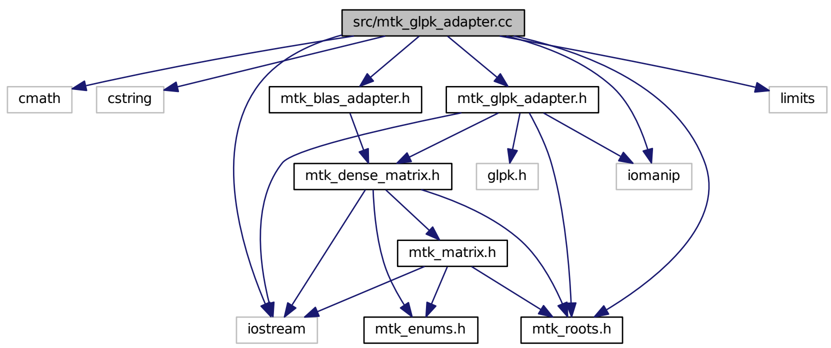
  return divergence_;
}
```

17.63 src/mtk_glpk_adapter.cc File Reference

Adapter class for the GLPK API.

```
#include <cmath>
#include <cstring>
#include <iostream>
#include <iomanip>
#include <limits>
#include "mtk_roots.h"
#include "mtk_blas_adapter.h"
#include "mtk_glpk_adapter.h"
```

Include dependency graph for mtk_glpk_adapter.cc:



17.63.1 Detailed Description

This class contains a collection of static classes, that posses direct access to the underlying structure of the matrices, thus allowing programmers to exploit some of the numerical methods implemented in the GLPK.

The **GLPK (GNU Linear Programming Kit)** package is intended for solving large-scale linear programming (LP), mixed integer programming (MIP), and other related problems. It is a set of routines written in ANSI C and organized in the form of a callable library.

See also

http://www.gnu.org/software/glpk/

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_glpk_adapter.cc.

17.64 mtk_glpk_adapter.cc

```

/*
```

```
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*/

#include <cmath>
#include <cstring>

#include <iostream>
#include <iomanip>
#include <limits>

#include "mtk_roots.h"
#include "mtk_blas_adapter.h"
#include "mtk_glpk_adapter.h"

mtk::Real mtk::GLPKAdapter::SolveSimplexAndCompare(mtk::Real *A,
                                                   int nrows,
                                                   int ncols,
                                                   int kk,
                                                   mtk::Real *hh,
                                                   mtk::Real *qq,
                                                   int robjective,
                                                   mtk::Real mimetic_threshold,
                                                   int copy) {

  #if MTK_DEBUG_LEVEL > 0
  char mps_file_name[18]; // File name for the MPS files.
  #endif
  char rname[5];          // Row name.
  char cname[5];          // Column name.

  glp_prob *lp; // Linear programming problem.

  int *ia;  // Array for the problem.
  int *ja;  // Array for the problem.

  int problem_size; // Size of the problem.
  int lp_nrows;     // Number of rows.
  int lp_ncols;     // Number of columns.
```

```
int matsize;      // Size of the matrix.
int glp_index{1}; // Index of the objective function.
int ii;           // Iterator.
int jj;           // Iterator.

mtk::Real *ar;             // Array for the problem.
mtk::Real *objective;      // Array containing the objective function.
mtk::Real *rhs;            // Array containing the rhs.
mtk::Real *err;            // Array of errors.

mtk::Real x1;              // Norm-2 of the error.

#if MTK_DEBUG_LEVEL > 0
mtk::Real obj_value;       // Value of the objective function.
#endif

lp_nrows = kk;
lp_ncols = kk;

matsize = lp_nrows*lp_ncols;


problem_size = lp_nrows*lp_ncols + 1;

try {
  ia = new int[problem_size];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(ia, 0, sizeof(ia[0])*problem_size);

try {
  ja = new int[problem_size];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(ja, 0, sizeof(ja[0])*problem_size);

try {
  ar = new mtk::Real[problem_size];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(ar, mtk::kZero, sizeof(ar[0])*problem_size);

try {
  objective = new mtk::Real[lp_ncols + 1];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(objective, mtk::kZero, sizeof(objective[0])*(lp_ncols + 1));

try {
  rhs = new mtk::Real[lp_nrows + 1];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(rhs, mtk::kZero, sizeof(rhs[0])*(lp_nrows + 1));

try {
  err = new mtk::Real[lp_nrows];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(err, mtk::kZero, sizeof(err[0])*(lp_nrows));

#if MTK_DEBUG_LEVEL > 0
std::cout << "Problem size: " << problem_size << std::endl;
std::cout << "lp_nrows = " << lp_nrows << std::endl;
```

```
std::cout << "lp_ncols = " << lp_ncols << std::endl;
std::cout << std::endl;
#endif

lp = glp_create_prob();

glp_set_prob_name (lp, "mtk::GLPKAdapter::Simplex");

glp_set_obj_dir (lp, GLP_MIN);


glp_add_rows(lp, lp_nrows);

for (ii = 1; ii <= lp_nrows; ++ii) {
  sprintf(rname, "R%02d",ii);
  glp_set_row_name(lp, ii, rname);
}

glp_add_cols(lp, lp_ncols);

for (ii = 1; ii <= lp_ncols; ++ii) {
  sprintf(cname, "Q%02d",ii);
  glp_set_col_name (lp, ii, cname);
}


#if MTK_DEBUG_LEVEL>0
std::cout << "Using row " << robjective + 1 << " as objective." << std::endl;
#endif
for (jj = 0; jj < kk; ++jj) {
  objective[glp_index] = A[jj + robjective * ncols];
  glp_index++;
}
#if MTK_DEBUG_LEVEL >0
std::cout << std::endl;
#endif


glp_index = 1;
rhs[0] = mtk::kZero;
for (ii = 0; ii <= lp_nrows; ++ii) {
  if (ii != robjective) {
    rhs[glp_index] = hh[ii];
    glp_set_row_bnds(lp, glp_index, GLP_UP, 0.0, rhs[glp_index]);
    glp_index++;
  }
}

#if MTK_DEBUG_LEVEL > 0
std::cout << "rhs =" << std::endl;
for (auto ii = 0; ii < lp_nrows; ++ii) {
  std::cout << std::setw(15) << rhs[ii] << std::endl;
}
std::cout << std::endl;
#endif


for (ii = 1; ii <= lp_ncols; ++ii) {
  glp_set_obj_coef (lp, ii, objective[ii]);
}


for (ii = 1; ii <= lp_ncols; ++ii) {
  glp_set_col_bnds (lp, ii, GLP_LO, mimetic_threshold, 0.0);
}


glp_index = 1;
for (ii = 0; ii <= kk; ++ii) {
  for (jj = 0; jj < kk; ++jj) {
    if (ii != robjective) {
      ar[glp_index] = A[jj + ii * ncols];
      glp_index++;
    }
  }
}

glp_index = 0;

for (ii = 1; ii < problem_size; ++ii) {
  if (((ii - 1) % lp_ncols) == 0) {
```

```
      glp_index++;
    }
    ia[ii] = glp_index;
    ja[ii] = (ii - 1) % lp_ncols + 1;
  }

  glp_load_matrix (lp, matsize, ia, ja, ar);

  #if MTK_DEBUG_LEVEL > 0
  sprintf(mps_file_name, "LP_MPS_row_%02d.mps", robjective);
  glp_write_mps(lp, GLP_MPS_FILE, nullptr, mps_file_name);
  #endif


  glp_simplex (lp, nullptr);

  // Check status of the solution.

  if (glp_get_status(lp) == GLP_OPT) {

    for(ii = 1; ii <= lp_ncols; ++ii) {
      err[ii - 1] = qq[ii - 1] - glp_get_col_prim(lp,ii);
    }

    #if MTK_DEBUG_LEVEL > 0
    obj_value = glp_get_obj_val (lp);
    std::cout << std::setw(12) << "CBS" << std::setw(12) << "CRS" << std::endl;
    for (ii = 0; ii < lp_ncols; ++ii) {
      std::cout << "q_" << ii + 1 << " = " << std::setw(12) <<
        glp_get_col_prim(lp,ii + 1) << std::setw(12) << qq[ii] << std::endl;
    }
    std::cout << "Objective function value (row " << robjective + 1 << ") = " <<
      obj_value << std::endl;
    #endif

    if (copy) {
      for(ii = 0; ii < lp_ncols; ++ii) {
        qq[ii] = glp_get_col_prim(lp,ii + 1);
      }
      // Preserve the bottom values of qq.
    }

    x1 = mtk::BLASAdapter::RealNRM2(err,lp_ncols);

  } else {
    x1 = std::numeric_limits<mtk::Real>::infinity();
  }

  glp_delete_prob (lp);
  glp_free_env ();

  delete [] ia;
  delete [] ja;
  delete [] ar;
  delete [] objective;
  delete [] rhs;
  delete [] err;

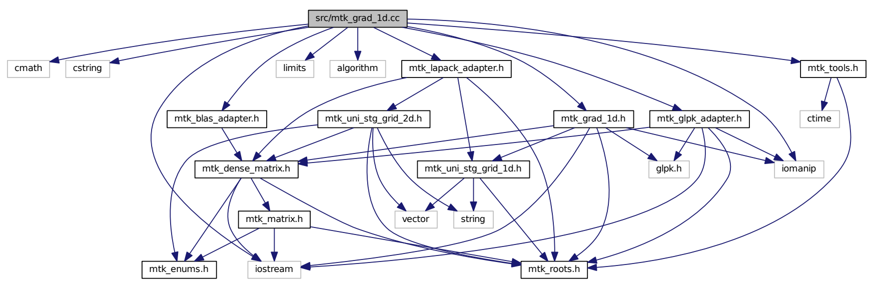
  return x1;
}
```

17.65 src/mtk_grad_1d.cc File Reference

Implements the class Grad1D.

```
#include <cmath>
#include <cstring>
#include <iostream>
#include <iomanip>
#include <limits>
#include <algorithm>
#include "mtk_tools.h"
#include "mtk_blas_adapter.h"
#include "mtk_lapack_adapter.h"
#include "mtk_glpk_adapter.h"
#include "mtk_grad_1d.h"
```

Include dependency graph for mtk_grad_1d.cc:



Namespaces

- mtk

    Mimetic Methods Toolkit namespace.

Functions

- std::ostream & mtk::operator<< (std::ostream &stream, mtk::Grad1D &in)

17.65.1 Detailed Description

This class implements a 1D gradient matrix operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Todo Overload ostream operator as in mtk::Lap1D.

Todo Implement creation of ■ w. mtk::BLASAdapter.

Definition in file mtk_grad_1d.cc.

17.66 mtk_grad_1d.cc

```

/*
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(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#include <cmath>
#include <cstring>

#include <iostream>
#include <iomanip>
#include <limits>
#include <algorithm>

#include "mtk_tools.h"

#include "mtk_blas_adapter.h"
#include "mtk_lapack_adapter.h"
#include "mtk_glpk_adapter.h"

#include "mtk_grad_1d.h"

namespace mtk {

std::ostream& operator <<(std::ostream &stream, mtk::Grad1D &in) {


  stream << "gradient_[0] = " << std::setw(9) << in.gradient_[0] << std::endl;


  stream << "gradient_[1:" << in.order_accuracy_ << "] = ";
  for (auto ii = 1; ii <= in.order_accuracy_; ++ii) {
    stream << std::setw(9) << in.gradient_[ii] << " ";
  }
  stream << std::endl;


```

```
  stream << "gradient_[" << in.order_accuracy_ + 1 << ":" <<
    2*in.order_accuracy_ << "] = ";
  for (auto ii = in.order_accuracy_ + 1; ii <= 2*in.order_accuracy_; ++ii) {
    stream << std::setw(9) << in.gradient_[ii] << " ";
  }
  stream << std::endl;


  int offset{2*in.order_accuracy_ + 1};
  int mm {};

  stream << "gradient_[" << offset + mm << ":" <<
    offset + mm + in.num_bndy_coeffs_ - 1 << "] = ";

  if (in.order_accuracy_ > mtk::kDefaultOrderAccuracy) {
    for (auto ii = 0; ii < in.num_bndy_approxs_ ; ++ii) {
      for (auto jj = 0; jj < in.num_bndy_coeffs_; jj++) {
        auto value = in.gradient_[offset + (mm)];
        stream << std::setw(9) << value << " ";
        mm++;
      }
    }
  } else {
    stream << std::setw(9) << in.gradient_[offset + 0] << ' ';
    stream << std::setw(9) << in.gradient_[offset + 1] << ' ';
    stream << std::setw(9) << in.gradient_[offset + 2] << ' ';
  }
  stream << std::endl;

  return stream;
}
}

mtk::Grad1D::Grad1D():
  order_accuracy_(mtk::kDefaultOrderAccuracy),
  dim_null_(),
  num_bndy_approxs_(),
  num_bndy_coeffs_(),
  gradient_length_(),
  minrow_(),
  row_(),
  coeffs_interior_(),
  prem_apps_(),
  weights_crs_(),
  weights_cbs_(),
  mim_bndy_(),
  gradient_(),
  mimetic_threshold_(mtk::kDefaultMimeticThreshold) {}

mtk::Grad1D::Grad1D(const Grad1D &grad):
  order_accuracy_(grad.order_accuracy_),
  dim_null_(grad.dim_null_),
  num_bndy_approxs_(grad.num_bndy_approxs_),
  num_bndy_coeffs_(grad.num_bndy_coeffs_),
  gradient_length_(grad.gradient_length_),
  minrow_(grad.minrow_),
  row_(grad.row_),
  coeffs_interior_(grad.coeffs_interior_),
  prem_apps_(grad.prem_apps_),
  weights_crs_(grad.weights_crs_),
  weights_cbs_(grad.weights_cbs_),
  mim_bndy_(grad.mim_bndy_),
  gradient_(grad.gradient_),
  mimetic_threshold_(grad.mimetic_threshold_) {}

mtk::Grad1D::~Grad1D() {

  delete[] coeffs_interior_;
  coeffs_interior_ = nullptr;

  delete[] prem_apps_;
  prem_apps_ = nullptr;

  delete[] weights_crs_;
  weights_crs_ = nullptr;

  delete[] weights_cbs_;
  weights_cbs_ = nullptr;

  delete[] mim_bndy_;
```

```
  mim_bndy_ = nullptr;

  delete[] gradient_;
  gradient_ = nullptr;
}

bool mtk::Grad1D::ConstructGrad1D(int order_accuracy,
Real mimetic_threshold) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(order_accuracy < 2, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent((order_accuracy%2) != 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(mimetic_threshold <= mtk::kZero,
                      __FILE__, __LINE__, __func__);

  if (order_accuracy >= mtk::kCriticalOrderAccuracyGrad) {
    std::cout << "WARNING: Numerical accuracy is high." << std::endl;
  }

  std::cout << "order_accuracy_ = " << order_accuracy << std::endl;
  std::cout << "mimetic_threshold_ = " << mimetic_threshold << std::endl;
  #endif

  order_accuracy_ = order_accuracy;
  mimetic_threshold_ = mimetic_threshold;

  bool abort_construction = ComputeStencilInteriorGrid();

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!abort_construction) {
    std::cerr << "Could NOT complete stage 1." << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif

  // At this point, we already have the values for the interior stencil stored
  // in the coeffs_interior_ array.

  dim_null_ = order_accuracy_/2 - 1;

  num_bndy_approxs_ = dim_null_ + 1;

  #ifdef MTK_PRECISION_DOUBLE
  num_bndy_coeffs_ = (int) (3.0*((mtk::Real) order_accuracy_)/2.0);
  #else
  num_bndy_coeffs_ = (int) (3.0f*((mtk::Real) order_accuracy_)/2.0f);
  #endif


  // For this we will follow recommendations given in:
  //
  // http://icl.cs.utk.edu/lapack-forum/viewtopic.php?f=5&t=4506
  //
  // We will compute the QR Factorization of the transpose, as in the
  // following (MATLAB) pseudo-code:
  //
  // [Q,R] = qr(V'); % Full QR as defined in
  // % http://www.stanford.edu/class/ee263/notes/qr_matlab.pdf
  //
  // null-space = Q(:, last (order_accuracy_/2 - 1) columns of Q );
  //
  // However, given the nature of the Vandermonde matrices we've just
  // computed, they all posses the same null-space. Therefore, we impose the
  // convention of computing the null-space of the first Vandermonde matrix
  // (west boundary).

  // In the case of the gradient, the first Vandermonde system has a unique
  // solution for the case of second-order-accuracy. Ergo, the Vandermonde
  // matrix used to assemble said system, will have an empty null-space.

  // Therefore, we only compute a rational basis for the case of order higher
  // than second.

  if (dim_null_ > 0) {

    abort_construction = ComputeRationalBasisNullSpace();

    #ifdef MTK_PERFORM_PREVENTIONS
    if (!abort_construction) {
      std::cerr << "Could NOT complete stage 2.1." << std::endl;
```

```
      std::cerr << "Exiting..." << std::endl;
      return false;
    }
    #endif
  }

  abort_construction = ComputePreliminaryApproximations();

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!abort_construction) {
    std::cerr << "Could NOT complete stage 2.2." << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif

  abort_construction = ComputeWeights();

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!abort_construction) {
    std::cerr << "Could NOT complete stage 2.3." << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif

  if (dim_null_ > 0) {

    abort_construction = ComputeStencilBoundaryGrid();

    #ifdef MTK_PERFORM_PREVENTIONS
    if (!abort_construction) {
      std::cerr << "Could NOT complete stage 2.4." << std::endl;
      std::cerr << "Exiting..." << std::endl;
      return false;
    }
    #endif
  }


  // Once we have the following three collections of data:
  //   (a) the coefficients for the interior,
  //   (b) the coefficients for the boundary (if it applies),
  //   (c) and the weights (if it applies),
  // we will store everything in the output array:

  abort_construction = AssembleOperator();

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!abort_construction) {
    std::cerr << "Could NOT complete stage 3." << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif

  return true;
}

int mtk::Grad1D::num_bndy_coeffs() const {

  return num_bndy_coeffs_;
}

mtk::Real *mtk::Grad1D::coeffs_interior() const {

  return coeffs_interior_;
}

mtk::Real *mtk::Grad1D::weights_crs() const {

  return weights_crs_;
}

mtk::Real *mtk::Grad1D::weights_cbs() const {

  return weights_cbs_;
}

mtk::DenseMatrix mtk::Grad1D::mim_bndy() const {

```

```
  mtk::DenseMatrix xx(dim_null_ + 1, 3*order_accuracy_/2);

  auto counter = 0;
  for (auto ii = 0; ii < dim_null_ + 1; ++ii) {
    for(auto jj = 0; jj < 3*order_accuracy_/2; ++jj) {
      xx.SetValue(ii,jj, gradient_[2*order_accuracy_ + 1 + counter]);
      counter++;
    }
  }

  return xx;
}

mtk::DenseMatrix mtk::Grad1D::ReturnAsDenseMatrix(
mtk::Real west,
                                                  mtk::Real east,
                                                  int num_cells_x) const {

  int nn{num_cells_x}; // Number of cells on the grid.

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(east < west, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(nn < 3*order_accuracy_ - 2, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(nn <= 0, __FILE__, __LINE__, __func__);
  #endif

  mtk::Real delta_x = (east - west)/((mtk::Real) num_cells_x);

  mtk::Real inv_delta_x{mtk::kOne/delta_x};

  int gg_num_rows = nn + 1;
  int gg_num_cols = nn + 2;
  int elements_per_row = num_bndy_coeffs_;
  int num_extra_rows = order_accuracy_/2;

  // Output matrix featuring sizes for gradient operators.
  mtk::DenseMatrix out(gg_num_rows, gg_num_cols);


  auto ee_index = 0;
  for (auto ii = 0; ii < num_extra_rows; ii++) {
    auto cc = 0;
    for(auto jj = 0 ; jj < gg_num_cols; jj++) {
      if(cc >= elements_per_row) {
        out.SetValue(ii, jj, mtk::kZero);
      } else {
        out.SetValue(ii,jj,
                     gradient_[2*order_accuracy_ + 1 + ee_index++]*inv_delta_x);
        cc++;
      }
    }
  }


  for (auto ii = num_extra_rows; ii < gg_num_rows - num_extra_rows; ii++) {
    auto jj = ii - num_extra_rows + 1;
    for (auto cc = 0; cc < order_accuracy_; cc++, jj++) {
      out.SetValue(ii, jj, coeffs_interior_[cc]*inv_delta_x);
    }
  }


  ee_index = 0;
  for (auto ii = gg_num_rows - 1; ii >= gg_num_rows - num_extra_rows; ii--) {
    auto cc = 0;
    for (auto jj = gg_num_cols - 1; jj >= 0; jj--) {
      if(cc >= elements_per_row) {
        out.SetValue(ii,jj,mtk::kZero);
      } else {
        out.SetValue(ii,jj,
                     -gradient_[2*order_accuracy_ + 1 +
ee_index++]*inv_delta_x);
        cc++;
      }
     }
  }

  return out;
}

mtk::DenseMatrix mtk::Grad1D::ReturnAsDenseMatrix(
```

```
  const UniStgGrid1D &grid) const {

  int nn{grid.num_cells_x()}; // Number of cells on the grid.

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(nn <= 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(nn < 3*order_accuracy_ - 2, __FILE__, __LINE__, __func__);
  #endif

  mtk::Real inv_delta_x{mtk::kOne/grid.delta_x()};

  int gg_num_rows = nn + 1;
  int gg_num_cols = nn + 2;
  int elements_per_row = num_bndy_coeffs_;
  int num_extra_rows = order_accuracy_/2;

  // Output matrix featuring sizes for gradient operators.
  mtk::DenseMatrix out(gg_num_rows, gg_num_cols);


  auto ee_index = 0;
  for (auto ii = 0; ii < num_extra_rows; ii++) {
    auto cc = 0;
    for(auto jj = 0 ; jj < gg_num_cols; jj++) {
      if(cc >= elements_per_row) {
        out.SetValue(ii, jj, mtk::kZero);
      } else {
        out.SetValue(ii,jj,
                     gradient_[2*order_accuracy_ + 1 + ee_index++]*inv_delta_x);
        cc++;
      }
    }
  }


  for (auto ii = num_extra_rows; ii < gg_num_rows - num_extra_rows; ii++) {
    auto jj = ii - num_extra_rows + 1;
    for (auto cc = 0; cc < order_accuracy_; cc++, jj++) {
      out.SetValue(ii, jj, coeffs_interior_[cc]*inv_delta_x);
    }
  }


  ee_index = 0;
  for (auto ii = gg_num_rows - 1; ii >= gg_num_rows - num_extra_rows; ii--) {
    auto cc = 0;
    for (auto jj = gg_num_cols - 1; jj >= 0; jj--) {
      if(cc >= elements_per_row) {
        out.SetValue(ii,jj,mtk::kZero);
      } else {
        out.SetValue(ii,jj,
                    -gradient_[2*order_accuracy_ + 1 + ee_index++]*inv_delta_x);
        cc++;
      }
     }
  }

  return out;
}

mtk::DenseMatrix mtk::Grad1D::ReturnAsDimensionlessDenseMatrix
(
  int num_cells_x) const {

  int nn{num_cells_x}; // Number of cells on the grid.

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(nn <= 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(nn < 3*order_accuracy_ - 2, __FILE__, __LINE__, __func__);
  #endif

  int gg_num_rows = nn + 1;
  int gg_num_cols = nn + 2;
  int elements_per_row = num_bndy_coeffs_;
  int num_extra_rows = order_accuracy_/2;

  // Output matrix featuring sizes for gradient operators.
  mtk::DenseMatrix out(gg_num_rows, gg_num_cols);


  auto ee_index = 0;
```

```
  for (auto ii = 0; ii < num_extra_rows; ii++) {
    auto cc = 0;
    for(auto jj = 0 ; jj < gg_num_cols; jj++) {
      if(cc >= elements_per_row) {
        out.SetValue(ii, jj, mtk::kZero);
      } else {
        out.SetValue(ii,jj,
                     gradient_[2*order_accuracy_ + 1 + ee_index++]);
        cc++;
      }
    }
  }


  for (auto ii = num_extra_rows; ii < gg_num_rows - num_extra_rows; ii++) {
    auto jj = ii - num_extra_rows + 1;
    for (auto cc = 0; cc < order_accuracy_; cc++, jj++) {
      out.SetValue(ii, jj, coeffs_interior_[cc]);
    }
  }


  ee_index = 0;
  for (auto ii = gg_num_rows - 1; ii >= gg_num_rows - num_extra_rows; ii--) {
    auto cc = 0;
    for (auto jj = gg_num_cols - 1; jj >= 0; jj--) {
      if(cc >= elements_per_row) {
        out.SetValue(ii,jj,mtk::kZero);
      } else {
        out.SetValue(ii,jj,
                     -gradient_[2*order_accuracy_ + 1 + ee_index++]);
        cc++;
      }
     }
  }

  return out;
}

bool mtk::Grad1D::ComputeStencilInteriorGrid() {


  mtk::Real* pp{}; // Spatial coordinates to create interior stencil.

  try {
    pp = new mtk::Real[order_accuracy_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(pp, mtk::kZero, sizeof(pp[0])*order_accuracy_);

  #ifdef MTK_PRECISION_DOUBLE
  pp[0] = 1.0/2.0 - ((mtk::Real) order_accuracy_)/2.0;
  #else
  pp[0] = 1.0f/2.0f - ((mtk::Real) order_accuracy_)/2.0f;
  #endif

  for (auto ii = 1; ii < order_accuracy_; ++ii) {
    pp[ii] = pp[ii - 1] + mtk::kOne;
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "pp =" << std::endl;
  for (auto ii = 0; ii < order_accuracy_; ++ii) {
    std::cout << std::setw(12) << pp[ii];
  }
  std::cout << std::endl << std::endl;
  #endif


  bool transpose{false};

  mtk::DenseMatrix vander_matrix(pp,order_accuracy_,order_accuracy_,transpose);

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "vander_matrix = " << std::endl;
  std::cout << vander_matrix << std::endl << std::endl;
  #endif

```

```

  try {
    coeffs_interior_ = new mtk::Real[order_accuracy_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(coeffs_interior_, mtk::kZero,
sizeof(coeffs_interior_[0])*order_accuracy_);

  coeffs_interior_[1] = mtk::kOne;

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "oo =" << std::endl;
  for (auto ii = 0; ii < order_accuracy_; ++ii) {
    std::cout << std::setw(12) << coeffs_interior_[ii] << std::endl;
  }
  std::cout << std::endl;
  #endif


  int info{mtk::LAPACKAdapter::SolveDenseSystem(vander_matrix,
                                               coeffs_interior_)};

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!info) {
    std::cout << "System solved! Interior stencil attained!" << std::endl;
    std::cout << std::endl;
  }
  else {
    std::cerr << "Something wrong solving system! info = " << info << std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  #endif

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "coeffs_interior_ =" << std::endl;
  for (auto ii = 0; ii < order_accuracy_; ++ii) {
    std::cout << std::setw(12) << coeffs_interior_[ii];
  }
  std::cout << std::endl << std::endl;
  #endif

  delete [] pp;
  pp = nullptr;

  return true;
}

bool mtk::Grad1D::ComputeRationalBasisNullSpace(void) {


  mtk::Real* gg{}; // Generator vector for the first Vandermonde matrix.

  try {
    gg = new mtk::Real[num_bndy_coeffs_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(gg, mtk::kZero, sizeof(gg[0])*num_bndy_coeffs_);

  #ifdef MTK_PRECISION_DOUBLE
  gg[1] = 1.0/2.0;
  #else
  gg[1] = 1.0f/2.0f;
  #endif
  for (auto ii = 2; ii < num_bndy_coeffs_; ++ii) {
    gg[ii] = gg[ii - 1] + mtk::kOne;
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "gg =" << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    std::cout << std::setw(12) << gg[ii];
  }
  std::cout << std::endl << std::endl;
  #endif
```

```
  bool tran{true}; // Should I transpose the Vandermonde matrix.

  mtk::DenseMatrix aa_west_t(gg, num_bndy_coeffs_, order_accuracy_ + 1, tran);

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "aa_west_t =" << std::endl;
  std::cout << aa_west_t << std::endl;
  #endif


  mtk::DenseMatrix qq_t(mtk::LAPACKAdapter::QRFactorDenseMatrix
(aa_west_t));

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "qq_t = " << std::endl;
  std::cout << qq_t << std::endl;
  #endif


  int kk_num_rows{num_bndy_coeffs_};
  int kk_num_cols{dim_null_};

  mtk::DenseMatrix kk(kk_num_rows, kk_num_cols);

  // In the case of the gradient, even though we must solve for a null-space
  // of dimension 2, we must only extract ONE basis for the kernel.
  // We perform this extraction here:

  int aux_{kk_num_rows - kk_num_cols};
  for (auto ii = kk_num_rows - kk_num_cols; ii < kk_num_rows; ii++) {
    aux_--;
    for (auto jj = 0; jj < kk_num_rows; jj++) {
      kk.data()[jj*kk_num_cols + (kk_num_rows - kk_num_cols - aux_ - 1)] =
        qq_t.data()[ii*num_bndy_coeffs_ + jj];
    }
  }

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "kk =" << std::endl;
  std::cout << kk << std::endl;
  std::cout << "kk.num_rows() = " << kk.num_rows() << std::endl;
  std::cout << "kk.num_cols() = " << kk.num_cols() << std::endl;
  std::cout << std::endl;
  #endif


  // Scale thus requesting that the last entries of the attained basis for the
  // null-space, adopt the pattern we require.
  // Essentially we will implement the following MATLAB pseudo-code:
  //  scalers = kk(num_bndy_approxs - (dim_null - 1):num_bndy_approxs,:)\B
  //  SK = kk*scalers
  // where SK is the scaled null-space.

  // In this point, we almost have all the data we need correctly allocated
  // in memory. We will create the matrix iden_, and elements we wish to scale
  // in the kk array. Using the concept of the leading dimension, we could just
  // use kk, with the correct leading dimension and that is it. BUT I DO NOT
  // GET how does it work. So I will just create a matrix with the content of
  // this array that we need, solve for the scalers and then scale the
  // whole kk:

  // We will then create memory for that sub-matrix of kk (subk).

  mtk::DenseMatrix subk(dim_null_, dim_null_);

  auto zz = 0;
  for (auto ii = order_accuracy_ + 1; ii < num_bndy_coeffs_; ii++) {
    for (auto jj = 0; jj < dim_null_; jj++) {
      subk.data()[zz*(dim_null_) + jj] = kk.data()[ii*(dim_null_) + jj];
    }
    zz++;
  }

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "subk =" << std::endl;
  std::cout << subk << std::endl;
  #endif

  subk.Transpose();
```

```
#if MTK_VERBOSE_LEVEL > 4
  std::cout << "subk_t =" << std::endl;
  std::cout << subk << std::endl;
  #endif

  bool padded{false};
  tran = false;

  mtk::DenseMatrix iden(dim_null_, padded, tran);

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "iden =" << std::endl;
  std::cout << iden << std::endl;
  #endif

  // Solve the system to compute the scalers.
  // An example of the system to solve, for k = 8, is:
  //
  // subk*scalers = iden or
  //
  // |  0.386018  -0.0339244   -0.129478 |           | 1 0 0 |
  // | -0.119774   0.0199423   0.0558632 |*scalers = | 0 1 0 |
  // | 0.0155708 -0.00349546 -0.00853182 |           | 0 0 1 |
  //
  // Notice this is a nrhs = 3 system.
  // Noteworthy: we do NOT ACTUALLY ALLOCATE space for the scalers... they
  // will be stored in the created identity matrix.
  // Let us first transpose subk (because of LAPACK):

  int info{mtk::LAPACKAdapter::SolveDenseSystem(subk, iden)};

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!info) {
    std::cout << "System successfully solved!" <<
      std::endl;
  } else {
    std::cerr << "Something went wrong solving system! info = " << info <<
      std::endl;
    std::cerr << "Exiting..." << std::endl;
    return false;
  }
  std::cout << std::endl;
  #endif

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "Computed scalers:" << std::endl;
  std::cout << iden << std::endl;
  #endif

  // Multiply the two matrices to attain a scaled basis for null-space.

  rat_basis_null_space_ = mtk::BLASAdapter::RealDenseMM(kk, iden);

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "Rational basis for the null-space:" << std::endl;
  std::cout << rat_basis_null_space_ << std::endl;
  #endif

  // At this point, we have a rational basis for the null-space, with the
  // pattern we need! :)

  delete [] gg;
  gg = nullptr;

  return true;
}

bool mtk::Grad1D::ComputePreliminaryApproximations() {


  mtk::Real *gg{}; // Generator vector for the first approximation.

  try {
    gg = new mtk::Real[num_bndy_coeffs_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(gg, mtk::kZero, sizeof(gg[0])*num_bndy_coeffs_);
```

```
  #ifdef MTK_PRECISION_DOUBLE
  gg[1] = 1.0/2.0;
  #else
  gg[1] = 1.0f/2.0f;
  #endif
  for (auto ii = 2; ii < num_bndy_coeffs_; ++ii) {
    gg[ii] = gg[ii - 1] + mtk::kOne;
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "gg0 =" << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    std::cout << std::setw(12) << gg[ii];
  }
  std::cout << std::endl << std::endl;
  #endif

  // Allocate 2D array to store the collection of preliminary approximations.
  try {
    prem_apps_ = new mtk::Real[num_bndy_coeffs_*num_bndy_approxs_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(prem_apps_,
         mtk::kZero,
         sizeof(prem_apps_[0])*num_bndy_coeffs_*num_bndy_approxs_);


  for (auto ll = 0; ll < num_bndy_approxs_; ++ll) {

    // Re-check new generator vector for every iteration except for the first.
    #if MTK_VERBOSE_LEVEL > 3
    if (ll > 0) {
      std::cout << "gg_" << ll << " =" << std::endl;
      for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
        std::cout << std::setw(12) << gg[ii];
      }
      std::cout << std::endl << std::endl;
    }
    #endif


    bool transpose{false};

    mtk::DenseMatrix aa(gg,
                         num_bndy_coeffs_, order_accuracy_ + 1,
                         transpose);

    #if MTK_VERBOSE_LEVEL > 4
    std::cout << "aa_" << ll << " =" << std::endl;
    std::cout << aa << std::endl;
    #endif


    mtk::Real *ob{};

    auto ob_ld = num_bndy_coeffs_;

    try {
      ob = new mtk::Real[ob_ld];
    } catch (std::bad_alloc &memory_allocation_exception) {
      std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
        std::endl;
      std::cerr << memory_allocation_exception.what() << std::endl;
    }
    memset(ob, mtk::kZero, sizeof(ob[0])*ob_ld);

    ob[1] = mtk::kOne;

    #if MTK_VERBOSE_LEVEL > 3
    std::cout << "ob = " << std::endl << std::endl;
    for (auto ii = 0; ii < ob_ld; ++ii) {
      std::cout << std::setw(12) << ob[ii] << std::endl;
    }
    std::cout << std::endl;
    #endif

```

```
  // However, this is an under-determined system of equations. So we can not
  // use the same LAPACK routine (dgesv_). We will instead use dgels_, through
  // our LAPACKAdapter class.

  int info_{
    mtk::LAPACKAdapter::SolveRectangularDenseSystem(aa, ob
, ob_ld)};

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!info_) {
    std::cout << "System successfully solved!" << std::endl << std::endl;
  } else {
    std::cerr << "Error solving system! info = " << info_ << std::endl;
    return false;
  }
  #endif

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "ob =" << std::endl;
  for (auto ii = 0; ii < ob_ld; ++ii) {
    std::cout << std::setw(12) << ob[ii] << std::endl;
  }
  std::cout << std::endl;
  #endif


  // This implies a DAXPY operation. However, we must construct the arguments
  // for this operation.

  // Save them into the ob_bottom array:

  Real *ob_bottom{}; // Bottom part of the attained kernel used to scale it.

  try {
    ob_bottom = new mtk::Real[dim_null_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(ob_bottom, mtk::kZero, sizeof(ob_bottom[0])*dim_null_);

  for (auto ii = 0; ii < dim_null_; ++ii) {
    ob_bottom[(dim_null_ - 1) - ii] = ob[num_bndy_coeffs_ - ii - 1];
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "ob_bottom =" << std::endl;
  for (auto ii = 0; ii < dim_null_; ++ii) {
    std::cout << std::setw(12) << ob_bottom[ii] << std::endl;
  }
  std::cout << std::endl;
  #endif


  // We must computed an scaled ob, sob, using the scaled null-space in
  // rat_basis_null_space_.
  // Such operation is: sob = ob - rat_basis_null_space_*ob_bottom
  // or:                 ob = -1.0*rat_basis_null_space_*ob_bottom + 1.0*ob
  // thus:                Y =    a*A    *x         +   b*Y (DAXPY).

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "Rational basis for the null-space:" << std::endl;
  std::cout << rat_basis_null_space_ << std::endl;
  #endif

  mtk::Real alpha{-mtk::kOne};
  mtk::Real beta{mtk::kOne};

  mtk::BLASAdapter::RealDenseMV(alpha, rat_basis_null_space_,
                                ob_bottom, beta, ob);

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "scaled ob:" << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    std::cout << std::setw(12) << ob[ii] << std::endl;
  }
  std::cout << std::endl;
  #endif

  // We save the recently scaled solution, into an array containing these.
```

```
    // We can NOT start building the pi matrix, simply because I want that part
    // to be separated since its construction depends on the algorithm we want
    // to implement.

    for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
      prem_apps_[ii*num_bndy_approxs_ + ll] = ob[ii];
    }

    // After the first iteration, simply shift the entries of the last
    // generator vector used:
    for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
      gg[ii]--;
    }

    // Garbage collection for this loop:
    delete[] ob;
    ob = nullptr;

    delete[] ob_bottom;
    ob_bottom = nullptr;
  } // End of: for (ll = 0; ll < dim_null; ll++);

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "Matrix post-scaled preliminary apps: " << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    for (auto jj = 0; jj < num_bndy_approxs_; ++jj) {
      std::cout << std::setw(12) << prem_apps_[ii*num_bndy_approxs_ + jj];
    }
    std::cout << std::endl;
  }
  std::cout << std::endl;
  #endif

  delete[] gg;
  gg = nullptr;

  return true;
}

bool mtk::Grad1D::ComputeWeights() {

  // Matrix to compute the weights as in the CRSA.
  mtk::DenseMatrix pi(num_bndy_coeffs_, num_bndy_coeffs_ - 1);


  // Assemble the pi matrix using:
  // 1. The collection of scaled preliminary approximations.
  // 2. The collection of coefficients approximating at the interior.
  // 3. The scaled basis for the null-space.

  // 1.1. Process array of scaled preliminary approximations.

  // These are queued in scaled_solutions. Each one of these, will be a column
  // of the pi matrix:
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    for (auto jj = 0; jj < num_bndy_approxs_; ++jj) {
      pi.data()[ii*(2*(num_bndy_approxs_ - 1) + (order_accuracy_/2 + 1)) + jj] =
        prem_apps_[ii*num_bndy_approxs_ + jj];
    }
  }

  // 1.2. Add columns from known stencil approximating at the interior.

  // However, these must be padded by zeros, according to their position in the
  // final pi matrix:
  auto mm = 1;
  for (auto jj = num_bndy_approxs_; jj < order_accuracy_; ++jj) {
    for (auto ii = 0; ii < order_accuracy_; ++ii) {
      auto de = (ii + mm)*(2*(num_bndy_approxs_ - 1) +
        (order_accuracy_/2 + 1)) + jj;
      pi.data()[de] = coeffs_interior_[ii];
    }
    ++mm;
  }

  rat_basis_null_space_.OrderColMajor();

  #if MTK_VERBOSE_LEVEL > 4
  std::cout << "Rational basis for the null-space (col. major):" << std::endl;
  std::cout << rat_basis_null_space_ << std::endl;
  #endif
```

```
// 1.3. Add final set of columns: rational basis for null-space.

for (auto jj = dim_null_ + (order_accuracy_/2 + 1);
     jj < num_bndy_coeffs_ - 1; ++jj) {
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    auto og =
      (jj - (dim_null_ + (order_accuracy_/2 + 1)))*num_bndy_coeffs_ + ii;
    auto de = ii*(2*dim_null_ + (order_accuracy_/2 + 1)) + jj;
    pi.data()[de] = rat_basis_null_space_.data()[og];
  }
}

#if MTK_VERBOSE_LEVEL > 4
std::cout << "coeffs_interior_ =" << std::endl;
for (auto ii = 0; ii < order_accuracy_; ++ii) {
  std::cout << std::setw(12) << coeffs_interior_[ii];
}
std::cout << std::endl << std::endl;
#endif

#if MTK_VERBOSE_LEVEL > 4
std::cout << "Constructed pi matrix for CRS Algorithm: " << std::endl;
std::cout << pi << std::endl;
#endif


// This imposes the mimetic condition.

mtk::Real *hh{};  // Right-hand side to compute weights in the C{R,B}SA.

try {
  hh = new mtk::Real[num_bndy_coeffs_];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(hh, mtk::kZero, sizeof(hh[0])*num_bndy_coeffs_);

hh[0] = -mtk::kOne;
for (auto ii = (order_accuracy_/2 + 2 - 1); ii < num_bndy_coeffs_; ++ii) {
  auto aux_xx = mtk::kZero;
  for (auto jj = 0; jj < ((ii - (order_accuracy_/2 - 1)) - 1); ++jj) {
    aux_xx += coeffs_interior_[jj];
  }
  hh[ii] = -mtk::kOne*aux_xx;
}


// That is, we construct a system, to solve for the weights.

// Once again we face the challenge of solving with LAPACK. However, for the
// CRSA, this matrix PI is over-determined, since it has more rows than
// unknowns. However, according to the theory, the solution to this system is
// unique. We will use dgels_.

try {
  weights_cbs_ = new mtk::Real[num_bndy_coeffs_];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(weights_cbs_, mtk::kZero, sizeof(weights_cbs_[0])*num_bndy_coeffs_);

int weights_ld{pi.num_cols() + 1};

// Preserve hh.
std::copy(hh, hh + weights_ld, weights_cbs_);

pi.Transpose();

int info{
  mtk::LAPACKAdapter::SolveRectangularDenseSystem(pi,
                                                  weights_cbs_, weights_ld)
};

#ifdef MTK_PERFORM_PREVENTIONS
if (!info) {
  std::cout << "System successfully solved!" << std::endl << std::endl;
```

```
} else {
  std::cerr << "Error solving system! info = " << info << std::endl;
  return false;
}
#endif

#if MTK_VERBOSE_LEVEL > 3
std::cout << "hh =" << std::endl;
for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
  std::cout << std::setw(11) << hh[ii] << std::endl;
}
std::cout << std::endl;
#endif

// Preserve the original weights for research.

try {
  weights_crs_ = new mtk::Real[num_bndy_coeffs_];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(weights_crs_, mtk::kZero, sizeof(weights_crs_[0])*num_bndy_coeffs_);

std::copy(weights_cbs_, weights_cbs_ + (weights_ld - 1), weights_crs_);

#if MTK_VERBOSE_LEVEL > 3
std::cout << "weights_CRSA + lambda =" << std::endl;
for (auto ii = 0; ii < weights_ld - 1; ++ii) {
  std::cout << std::setw(12) << weights_crs_[ii] << std::endl;
}
std::cout << std::endl;
#endif


if (order_accuracy_ >= mtk::kCriticalOrderAccuracyGrad) {

  int minrow_{std::numeric_limits<int>::infinity()};

  mtk::Real norm{mtk::BLASAdapter::RealNRM2(weights_cbs_,
order_accuracy_)};
  mtk::Real minnorm{std::numeric_limits<mtk::Real>::infinity()};


  mtk::DenseMatrix phi(order_accuracy_ + 1, order_accuracy_);

  // 6.1. Insert preliminary approximations to first set of columns.

  for (auto ii = 0; ii < order_accuracy_ + 1; ++ii) {
    for (auto jj = 0; jj < num_bndy_approxs_; ++jj) {
      phi.data()[ii*(order_accuracy_) + jj] =
        prem_apps_[ii*num_bndy_approxs_ + jj];
    }
  }

  // 6.2. Skip a column and negate preliminary approximations.

  for (auto jj = 0; jj < order_accuracy_ + 1; jj++) {
    for (auto ii = 1; ii < num_bndy_approxs_; ii++) {
      auto de = (ii+ order_accuracy_ - num_bndy_approxs_+ jj*order_accuracy_);
      auto og = (num_bndy_approxs_ - ii + (jj)*num_bndy_approxs_);
      phi.data()[de] = -prem_apps_[og];
    }
  }

  // 6.3. Flip negative columns up-down.

  for (auto ii = 0; ii < order_accuracy_/2; ii++) {
    for (auto jj = num_bndy_approxs_ + 1; jj < order_accuracy_; jj++) {
      auto aux = phi.data()[ii*order_accuracy_ + jj];
      phi.data()[ii*order_accuracy_ + jj] =
        phi.data()[(order_accuracy_ - ii)*order_accuracy_ + jj];
      phi.data()[(order_accuracy_ - ii)*order_accuracy_ + jj] = aux;
    }
  }

  // 6.4. Insert stencil.

  auto mm = 0;
  for (auto jj = num_bndy_approxs_; jj < num_bndy_approxs_ +  1; jj++) {
```

```
      for (auto ii = 0; ii < order_accuracy_ + 1; ii++) {
        if (ii == 0) {
          phi.data()[jj] = 0.0;
        } else {
          phi.data()[(ii + mm)*order_accuracy_ + jj] = coeffs_interior_[ii - 1];
        }
      }
      mm++;
    }

    #if MTK_VERBOSE_LEVEL > 4
    std::cout << "phi =" << std::endl;
    std::cout << phi << std::endl;
    #endif


    mtk::Real *lamed{};  // Used to build big lambda.

    try {
      lamed = new mtk::Real[num_bndy_approxs_ - 1];
    } catch (std::bad_alloc &memory_allocation_exception) {
      std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
        std::endl;
      std::cerr << memory_allocation_exception.what() << std::endl;
    }
    memset(lamed, mtk::kZero, sizeof(lamed[0])*(num_bndy_approxs_ - 1));

    for (auto ii = 0; ii < num_bndy_approxs_ - 1; ++ii) {
      lamed[ii] = hh[ii + order_accuracy_ + 1] ;
    }

    #if MTK_VERBOSE_LEVEL > 3
    std::cout << "lamed =" << std::endl;
    for (auto ii = 0; ii < num_bndy_approxs_ - 1; ++ii) {
      std::cout << std::setw(12) << lamed[ii] << std::endl;
    }
    std::cout << std::endl;
    #endif

    for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
      mtk::Real temp = mtk::kZero;
      for(auto jj = 0; jj < num_bndy_approxs_ - 1; ++jj) {
        temp = temp +
          lamed[jj]*rat_basis_null_space_.data()[jj*num_bndy_coeffs_ + ii];
      }
      hh[ii] = hh[ii] - temp;
    }

    #if MTK_VERBOSE_LEVEL > 3
    std::cout << "big_lambda =" << std::endl;
    for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
      std::cout << std::setw(12) << hh[ii] << std::endl;
    }
    std::cout << std::endl;
    #endif


    int copy_result{};  // Should I replace the solution... not for now.

    mtk::Real normerr_; // Norm of the error for the solution on each row.

    for(auto row_= 0; row_ < order_accuracy_ + 1; ++row_) {
      normerr_ = mtk::GLPKAdapter::SolveSimplexAndCompare(phi.
  data(),
                                                          order_accuracy_ + 1,
                                                          order_accuracy_,
                                                          order_accuracy_,
                                                          hh,
                                                          weights_cbs_,
                                                          row_,
                                                          mimetic_threshold_,
                                                          copy_result);
      mtk::Real aux{normerr_/norm};

      #if MTK_VERBOSE_LEVEL > 2
      std::cout << "Relative norm: " << aux << " " << std::endl;
      std::cout << std::endl;
      #endif

      if (aux < minnorm) {
        minnorm = aux;
```

```
        minrow_= row_;
      }
    }

    #if MTK_VERBOSE_LEVEL > 3
    std::cout << "weights_CBSA + lambda (after brute force search):" <<
      std::endl;
    for (auto ii = 0; ii < num_bndy_coeffs_ - 1; ++ii) {
      std::cout << std::setw(12) << weights_cbs_[ii] << std::endl;
    }
    std::cout << std::endl;
    #endif


    // After we know which row yields the smallest relative norm that row is
    // chosen to be the objective function and the result of the optimizer is
    // chosen to be the new weights_.

    #if MTK_VERBOSE_LEVEL > 2
    std::cout << "Minimum Relative Norm " << minnorm << " found at row " <<
      minrow_ + 1 << std::endl;
    std::cout << std::endl;
    #endif

    copy_result = 1;
    normerr_ = mtk::GLPKAdapter::SolveSimplexAndCompare(phi.data(),
                                                         order_accuracy_ + 1,
                                                         order_accuracy_,
                                                         order_accuracy_,
                                                         hh,
                                                         weights_cbs_,
                                                         minrow_,
                                                         mimetic_threshold_,
                                                         copy_result);
    mtk::Real aux_{normerr_/norm};
    #if MTK_VERBOSE_LEVEL > 2
    std::cout << "Relative norm: " << aux_ << std::endl;
    std::cout << std::endl;
    #endif

    delete [] lamed;
    lamed = nullptr;
  }

  delete [] hh;
  hh = nullptr;

  return true;
}

bool mtk::Grad1D::ComputeStencilBoundaryGrid(void) {

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "weights_* + lambda =" << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_ - 1; ++ii) {
    std::cout << std::setw(12) << weights_cbs_[ii] << std::endl;
  }
  std::cout << std::endl;
  #endif


  mtk::Real *lambda{}; // Collection of bottom values from weights_.

  try {
    lambda = new mtk::Real[dim_null_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(lambda, mtk::kZero, sizeof(lambda[0])*dim_null_);

  for (auto ii = 0; ii < dim_null_; ++ii) {
    lambda[ii] = weights_cbs_[order_accuracy_ + ii];
  }

  #if MTK_VERBOSE_LEVEL > 3
  std::cout << "lambda =" << std::endl;
  for (auto ii = 0; ii < dim_null_; ++ii) {
    std::cout << std::setw(12) << lambda[ii] << std::endl;
```

```
  }
  std::cout << std::endl;
#endif


  mtk::Real *alpha{}; // Collection of alpha values.

  try {
    alpha = new mtk::Real[dim_null_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(alpha, mtk::kZero, sizeof(alpha[0])*dim_null_);

  for (auto ii = 0; ii < dim_null_; ++ii) {
    alpha[ii] = lambda[ii]/weights_cbs_[ii] ;
  }

#if MTK_VERBOSE_LEVEL > 3
  std::cout << "alpha =" << std::endl;
  for (auto ii = 0; ii < dim_null_; ++ii) {
    std::cout << std::setw(12) << alpha[ii] << std::endl;
  }
  std::cout << std::endl;
#endif


  try {
    mim_bndy_ = new mtk::Real[num_bndy_coeffs_*num_bndy_approxs_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(mim_bndy_,
         mtk::kZero,
         sizeof(mim_bndy_[0])*num_bndy_coeffs_*num_bndy_approxs_);

  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    for (auto jj = 0; jj < (num_bndy_approxs_ - 1); ++jj) {
      mim_bndy_[ii*num_bndy_approxs_ + jj] =
        prem_apps_[ii*num_bndy_approxs_ + jj] +
        alpha[jj]*rat_basis_null_space_.data()[jj*num_bndy_coeffs_ + ii];
    }
  }

  for(auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    mim_bndy_[ii*num_bndy_approxs_ + (num_bndy_approxs_ - 1)] =
      prem_apps_[ii*num_bndy_approxs_ + (num_bndy_approxs_ - 1)];
  }

#if MTK_VERBOSE_LEVEL > 4
  std::cout << "Collection of mimetic approximations:" << std::endl;
  for (auto ii = 0; ii < num_bndy_coeffs_; ++ii) {
    for (auto jj = 0; jj < num_bndy_approxs_; ++jj) {
      std::cout << std::setw(13) << mim_bndy_[ii*num_bndy_approxs_ + jj];
    }
    std::cout << std::endl;
  }
  std::cout << std::endl;
#endif

  delete[] lambda;
  lambda = nullptr;

  delete[] alpha;
  alpha = nullptr;

  return true;
}

bool mtk::Grad1D::AssembleOperator(void) {

  // The output array will have this form:
  // 1. The first entry of the array will contain the used order kk.
  // 2. The second entry of the array will contain the collection of
  // approximating coefficients for the interior of the grid.
  // 3. The third entry will contain a collection of weights.
  // 4. The next dim_null - 1 entries will contain the collections of
```

```
  // approximating coefficients for the west boundary of the grid.

  gradient_length_ = 1 + order_accuracy_ + order_accuracy_ +
    num_bndy_approxs_*num_bndy_coeffs_;

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "gradient_length_ = " << gradient_length_ << std::endl;
  #endif

  try {
    gradient_ = new mtk::Real[gradient_length_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(gradient_, mtk::kZero, sizeof(gradient_[0])*gradient_length_);


  gradient_[0] = order_accuracy_;


  for (auto ii = 0; ii < order_accuracy_; ++ii) {
    gradient_[ii + 1] = coeffs_interior_[ii];
  }


  for (auto ii = 0; ii < order_accuracy_; ++ii) {
    gradient_[(order_accuracy_ + 1) + ii] = weights_cbs_[ii];
  }


  int offset{2*order_accuracy_ + 1};

  int aux {}; // Auxiliary variable.

  if (order_accuracy_ > mtk::kDefaultOrderAccuracy) {
    for (auto ii = 0; ii < num_bndy_approxs_ ; ii++) {
      for (auto jj = 0; jj < num_bndy_coeffs_; jj++) {
        gradient_[offset + aux] = mim_bndy_[jj*num_bndy_approxs_ + ii];
        aux++;
      }
    }
  } else {
    gradient_[offset + 0] = prem_apps_[0];
    gradient_[offset + 1] = prem_apps_[1];
    gradient_[offset + 2] = prem_apps_[2];
  }

  #if MTK_VERBOSE_LEVEL > 1
  std::cout << "1D " << order_accuracy_ << "-order grad built!" << std::endl;
  std::cout << std::endl;
  #endif

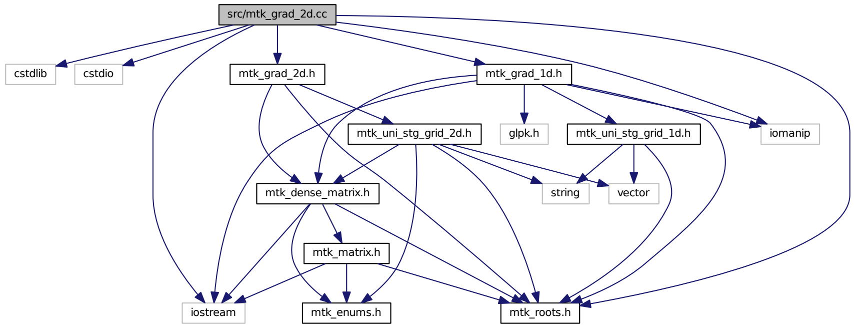
  return true;
}
```

17.67 src/mtk_grad_2d.cc File Reference

Implements the class Grad2D.

```
#include <cstdlib>
#include <cstdio>
#include <iostream>
#include <iomanip>
#include "mtk_roots.h"
#include "mtk_grad_1d.h"
#include "mtk_grad_2d.h"
```

Include dependency graph for mtk_grad_2d.cc:



17.67.1 Detailed Description

This class implements a 2D gradient operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (C←BSA).

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_grad_2d.cc.

17.68 mtk_grad_2d.cc

```
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```
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*/

#include <cstdlib>
#include <cstdio>

#include <iostream>
#include <iomanip>

#include "mtk_roots.h"
#include "mtk_grad_1d.h"
#include "mtk_grad_2d.h"

mtk::Grad2D::Grad2D():
  order_accuracy_(),
  mimetic_threshold_() {}

mtk::Grad2D::Grad2D(const Grad2D &grad):
  order_accuracy_(grad.order_accuracy_),
  mimetic_threshold_(grad.mimetic_threshold_) {}

mtk::Grad2D::~Grad2D() {}

bool mtk::Grad2D::ConstructGrad2D(const mtk::UniStgGrid2D &grid,
                                  int order_accuracy,
                                  mtk::Real mimetic_threshold) {

  int num_cells_x = grid.num_cells_x();
  int num_cells_y = grid.num_cells_y();

  int mx = num_cells_x + 1;  // Gx vertical dimension
  int nx = num_cells_x + 2;  // Gx horizontal dimension
  int my = num_cells_y + 1;  // Gy vertical dimension
  int ny = num_cells_y + 2;  // Gy horizontal dimension

  mtk::Grad1D grad;

  bool info = grad.ConstructGrad1D(order_accuracy, mimetic_threshold);

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!info) {
    std::cerr << "Mimetic grad could not be built." << std::endl;
    return info;
  }
  #endif

  auto west = grid.west_bndy();
  auto east = grid.east_bndy();
  auto south = grid.south_bndy();
  auto north = grid.east_bndy();

  mtk::UniStgGrid1D grid_x(west, east, num_cells_x);
  mtk::UniStgGrid1D grid_y(south, north, num_cells_y);

  mtk::DenseMatrix Gx(grad.ReturnAsDenseMatrix(grid_x));
  mtk::DenseMatrix Gy(grad.ReturnAsDenseMatrix(grid_y));

  bool padded{true};
  bool transpose{true};

  mtk::DenseMatrix tix(num_cells_x, padded, transpose);
  mtk::DenseMatrix tiy(num_cells_y, padded, transpose);

  mtk::DenseMatrix gxy(mtk::DenseMatrix::Kron(tiy, Gx));
  mtk::DenseMatrix gyx(mtk::DenseMatrix::Kron(Gy, tix));

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "Gx: " << mx << " by " << nx << std::endl;
  std::cout << "Transpose Iy: " << num_cells_y << " by " << ny  << std::endl;
```
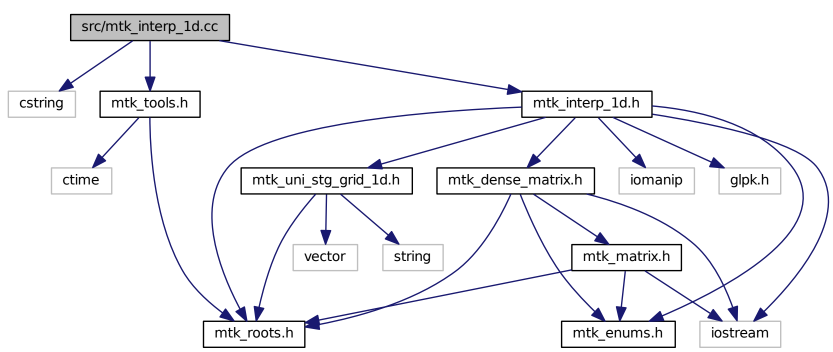

```
  std::cout << "Gy: " << my << " by " << ny << std::endl;
  std::cout << "Transpose Ix: " << num_cells_x << " by " << nx  << std::endl;
  std::cout << "Grad 2D: " << mx*num_cells_y + my*num_cells_x << " by " <<
    nx*ny <<std::endl;
  #endif

  mtk::DenseMatrix g2d(mx*num_cells_y + my*num_cells_x, nx*ny);

  for(auto ii = 0; ii < nx*ny; ii++) {
    for(auto jj = 0; jj < mx*num_cells_y; jj++) {
      g2d.SetValue(jj,ii, gxy.GetValue(jj,ii));
    }
    for(auto kk = 0; kk < my*num_cells_x; kk++) {
      g2d.SetValue(kk + mx*num_cells_y, ii, gyx.GetValue(kk,ii));
    }
  }

  gradient_ = g2d;

  return info;
}

mtk::DenseMatrix mtk::Grad2D::ReturnAsDenseMatrix() const {

  return gradient_;
}
```

17.69 src/mtk_interp_1d.cc File Reference

Includes the implementation of the class Interp1D.

```
#include <cstring>
#include "mtk_tools.h"
#include "mtk_interp_1d.h"
```

Include dependency graph for mtk_interp_1d.cc:



Namespaces

- mtk

    Mimetic Methods Toolkit namespace.

Functions

- std::ostream & mtk::operator<< (std::ostream &stream, mtk::Interp1D &in)

17.69.1 Detailed Description

This class implements a 1D interpolation operator.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu
: Johnny Corbino - jcorbino at mail dot sdsu dot edu

Definition in file mtk_interp_1d.cc.

17.70 mtk_interp_1d.cc

```

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*/

#include <cstring>

#include "mtk_tools.h"

#include "mtk_interp_1d.h"

namespace mtk {

std::ostream& operator <<(std::ostream &stream, mtk::Interp1D &in) {


  stream << "coeffs_interior_[1:" << in.order_accuracy_ << "] = ";
  for (auto ii = 0; ii < in.order_accuracy_; ++ii) {
```

```
    stream << std::setw(9) << in.coeffs_interior_[ii] << " ";
  }
  stream << std::endl;

  return stream;
}
}

mtk::Interp1D::Interp1D():
  dir_interp_(mtk::SCALAR_TO_VECTOR),
  order_accuracy_(mtk::kDefaultOrderAccuracy),
  coeffs_interior_(nullptr) {}

mtk::Interp1D::Interp1D(const Interp1D &interp):
  dir_interp_(interp.dir_interp_),
  order_accuracy_(interp.order_accuracy_),
  coeffs_interior_(interp.coeffs_interior_) {}

mtk::Interp1D::~Interp1D() {

  delete[] coeffs_interior_;
  coeffs_interior_ = nullptr;
}

bool mtk::Interp1D::ConstructInterp1D(int order_accuracy, mtk::DirInterp dir) {

  #if MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(order_accuracy < 2, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent((order_accuracy%2) != 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(dir < mtk::SCALAR_TO_VECTOR &&
                      dir > mtk::VECTOR_TO_SCALAR,
                      __FILE__, __LINE__, __func__);
  #endif

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "order_accuracy_ = " << order_accuracy << std::endl;
  #endif

  order_accuracy_ = order_accuracy;


  try {
    coeffs_interior_ = new mtk::Real[order_accuracy_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(coeffs_interior_,
         mtk::kZero,
         sizeof(coeffs_interior_[0])*order_accuracy_);

  for (int ii = 0; ii < order_accuracy_; ++ii) {
    coeffs_interior_[ii] = mtk::kOne;
  }

  return true;
}

mtk::Real *mtk::Interp1D::coeffs_interior() const {

  return coeffs_interior_;
}

mtk::DenseMatrix mtk::Interp1D::ReturnAsDenseMatrix(
  const UniStgGrid1D &grid) const {

  int nn{grid.num_cells_x()}; // Number of cells on the grid.

  #if MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(nn <= 0, __FILE__, __LINE__, __func__);
  #endif

  int gg_num_rows{};  // Number of rows.
  int gg_num_cols{};  // Number of columns.

  if (dir_interp_ == mtk::SCALAR_TO_VECTOR) {
    gg_num_rows = nn + 1;
    gg_num_cols = nn + 2;
  } else {
```

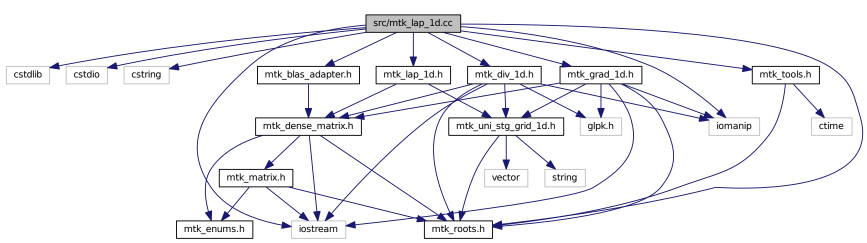
```
    gg_num_rows = nn + 2;
    gg_num_cols = nn + 1;
  }

  // Output matrix featuring sizes for gradient operators.

  mtk::DenseMatrix out(gg_num_rows, gg_num_cols);


  out.SetValue(0, 0, mtk::kOne);


  for (auto ii = 1; ii < gg_num_rows - 1; ++ii) {
    for(auto jj = ii ; jj < order_accuracy_ + ii; ++jj) {
      out.SetValue(ii, jj, mtk::kOne/order_accuracy_);
    }
  }


  out.SetValue(gg_num_rows - 1, gg_num_cols - 1, mtk::kOne);

  return out;
}
```

17.71 src/mtk_lap_1d.cc File Reference

Includes the implementation of the class Lap1D.

```
#include <cstdlib>
#include <cstdio>
#include <cstring>
#include <iostream>
#include <iomanip>
#include "mtk_roots.h"
#include "mtk_tools.h"
#include "mtk_blas_adapter.h"
#include "mtk_grad_1d.h"
#include "mtk_div_1d.h"
#include "mtk_lap_1d.h"
```

Include dependency graph for mtk_lap_1d.cc:



Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

Functions

- std::ostream & mtk::operator<< (std::ostream &stream, mtk::Lap1D &in)

17.71.1 Detailed Description

This class implements a 1D Laplacian operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (CBSA).

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_lap_1d.cc.

17.72 mtk_lap_1d.cc

```
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*/

#include <cstdlib>
#include <cstdio>
#include <cstring>

#include <iostream>
```

```
#include <iomanip>

#include "mtk_roots.h"
#include "mtk_tools.h"
#include "mtk_blas_adapter.h"
#include "mtk_grad_1d.h"
#include "mtk_div_1d.h"
#include "mtk_lap_1d.h"

namespace mtk {

std::ostream& operator <<(std::ostream &stream, mtk::Lap1D &in) {


  stream << "laplacian_[0] = " << in.laplacian_[0] << std::endl << std::endl;


  stream << "laplacian_[1:" << 2*in.order_accuracy_ - 1 << "] = " <<
    std::endl << std::endl;
  for (auto ii = 1; ii <= (2*in.order_accuracy_ - 1); ++ii) {
    stream << std::setw(13) << in.laplacian_[ii] << " ";
  }
  stream << std::endl << std::endl;


  auto offset = 1 + (2*in.order_accuracy_ - 1);

  stream << "laplacian_[" << offset << ":" << offset +
    (in.order_accuracy_ - 1)*(2*in.order_accuracy_) - 1 << "] = " <<
    std::endl << std::endl;

  for (auto ii = 0; ii < in.order_accuracy_ - 1; ++ii) {
    for (auto jj = 0; jj < 2*in.order_accuracy_; ++jj) {
      stream << std::setw(13) <<
        in.laplacian_[offset + ii*(2*in.order_accuracy_) + jj];
    }
    stream << std::endl;
  }

  return stream;
}
}

mtk::Lap1D::Lap1D():
  order_accuracy_(mtk::kDefaultOrderAccuracy),
  laplacian_length_(),
  delta_(mtk::kZero),
  mimetic_threshold_(mtk::kDefaultMimeticThreshold) {}

mtk::Lap1D::~Lap1D() {

  delete [] laplacian_;
  laplacian_ = nullptr;
}

int mtk::Lap1D::order_accuracy() const {

  return order_accuracy_;
}

mtk::Real mtk::Lap1D::mimetic_threshold() const {

  return mimetic_threshold_;
}

mtk::Real mtk::Lap1D::delta() const {

  return delta_;
}

bool mtk::Lap1D::ConstructLap1D(int order_accuracy,
                                mtk::Real mimetic_threshold) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(order_accuracy < 2, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent((order_accuracy%2) != 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(mimetic_threshold <= mtk::kZero,
                      __FILE__, __LINE__, __func__);

  if (order_accuracy >= mtk::kCriticalOrderAccuracyDiv) {
    std::cout << "WARNING: Numerical accuracy is high." << std::endl;
```

```
}

std::cout << "order_accuracy_ = " << order_accuracy << std::endl;
std::cout << "mimetic_threshold_ = " << mimetic_threshold << std::endl;
#endif

order_accuracy_ = order_accuracy;
mimetic_threshold_ = mimetic_threshold;

mtk::Grad1D grad; // Mimetic gradient.

bool info = grad.ConstructGrad1D(order_accuracy_, mimetic_threshold_);

#ifdef MTK_PERFORM_PREVENTIONS
if (!info) {
  std::cerr << "Mimetic grad could not be built." << std::endl;
  return false;
}
#endif


mtk::Div1D div; // Mimetic divergence.

info = div.ConstructDiv1D(order_accuracy_, mimetic_threshold_);

#ifdef MTK_PERFORM_PREVENTIONS
if (!info) {
  std::cerr << "Mimetic div could not be built." << std::endl;
  return false;
}
#endif


// Since these are mimetic operator, we must multiply the matrices arising
// from both the divergence and the Laplacian, in order to get the
// approximating coefficients for the Laplacian operator.

// However, we must choose a grid that implied a step size of 1, so to get
// the approximating coefficients, without being affected from the
// normalization with respect to the grid (dimensionless).

// Also, the grid must be of the minimum size to support the requested order
// of accuracy. We must please the divergence for this!

mtk::UniStgGrid1D aux(mtk::kZero,
                      (mtk::Real) 3*order_accuracy_ - 1,
                      3*order_accuracy_ - 1);

#if MTK_VERBOSE_LEVEL > 2
std::cout << "aux =" << std::endl;
std::cout << aux << std::endl;
std::cout <<"aux.delta_x() = " << aux.delta_x() << std::endl;
std::cout << std::endl;
#endif

mtk::DenseMatrix grad_m(grad.ReturnAsDenseMatrix(aux));

#if MTK_VERBOSE_LEVEL > 4
std::cout << "grad_m =" << std::endl;
std::cout << grad_m << std::endl;
#endif

mtk::DenseMatrix div_m(div.ReturnAsDenseMatrix(aux));

#if MTK_VERBOSE_LEVEL > 4
std::cout << "div_m =" << std::endl;
std::cout << div_m << std::endl;
#endif


mtk::DenseMatrix lap; // Laplacian matrix to hold to computed coefficients.

lap = mtk::BLASAdapter::RealDenseMM(div_m, grad_m);

#if MTK_VERBOSE_LEVEL > 4
std::cout << "lap =" << std::endl;
std::cout << lap << std::endl;
#endif
```

```
  // The output array will have this form:
  // 1. The first entry of the array will contain the used order kk.
  // 2. The second entry of the array will contain the collection of
  // approximating coefficients for the interior of the grid.
  // 3. The next entries will contain the collections of approximating
  // coefficients for the west boundary of the grid.

  laplacian_length_ = 1 + (2*order_accuracy_ - 1) +
    (order_accuracy_ - 1)*(2*order_accuracy_);

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "laplacian_length_ = " << laplacian_length_ << std::endl;
  std::cout << std::endl;
  #endif

  try {
    laplacian_ = new mtk::Real[laplacian_length_];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(laplacian_, mtk::kZero, sizeof(laplacian_[0])*laplacian_length_);


  laplacian_[0] = order_accuracy_;


  for (auto ii = 0; ii < 2*order_accuracy_ - 1; ++ii) {
    laplacian_[ii + 1] = lap.GetValue(1 + (order_accuracy_ - 1), ii + 1);
  }


  auto offset = 1 + (2*order_accuracy_ - 1);

  for (auto ii = 0; ii < order_accuracy_ - 1; ++ii) {
    for (auto jj = 0; jj < 2*order_accuracy_; ++jj) {
      laplacian_[offset + ii*(2*order_accuracy_) + jj] =
        lap.GetValue(1 + ii,jj);
    }
  }

  delta_ = mtk::kZero;

  return true;
}

mtk::DenseMatrix mtk::Lap1D::ReturnAsDenseMatrix(
  const UniStgGrid1D &grid) const {

  int nn{grid.num_cells_x()};  // Number of cells on the grid.

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(nn <= 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(nn < 3*order_accuracy_ - 1, __FILE__, __LINE__, __func__);
  #endif

  mtk::DenseMatrix lap(nn + 2, nn + 2); // Laplacian matrix to be returned.

  delta_ = grid.delta_x();

  mtk::Real idx{mtk::kOne/(grid.delta_x()*grid.delta_x())}; // Inverse of
 dx^2.


  auto offset = (1 + 2*order_accuracy_ - 1);

  for (auto ii = 0; ii < order_accuracy_ - 1; ++ii) {
    for (auto jj = 0; jj < 2*order_accuracy_; ++jj) {
      lap.SetValue(1 + ii,
                   jj,
                   idx*laplacian_[offset + ii*2*order_accuracy_ + jj]);
    }
  }


  offset = 1 + (order_accuracy_ - 1);

  int kk{1};
  for (auto ii = order_accuracy_; ii <= nn - (order_accuracy_ - 1); ++ii) {
    int mm{1};
```

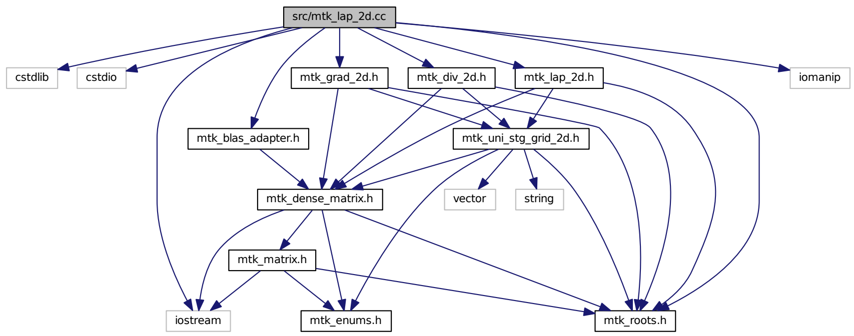
```
    for (auto jj = 0; jj < 2*order_accuracy_ - 1; ++jj) {
      lap.SetValue(ii, jj + kk, idx*laplacian_[mm]);
      mm = mm + 1;
    }
    kk = kk + 1;
  }


  offset = (1 + 2*order_accuracy_ - 1);

  auto aux = order_accuracy_ + (nn - 2*(order_accuracy_ - 1));

  auto ll = 1;
  auto rr = 1;
  for (auto ii = nn; ii > aux - 1; --ii) {
    auto cc = 0;
    for (auto jj = nn + 2 - 1; jj >= (nn + 2) - 2*order_accuracy_; --jj) {
      lap.SetValue(ii, jj, lap.GetValue(rr,cc));
      ++ll;
      ++cc;
    }
    rr++;
  }


  return lap;
}

const mtk::Real* mtk::Lap1D::data(const UniStgGrid1D &grid) const {

  mtk::DenseMatrix tmp;

  tmp = ReturnAsDenseMatrix(grid);

  return tmp.data();
}
```

17.73 src/mtk_lap_2d.cc File Reference

Includes the implementation of the class Lap2D.

#include <cstdlib>
#include <cstdio>
#include <iostream>
#include <iomanip>
#include "mtk_roots.h"
#include "mtk_blas_adapter.h"
#include "mtk_grad_2d.h"
#include "mtk_div_2d.h"
#include "mtk_lap_2d.h"

Include dependency graph for mtk_lap_2d.cc:



17.73.1 Detailed Description

This class implements a 2D Laplacian operator, constructed using the Castillo-Blomgren-Sanchez (CBS) Algorithm (CBSA).

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_lap_2d.cc.

17.74 mtk_lap_2d.cc

```

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(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#include <cstdlib>
#include <cstdio>

#include <iostream>
#include <iomanip>

#include "mtk_roots.h"
#include "mtk_blas_adapter.h"
#include "mtk_grad_2d.h"
#include "mtk_div_2d.h"
#include "mtk_lap_2d.h"

mtk::Lap2D::Lap2D(): order_accuracy_(), mimetic_threshold_() {}

mtk::Lap2D::Lap2D(const Lap2D &lap):
  order_accuracy_(lap.order_accuracy_),
  mimetic_threshold_(lap.mimetic_threshold_) {}

mtk::Lap2D::~Lap2D() {}

bool mtk::Lap2D::ConstructLap2D(const mtk::UniStgGrid2D &grid,
                                int order_accuracy,
                                mtk::Real mimetic_threshold) {

  mtk::Grad2D gg;
  mtk::Div2D dd;

  bool info{gg.ConstructGrad2D(grid, order_accuracy, mimetic_threshold)};

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!info) {
    std::cerr << "Mimetic lap could not be built." << std::endl;
    return info;
  }
  #endif

  info = dd.ConstructDiv2D(grid, order_accuracy, mimetic_threshold);

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!info) {
    std::cerr << "Mimetic div could not be built." << std::endl;
    return info;
  }
  #endif

  mtk::DenseMatrix ggm(gg.ReturnAsDenseMatrix());
  mtk::DenseMatrix ddm(dd.ReturnAsDenseMatrix());

  laplacian_ = mtk::BLASAdapter::RealDenseMM(ddm, ggm);

  return info;
}

mtk::DenseMatrix mtk::Lap2D::ReturnAsDenseMatrix() const {

  return laplacian_;
}

mtk::Real *mtk::Lap2D::data() const {

  return laplacian_.data();
}
```
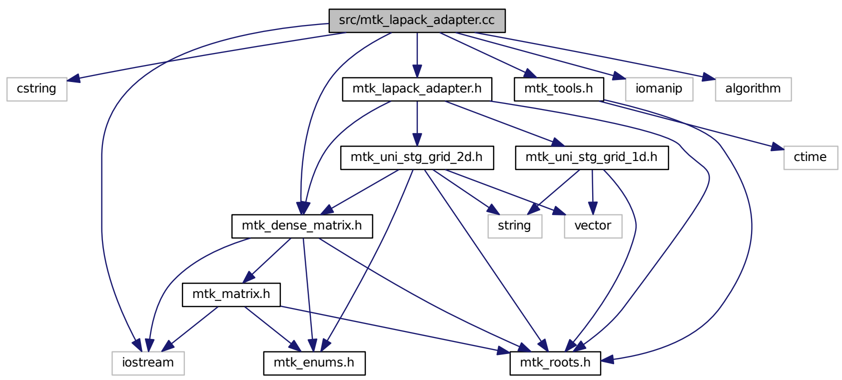

17.75 src/mtk_lapack_adapter.cc File Reference

Adapter class for the LAPACK API.

```
#include <cstring>
#include <iostream>
#include <iomanip>
#include <algorithm>
#include "mtk_tools.h"
#include "mtk_dense_matrix.h"
#include "mtk_lapack_adapter.h"
```

Include dependency graph for mtk_lapack_adapter.cc:



Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

Functions

- void mtk::sgesv_ (int ∗n, int ∗nrhs, Real ∗a, int ∗lda, int ∗ipiv, Real ∗b, int ∗ldb, int ∗info)
- void mtk::sgels_ (char ∗trans, int ∗m, int ∗n, int ∗nrhs, Real ∗a, int ∗lda, Real ∗b, int ∗ldb, Real ∗work, int ∗lwork, int ∗info)

  Single-precision GEneral matrix Least Squares solver.
- void mtk::sgeqrf_ (int ∗m, int ∗n, Real ∗a, int ∗lda, Real ∗tau, Real ∗work, int ∗lwork, int ∗info)

  Single-precision GEneral matrix QR Factorization.
- void mtk::sormqr_ (char ∗side, char ∗trans, int ∗m, int ∗n, int ∗k, Real ∗a, int ∗lda, Real ∗tau, Real ∗c, int ∗ldc, Real ∗work, int ∗lwork, int ∗info)

  Single-precision Orthogonal Matrix from QR factorization.

17.75.1 Detailed Description

This class contains a collection of static classes, that posses direct access to the underlying structure of the matrices, thus allowing programmers to exploit some of the numerical methods implemented in the LAPACK.

The **LAPACK (Linear Algebra PACKage)** is written in Fortran 90 and provides routines for solving systems of simultaneous linear equations, least-squares solutions of linear systems of equations, eigenvalue problems, and singular value problems.

See also

http://www.netlib.org/lapack/

Todo Write documentation using LaTeX.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_lapack_adapter.cc.

17.76 mtk_lapack_adapter.cc

```

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*/

#include <cstring>

#include <iostream>
#include <iomanip>
```

```

#include <algorithm>

#include "mtk_tools.h"
#include "mtk_dense_matrix.h"
#include "mtk_lapack_adapter.h"

namespace mtk {

extern "C" {

#ifdef MTK_PRECISION_DOUBLE

void dgesv_(int* n,
            int* nrhs,
            Real* a,
            int* lda,
            int* ipiv,
            Real* b,
            int* ldb,
            int* info);
#else

void sgesv_(int* n,
            int* nrhs,
            Real* a,
            int* lda,
            int* ipiv,
            Real* b,
            int* ldb,
            int* info);
#endif

#ifdef MTK_PRECISION_DOUBLE

void dgels_(char* trans,
            int* m,
            int* n,
            int* nrhs,
            Real* a,
            int* lda,
            Real* b,
            int* ldb,
            Real* work,
            int* lwork,
            int* info);
#else

void sgels_(char* trans,
            int* m,
            int* n,
            int* nrhs,
            Real* a,
            int* lda,
            Real* b,
            int* ldb,
            Real* work,
            int* lwork,
            int* info);
#endif

#ifdef MTK_PRECISION_DOUBLE

void dgeqrf_(int *m,
             int *n,
             Real *a,
             int *lda,
             Real *tau,
             Real *work,
             int *lwork,
             int *info);
#else

void sgeqrf_(int *m,
             int *n,
             Real *a,
             int *lda,
             Real *tau,
             Real *work,
             int *lwork,
             int *info);
```

```
#endif

#ifdef MTK_PRECISION_DOUBLE

void dormqr_(char *side,
             char *trans,
             int *m,
             int *n,
             int *k,
             Real *a,
             int *lda,
             Real *tau,
             Real *c,
             int *ldc,
             Real *work,
             int *lwork,
             int *info);
#else

void sormqr_(char *side,
             char *trans,
             int *m,
             int *n,
             int *k,
             Real *a,
             int *lda,
             Real *tau,
             Real *c,
             int *ldc,
             Real *work,
             int *lwork,
             int *info);
#endif
}
}

int mtk::LAPACKAdapter::SolveDenseSystem(
mtk::DenseMatrix &mm,
                                          mtk::Real *rhs) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(rhs == nullptr, __FILE__, __LINE__, __func__);
  #endif

  int *ipiv{};                 // Array for pivoting information.
  int nrhs{1};                 // Number of right-hand sides.
  int info{};                  // Status of the solution.
  int mm_rank{mm.num_rows()}; // Rank of the matrix.

  try {
    ipiv = new int[mm_rank];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(ipiv, 0, sizeof(ipiv[0])*mm_rank);

  int ldbb = mm_rank;
  int mm_ld = mm_rank;

  #ifdef MTK_PRECISION_DOUBLE
  dgesv_(&mm_rank, &nrhs, mm.data(), &mm_ld, ipiv, rhs, &ldbb, &info);
  #else
  fgesv_(&mm_rank, &nrhs, mm.data(), &mm_ld, ipiv, rhs, &ldbb, &info);
  #endif

  delete [] ipiv;

  return info;
}

int mtk::LAPACKAdapter::SolveDenseSystem(
mtk::DenseMatrix &mm,
                                          mtk::DenseMatrix &bb) {

  int nrhs{bb.num_rows()};  // Number of right-hand sides.

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(nrhs <= 0, __FILE__, __LINE__, __func__);
  #endif
```

```

  int *ipiv{};                // Array for pivoting information.
  int info{};                 // Status of the solution.
  int mm_rank{mm.num_rows()}; // Rank of the matrix.

  try {
    ipiv = new int[mm_rank];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(ipiv, 0, sizeof(ipiv[0])*mm_rank);

  int ldbb = mm_rank;
  int mm_ld = mm_rank;

  #ifdef MTK_PRECISION_DOUBLE
  dgesv_(&mm_rank, &nrhs, mm.data(), &mm_ld, ipiv, bb.data(), &ldbb, &info);
  #else
  fgesv_(&mm_rank, &nrhs, mm.data(), &mm_ld, ipiv, bb.data(), &ldbb, &info);
  #endif

  delete [] ipiv;

  // After output, the data in the matrix will be column-major ordered.

  bb.SetOrdering(mtk::COL_MAJOR);

  #if MTK_VERBOSE_LEVEL > 12
  std::cout << "bb_col_maj_ord =" << std::endl;
  std::cout << bb << std::endl;
  #endif

  bb.OrderRowMajor();

  #if MTK_VERBOSE_LEVEL > 12
  std::cout << "bb_row_maj_ord =" << std::endl;
  std::cout << bb << std::endl;
  #endif

  return info;
}

int mtk::LAPACKAdapter::SolveDenseSystem(mtk::DenseMatrix &mm,
                                          mtk::UniStgGrid1D &rhs) {

  int nrhs{1};  // Number of right-hand sides.

  int *ipiv{};                // Array for pivoting information.
  int info{};                 // Status of the solution.
  int mm_rank{mm.num_rows()}; // Rank of the matrix.

  try {
    ipiv = new int[mm_rank];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(ipiv, 0, sizeof(ipiv[0])*mm_rank);

  int ldbb = mm_rank;
  int mm_ld = mm_rank;

  mm.OrderColMajor();

  #ifdef MTK_PRECISION_DOUBLE
  dgesv_(&mm_rank, &nrhs, mm.data(), &mm_ld, ipiv,
         rhs.discrete_field(), &ldbb, &info);
  #else
  fgesv_(&mm_rank, &nrhs, mm.data(), &mm_ld, ipiv,
         rhs.discrete_field(), &ldbb, &info);
  #endif

  mm.OrderRowMajor();

  delete [] ipiv;

  return info;
```

```
}

int mtk::LAPACKAdapter::SolveDenseSystem(
mtk::DenseMatrix &mm,
                                        mtk::UniStgGrid2D &rhs) {

  int nrhs{1};  // Number of right-hand sides.

  int *ipiv{};                // Array for pivoting information.
  int info{};                 // Status of the solution.
  int mm_rank{mm.num_rows()}; // Rank of the matrix.

  try {
    ipiv = new int[mm_rank];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(ipiv, 0, sizeof(ipiv[0])*mm_rank);

  int ldbb = mm_rank;
  int mm_ld = mm_rank;

  mm.OrderColMajor();

  #ifdef MTK_PRECISION_DOUBLE
  dgesv_(&mm_rank, &nrhs, mm.data(), &mm_ld, ipiv,
         rhs.discrete_field(), &ldbb, &info);
  #else
  fgesv_(&mm_rank, &nrhs, mm.data(), &mm_ld, ipiv,
         rhs.discrete_field(), &ldbb, &info);
  #endif

  mm.OrderRowMajor();

  delete [] ipiv;

  return info;
}

mtk::DenseMatrix mtk::LAPACKAdapter::QRFactorDenseMatrix
(mtk::DenseMatrix &aa) {

  mtk::Real *work{}; // Working array.
  mtk::Real *tau{};  // Array for the Householder scalars.

  // Prepare to factorize: allocate and inquire for the value of lwork.
  try {
    work = new mtk::Real[1];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(work, mtk::kZero, sizeof(aa.data()[0])*1);

  int lwork{-1};
  int info{};

  int aa_num_cols = aa.num_cols();
  int aaT_num_rows = aa.num_cols();
  int aaT_num_cols = aa.num_rows();

  #if MTK_VERBOSE_LEVEL > 12
  std::cout << "Input matrix BEFORE QR factorization:" << std::endl;
  std::cout << aa << std::endl;
  #endif

  #ifdef MTK_PRECISION_DOUBLE
  dgeqrf_(&aaT_num_rows, &aaT_num_cols, aa.data(), &aaT_num_rows,
          tau,
          work, &lwork, &info);
  #else
  fgeqrf_(&aaT_num_rows, &aaT_num_cols, aa.data(), &aaT_num_rows,
          tau,
          work, &lwork, &info);
  #endif

  if (info == 0) {
    lwork = (int) work[0];
```

```
} else {
  std::cerr << "Could not get value for lwork on line " << __LINE__ - 5 <<
    std::endl;
  std::cerr << "Exiting..." << std::endl;
}

#if MTK_VERBOSE_LEVEL > 10
std::cout << "lwork = " << std::endl << std::setw(12) << lwork << std::endl
  << std::endl;
#endif

delete [] work;
work = nullptr;

// Once we know lwork, we can actually invoke the factorization:
try {
  work = new mtk::Real [lwork];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(work, mtk::kZero, sizeof(work[0])*lwork);

int ltau = std::min(aaT_num_rows,aaT_num_cols);

try {
  tau = new mtk::Real [ltau];
} catch (std::bad_alloc &memory_allocation_exception) {
  std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
    std::endl;
  std::cerr << memory_allocation_exception.what() << std::endl;
}
memset(tau, mtk::kZero, sizeof(0.0)*ltau);

#ifdef MTK_PRECISION_DOUBLE
dgeqrf_(&aaT_num_rows, &aaT_num_cols, aa.data(), &aaT_num_rows,
        tau, work, &lwork, &info);
#else
fgeqrf_(&aaT_num_rows, &aaT_num_cols, aa.data(), &aaT_num_rows,
        tau, work, &lwork, &info);
#endif

#ifdef MTK_PERFORM_PREVENTIONS
if (!info) {
  std::cout << "QR factorization completed!" << std::endl << std::endl;
} else {
  std::cerr << "Error solving system! info = " << info << std::endl;
  std::cerr << "Exiting..." << std::endl;
}
#endif

#if MTK_VERBOSE_LEVEL > 12
std::cout << "Input matrix AFTER QR factorization:" << std::endl;
std::cout << aa << std::endl;
#endif

// We now generate the real matrix Q with orthonormal columns. This has to
// be done separately since the actual output of dgeqrf_ (AA_) represents
// the orthogonal matrix Q as a product of min(aa_num_rows,aa_num_cols)
// elementary Householder reflectors. Notice that we must re-inquire the new
// value for lwork that is used.

bool padded{false};

bool transpose{false};

mtk::DenseMatrix QQ_(aa.num_cols(),padded,transpose);

#if MTK_VERBOSE_LEVEL > 12
std::cout << "Initialized QQ_T: " << std::endl;
std::cout << QQ_ << std::endl;
#endif

// Assemble the QQ_ matrix:
lwork = -1;

delete[] work;
work = nullptr;

try {
```

```
    work = new mtk::Real[1];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() <<
      std::endl;
  }
  memset(work, mtk::kZero, sizeof(work[0])*1);

  char side_{'L'};
  char trans_{'N'};

  int aux = QQ_.num_rows();

  #ifdef MTK_PRECISION_DOUBLE
  dormqr_(&side_, &trans_,
          &aa_num_cols, &aa_num_cols, &ltau, aa.data(), &aaT_num_rows, tau,
          QQ_.data(), &aux, work, &lwork, &info);
  #else
  formqr_(&side_, &trans_,
          &aa_num_cols, &aa_num_cols, &ltau, aa.data(), &aaT_num_rows, tau,
          QQ_.data(), &aux, work, &lwork, &info);
  #endif

  if (info == 0) {
    lwork = (int) work[0];
  } else {
    std::cerr << "Could not get lwork on line " << __LINE__ - 5 << std::endl;
    std::cerr << "Exiting..." << std::endl;
  }

  #if MTK_VERBOSE_LEVEL > 10
  std::cout << "lwork = " << std::endl << std::setw(12) << lwork <<
    std::endl << std::endl;
  #endif

  delete[] work;
  work = nullptr;

  try {
    work = new mtk::Real[lwork];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(work, mtk::kZero, sizeof(work[0])*lwork);

  #ifdef MTK_PRECISION_DOUBLE
  dormqr_(&side_, &trans_,
          &aa_num_cols, &aa_num_cols, &ltau, aa.data(), &aaT_num_rows, tau,
          QQ_.data(), &aux, work, &lwork, &info);
  #else
  formqr_(&side_, &trans_,
          &aa_num_cols, &aa_num_cols, &ltau, aa.data(), &aaT_num_rows, tau,
          QQ_.data(), &aux, work, &lwork, &info);
  #endif

  #ifdef MTK_PERFORM_PREVENTIONS
  if (!info) {
    std::cout << "Q matrix successfully assembled!" << std::endl << std::endl;
  } else {
    std::cerr << "Something went wrong solving system! info = " << info <<
      std::endl;
    std::cerr << "Exiting..." << std::endl;
  }
  #endif

  delete[] work;
  work = nullptr;

  delete[] tau;
  tau = nullptr;

  return QQ_;
}

int mtk::LAPACKAdapter::SolveRectangularDenseSystem(const
mtk::DenseMatrix &aa,
                                                    mtk::Real *ob_,
                                                    int ob_ld_) {
```

```

  // We first invoke the solver to query for the value of lwork. For this,
  // we must at least allocate enough space to allow access to WORK(1), or
  // work[0]:

  // If LWORK = -1, then a workspace query is assumed; the routine only
  // calculates the optimal size of the WORK array, returns this value as
  // the first entry of the WORK array, and no error message related to
  // LWORK is issued by XERBLA.

  mtk::Real *work{}; // Work array.

  try {
    work = new mtk::Real[1];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 <<
      std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(work, mtk::kZero, sizeof(work[0])*1);

  char trans_{'N'};
  int nrhs_{1};
  int info{0};
  int lwork{-1};

  int AA_num_rows_  = aa.num_cols();
  int AA_num_cols_  = aa.num_rows();
  int AA_ld_ = std::max(1,aa.num_cols());

  #ifdef MTK_PRECISION_DOUBLE
  dgels_(&trans_, &AA_num_rows_, &AA_num_cols_, &nrhs_, aa.data(), &AA_ld_,
         ob_, &ob_ld_,
         work, &lwork, &info);
  #else
  sgels_(&trans_, &AA_num_rows_, &AA_num_cols_, &nrhs_, aa.data(), &AA_ld_,
         ob_, &ob_ld_,
         work, &lwork, &info);
  #endif

  if (info == 0) {
    lwork = (int) work[0];
  } else {
    std::cerr << "Could not get value for lwork on line " << __LINE__ - 2 <<
      std::endl;
    std::cerr << "Exiting..." << std::endl;
    return info;
  }

  #if MTK_VERBOSE_LEVEL > 10
  std::cout << "lwork = " << std::endl << std::setw(12)<< lwork <<
    std::endl << std::endl;
  #endif

  // We then use lwork's new value to create the work array:
  delete[] work;
  work = nullptr;

  try {
    work = new mtk::Real[lwork];
  } catch (std::bad_alloc &memory_allocation_exception) {
    std::cerr << "Memory allocation exception on line " << __LINE__ - 3 << std::endl;
    std::cerr << memory_allocation_exception.what() << std::endl;
  }
  memset(work, 0.0, sizeof(work[0])*lwork);

  // We now invoke the solver again:
  #ifdef MTK_PRECISION_DOUBLE
  dgels_(&trans_, &AA_num_rows_, &AA_num_cols_, &nrhs_, aa.data(), &AA_ld_,
         ob_, &ob_ld_,
         work, &lwork, &info);
  #else
  sgels_(&trans_, &AA_num_rows_, &AA_num_cols_, &nrhs_, aa.data(), &AA_ld_,
         ob_, &ob_ld_,
         work, &lwork, &info);
  #endif

  delete [] work;
  work = nullptr;

  return info;
```

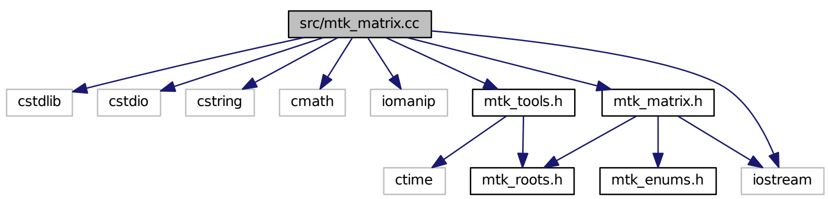
```
}
```

17.77 src/mtk_matrix.cc File Reference

Implementing the representation of a matrix in the MTK.

```
#include <cstdlib>
#include <cstdio>
#include <cstring>
#include <cmath>
#include <iomanip>
#include <iostream>
#include "mtk_tools.h"
#include "mtk_matrix.h"
```

Include dependency graph for mtk_matrix.cc:



17.77.1 Detailed Description

Implementation of the representation for the matrices implemented in the MTK.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_matrix.cc.

17.78 mtk_matrix.cc

```

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```

```
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SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#include <cstdlib>
#include <cstdio>
#include <cstring>
#include <cmath>

#include <iomanip>
#include <iostream>

#include "mtk_tools.h"
#include "mtk_matrix.h"

mtk::Matrix::Matrix():
  storage_(mtk::DENSE),
  ordering_(mtk::ROW_MAJOR),
  num_rows_(),
  num_cols_(),
  num_values_(),
  ld_(),
  num_zero_(),
  num_non_zero_(),
  num_null_(),
  num_non_null_(),
  kl_(),
  ku_(),
  bandwidth_(),
  abs_density_(),
  rel_density_(),
  abs_sparsity_(),
  rel_sparsity_() {}

mtk::Matrix::Matrix(const Matrix &in):
  storage_(in.storage_),
  ordering_(in.ordering_),
  num_rows_(in.num_rows_),
  num_cols_(in.num_cols_),
  num_values_(in.num_values_),
  ld_(in.ld_),
  num_zero_(in.num_zero_),
  num_non_zero_(in.num_non_zero_),
  num_null_(in.num_null_),
  num_non_null_(in.num_non_null_),
  kl_(in.kl_),
  ku_(in.ku_),
  bandwidth_(in.bandwidth_),
  abs_density_(in.abs_density_),
  rel_density_(in.rel_density_),
  abs_sparsity_(in.abs_sparsity_),
  rel_sparsity_(in.rel_sparsity_) {}

mtk::Matrix::~Matrix() noexcept {}

```

```
mtk::MatrixStorage mtk::Matrix::storage() const noexcept {

  return storage_;
}

mtk::MatrixOrdering mtk::Matrix::ordering() const noexcept {

  return ordering_;
}

int mtk::Matrix::num_rows() const noexcept {

  return num_rows_;
}

int mtk::Matrix::num_cols() const noexcept {

  return num_cols_;
}

int mtk::Matrix::num_values() const noexcept {

  return num_values_;
}

int mtk::Matrix::ld() const noexcept {

  return ld_;
}

int mtk::Matrix::num_zero() const noexcept {

  return num_zero_;
}

int mtk::Matrix::num_non_zero() const noexcept {

  return num_non_zero_;
}

int mtk::Matrix::num_null() const noexcept {

  return num_null_;
}

int mtk::Matrix::num_non_null() const noexcept {

  return num_non_null_;
}

int mtk::Matrix::kl() const noexcept {

  return kl_;
}

int mtk::Matrix::ku() const noexcept {

  return ku_;
}

int mtk::Matrix::bandwidth() const noexcept {

  return bandwidth_;
}

mtk::Real mtk::Matrix::rel_density() const noexcept {

  return rel_density_;
}

mtk::Real mtk::Matrix::abs_sparsity() const noexcept {

  return abs_sparsity_;
}

mtk::Real mtk::Matrix::rel_sparsity() const noexcept {

  return rel_sparsity_;
}

void mtk::Matrix::set_storage(const mtk::MatrixStorage &ss)
```

```
noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(!(ss == mtk::DENSE ||
                        ss == mtk::BANDED ||
                        ss == mtk::CRS),
                      __FILE__, __LINE__, __func__);
  #endif

  storage_ = ss;
}

void mtk::Matrix::set_ordering(const
mtk::MatrixOrdering &oo) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(!(oo == mtk::ROW_MAJOR || oo ==
mtk::COL_MAJOR),
                      __FILE__, __LINE__, __func__);
  #endif

  ordering_ = oo;

  ld_ = (ordering_ == mtk::ROW_MAJOR)?
    std::max(1,num_cols_): std::max(1,num_rows_);
}

void mtk::Matrix::set_num_rows(const int &in) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(in < 1, __FILE__, __LINE__, __func__);
  #endif

  num_rows_ = in;
  num_values_ = num_rows_*num_cols_;
  ld_ = (ordering_ == mtk::ROW_MAJOR)?
    std::max(1,num_cols_): std::max(1,num_rows_);
}

void mtk::Matrix::set_num_cols(const int &in) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(in < 1, __FILE__, __LINE__, __func__);
  #endif

  num_cols_ = in;
  num_values_ = num_rows_*num_cols_;
  ld_ = (ordering_ == mtk::ROW_MAJOR)?
    std::max(1,num_cols_): std::max(1,num_rows_);
}

void mtk::Matrix::set_num_zero(const int &in) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(in < 0, __FILE__, __LINE__, __func__);
  #endif

  num_zero_ = in;
  num_non_zero_ = num_values_ - num_zero_;

  rel_density_ = (mtk::Real) num_non_zero_/num_values_;
  rel_sparsity_ = 1.0 - rel_density_;
}

void mtk::Matrix::set_num_null(const int &in) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(in < 0, __FILE__, __LINE__, __func__);
  #endif

  num_null_ = in;
  num_non_null_ = num_values_ - num_null_;

  abs_density_ = (mtk::Real) num_non_null_/num_values_;
  abs_sparsity_ = 1.0 - abs_density_;
}

void mtk::Matrix::IncreaseNumZero() noexcept {


  num_zero_++;
```

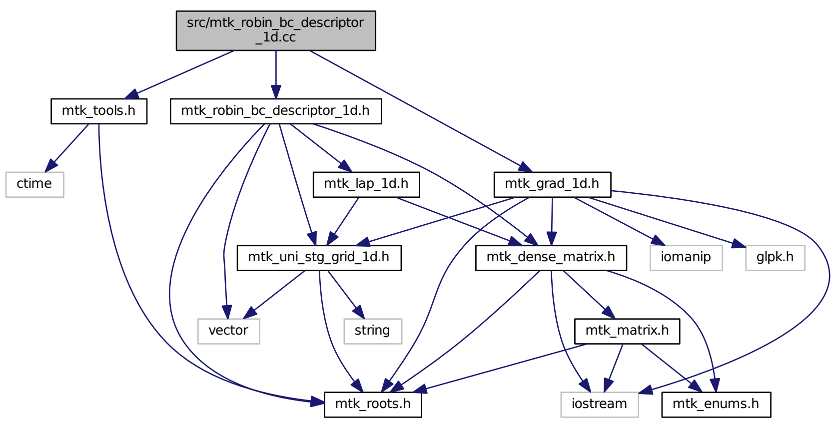
```
  num_non_zero_ = num_values_ - num_zero_;
  rel_density_ = (mtk::Real) num_non_zero_/num_values_;
  rel_sparsity_ = 1.0 - rel_density_;
}

void mtk::Matrix::IncreaseNumNull() noexcept {


  num_null_++;
  num_non_null_ = num_values_ - num_null_;
  abs_density_ = (mtk::Real) num_non_null_/num_values_;
  abs_sparsity_ = 1.0 - abs_density_;
}
```

17.79 src/mtk_robin_bc_descriptor_1d.cc File Reference

Impose Robin boundary conditions on the operators and on the grids.

```
#include "mtk_tools.h"
#include "mtk_grad_1d.h"
#include "mtk_robin_bc_descriptor_1d.h"
```

Include dependency graph for mtk_robin_bc_descriptor_1d.cc:



17.79.1 Detailed Description

This class presents an interface for the user to specify Robin boundary conditions on 1D mimetic operators and the grids they are acting on.

Def. Let $u(\mathbf{x},t) : \Omega \times [t_0,t_n] \mapsto \mathbb{R}$ be the solution to an ordinary or partial differential equation of interest. We say that u satisfies a **Robin boundary condition on** $\partial\Omega$ if and only if there exists $\beta(\mathbf{x},t) : \Omega \times [t_0,t_n] \mapsto \mathbb{R}$ so that:

$$\forall t \in [t_0,t_n] \; \forall \mathbf{x} \in \partial\Omega : \delta(\mathbf{x},t)u(\mathbf{x},t) + \eta(\mathbf{x},t)(\hat{\mathbf{n}} \cdot \nabla u) = \beta(\mathbf{x},t).$$

Intuitively, a **Robin boundary condition** is a constraint that must be satisfied by any linear combination of any scalar field u and its first normal derivative, in order for u to represent a unique solution to a given ordinary or partial differential equation of interest.

In a 1D context ($\partial\Omega = \{a,b\} \subset \mathbb{R}$), this condition can be written as follows:

$$\delta_a(a,t)u(a,t) - \eta_a(a,t)u'(a,t) = \beta_a(a,t),$$

$$\delta_b(b,t)u(b,t) + \eta_b(b,t)u'(b,t) = \beta_b(b,t).$$

Instances of this class receive information about the coefficient functions and each condition for any subset of the boundary (west and east, in 1D). These instances then handle the complexity of placing the coefficients in the differentiation matrices and the condition in the grids.

See also

http://mathworld.wolfram.com/NormalVector.html

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_robin_bc_descriptor_1d.cc.

17.80 mtk_robin_bc_descriptor_1d.cc

```

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*/

#include "mtk_tools.h"
#include "mtk_grad_1d.h"
#include "mtk_robin_bc_descriptor_1d.h"

mtk::RobinBCDescriptor1D::RobinBCDescriptor1D():
```

```
  highest_order_diff_west_(-1),
  highest_order_diff_east_(-1),
  west_condition_(nullptr),
  east_condition_(nullptr) {}

mtk::RobinBCDescriptor1D::RobinBCDescriptor1D(
    const mtk::RobinBCDescriptor1D &desc):
  highest_order_diff_west_(desc.highest_order_diff_west_),
  highest_order_diff_east_(desc.highest_order_diff_east_),
  west_condition_(desc.west_condition_),
  east_condition_(desc.east_condition_) {}

mtk::RobinBCDescriptor1D::~RobinBCDescriptor1D() noexcept {}

int mtk::RobinBCDescriptor1D::highest_order_diff_west()
const noexcept {

  return highest_order_diff_west_;
}

int mtk::RobinBCDescriptor1D::highest_order_diff_east()
const noexcept {

  return highest_order_diff_east_;
}

void mtk::RobinBCDescriptor1D::PushBackWestCoeff(
    mtk::CoefficientFunction0D cw) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(cw == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(highest_order_diff_west_ > 1,
                      __FILE__, __LINE__, __func__);
  #endif

  west_coefficients_.push_back(cw);

  highest_order_diff_west_++;
}

void mtk::RobinBCDescriptor1D::PushBackEastCoeff(
    mtk::CoefficientFunction0D ce) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(ce == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(highest_order_diff_east_ > 1,
                      __FILE__, __LINE__, __func__);
  #endif

  east_coefficients_.push_back(ce);

  highest_order_diff_east_++;
}

void mtk::RobinBCDescriptor1D::set_west_condition(
    mtk::Real (*west_condition)(const mtk::Real &tt)) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(west_condition == nullptr, __FILE__, __LINE__, __func__);
  #endif

  west_condition_ = west_condition;
}

void mtk::RobinBCDescriptor1D::set_east_condition(
    mtk::Real (*east_condition)(const mtk::Real &tt)) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(east_condition == nullptr, __FILE__, __LINE__, __func__);
  #endif

  east_condition_ = east_condition;
}

bool mtk::RobinBCDescriptor1D::ImposeOnLaplacianMatrix(
    const mtk::Lap1D &lap,
    mtk::DenseMatrix &matrix,
    const mtk::Real &time) const {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(highest_order_diff_west_ == -1,
```

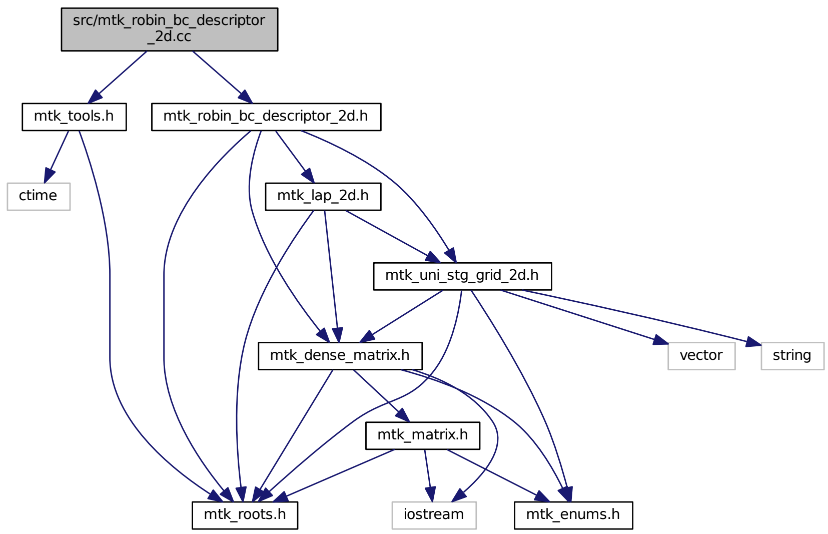
```
                      __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(highest_order_diff_east_ == -1,
                      __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(matrix.num_rows() == 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(matrix.num_cols() == 0, __FILE__, __LINE__, __func__);
  #endif

  matrix.SetValue(0, 0, (west_coefficients_[0])(time));

  matrix.SetValue(matrix.num_rows() - 1,
                  matrix.num_cols() - 1,
                  (east_coefficients_[0])(time));

  if (highest_order_diff_west_ > 0) {

    mtk::Grad1D grad;
    if (!grad.ConstructGrad1D(lap.order_accuracy(),
                              lap.mimetic_threshold())) {
      return false;
    }


    mtk::DenseMatrix coeffs(grad.mim_bndy());

    mtk::Real idx = mtk::kOne/lap.delta();

    for (int ii = 0; ii < coeffs.num_cols(); ++ii) {
      mtk::Real aux{idx*coeffs.GetValue(0, ii)};
      mtk::Real unit_normal{-mtk::kOne};
      aux *= unit_normal*(west_coefficients_[1])(time);
      matrix.SetValue(0, ii, matrix.GetValue(0, ii) + aux);
    }



    for (int ii = 0; ii < coeffs.num_cols(); ++ii) {
      mtk::Real aux{idx*coeffs.GetValue(0, ii)};
      mtk::Real unit_normal{mtk::kOne};
      aux *= -unit_normal*(east_coefficients_[1])(time);
      matrix.SetValue(matrix.num_rows() - 1,
                      matrix.num_rows() - 1 - ii,
                      matrix.GetValue(matrix.num_rows() - 1,
                                      matrix.num_rows() - 1 -ii) + aux);
    }
  }

  return true;
}

void mtk::RobinBCDescriptor1D::ImposeOnGrid(
    UniStgGrid1D &grid,
    const mtk::Real &time) const {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(grid.num_cells_x() == 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(west_condition_ == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(east_condition_ == nullptr, __FILE__, __LINE__, __func__);
  #endif

  (grid.discrete_field())[0] = west_condition_(time);
  (grid.discrete_field())[grid.num_cells_x() + 1] = east_condition_(time);
}
```

17.81 src/mtk_robin_bc_descriptor_2d.cc File Reference

Impose Robin boundary conditions on the operators and on the grids.

```
#include "mtk_tools.h"
#include "mtk_robin_bc_descriptor_2d.h"
```

Include dependency graph for mtk_robin_bc_descriptor_2d.cc:



17.81.1 Detailed Description

This class presents an interface for the user to specify Robin boundary conditions on 2D mimetic operators and the grids they are acting on.

Def. Let $u(\mathbf{x},t) : \Omega \times [t_0,t_n] \mapsto \mathbb{R}$ be the solution to an ordinary or partial differential equation of interest. We say that u satisfies a **Robin boundary condition on** $\partial\Omega$ if and only if there exists $\beta(\mathbf{x},t) : \Omega \times [t_0,t_n] \mapsto \mathbb{R}$ so that:

$$\forall t \in [t_0,t_n]\ \forall \mathbf{x} \in \partial\Omega : \delta(\mathbf{x},t)u(\mathbf{x},t) + \eta(\mathbf{x},t)(\hat{\mathbf{n}} \cdot \nabla u) = \beta(\mathbf{x},t).$$

Intuitively, a **Robin boundary condition** is a constraint that must be satisfied by any linear combination of any scalar field u and its first normal derivative, in order for u to represent a unique solution to a given ordinary or partial differential equation of interest.

Instances of this class receive information about the coefficient functions and each condition for any subset of the boundary (west, east, south and north in 2D). These instances then handle the complexity of placing the coefficients in the differentiation matrices and the conditions in the grids.

See also

`http://mathworld.wolfram.com/NormalVector.html`

Author

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Definition in file mtk_robin_bc_descriptor_2d.cc.

17.82 mtk_robin_bc_descriptor_2d.cc

```
/*
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(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#include "mtk_tools.h"

#include "mtk_robin_bc_descriptor_2d.h"

mtk::RobinBCDescriptor2D::RobinBCDescriptor2D():
  highest_order_diff_west_(-1),
  highest_order_diff_east_(-1),
  highest_order_diff_south_(-1),
  highest_order_diff_north_(-1),
  west_condition_(),
  east_condition_(),
  south_condition_(),
  north_condition_() {}

mtk::RobinBCDescriptor2D::RobinBCDescriptor2D(
    const mtk::RobinBCDescriptor2D &desc):
  highest_order_diff_west_(desc.highest_order_diff_west_),
  highest_order_diff_east_(desc.highest_order_diff_east_),
  highest_order_diff_south_(desc.highest_order_diff_south_),
  highest_order_diff_north_(desc.highest_order_diff_north_),
  west_condition_(desc.west_condition_),
  east_condition_(desc.east_condition_),
  south_condition_(desc.south_condition_),
  north_condition_(desc.north_condition_) {}

mtk::RobinBCDescriptor2D::~RobinBCDescriptor2D() noexcept {}

int mtk::RobinBCDescriptor2D::highest_order_diff_west()
const noexcept {

  return highest_order_diff_west_;
```

```
}

int mtk::RobinBCDescriptor2D::highest_order_diff_east() const noexcept {

  return highest_order_diff_east_;
}

int mtk::RobinBCDescriptor2D::highest_order_diff_south() const noexcept {

  return highest_order_diff_south_;
}

int mtk::RobinBCDescriptor2D::highest_order_diff_north() const noexcept {

  return highest_order_diff_north_;
}

void mtk::RobinBCDescriptor2D::PushBackWestCoeff(
    mtk::CoefficientFunction1D cw) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(cw == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(highest_order_diff_west_ > 1,
                      __FILE__, __LINE__, __func__);
  #endif

  west_coefficients_.push_back(cw);

  highest_order_diff_west_++;
}

void mtk::RobinBCDescriptor2D::PushBackEastCoeff(
    mtk::CoefficientFunction1D ce) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(ce == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(highest_order_diff_east_ > 1,
                      __FILE__, __LINE__, __func__);
  #endif

  east_coefficients_.push_back(ce);

  highest_order_diff_east_++;
}

void mtk::RobinBCDescriptor2D::PushBackSouthCoeff(
    mtk::CoefficientFunction1D cs) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(cs == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(highest_order_diff_south_ > 1,
                      __FILE__, __LINE__, __func__);
  #endif

  south_coefficients_.push_back(cs);

  highest_order_diff_south_++;
}

void mtk::RobinBCDescriptor2D::PushBackNorthCoeff(
    mtk::CoefficientFunction1D cn) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(cn == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(highest_order_diff_north_ > 1,
                      __FILE__, __LINE__, __func__);
  #endif

  north_coefficients_.push_back(cn);

  highest_order_diff_north_++;
}

void mtk::RobinBCDescriptor2D::set_west_condition(
    mtk::Real (*west_condition)(const mtk::Real &yy,
                                const mtk::Real &tt)) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
```

```
  mtk::Tools::Prevent(west_condition == nullptr, __FILE__, __LINE__, __func__);
  #endif

  west_condition_ = west_condition;
}

void mtk::RobinBCDescriptor2D::set_east_condition(
    mtk::Real (*east_condition)(const mtk::Real &yy,
                                const mtk::Real &tt)) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(east_condition == nullptr, __FILE__, __LINE__, __func__);
  #endif

  east_condition_ = east_condition;
}

void mtk::RobinBCDescriptor2D::set_south_condition(
    mtk::Real (*south_condition)(const mtk::Real &xx,
                                 const mtk::Real &tt)) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(south_condition == nullptr,
                      __FILE__, __LINE__, __func__);
  #endif

  south_condition_ = south_condition;
}

void mtk::RobinBCDescriptor2D::set_north_condition(
    mtk::Real (*north_condition)(const mtk::Real &xx,
                                 const mtk::Real &tt)) noexcept {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(north_condition == nullptr,
                      __FILE__, __LINE__, __func__);
  #endif

  north_condition_ = north_condition;
}

bool mtk::RobinBCDescriptor2D::ImposeOnSouthBoundaryNoSpace(
    const mtk::Lap2D &lap,
    const mtk::UniStgGrid2D &grid,
    mtk::DenseMatrix &matrix,
    const mtk::Real &time) const {


  // For the south-west corner:
  auto cc = (south_coefficients_[0])(grid.west_bndy(), time);

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "Matrix has " << matrix.num_rows() << " rows and " <<
    matrix.num_cols() << " columns." << std::endl;
  std::cout << "Setting at " << 0 << ' ' << 0 << std::endl;
  #endif

  matrix.SetValue(0, 0, cc);

  // Compute first centers per dimension.
  auto first_center_x = grid.west_bndy() + grid.delta_x()/mtk::kTwo;

  // For each entry on the diagonal (south boundary):
  for (int ii = 0; ii < grid.num_cells_x(); ++ii) {
    // Evaluate next set spatial coordinates to evaluate the coefficient.
    mtk::Real xx = first_center_x + ii*grid.delta_x();
    // Evaluate and assign the Dirichlet coefficient.
    cc = (south_coefficients_[0])(xx, time);

    #if MTK_VERBOSE_LEVEL > 2
    std::cout << "Setting at " << ii + 1 << ' ' << ii + 1 << std::endl;
    #endif

    matrix.SetValue(ii + 1, ii + 1, cc);
  }

  // For the south-east corner:
  cc = (south_coefficients_[0])(grid.east_bndy(), time);

```

```
  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "Setting at " << grid.num_cells_x() + 1 << ' ' <<
    grid.num_cells_x() + 1 << std::endl;
  #endif

  matrix.SetValue(grid.num_cells_x() + 1, grid.num_cells_x() + 1, cc);

  if (highest_order_diff_south_ > 0) {

  }

  return true;
}

bool mtk::RobinBCDescriptor2D::ImposeOnSouthBoundaryWithSpace(
    const mtk::Lap2D &lap,
    const mtk::UniStgGrid2D &grid,
    mtk::DenseMatrix &matrix,
    const mtk::Real &time) const {



  // For each entry on the diagonal:
  for (int ii = 0; ii < grid.num_cells_x() + 2; ++ii) {
    // Evaluate next set spatial coordinates to evaluate the coefficient.
    mtk::Real xx{(grid.discrete_domain_x())[ii]};
    // Evaluate and assign the Dirichlet coefficient.
    mtk::Real cc = (south_coefficients_[0])(xx, time);
    matrix.SetValue(ii, ii, cc);
  }

  if (highest_order_diff_south_ > 0) {

  }

  return true;
}

bool mtk::RobinBCDescriptor2D::ImposeOnNorthBoundaryNoSpace(
    const mtk::Lap2D &lap,
    const mtk::UniStgGrid2D &grid,
    mtk::DenseMatrix &matrix,
    const mtk::Real &time) const {

  int north_offset{(grid.num_cells_y() + 1)*(grid.num_cells_x() + 2)};


  // For the north-west corner:
  mtk::Real cc =
    (north_coefficients_[0])(grid.west_bndy(), time);

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "Matrix has " << matrix.num_rows() << " rows and " <<
    matrix.num_cols() << " columns." << std::endl;
  std::cout << "Setting at " << north_offset << ' ' << north_offset <<
    std::endl;
  #endif

  matrix.SetValue(north_offset, north_offset, cc);

  // Compute first centers per dimension.
  auto first_center_x = grid.west_bndy() + grid.delta_x()/mtk::kTwo;

  // For each entry on the diagonal (north boundary):
  for (int ii = 0; ii < grid.num_cells_x(); ++ii) {
    // Evaluate next set spatial coordinates to evaluate the coefficient.
    mtk::Real xx = first_center_x + ii*grid.delta_x();
    // Evaluate and assign the Dirichlet coefficient.
    cc = (north_coefficients_[0])(xx, time);

    #if MTK_VERBOSE_LEVEL > 2
    std::cout << "Setting at " << north_offset + ii + 1 << ' ' <<
      north_offset + ii + 1 << std::endl;
    #endif

    matrix.SetValue(north_offset + ii + 1, north_offset + ii + 1, cc);
  }

```

```
  // For the north-east corner:
  cc = (north_coefficients_[0])(grid.east_bndy(), time);

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "Setting at " << north_offset + grid.num_cells_x() + 1 <<
    ' ' << north_offset + grid.num_cells_x() + 1 << std::endl;
  #endif

  matrix.SetValue(north_offset + grid.num_cells_x() + 1,
                  north_offset + grid.num_cells_x() + 1, cc);

  if (highest_order_diff_north_ > 0) {

  }

  return true;
}

bool mtk::RobinBCDescriptor2D::ImposeOnNorthBoundaryWithSpace(
    const mtk::Lap2D &lap,
    const mtk::UniStgGrid2D &grid,
    mtk::DenseMatrix &matrix,
    const mtk::Real &time) const {


  int north_offset{(grid.num_cells_y() + 1)*(grid.num_cells_x() + 2)};

  for (int ii = 0; ii < grid.num_cells_x() + 2; ++ii) {
    mtk::Real xx{(grid.discrete_domain_x())[ii]};
    mtk::Real cc = (north_coefficients_[0])(xx, time);
    matrix.SetValue(north_offset + ii, north_offset + ii, cc);
  }

  if (highest_order_diff_north_ > 0) {

  }

  return true;
}

bool mtk::RobinBCDescriptor2D::ImposeOnWestBoundaryNoSpace(
    const mtk::Lap2D &lap,
    const mtk::UniStgGrid2D &grid,
    mtk::DenseMatrix &matrix,
    const mtk::Real &time) const {


  // For the south-west corner:
  auto cc = (west_coefficients_[0])(grid.south_bndy(), time);

  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "Matrix has " << matrix.num_rows() << " rows and " <<
    matrix.num_cols() << " columns." << std::endl;
  std::cout << "Setting at " << 0 << ' ' << 0 << std::endl;
  #endif


  mtk::Real harmonic_mean = mtk::kOne/matrix.GetValue(0, 0) + mtk::kOne/cc;
  harmonic_mean = mtk::kTwo/harmonic_mean;

  matrix.SetValue(0, 0, harmonic_mean);

  int west_offset{grid.num_cells_x() + 1};

  auto first_center_y = grid.south_bndy() + grid.delta_y()/mtk::kTwo;

  // For each west entry on the diagonal (west boundary):
  for (int ii = 0; ii < grid.num_cells_y(); ++ii) {
    // Evaluate next set spatial coordinates to evaluate the coefficient.
    mtk::Real yy = first_center_y + ii*grid.delta_y();
    // Evaluate and assign the Dirichlet coefficient.
    cc = (west_coefficients_[0])(yy, time);

    #if MTK_VERBOSE_LEVEL > 2
    std::cout << "Setting at " << west_offset + ii + 1 << ' ' <<
      west_offset + ii + 1 << std::endl;
    #endif
```

```

    matrix.SetValue(west_offset + ii + 1, west_offset + ii + 1, cc);

    west_offset += grid.num_cells_x() + 1;
  }

  // For the north-west corner:
  cc = (west_coefficients_[0])(grid.north_bndy(), time);

  west_offset += grid.num_cells_x() + 1;
  int aux{west_offset};
  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "Setting at " << aux << ' ' << aux << std::endl;
  #endif

  harmonic_mean = mtk::kOne/matrix.GetValue(aux, aux) + mtk::kOne/cc;
  harmonic_mean = mtk::kTwo/harmonic_mean;

  matrix.SetValue(aux, aux, harmonic_mean);

  if (highest_order_diff_west_ > 0) {

  }

  return true;
}

bool mtk::RobinBCDescriptor2D::ImposeOnWestBoundaryWithSpace (
    const mtk::Lap2D &lap,
    const mtk::UniStgGrid2D &grid,
    mtk::DenseMatrix &matrix,
    const mtk::Real &time) const {


  int west_offset{grid.num_cells_x() + 1};
  // For each west entry on the diagonal:
  for (int ii = 0; ii < grid.num_cells_y() + 2; ++ii) {
    // Evaluate next set spatial coordinates to evaluate the coefficient.
    mtk::Real yy{(grid.discrete_domain_y())[ii]};
    // Evaluate and assign the Dirichlet coefficient.
    mtk::Real cc = (west_coefficients_[0])(yy, time);
    matrix.SetValue(west_offset + ii, west_offset + ii, cc);
    west_offset += grid.num_cells_x() + 1;
  }

  if (highest_order_diff_west_ > 0) {

  }

  return true;
}

bool mtk::RobinBCDescriptor2D::ImposeOnEastBoundaryNoSpace (
    const mtk::Lap2D &lap,
    const mtk::UniStgGrid2D &grid,
    mtk::DenseMatrix &matrix,
    const mtk::Real &time) const {


  // For the south-east corner:
  auto cc = (east_coefficients_[0])(grid.south_bndy(), time);

  int east_offset{grid.num_cells_x() + 1};
  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "Matrix has " << matrix.num_rows() << " rows and " <<
    matrix.num_cols() << " columns." << std::endl;
  std::cout << "Setting at " << east_offset << ' ' << east_offset <<
    std::endl;
  #endif

  mtk::Real harmonic_mean =
    mtk::kOne/matrix.GetValue(east_offset,east_offset) + mtk::kOne/cc;
  harmonic_mean = mtk::kTwo/harmonic_mean;

  matrix.SetValue(east_offset, east_offset, harmonic_mean);

  auto first_center_y = grid.south_bndy() + grid.delta_y()/
```

```
      mtk::kTwo;

  // For each east entry on the diagonal (east boundary):
  for (int ii = 0; ii < grid.num_cells_y(); ++ii) {

    east_offset += grid.num_cells_x() + 1;

    // Evaluate next set spatial coordinates to evaluate the coefficient.
    mtk::Real yy = first_center_y + ii*grid.delta_y();
    // Evaluate and assign the Dirichlet coefficient.
    cc = (east_coefficients_[0])(yy, time);

    #if MTK_VERBOSE_LEVEL > 2
    std::cout << "Setting at " << east_offset + ii + 1 << ' ' <<
      east_offset + ii + 1 << std::endl;
    #endif

    matrix.SetValue(east_offset + ii + 1, east_offset + ii + 1, cc);
  }

  // For the north-east corner:
  cc = (east_coefficients_[0])(grid.north_bndy(), time);

  east_offset += grid.num_cells_x() + 1;
  east_offset += grid.num_cells_x() + 1;
  int aux{east_offset};
  #if MTK_VERBOSE_LEVEL > 2
  std::cout << "Setting at " << aux << ' ' << aux << std::endl;
  #endif

  harmonic_mean =
    mtk::kOne/matrix.GetValue(aux, aux) + mtk::kOne/cc;
  harmonic_mean = mtk::kTwo/harmonic_mean;

  matrix.SetValue(aux, aux, harmonic_mean);

  if (highest_order_diff_east_ > 0) {

  }

  return true;
}

bool mtk::RobinBCDescriptor2D::ImposeOnEastBoundaryWithSpace
(
    const mtk::Lap2D &lap,
    const mtk::UniStgGrid2D &grid,
    mtk::DenseMatrix &matrix,
    const mtk::Real &time) const {


  int east_offset{grid.num_cells_x() + 1};
  // For each west entry on the diagonal:
  for (int ii = 0; ii < grid.num_cells_y() + 2; ++ii) {
    east_offset += grid.num_cells_x() + 1;
    // Evaluate next set spatial coordinates to evaluate the coefficient.
    mtk::Real yy{(grid.discrete_domain_y())[ii]};
    // Evaluate and assign the arithmetic mean of Dirichlet coefficients.
    mtk::Real cc = (east_coefficients_[0])(yy, time);
    matrix.SetValue(east_offset + ii, east_offset + ii, cc);
  }

  if (highest_order_diff_east_ > 0) {

  }

  return true;
}

bool mtk::RobinBCDescriptor2D::ImposeOnLaplacianMatrix(
    const mtk::Lap2D &lap,
    const mtk::UniStgGrid2D &grid,
    mtk::DenseMatrix &matrix,
    const mtk::Real &time) const {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(highest_order_diff_south_ == -1,
                      __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(highest_order_diff_north_ == -1,
                      __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(highest_order_diff_west_ == -1,
```

```
                      __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(highest_order_diff_east_ == -1,
                      __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(grid.nature() != mtk::SCALAR,
                      __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(grid.num_cells_x() == 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(grid.num_cells_y() == 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(matrix.num_rows() == 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(matrix.num_cols() == 0, __FILE__, __LINE__, __func__);
  #endif


  bool success{true};

  if (!grid.Bound()) {
    success = ImposeOnSouthBoundaryNoSpace(lap, grid, matrix, time);
    #ifdef MTK_PERFORM_PREVENTIONS
    if (!success) {
      return false;
    }
    #endif
    success = ImposeOnNorthBoundaryNoSpace(lap, grid, matrix, time);
    #ifdef MTK_PERFORM_PREVENTIONS
    if (!success) {
      return false;
    }
    #endif
    success = ImposeOnWestBoundaryNoSpace(lap, grid, matrix, time);
    #ifdef MTK_PERFORM_PREVENTIONS
    if (!success) {
      return false;
    }
    #endif
    success = ImposeOnEastBoundaryNoSpace(lap, grid, matrix, time);
    #ifdef MTK_PERFORM_PREVENTIONS
    if (!success) {
      return false;
    }
    #endif
  } else {
    success = ImposeOnSouthBoundaryWithSpace(lap, grid, matrix, time);
    #ifdef MTK_PERFORM_PREVENTIONS
    if (!success) {
      return false;
    }
    #endif
    success = ImposeOnNorthBoundaryWithSpace(lap, grid, matrix, time);
    #ifdef MTK_PERFORM_PREVENTIONS
    if (!success) {
      return false;
    }
    #endif
    success = ImposeOnWestBoundaryWithSpace(lap, grid, matrix, time);
    #ifdef MTK_PERFORM_PREVENTIONS
    if (!success) {
      return false;
    }
    #endif
    success = ImposeOnEastBoundaryWithSpace(lap, grid, matrix, time);
    #ifdef MTK_PERFORM_PREVENTIONS
    if (!success) {
      return false;
    }
    #endif
  }

  return success;
}

void mtk::RobinBCDescriptor2D::ImposeOnGrid(
    mtk::UniStgGrid2D &grid,
    const mtk::Real &time) const {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(grid.num_cells_x() == 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(grid.num_cells_y() == 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(west_condition_ == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(east_condition_ == nullptr, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(south_condition_ == nullptr,
                      __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(north_condition_ == nullptr,
```

```
                      __FILE__, __LINE__, __func__);
#endif

if (grid.nature() == mtk::SCALAR) {


  mtk::Real xx = grid.west_bndy();
  (grid.discrete_field())[0] = south_condition_(xx, time);

  xx = xx + grid.delta_x()/mtk::kTwo;
  // For every point on the south boundary:
  for (int ii = 0; ii < grid.num_cells_x(); ++ii) {
    (grid.discrete_field())[ii + 1] =
      south_condition_(xx + ii*grid.delta_x(), time);
  }

  xx = grid.east_bndy();
  (grid.discrete_field())[grid.num_cells_x() + 1] =
    south_condition_(xx, time);


  xx = grid.west_bndy();
  int north_offset{(grid.num_cells_y() + 1)*(grid.num_cells_x() + 2)};
  (grid.discrete_field())[north_offset] = north_condition_(xx, time);

  xx = xx + grid.delta_x()/mtk::kTwo;
  for (int ii = 0; ii < grid.num_cells_x(); ++ii) {
    (grid.discrete_field())[north_offset + ii + 1] =
      north_condition_(xx + ii*grid.delta_x(), time);
  }

  xx = grid.east_bndy();
  (grid.discrete_field())[north_offset + grid.num_cells_x() + 1] =
      north_condition_(xx, time);


  mtk::Real yy = grid.south_bndy();
  (grid.discrete_field())[0] =
    ((grid.discrete_field())[0] + west_condition_(yy, time))/
mtk::kTwo;

  int west_offset{grid.num_cells_x() + 1 + 1};
  yy = yy + grid.delta_y()/mtk::kTwo;
  for (int ii = 0; ii < grid.num_cells_y(); ++ii) {
    #if MTK_VERBOSE_LEVEL > 2
    std::cout << "Adding on " << west_offset << "-th position." << std::endl;
    #endif
    (grid.discrete_field())[west_offset] =
      west_condition_(yy + ii*grid.delta_y(), time);
    west_offset += grid.num_cells_x() + 1 + 1;
  }

  yy = grid.north_bndy();
  north_offset = (grid.num_cells_y() + 1)*(grid.num_cells_x() + 2);
  (grid.discrete_field())[north_offset] =
    ((grid.discrete_field())[north_offset] + west_condition_(yy, time))/
      mtk::kTwo;


  yy = grid.south_bndy();
  int east_offset{grid.num_cells_x() + 1};
  (grid.discrete_field())[east_offset] =
    ((grid.discrete_field())[east_offset] + east_condition_(yy, time))/
      mtk::kTwo;

  yy = yy + grid.delta_y()/mtk::kTwo;
  for (int ii = 0; ii < grid.num_cells_y(); ++ii) {
    east_offset += grid.num_cells_x() + 1 + 1;
    #if MTK_VERBOSE_LEVEL > 2
    std::cout << "Adding on " << east_offset << "-th position." << std::endl;
    #endif
    (grid.discrete_field())[east_offset] =
      east_condition_(yy + ii*grid.delta_y(), time);
  }

  yy = grid.north_bndy();
  (grid.discrete_field())[north_offset + grid.num_cells_x() + 1] =
    ((grid.discrete_field())[north_offset + grid.num_cells_x() + 1] +
    east_condition_(yy, time))/mtk::kTwo;

} else {
```

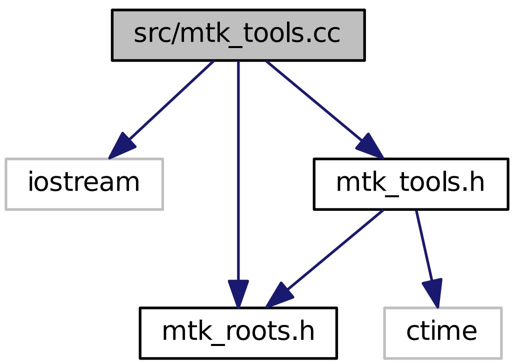
```


  }
}
```

17.83 src/mtk_tools.cc File Reference

Implements a execution tool manager class.

```
#include <iostream>
#include "mtk_roots.h"
#include "mtk_tools.h"
```

Include dependency graph for mtk_tools.cc:



17.83.1 Detailed Description

Basic tools to ensure execution correctness.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_tools.cc.

17.84 mtk_tools.cc

```

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```

```
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*/

#include <iostream>

#include "mtk_roots.h"
#include "mtk_tools.h"

void mtk::Tools::Prevent(const bool condition,
                         const char *const fname,
                         int lineno,
                         const char *const fxname) noexcept {

  if (lineno < 1) {
    std::cerr << __FILE__ << ": " << "Incorrect parameter at line " <<
    __LINE__ - 2 << " (" << __func__ << ")" << std::endl;
    exit(EXIT_FAILURE);
  }

  if (condition) {
    std::cerr << fname << ": " << "Incorrect parameter at line " <<
    lineno << " (" << fxname << ")" << std::endl;
    exit(EXIT_FAILURE);
  }
}


int mtk::Tools::test_number_;  // Used to control the correctness of the test.

mtk::Real mtk::Tools::duration_;  // Duration of the current test.

clock_t mtk::Tools::begin_time_;  // Used to time tests.

void mtk::Tools::BeginUnitTestNo(const int &nn) noexcept {

  #if MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(nn <= 0, __FILE__, __LINE__, __func__);
  #endif

  test_number_ = nn;

  std::cout << "Beginning test " << nn << "." << std::endl;
  begin_time_ = clock();
}

void mtk::Tools::EndUnitTestNo(const int &nn) noexcept {
```
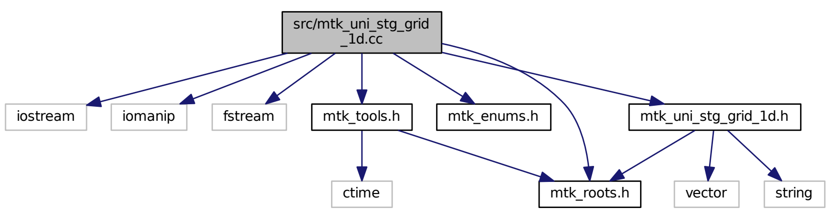

```

#if MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(test_number_ != nn, __FILE__, __LINE__, __func__);
#endif

  duration_ = mtk::Real(clock() - begin_time_)/CLOCKS_PER_SEC;
}

void mtk::Tools::Assert(const bool &condition) noexcept {

  if (condition) {
    std::cout << "Test " << test_number_ << ": PASSED in " << duration_ <<
      " s." << std::endl;
  } else {
    std::cout << "Test " << test_number_ << ": FAILED in " << duration_ <<
      " s." << std::endl;
  }
}
```

17.85 src/mtk_uni_stg_grid_1d.cc File Reference

Implementation of an 1D uniform staggered grid.

```
#include <iostream>
#include <iomanip>
#include <fstream>
#include "mtk_roots.h"
#include "mtk_enums.h"
#include "mtk_tools.h"
#include "mtk_uni_stg_grid_1d.h"
```

Include dependency graph for mtk_uni_stg_grid_1d.cc:



Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

Functions

- std::ostream & mtk::operator<< (std::ostream &stream, mtk::UniStgGrid1D &in)

17.85.1 Detailed Description

Implementation of an 1D uniform staggered grid.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_uni_stg_grid_1d.cc.

17.86 mtk_uni_stg_grid_1d.cc

```
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page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
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*/

#include <iostream>
#include <iomanip>
#include <fstream>

#include "mtk_roots.h"
#include "mtk_enums.h"
#include "mtk_tools.h"

#include "mtk_uni_stg_grid_1d.h"

namespace mtk {

std::ostream& operator <<(std::ostream &stream, mtk::UniStgGrid1D &in) {

  stream << '[' << in.west_bndy_x_ << ':' << in.num_cells_x_ << ':' <<
  in.east_bndy_x_ << "] = " << std::endl << std::endl;


  stream << "x:";
  for (unsigned int ii = 0; ii < in.discrete_domain_x_.size(); ++ii) {
    stream << std::setw(10) << in.discrete_domain_x_[ii];
```

```
  }
  stream << std::endl;


  if (in.nature_ == mtk::SCALAR) {
    stream << "u:";
  }
  else {
    stream << "v:";
  }
  for (unsigned int ii = 0; ii < in.discrete_field_.size(); ++ii) {
    stream << std::setw(10) << in.discrete_field_[ii];
  }

  stream << std::endl;

  return stream;
}
}

mtk::UniStgGrid1D::UniStgGrid1D():
    nature_(),
    discrete_domain_x_(),
    discrete_field_(),
    west_bndy_x_(),
    east_bndy_x_(),
    num_cells_x_(),
    delta_x_() {}

mtk::UniStgGrid1D::UniStgGrid1D(const UniStgGrid1D &grid):
    nature_(grid.nature_),
    west_bndy_x_(grid.west_bndy_x_),
    east_bndy_x_(grid.east_bndy_x_),
    num_cells_x_(grid.num_cells_x_),
    delta_x_(grid.delta_x_) {

    std::copy(grid.discrete_domain_x_.begin(),
              grid.discrete_domain_x_.begin() + grid.discrete_domain_x_.size(),
              discrete_domain_x_.begin());

    std::copy(grid.discrete_field_.begin(),
              grid.discrete_field_.begin() + grid.discrete_field_.size(),
              discrete_field_.begin());
}

mtk::UniStgGrid1D::UniStgGrid1D(const Real &west_bndy_x,
                                const Real &east_bndy_x,
                                const int &num_cells_x,
                                const mtk::FieldNature &nature) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(west_bndy_x < mtk::kZero, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(east_bndy_x < mtk::kZero, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(east_bndy_x <= west_bndy_x, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(num_cells_x < 0, __FILE__, __LINE__, __func__);
  #endif

  nature_ = nature;
  west_bndy_x_ = west_bndy_x;
  east_bndy_x_ = east_bndy_x;
  num_cells_x_ = num_cells_x;

  delta_x_ = (east_bndy_x - west_bndy_x)/((mtk::Real) num_cells_x);
}

mtk::UniStgGrid1D::~UniStgGrid1D() {}

mtk::Real mtk::UniStgGrid1D::west_bndy_x() const {

  return west_bndy_x_;
}

mtk::Real mtk::UniStgGrid1D::east_bndy_x() const {

  return east_bndy_x_;
}

mtk::Real mtk::UniStgGrid1D::delta_x() const {

```

```
  return delta_x_;
}

const mtk::Real *mtk::UniStgGrid1D::discrete_domain_x() const
{

  return discrete_domain_x_.data();
}

mtk::Real *mtk::UniStgGrid1D::discrete_field() {

  return discrete_field_.data();
}

int mtk::UniStgGrid1D::num_cells_x() const {

  return num_cells_x_;
}

void mtk::UniStgGrid1D::BindScalarField(
    mtk::Real (*ScalarField)(const mtk::Real &xx)) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(nature_ == mtk::VECTOR, __FILE__, __LINE__, __func__);
  #endif


  discrete_domain_x_.reserve(num_cells_x_ + 2);

  discrete_domain_x_.push_back(west_bndy_x_);
  #ifdef MTK_PRECISION_DOUBLE
  auto first_center = west_bndy_x_ + delta_x_/2.0;
  #else
  auto first_center = west_bndy_x_ + delta_x_/2.0f;
  #endif
  discrete_domain_x_.push_back(first_center);
  for (auto ii = 1; ii < num_cells_x_; ++ii) {
    discrete_domain_x_.push_back(first_center + ii*delta_x_);
  }
  discrete_domain_x_.push_back(east_bndy_x_);


  discrete_field_.reserve(num_cells_x_ + 2);

  discrete_field_.push_back(ScalarField(west_bndy_x_));

  discrete_field_.push_back(ScalarField(first_center));
  for (auto ii = 1; ii < num_cells_x_; ++ii) {
    discrete_field_.push_back(ScalarField(first_center + ii*delta_x_));
  }
  discrete_field_.push_back(ScalarField(east_bndy_x_));
}

void mtk::UniStgGrid1D::BindVectorField(
    mtk::Real (*VectorField)(mtk::Real xx)) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(nature_ == mtk::SCALAR, __FILE__, __LINE__, __func__);
  #endif


  discrete_domain_x_.reserve(num_cells_x_ + 1);

  discrete_domain_x_.push_back(west_bndy_x_);
  for (auto ii = 1; ii < num_cells_x_; ++ii) {
    discrete_domain_x_.push_back(west_bndy_x_ + ii*delta_x_);
  }
  discrete_domain_x_.push_back(east_bndy_x_);


  discrete_field_.reserve(num_cells_x_ + 1);

  discrete_field_.push_back(VectorField(west_bndy_x_));
  for (auto ii = 1; ii < num_cells_x_; ++ii) {
    discrete_field_.push_back(VectorField(west_bndy_x_ + ii*delta_x_));
  }
  discrete_field_.push_back(VectorField(east_bndy_x_));
}

bool mtk::UniStgGrid1D::WriteToFile(std::string filename,
                                    std::string space_name,
```

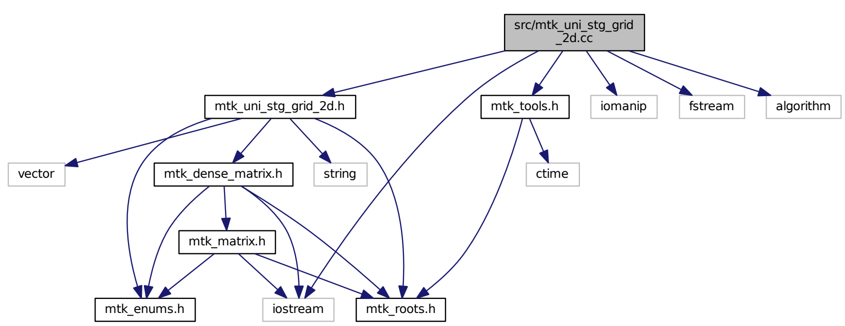
```
                                  std::string field_name) const {

  std::ofstream output_dat_file;  // Output file.

  output_dat_file.open(filename);

  if (!output_dat_file.is_open()) {
    return false;
  }

  output_dat_file << "# " << space_name <<  ' ' << field_name << std::endl;
  for (unsigned int ii = 0; ii < discrete_domain_x_.size(); ++ii) {
    output_dat_file << discrete_domain_x_[ii] << ' ' << discrete_field_[ii] <<
      std::endl;
  }

  output_dat_file.close();

  return true;
}
```

17.87 src/mtk_uni_stg_grid_2d.cc File Reference

Implementation of a 2D uniform staggered grid.

```
#include <iostream>
#include <iomanip>
#include <fstream>
#include <algorithm>
#include "mtk_tools.h"
#include "mtk_uni_stg_grid_2d.h"
```

Include dependency graph for mtk_uni_stg_grid_2d.cc:



Namespaces

- mtk

  Mimetic Methods Toolkit namespace.

Functions

- std::ostream & mtk::operator<< (std::ostream &stream, mtk::UniStgGrid2D &in)

17.87.1 Detailed Description

Implementation of a 2D uniform staggered grid.

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_uni_stg_grid_2d.cc.

17.88 mtk_uni_stg_grid_2d.cc

```

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*/

#include <iostream>
#include <iomanip>
#include <fstream>

#include <algorithm>

#include "mtk_tools.h"
#include "mtk_uni_stg_grid_2d.h"

namespace mtk {

std::ostream& operator <<(std::ostream &stream, mtk::UniStgGrid2D &in) {

  stream << '[' << in.west_bndy_ << ':' << in.num_cells_x_ << ':' <<
```

```
  in.east_bndy_ << "] x ";

  stream << '[' << in.south_bndy_ << ':' << in.num_cells_y_ << ':' <<
  in.north_bndy_ << "] = " << std::endl << std::endl;


  stream << "x:";
  for (unsigned int ii = 0; ii < in.discrete_domain_x_.size(); ++ii) {
    stream << std::setw(10) << in.discrete_domain_x_[ii];
  }
  stream << std::endl;

  stream << "y:";
  for (unsigned int ii = 0; ii < in.discrete_domain_y_.size(); ++ii) {
    stream << std::setw(10) << in.discrete_domain_y_[ii];
  }
  stream << std::endl;


  if (in.nature_ == mtk::SCALAR) {
    stream << "u:" << std::endl;
    if (in.discrete_field_.size() > 0) {
      for (int ii = 0; ii < in.num_cells_x_ + 2; ++ii) {
        for (int jj = 0; jj < in.num_cells_y_ + 2; ++jj) {
          stream << std::setw(10) << in.discrete_field_[ii*in.num_cells_y_ + jj];
        }
        stream << std::endl;
      }
    }
  } else {

    int mm{in.num_cells_x_};
    int nn{in.num_cells_y_};
    int p_offset{nn*(mm + 1) - 1};

    stream << "p(x,y):" << std::endl;
    for (int ii = 0; ii < nn; ++ii) {
      for (int jj = 0; jj < mm + 1; ++jj) {
        stream << std::setw(10) << in.discrete_field_[ii*(mm + 1) + jj];
      }
      stream << std::endl;
    }
    stream << std::endl;

    stream << "q(x,y):" << std::endl;
    for (int ii = 0; ii < nn + 1; ++ii) {
      for (int jj = 0; jj < mm; ++jj) {
        stream << std::setw(10) <<
          in.discrete_field_[p_offset + ii*mm + jj];
      }
      stream << std::endl;
    }
    stream << std::endl;
  }

  return stream;
}
}

mtk::UniStgGrid2D::UniStgGrid2D():
    discrete_domain_x_(),
    discrete_domain_y_(),
    discrete_field_(),
    nature_(),
    west_bndy_(),
    east_bndy_(),
    num_cells_x_(),
    delta_x_(),
    south_bndy_(),
    north_bndy_(),
    num_cells_y_(),
    delta_y_() {}

mtk::UniStgGrid2D::UniStgGrid2D(const UniStgGrid2D &grid):
    nature_(grid.nature_),
    west_bndy_(grid.west_bndy_),
    east_bndy_(grid.east_bndy_),
    num_cells_x_(grid.num_cells_x_),
    delta_x_(grid.delta_x_),
```

```
    south_bndy_(grid.south_bndy_),
    north_bndy_(grid.north_bndy_),
    num_cells_y_(grid.num_cells_y_),
    delta_y_(grid.delta_y_) {

    std::copy(grid.discrete_domain_x_.begin(),
              grid.discrete_domain_x_.begin() + grid.discrete_domain_x_.size(),
              discrete_domain_x_.begin());

    std::copy(grid.discrete_domain_y_.begin(),
              grid.discrete_domain_y_.begin() + grid.discrete_domain_y_.size(),
              discrete_domain_y_.begin());

    std::copy(grid.discrete_field_.begin(),
              grid.discrete_field_.begin() + grid.discrete_field_.size(),
              discrete_field_.begin());
}

mtk::UniStgGrid2D::UniStgGrid2D(const Real &west_bndy,
                                const Real &east_bndy,
                                const int &num_cells_x,
                                const Real &south_bndy,
                                const Real &north_bndy,
                                const int &num_cells_y,
                                const mtk::FieldNature &nature) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(west_bndy < mtk::kZero, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(east_bndy < mtk::kZero, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(east_bndy <= west_bndy, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(num_cells_x < 0, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(south_bndy < mtk::kZero, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(north_bndy < mtk::kZero, __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(north_bndy <= south_bndy,
                      __FILE__, __LINE__, __func__);
  mtk::Tools::Prevent(num_cells_y < 0, __FILE__, __LINE__, __func__);
  #endif

  nature_ = nature;

  west_bndy_ = west_bndy;
  east_bndy_ = east_bndy;
  num_cells_x_ = num_cells_x;

  south_bndy_ = south_bndy;
  north_bndy_ = north_bndy;
  num_cells_y_ = num_cells_y;

  delta_x_ = (east_bndy_ - west_bndy_)/((mtk::Real) num_cells_x);
  delta_y_ = (north_bndy_ - south_bndy_)/((mtk::Real) num_cells_y);
}

mtk::UniStgGrid2D::~UniStgGrid2D() {}

mtk::FieldNature mtk::UniStgGrid2D::nature() const {

  return nature_;
}

mtk::Real mtk::UniStgGrid2D::west_bndy() const {

  return west_bndy_;
}

mtk::Real mtk::UniStgGrid2D::east_bndy() const {

  return east_bndy_;
}

int mtk::UniStgGrid2D::num_cells_x() const {

  return num_cells_x_;
}

mtk::Real mtk::UniStgGrid2D::delta_x() const {

  return delta_x_;
}

```

```
const mtk::Real* mtk::UniStgGrid2D::discrete_domain_x() const
{

  return discrete_domain_x_.data();
}

mtk::Real mtk::UniStgGrid2D::south_bndy() const {

  return south_bndy_;
}

mtk::Real mtk::UniStgGrid2D::north_bndy() const {

  return north_bndy_;
}

int mtk::UniStgGrid2D::num_cells_y() const {

  return num_cells_y_;
}

mtk::Real mtk::UniStgGrid2D::delta_y() const {

  return delta_y_;
}

bool mtk::UniStgGrid2D::Bound() const {

  return discrete_field_.size() != 0;
}

const mtk::Real* mtk::UniStgGrid2D::discrete_domain_y() const
{

  return discrete_domain_y_.data();
}

mtk::Real* mtk::UniStgGrid2D::discrete_field() {

  return discrete_field_.data();
}

int mtk::UniStgGrid2D::Size() const {

  return discrete_field_.size();
}

void mtk::UniStgGrid2D::BindScalarField(
    Real (*ScalarField)(const Real &xx, const Real &yy)) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(nature_ != mtk::SCALAR, __FILE__, __LINE__, __func__);
  #endif


  discrete_domain_x_.reserve(num_cells_x_ + 2);

  discrete_domain_x_.push_back(west_bndy_);
  #ifdef MTK_PRECISION_DOUBLE
  auto first_center = west_bndy_ + delta_x_/2.0;
  #else
  auto first_center = west_bndy_ + delta_x_/2.0f;
  #endif
  discrete_domain_x_.push_back(first_center);
  for (auto ii = 1; ii < num_cells_x_; ++ii) {
    discrete_domain_x_.push_back(first_center + ii*delta_x_);
  }
  discrete_domain_x_.push_back(east_bndy_);


  discrete_domain_y_.reserve(num_cells_y_ + 2);

  discrete_domain_y_.push_back(south_bndy_);
  #ifdef MTK_PRECISION_DOUBLE
  first_center = south_bndy_ + delta_x_/2.0;
  #else
  first_center = south_bndy_ + delta_x_/2.0f;
  #endif
  discrete_domain_y_.push_back(first_center);
  for (auto ii = 1; ii < num_cells_y_; ++ii) {
    discrete_domain_y_.push_back(first_center + ii*delta_y_);
```

```
  }
  discrete_domain_y_.push_back(north_bndy_);


  discrete_field_.reserve((num_cells_x_ + 2)*(num_cells_y_ + 2));

  for (int ii = 0; ii < num_cells_y_ + 2; ++ii) {
    for (int jj = 0; jj < num_cells_x_ + 2; ++jj) {
      #if MTK_VERBOSE_LEVEL > 6
      std::cout << "Pushing value for x = " << discrete_domain_x_[jj] <<
        " y = " << discrete_domain_y_[ii] << std::endl;
      #endif
      discrete_field_.push_back(ScalarField(discrete_domain_x_[jj],
                                            discrete_domain_y_[ii]));
    }
  }
}

void mtk::UniStgGrid2D::BindVectorFieldPComponent(
  mtk::Real (*VectorField)(const mtk::Real &xx, const
mtk::Real &yy)) {

  int mm{num_cells_x_};
  int nn{num_cells_y_};

  int total{nn*(mm + 1) + mm*(nn + 1)};

  #ifdef MTK_PRECISION_DOUBLE
  double half_delta_x{delta_x_/2.0};
  double half_delta_y{delta_y_/2.0};
  #else
  float half_delta_x{delta_x_/2.0f};
  float half_delta_y{delta_y_/2.0f};
  #endif


  // We need every data point of the discrete domain; i.e. we need all the
  // nodes and all the centers. There are mm centers for the x direction, and
  // nn centers for the y direction. Since there is one node per center, that
  // amounts to 2*mm. If we finally consider the final boundary node, it
  // amounts to a total of 2*mm + 1 for the x direction. Analogously, for the
  // y direction, this amounts to 2*nn + 1.

  discrete_domain_x_.reserve(2*mm + 1);

  discrete_domain_x_.push_back(west_bndy_);
  for (int ii = 1; ii < (2*mm + 1); ++ii) {
    discrete_domain_x_.push_back(west_bndy_ + ii*half_delta_x);
  }


  discrete_domain_y_.reserve(2*nn + 1);

  discrete_domain_y_.push_back(south_bndy_);
  for (int ii = 1; ii < (2*nn + 1); ++ii) {
    discrete_domain_y_.push_back(south_bndy_ + ii*half_delta_y);
  }


  discrete_field_.reserve(total);

  // For each y-center.
  for (int ii = 1; ii < 2*nn + 1; ii += 2) {

    // Bind all of the x-nodes for this y-center.
    for (int jj = 0; jj < 2*mm + 1; jj += 2) {
      discrete_field_.push_back(VectorField(discrete_domain_x_[jj],
                                            discrete_domain_y_[ii]));

      #if MTK_VERBOSE_LEVEL > 6
      std::cout << "Binding v at x = " << discrete_domain_x_[jj] << " y = " <<
        discrete_domain_y_[ii] << " = " <<
        VectorField(discrete_domain_x_[jj],discrete_domain_y_[ii]) << std::endl;
      #endif
    }
  }
  #if MTK_VERBOSE_LEVEL > 6
  std::cout << std::endl;
  #endif
}

```

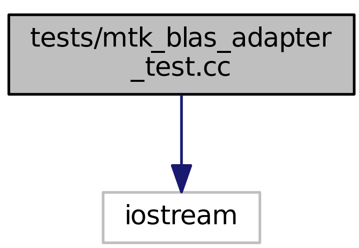
```
void mtk::UniStgGrid2D::BindVectorFieldQComponent(
  mtk::Real (*VectorField)(const mtk::Real &xx, const mtk::Real &yy)) {

  int mm{num_cells_x_};
  int nn{num_cells_y_};


  // For each y-node.
  for (int ii = 0; ii < 2*nn + 1; ii += 2) {

    // Bind all of the x-center for this y-node.
    for (int jj = 1; jj < 2*mm + 1; jj += 2) {
      discrete_field_.push_back(VectorField(discrete_domain_x_[jj],
                                            discrete_domain_y_[ii]));

      #if MTK_VERBOSE_LEVEL > 6
      std::cout << "Binding v at x = " << discrete_domain_x_[jj] << " y = " <<
        discrete_domain_y_[ii] << " = " <<
        VectorField(discrete_domain_x_[jj],discrete_domain_y_[ii]) << std::endl;
      #endif
    }
  }
  #if MTK_VERBOSE_LEVEL > 6
  std::cout << std::endl;
  #endif
}

void mtk::UniStgGrid2D::BindVectorField(
  Real (*VectorFieldPComponent)(const Real &xx, const Real &yy),
  Real (*VectorFieldQComponent)(const Real &xx, const Real &yy)) {

  #ifdef MTK_PERFORM_PREVENTIONS
  mtk::Tools::Prevent(nature_ != mtk::VECTOR, __FILE__, __LINE__, __func__);
  #endif

  BindVectorFieldPComponent(VectorFieldPComponent);
  BindVectorFieldQComponent(VectorFieldQComponent);
}

bool mtk::UniStgGrid2D::WriteToFile(std::string filename,
                                    std::string space_name_x,
                                    std::string space_name_y,
                                    std::string field_name) const {

  std::ofstream output_dat_file;  // Output file.

  output_dat_file.open(filename);

  if (!output_dat_file.is_open()) {
    return false;
  }

  if (nature_ == mtk::SCALAR) {
    output_dat_file << "# " << space_name_x <<  ' ' << space_name_y << ' ' <<
      field_name << std::endl;

    int idx{};
    for (unsigned int ii = 0; ii < discrete_domain_y_.size(); ++ii) {
      for (unsigned int jj = 0; jj < discrete_domain_x_.size(); ++jj) {
        output_dat_file << discrete_domain_x_[jj] << ' ' <<
                           discrete_domain_y_[ii] << ' ' <<
                           discrete_field_[idx] <<
                          std::endl;
        idx++;
      }
      output_dat_file << std::endl;
    }
  } else {
    output_dat_file << "# " << space_name_x <<  ' ' << space_name_y << ' ' <<
      field_name << std::endl;

    output_dat_file << "# Horizontal component:" << std::endl;

    int mm{num_cells_x_};
    int nn{num_cells_y_};


    // For each y-center.
    int idx{};
    for (int ii = 1; ii < 2*nn + 1; ii += 2) {
```

```
        // Bind all of the x-nodes for this y-center.
        for (int jj = 0; jj < 2*mm + 1; jj += 2) {

          output_dat_file << discrete_domain_x_[jj] << ' ' <<
            discrete_domain_y_[ii] << ' ' << discrete_field_[idx] << ' ' <<
            mtk::kZero << std::endl;

          ++idx;
        }
      }

      int p_offset{nn*(mm + 1) - 1};
      idx = 0;
      output_dat_file << "# Vertical component:" << std::endl;
      // For each y-node.
      for (int ii = 0; ii < 2*nn + 1; ii += 2) {
        // Bind all of the x-center for this y-node.
        for (int jj = 1; jj < 2*mm + 1; jj += 2) {

          output_dat_file << discrete_domain_x_[jj] << ' ' <<
            discrete_domain_y_[ii] << ' ' << mtk::kZero << ' ' <<
            discrete_field_[p_offset + idx] << std::endl;

          ++idx;
        }
      }
    }

    output_dat_file.close();

    return true;
}
```

17.89 tests/mtk_blas_adapter_test.cc File Reference

Test file for the mtk::BLASAdapter class.

#include <iostream>
Include dependency graph for mtk_blas_adapter_test.cc:



Functions

- int main ()

17.89.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_blas_adapter_test.cc.

17.89.2 Function Documentation

17.89.2.1 int main ( )

Definition at line 109 of file mtk_blas_adapter_test.cc.

17.90 mtk_blas_adapter_test.cc

```
00001
00008 /*
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00016 and a copy of the modified files should be reported once modifications are
00017 completed, unless these modifications are made through the project's GitHub
00018 page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
00019 should be developed and included in any deliverable.
00020
00021 2. Redistributions of source code must be done through direct
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00050 (INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
00051 SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
00052 */
00053
00054 #if __cplusplus == 201103L
00055
00056 #include <iostream>
00057
00058 #include "mtk.h"
00059
00060 void TestRealDenseMM() {
00061
00062   mtk::Tools::BeginUnitTestNo(1);
00063
```
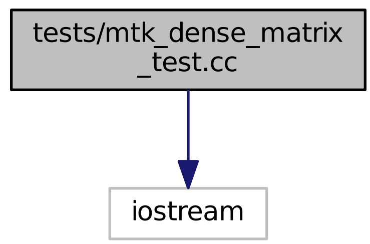

```
  int rr = 2;
  int cc = 3;

  mtk::DenseMatrix aa(rr,cc);

  aa.SetValue(0,0,1.0);
  aa.SetValue(0,1,2.0);
  aa.SetValue(0,2,3.0);
  aa.SetValue(1,0,4.0);
  aa.SetValue(1,1,5.0);
  aa.SetValue(1,2,6.0);

  mtk::DenseMatrix bb(cc,rr);

  bb.SetValue(0,0,7.0);
  bb.SetValue(0,1,8.0);
  bb.SetValue(1,0,9.0);
  bb.SetValue(1,1,10.0);
  bb.SetValue(2,0,11.0);
  bb.SetValue(2,1,12.0);

  mtk::DenseMatrix pp = mtk::BLASAdapter::RealDenseMM(aa,bb);

  mtk::DenseMatrix ff(rr,rr);

  ff.SetValue(0,0,58.0);
  ff.SetValue(0,1,64.00);
  ff.SetValue(1,0,139.0);
  ff.SetValue(1,1,154.0);

  mtk::Tools::EndUnitTestNo(1);
  mtk::Tools::Assert(pp == ff);
}

int main () {

  std::cout << "Testing mtk::BLASAdapter class." << std::endl;

  TestRealDenseMM();
}

#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

17.91 tests/mtk_dense_matrix_test.cc File Reference

Test file for the mtk::DenseMatrix class.

```
#include <iostream>
```

Include dependency graph for mtk_dense_matrix_test.cc:



Functions

- int main ()

17.91.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_dense_matrix_test.cc.

17.91.2 Function Documentation

17.91.2.1 int main ( )

Definition at line 330 of file mtk_dense_matrix_test.cc.

17.92 mtk_dense_matrix_test.cc

```
00001
00008 /*
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00016 and a copy of the modified files should be reported once modifications are
00017 completed, unless these modifications are made through the project's GitHub
00018 page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
00019 should be developed and included in any deliverable.
00020
00021 2. Redistributions of source code must be done through direct
00022 downloads from the project's GitHub page: http://www.csrc.sdsu.edu/mtk
00023
```

```
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SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#if __cplusplus == 201103L

#include <iostream>
#include <ctime>

#include "mtk.h"

void TestDefaultConstructor() {

  mtk::Tools::BeginUnitTestNo(1);

  mtk::DenseMatrix m1;

  mtk::Tools::EndUnitTestNo(1);
  mtk::Tools::Assert(m1.data() == nullptr);
}

void TestConstructorWithNumRowsNumCols() {

  mtk::Tools::BeginUnitTestNo(2);

  int rr = 4;
  int cc = 7;

  mtk::DenseMatrix m2(rr,cc);

  mtk::Tools::EndUnitTestNo(2);

  bool assertion =
    m2.data() != nullptr && m2.num_rows() == rr && m2.num_cols() == cc;

  mtk::Tools::Assert(assertion);
}

void TestConstructAsIdentity() {

  mtk::Tools::BeginUnitTestNo(3);

  int rank = 5;
  bool padded = true;
  bool transpose = false;

  mtk::DenseMatrix m3(rank,padded,transpose);

  mtk::DenseMatrix rr(rank + 2,rank);

  for (int ii = 0; ii < rank; ++ii) {
    rr.SetValue(ii + 1, ii, mtk::kOne);
  }

  mtk::Tools::EndUnitTestNo(3);
```

```
  mtk::Tools::Assert(m3 == rr);
}

  void TestConstructAsVandermonde() {

  mtk::Tools::BeginUnitTestNo(4);

  int rank = 5;
  bool padded = false;
  bool transpose = false;

  mtk::DenseMatrix m4(rank,padded,transpose);

  mtk::DenseMatrix rr(rank,rank);

  for (int ii = 0; ii < rank; ++ii) {
    rr.SetValue(ii, ii, mtk::kOne);
  }

  mtk::Tools::EndUnitTestNo(4);
  mtk::Tools::Assert(m4 == rr);
}

void TestSetValueGetValue() {

  mtk::Tools::BeginUnitTestNo(5);

  int rr = 4;
  int cc = 7;

  mtk::DenseMatrix m5(rr,cc);

  for (auto ii = 0; ii < rr; ++ii) {
    for (auto jj = 0; jj < cc; ++jj) {
      m5.SetValue(ii,jj,(mtk::Real) ii + jj);
    }
  }

  mtk::Real *vals = m5.data();

  bool assertion{true};

  for (auto ii = 0; ii < rr && assertion; ++ii) {
    for (auto jj = 0; jj < cc  && assertion; ++jj) {
      assertion = assertion && m5.GetValue(ii,jj) == vals[ii*cc + jj];
    }
  }

  mtk::Tools::EndUnitTestNo(5);
  mtk::Tools::Assert(assertion);
}

void TestConstructAsVandermondeTranspose() {

  mtk::Tools::BeginUnitTestNo(6);

  bool transpose = false;
  int generator_length = 3;
  int progression_length = 4;

  mtk::Real generator[] = {-0.5, 0.5, 1.5};

  mtk::DenseMatrix m6(generator,generator_length,progression_length,transpose);

  transpose = true;

  mtk::DenseMatrix m7(generator,generator_length,progression_length,transpose);
  mtk::DenseMatrix rr(progression_length, generator_length);

  rr.SetValue(0, 0, 1.0);
  rr.SetValue(0, 1, 1.0);
  rr.SetValue(0, 2, 1.0);

  rr.SetValue(1, 0, -0.5);
  rr.SetValue(1, 1, 0.5);
  rr.SetValue(1, 2, 1.5);

  rr.SetValue(2, 0, 0.25);
  rr.SetValue(2, 1, 0.25);
  rr.SetValue(2, 2, 2.25);

```

```
  rr.SetValue(3, 0, -0.125);
  rr.SetValue(3, 1, 0.125);
  rr.SetValue(3, 2, 3.375);

  mtk::Tools::EndUnitTestNo(6);
  mtk::Tools::Assert(m7 == rr);
}

void TestKron() {

  mtk::Tools::BeginUnitTestNo(7);

  bool padded = false;
  bool transpose = false;
  int lots_of_rows = 2;
  int lots_of_cols = 5;
  mtk::DenseMatrix m8(lots_of_rows,padded,transpose);

  mtk::DenseMatrix m9(lots_of_rows,lots_of_cols);

  for (auto ii = 0; ii < lots_of_rows; ++ii) {
    for (auto jj = 0; jj < lots_of_cols; ++jj) {
      m9.SetValue(ii,jj,(mtk::Real) ii*lots_of_cols + jj + 1);
    }
  }

  mtk::DenseMatrix m10 = mtk::DenseMatrix::Kron(m8,m9);

  mtk::DenseMatrix rr(lots_of_rows*lots_of_rows, lots_of_rows*lots_of_cols);

  rr.SetValue(0,0,1.0);
  rr.SetValue(0,1,2.0);
  rr.SetValue(0,2,3.0);
  rr.SetValue(0,3,4.0);
  rr.SetValue(0,4,5.0);
  rr.SetValue(0,5,0.0);
  rr.SetValue(0,6,0.0);
  rr.SetValue(0,7,0.0);
  rr.SetValue(0,8,0.0);
  rr.SetValue(0,9,0.0);

  rr.SetValue(1,0,6.0);
  rr.SetValue(1,1,7.0);
  rr.SetValue(1,2,8.0);
  rr.SetValue(1,3,9.0);
  rr.SetValue(1,4,10.0);
  rr.SetValue(1,5,0.0);
  rr.SetValue(1,6,0.0);
  rr.SetValue(1,7,0.0);
  rr.SetValue(1,8,0.0);
  rr.SetValue(1,9,0.0);

  rr.SetValue(2,0,0.0);
  rr.SetValue(2,1,0.0);
  rr.SetValue(2,2,0.0);
  rr.SetValue(2,3,0.0);
  rr.SetValue(2,4,0.0);
  rr.SetValue(2,5,1.0);
  rr.SetValue(2,6,2.0);
  rr.SetValue(2,7,3.0);
  rr.SetValue(2,8,4.0);
  rr.SetValue(2,9,5.0);

  rr.SetValue(3,0,0.0);
  rr.SetValue(3,1,0.0);
  rr.SetValue(3,2,0.0);
  rr.SetValue(3,3,0.0);
  rr.SetValue(3,4,0.0);
  rr.SetValue(3,5,6.0);
  rr.SetValue(3,6,7.0);
  rr.SetValue(3,7,8.0);
  rr.SetValue(3,8,9.0);
  rr.SetValue(3,9,10.0);

  mtk::Tools::EndUnitTestNo(7);
  mtk::Tools::Assert(m10 == rr);
}

void TestConstructWithNumRowsNumColsAssignmentOperator() {

  mtk::Tools::BeginUnitTestNo(8);
```

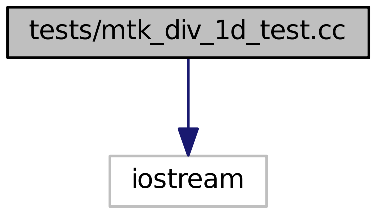
```
  int lots_of_rows = 4;
  int lots_of_cols = 3;
  mtk::DenseMatrix m11(lots_of_rows,lots_of_cols);

  for (auto ii = 0; ii < lots_of_rows; ++ii) {
    for (auto jj = 0; jj < lots_of_cols; ++jj) {
      m11.SetValue(ii,jj,(mtk::Real) ii*lots_of_cols + jj + 1);
    }
  }

  m11.Transpose();

  mtk::DenseMatrix m12;

  m12 = m11;

  mtk::Tools::EndUnitTestNo(8);
  mtk::Tools::Assert(m11 == m12);
}

void TestConstructAsVandermondeTransposeAssignmentOperator() {

  mtk::Tools::BeginUnitTestNo(9);

  bool transpose = false;
  int gg_l = 3;
  int progression_length = 4;
  mtk::Real gg[] = {-0.5, 0.5, 1.5};

  mtk::DenseMatrix m13(gg, gg_l ,progression_length, transpose);

  mtk::DenseMatrix m14;

  m14 = m13;

  m13.Transpose();

  m14 = m13;

  mtk::Tools::EndUnitTestNo(9);
  mtk::Tools::Assert(m13 == m14);
}

int main () {

  std::cout << "Testing mtk::DenseMatrix class." << std::endl;

  TestDefaultConstructor();
  TestConstructorWithNumRowsNumCols();
  TestConstructAsIdentity();
  TestConstructAsVandermonde();
  TestSetValueGetValue();
  TestConstructAsVandermondeTranspose();
  TestKron();
  TestConstructWithNumRowsNumColsAssignmentOperator();
  TestConstructAsVandermondeTransposeAssignmentOperator();
}

#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

17.93 tests/mtk_div_1d_test.cc File Reference

Testing the mimetic 1D divergence, constructed with the CBS algorithm.

```
#include <iostream>
```

Include dependency graph for mtk_div_1d_test.cc:



Functions

- int main ()

17.93.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_div_1d_test.cc.

17.93.2 Function Documentation

17.93.2.1 int main ( )

Definition at line 288 of file mtk_div_1d_test.cc.

17.94 mtk_div_1d_test.cc

```
00001
00008 /*
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00010 University. All rights reserved.
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00016 and a copy of the modified files should be reported once modifications are
00017 completed, unless these modifications are made through the project's GitHub
00018 page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
00019 should be developed and included in any deliverable.
00020
00021 2. Redistributions of source code must be done through direct
00022 downloads from the project's GitHub page: http://www.csrc.sdsu.edu/mtk
00023
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ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT
(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#if __cplusplus == 201103L

#include <iostream>

#include "mtk.h"

void TestDefaultConstructorFactoryMethodDefault() {

  mtk::Tools::BeginUnitTestNo(1);

  mtk::Div1D div2;

  bool assertion = div2.ConstructDiv1D();

  if (!assertion) {
    std::cerr << "Mimetic div (2nd order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(1);
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodFourthOrder() {

  mtk::Tools::BeginUnitTestNo(2);

  mtk::Div1D div4;

  bool assertion = div4.ConstructDiv1D(4);

  if (!assertion) {
    std::cerr << "Mimetic div (4th order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(2);
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodSixthOrder() {

  mtk::Tools::BeginUnitTestNo(3);

  mtk::Div1D div6;

  bool assertion = div6.ConstructDiv1D(6);

  if (!assertion) {
    std::cerr << "Mimetic div (6th order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(3);
  mtk::Tools::Assert(assertion);
```

```
}

void TestDefaultConstructorFactoryMethodEightOrderDefThreshold() {

  mtk::Tools::BeginUnitTestNo(4);

  mtk::Div1D div8;

  bool assertion = div8.ConstructDiv1D(8);

  if (!assertion) {
    std::cerr << "Mimetic div (8th order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(4);
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodTenthOrderDefThreshold() {

  mtk::Tools::BeginUnitTestNo(5);

  mtk::Div1D div10;

  bool assertion = div10.ConstructDiv1D(10);

  if (!assertion) {
    std::cerr << "Mimetic div (10th order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(5);
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodTwelfthOrderDefThreshold() {

  mtk::Tools::BeginUnitTestNo(6);

  mtk::Div1D div12;

  bool assertion = div12.ConstructDiv1D(12);

  if (!assertion) {
    std::cerr << "Mimetic div (12th order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(6);
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodFourteenthOrderDefThreshold() {

  mtk::Tools::BeginUnitTestNo(7);

  mtk::Div1D div14;

  bool assertion = div14.ConstructDiv1D(14);

  if (!assertion) {
    std::cerr << "Mimetic div (14th order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(7);
  mtk::Tools::Assert(assertion);
}

void TestSecondOrderReturnAsDenseMatrixWithGrid() {

  mtk::Tools::BeginUnitTestNo(8);

  mtk::Div1D div2;

  bool assertion = div2.ConstructDiv1D();

  if (!assertion) {
    std::cerr << "Mimetic div (2nd order) could not be built." << std::endl;
  }

  mtk::UniStgGrid1D grid(0.0, 1.0, 5);

  mtk::DenseMatrix div2m(div2.ReturnAsDenseMatrix(grid));
```

```
  int rr{7};
  int cc{6};

  mtk::DenseMatrix ref(rr, cc);

  // Row 2.
  ref.SetValue(1,0,-5.0);
  ref.SetValue(1,1,5.0);
  ref.SetValue(1,2,0.0);
  ref.SetValue(1,3,0.0);
  ref.SetValue(1,4,0.0);
  ref.SetValue(1,5,0.0);
  ref.SetValue(1,6,0.0);

  // Row 3.
  ref.SetValue(2,0,0.0);
  ref.SetValue(2,1,-5.0);
  ref.SetValue(2,2,5.0);
  ref.SetValue(2,3,0.0);
  ref.SetValue(2,4,0.0);
  ref.SetValue(2,5,0.0);
  ref.SetValue(2,6,0.0);

  // Row 4.
  ref.SetValue(3,0,0.0);
  ref.SetValue(3,1,0.0);
  ref.SetValue(3,2,-5.0);
  ref.SetValue(3,3,5.0);
  ref.SetValue(3,4,0.0);
  ref.SetValue(3,5,0.0);
  ref.SetValue(3,6,0.0);

  // Row 5.
  ref.SetValue(4,0,0.0);
  ref.SetValue(4,1,0.0);
  ref.SetValue(4,2,0.0);
  ref.SetValue(4,3,-5.0);
  ref.SetValue(4,4,5.0);
  ref.SetValue(4,5,0.0);
  ref.SetValue(4,6,0.0);

  // Row 6.
  ref.SetValue(5,0,0.0);
  ref.SetValue(5,1,0.0);
  ref.SetValue(5,2,0.0);
  ref.SetValue(5,3,0.0);
  ref.SetValue(5,4,-5.0);
  ref.SetValue(5,5,5.0);
  ref.SetValue(5,6,0.0);

  assertion = assertion && (div2m == ref);

  mtk::Tools::EndUnitTestNo(8);
  mtk::Tools::Assert(assertion);
}

void TestFourthOrderReturnAsDenseMatrixWithGrid() {

  mtk::Tools::BeginUnitTestNo(9);

  mtk::Div1D div4;

  bool assertion = div4.ConstructDiv1D(4);

  if (!assertion) {
    std::cerr << "Mimetic div (4th order) could not be built." << std::endl;
  }

  std::cout << div4 << std::endl;

  mtk::UniStgGrid1D grid(0.0, 1.0, 11);

  std::cout << grid << std::endl;

  mtk::DenseMatrix div4m(div4.ReturnAsDenseMatrix(grid));

  std::cout << div4m << std::endl;

  mtk::Tools::EndUnitTestNo(9);
}
```

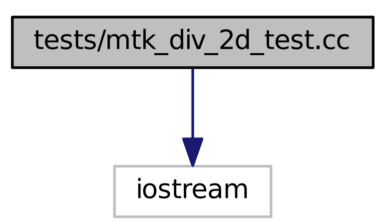
```
int main () {

  std::cout << "Testing mtk::Div1D class." << std::endl;

  TestDefaultConstructorFactoryMethodDefault();
  TestDefaultConstructorFactoryMethodFourthOrder();
  TestDefaultConstructorFactoryMethodSixthOrder();
  TestDefaultConstructorFactoryMethodEightOrderDefThreshold();
  TestDefaultConstructorFactoryMethodTenthOrderDefThreshold();
  TestDefaultConstructorFactoryMethodTwelfthOrderDefThreshold();
  TestDefaultConstructorFactoryMethodFourteenthOrderDefThreshold();
  TestSecondOrderReturnAsDenseMatrixWithGrid();
  TestFourthOrderReturnAsDenseMatrixWithGrid();
}

#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

17.95 tests/mtk_div_2d_test.cc File Reference

Test file for the mtk::Div2D class.

`#include <iostream>`

Include dependency graph for mtk_div_2d_test.cc:



Functions

- int main ()

17.95.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_div_2d_test.cc.

17.95.2 Function Documentation

17.95.2.1 int main ( )

Definition at line 139 of file mtk_div_2d_test.cc.

17.96 mtk_div_2d_test.cc

```
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ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT
(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#if __cplusplus == 201103L

#include <cmath>
#include <ctime>

#include <iostream>

#include "mtk.h"

void TestDefaultConstructorFactory() {

  mtk::Tools::BeginUnitTestNo(1);

  mtk::Div2D dd;

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
  mtk::Real cc = 0.0;
  mtk::Real ee = 1.0;

```
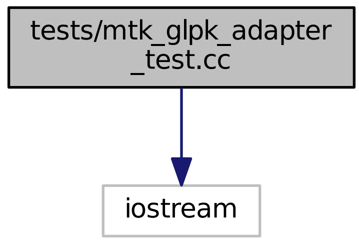

```
  int nn = 5;
  int mm = 5;

  mtk::UniStgGrid2D ddg(aa, bb, nn, cc, ee, mm);

  bool assertion = dd.ConstructDiv2D(ddg);

  if (!assertion) {
    std::cerr << "Mimetic div (2nd order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(1);
  mtk::Tools::Assert(assertion);
}

void TestReturnAsDenseMatrixWriteToFile() {

  mtk::Tools::BeginUnitTestNo(2);

  mtk::Div2D dd;

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
  mtk::Real cc = 0.0;
  mtk::Real ee = 1.0;

  int nn = 5;
  int mm = 5;

  mtk::UniStgGrid2D ddg(aa, bb, nn, cc, ee, mm);

  bool assertion = dd.ConstructDiv2D(ddg);

  if (!assertion) {
    std::cerr << "Mimetic div (2nd order) could not be built." << std::endl;
  }

  mtk::DenseMatrix ddm(dd.ReturnAsDenseMatrix());

  assertion = assertion && (ddm.num_rows() != mtk::kZero);

  std::cout << ddm << std::endl;

  assertion = assertion && ddm.WriteToFile("mtk_div_2d_test_02.dat");

  if(!assertion) {
    std::cerr << "Error writing to file." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(2);
  mtk::Tools::Assert(assertion);
}

int main () {

  std::cout << "Testing mtk::Div2D class." << std::endl;

  TestDefaultConstructorFactory();
  TestReturnAsDenseMatrixWriteToFile();
}

#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

17.97 tests/mtk_glpk_adapter_test.cc File Reference

Test file for the mtk::GLPKAdapter class.

`#include <iostream>`
Include dependency graph for mtk_glpk_adapter_test.cc:



Functions

- int main ()

17.97.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Todo Test the mtk::GLPKAdapter class.

Definition in file mtk_glpk_adapter_test.cc.

17.97.2 Function Documentation

17.97.2.1 int main ( )

Definition at line 81 of file mtk_glpk_adapter_test.cc.

17.98 mtk_glpk_adapter_test.cc

```
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00010 /*
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00018 and a copy of the modified files should be reported once modifications are
00019 completed, unless these modifications are made through the project's GitHub
00020 page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
00021 should be developed and included in any deliverable.
```

```

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*/

#if __cplusplus == 201103L

#include <iostream>
#include <ctime>

#include "mtk.h"

void Test1() {

  mtk::Tools::BeginUnitTestNo(1);

  mtk::Tools::EndUnitTestNo(1);
}

int main () {

  std::cout << "Testing mtk::GLPKAdapter class." << std::endl;

  Test1();
}

#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```
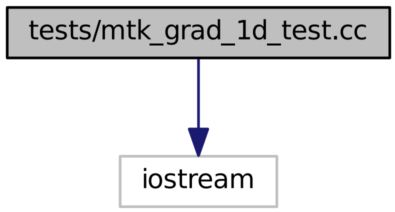

17.99 tests/mtk_grad_1d_test.cc File Reference

Testing the mimetic 1D gradient, constructed with the CBS algorithm.

```
#include <iostream>
```

Include dependency graph for mtk_grad_1d_test.cc:



Functions

- int main ()

17.99.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_grad_1d_test.cc.

17.99.2 Function Documentation

17.99.2.1 int main ( )

Definition at line 319 of file mtk_grad_1d_test.cc.

17.100 mtk_grad_1d_test.cc

```
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page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
should be developed and included in any deliverable.

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```
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(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#if __cplusplus == 201103L

#include <iostream>

#include "mtk.h"

void TestDefaultConstructorFactoryMethodDefault() {

  mtk::Tools::BeginUnitTestNo(1);

  mtk::Grad1D grad2;

  bool assertion = grad2.ConstructGrad1D();

  if (!assertion) {
    std::cerr << "Mimetic grad (2nd order) could not be built." << std::endl;

  }

  std::cout << grad2 << std::endl;

  mtk::Tools::EndUnitTestNo(1);
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodFourthOrder() {

  mtk::Tools::BeginUnitTestNo(2);

  mtk::Grad1D grad4;

  bool assertion = grad4.ConstructGrad1D(4);

  if (!assertion) {
    std::cerr << "Mimetic grad (4th order) could not be built." << std::endl;
  }

  std::cout << grad4 << std::endl;

  mtk::Tools::EndUnitTestNo(2);
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodSixthOrder() {

  mtk::Tools::BeginUnitTestNo(3);

  mtk::Grad1D grad6;

  bool assertion = grad6.ConstructGrad1D(6);

  if (!assertion) {
```

```
    std::cerr << "Mimetic grad (6th order) could not be built." << std::endl;
  }

  std::cout << grad6 << std::endl;

  mtk::Tools::EndUnitTestNo(3);
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodEightOrderDefThreshold() {

  mtk::Tools::BeginUnitTestNo(4);

  mtk::Grad1D grad8;

  bool assertion = grad8.ConstructGrad1D(8);

  if (!assertion) {
    std::cerr << "Mimetic grad (8th order) could not be built." << std::endl;
  }

  std::cout << grad8 << std::endl;

  mtk::Tools::EndUnitTestNo(4);
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodTenthOrderDefThreshold() {

  mtk::Tools::BeginUnitTestNo(5);

  mtk::Grad1D grad10;

  bool assertion = grad10.ConstructGrad1D(10);

  if (!assertion) {
    std::cerr << "Mimetic grad (10th order) could not be built." << std::endl;
  }

  std::cout << grad10 << std::endl;

  mtk::Tools::EndUnitTestNo(5);
  mtk::Tools::Assert(assertion);
}

void TestReturnAsDenseMatrixWithGrid() {

  mtk::Tools::BeginUnitTestNo(6);

  mtk::Grad1D grad2;

  bool assertion = grad2.ConstructGrad1D();

  if (!assertion) {
    std::cerr << "Mimetic grad (2nd order) could not be built." << std::endl;
  }

  mtk::UniStgGrid1D grid(0.0, 1.0, 5);

  mtk::DenseMatrix grad2m(grad2.ReturnAsDenseMatrix(grid));

  int rr{6};
  int cc{7};

  mtk::DenseMatrix ref(rr, cc);

  // Row 1.
  ref.SetValue(0,0,-13.3333);
  ref.SetValue(0,1,15);
  ref.SetValue(0,2,-1.66667);
  ref.SetValue(0,3,0.0);
  ref.SetValue(0,4,0.0);
  ref.SetValue(0,5,0.0);
  ref.SetValue(0,6,0.0);

  // Row 2.
  ref.SetValue(1,0,0.0);
  ref.SetValue(1,1,-5.0);
  ref.SetValue(1,2,5.0);
  ref.SetValue(1,3,0.0);
  ref.SetValue(1,4,0.0);
```

```
  ref.SetValue(1,5,0.0);
  ref.SetValue(1,6,0.0);

  // Row 3.
  ref.SetValue(2,0,0.0);
  ref.SetValue(2,1,0.0);
  ref.SetValue(2,2,-5.0);
  ref.SetValue(2,3,5.0);
  ref.SetValue(2,4,0.0);
  ref.SetValue(2,5,0.0);
  ref.SetValue(2,6,0.0);

  // Row 4.
  ref.SetValue(3,0,0.0);
  ref.SetValue(3,1,0.0);
  ref.SetValue(3,2,0.0);
  ref.SetValue(3,3,-5.0);
  ref.SetValue(3,4,5.0);
  ref.SetValue(3,5,0.0);
  ref.SetValue(3,6,0.0);

  // Row 5.
  ref.SetValue(4,0,0.0);
  ref.SetValue(4,1,0.0);
  ref.SetValue(4,2,0.0);
  ref.SetValue(4,3,0.0);
  ref.SetValue(4,4,-5.0);
  ref.SetValue(4,5,5.0);
  ref.SetValue(4,6,0.0);

  // Row 6.
  ref.SetValue(5,0,0.0);
  ref.SetValue(5,1,0.0);
  ref.SetValue(5,2,0.0);
  ref.SetValue(5,3,0.0);
  ref.SetValue(5,4,1.66667);
  ref.SetValue(5,5,-15.0);
  ref.SetValue(5,6,13.3333);

  mtk::Tools::EndUnitTestNo(6);
  mtk::Tools::Assert(grad2m == ref);
}

void TestReturnAsDimensionlessDenseMatrix() {

  mtk::Tools::BeginUnitTestNo(7);

  mtk::Grad1D grad4;

  bool assertion = grad4.ConstructGrad1D(4);

  if (!assertion) {
    std::cerr << "Mimetic grad (4th order) could not be built." << std::endl;
  }

  mtk::DenseMatrix grad4m(grad4.ReturnAsDimensionlessDenseMatrix
(10));

  std::cout << grad4m << std::endl;

  mtk::Tools::EndUnitTestNo(7);
  mtk::Tools::Assert(assertion);
}

void TestWriteToFile() {

  mtk::Tools::BeginUnitTestNo(8);

  mtk::Grad1D grad2;

  bool assertion = grad2.ConstructGrad1D();

  if (!assertion) {
    std::cerr << "Mimetic grad (2nd order) could not be built." << std::endl;
  }

  mtk::UniStgGrid1D grid(0.0, 1.0, 50);

  mtk::DenseMatrix grad2m(grad2.ReturnAsDenseMatrix(grid));

  std::cout << grad2m << std::endl;
```

```
  assertion = assertion && grad2m.WriteToFile("mtk_grad_1d_test_08.dat");

  if(!assertion) {
    std::cerr << "Error writing to file." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(8);
  mtk::Tools::Assert(assertion);
}

void TestMimBndy() {

  mtk::Tools::BeginUnitTestNo(9);

  mtk::Grad1D grad2;

  bool assertion = grad2.ConstructGrad1D();

  if (!assertion) {
    std::cerr << "Mimetic grad (2nd order) could not be built." << std::endl;
  }

  std::cout << grad2 << std::endl;

  mtk::DenseMatrix grad2m(grad2.mim_bndy());

  std::cout << grad2m << std::endl;

  mtk::Tools::EndUnitTestNo(9);
  mtk::Tools::Assert(assertion);
}

int main () {

  std::cout << "Testing mtk::Grad1D class." << std::endl;

  TestDefaultConstructorFactoryMethodDefault();
  TestDefaultConstructorFactoryMethodFourthOrder();
  TestDefaultConstructorFactoryMethodSixthOrder();
  TestDefaultConstructorFactoryMethodEightOrderDefThreshold();
  TestDefaultConstructorFactoryMethodTenthOrderDefThreshold();
  TestReturnAsDenseMatrixWithGrid();
  TestReturnAsDimensionlessDenseMatrix();
  TestWriteToFile();
  TestMimBndy();
}

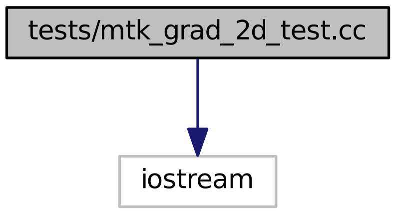
#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

17.101 tests/mtk_grad_2d_test.cc File Reference

Test file for the mtk::Grad2D class.

```
#include <iostream>
```

Include dependency graph for mtk_grad_2d_test.cc:



Functions

- int main ()

17.101.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_grad_2d_test.cc.

17.101.2 Function Documentation

17.101.2.1 int main ( )

Definition at line 139 of file mtk_grad_2d_test.cc.

17.102 mtk_grad_2d_test.cc

```

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```
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*/

#if __cplusplus == 201103L

#include <cmath>
#include <ctime>

#include <iostream>

#include "mtk.h"

void TestDefaultConstructorFactory() {

  mtk::Tools::BeginUnitTestNo(1);

  mtk::Grad2D gg;

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
  mtk::Real cc = 0.0;
  mtk::Real dd = 1.0;

  int nn = 5;
  int mm = 5;

  mtk::UniStgGrid2D ggg(aa, bb, nn, cc, dd, mm, mtk::VECTOR);

  bool assertion = gg.ConstructGrad2D(ggg);

  if (!assertion) {
    std::cerr << "Mimetic grad (2nd order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(1);
  mtk::Tools::Assert(assertion);
}

void TestReturnAsDenseMatrixWriteToFile() {

  mtk::Tools::BeginUnitTestNo(2);

  mtk::Grad2D gg;

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
  mtk::Real cc = 0.0;
  mtk::Real dd = 1.0;

  int nn = 5;
  int mm = 5;

  mtk::UniStgGrid2D ggg(aa, bb, nn, cc, dd, mm, mtk::VECTOR);

  bool assertion = gg.ConstructGrad2D(ggg);
```
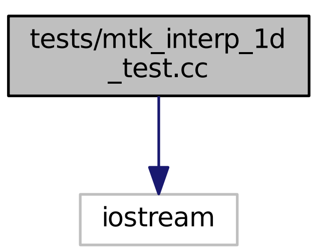

```

  if (!assertion) {
    std::cerr << "Mimetic grad (2nd order) could not be built." << std::endl;
  }

  mtk::DenseMatrix ggm(gg.ReturnAsDenseMatrix());

  assertion = assertion && (ggm.num_rows() != mtk::kZero);

  std::cout << ggm << std::endl;

  assertion = assertion && ggm.WriteToFile("mtk_grad_2d_test_02.dat");

  if(!assertion) {
    std::cerr << "Error writing to file." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(2);
  mtk::Tools::Assert(assertion);
}

int main () {

  std::cout << "Testing mtk::Grad2D class." << std::endl;

  TestDefaultConstructorFactory();
  TestReturnAsDenseMatrixWriteToFile();
}

#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

17.103 tests/mtk_interp_1d_test.cc File Reference

Testing the 1D interpolation.

`#include <iostream>`
Include dependency graph for mtk_interp_1d_test.cc:



Functions

- int main ()

17.103.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu
: Johnny Corbino - jcorbino at mail dot sdsu dot edu

Definition in file mtk_interp_1d_test.cc.

17.103.2 Function Documentation

17.103.2.1 int main ( )

Definition at line 113 of file mtk_interp_1d_test.cc.

17.104 mtk_interp_1d_test.cc

```
00001
00010 /*
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00013
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00016
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00018 and a copy of the modified files should be reported once modifications are
00019 completed, unless these modifications are made through the project's GitHub
00020 page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
00021 should be developed and included in any deliverable.
00022
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00051 ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT
00052 (INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
00053 SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
00054 */
00055
00056 #if __cplusplus == 201103L
00057
00058 #include <iostream>
00059
00060 #include "mtk.h"
```
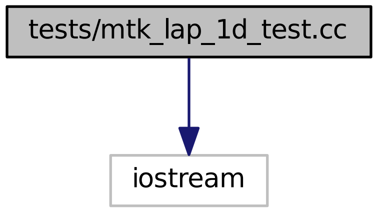

```

void TestDefaultConstructorFactoryMethodDefault() {

  mtk::Tools::BeginUnitTestNo(1);

  mtk::Interp1D inter;

  bool assertion = inter.ConstructInterp1D();

  if (!assertion) {
    std::cerr << "Mimetic interp could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(1);
  mtk::Tools::Assert(assertion);
}

void TestReturnAsDenseMatrixWithGrid() {

  mtk::Tools::BeginUnitTestNo(2);

  mtk::Interp1D inter;

  bool assertion = inter.ConstructInterp1D();

  if (!assertion) {
    std::cerr << "Mimetic grad (2nd order) could not be built." << std::endl;
  }

  mtk::UniStgGrid1D grid(0.0, 1.0, 5);

  mtk::DenseMatrix interpm(inter.ReturnAsDenseMatrix(grid));

  assertion =
    assertion && interpm.GetValue(0,0) == 1.0 && interpm.GetValue(5,6) == 1.0;

  mtk::Tools::EndUnitTestNo(2);
  mtk::Tools::Assert(assertion);
}

int main () {

  std::cout << "Testing mtk::Interp1D class." << std::endl;

  TestDefaultConstructorFactoryMethodDefault();
  TestReturnAsDenseMatrixWithGrid();
}

#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

17.105 tests/mtk_lap_1d_test.cc File Reference

Testing the 1D Laplacian operator.

`#include <iostream>`

Include dependency graph for mtk_lap_1d_test.cc:



Functions

- int main ()

17.105.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu
: Johnny Corbino - jcorbino at mail dot sdsu dot edu

Definition in file mtk_lap_1d_test.cc.

17.105.2 Function Documentation

17.105.2.1 int main ( )

Definition at line 193 of file mtk_lap_1d_test.cc.

17.106 mtk_lap_1d_test.cc

```

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```

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*/

#if __cplusplus == 201103L

#include <iostream>

#include "mtk.h"

void TestDefaultConstructorFactoryMethodDefault() {

  mtk::Tools::BeginUnitTestNo(1);

  mtk::Lap1D lap2;

  bool assertion = lap2.ConstructLap1D();

  if (!assertion) {
    std::cerr << "Mimetic lap (2nd order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(1);
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodFourthOrder() {

  mtk::Tools::BeginUnitTestNo(2);

  mtk::Lap1D lap4;

  bool assertion = lap4.ConstructLap1D(4);

  if (!assertion) {
    std::cerr << "Mimetic lap (4th order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(2);
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodSixthOrder() {

  mtk::Tools::BeginUnitTestNo(3);

  mtk::Lap1D lap6;

  bool assertion = lap6.ConstructLap1D(6);

  if (!assertion) {
    std::cerr << "Mimetic lap (6th order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(3);
```

```
  mtk::Tools::Assert(assertion);
}

void TestDefaultConstructorFactoryMethodEightOrderDefThreshold() {

  mtk::Tools::BeginUnitTestNo(4);

  mtk::Lap1D lap8;

  bool assertion = lap8.ConstructLap1D(8);

  if (!assertion) {
    std::cerr << "Mimetic lap (8th order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(4);
}

void TestDefaultConstructorFactoryMethodTenthOrderDefThreshold() {

  mtk::Tools::BeginUnitTestNo(5);

  mtk::Lap1D lap10;

  bool assertion = lap10.ConstructLap1D(10);

  if (!assertion) {
    std::cerr << "Mimetic lap (10th order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(5);
}

void TestDefaultConstructorFactoryMethodTwelfthOrderDefThreshold() {

  mtk::Tools::BeginUnitTestNo(6);

  mtk::Lap1D lap12;

  bool assertion = lap12.ConstructLap1D(12);

  if (!assertion) {
    std::cerr << "Mimetic lap (12th order) could not be built." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(6);
}

void TestReturnAsDenseMatrix() {

  mtk::Tools::BeginUnitTestNo(8);

  mtk::Lap1D lap4;

  bool assertion = lap4.ConstructLap1D(4);

  if (!assertion) {
    std::cerr << "Mimetic lap (4th order) could not be built." << std::endl;
  }

  mtk::UniStgGrid1D aux(0.0, 1.0, 11);

  mtk::DenseMatrix lap4_m(lap4.ReturnAsDenseMatrix(aux));

  assertion = assertion &&
      abs(lap4_m.GetValue(1, 0) - 385.133) < mtk::kDefaultTolerance &&
      abs(lap4_m.GetValue(11, 12) - 385.133) < mtk::kDefaultTolerance;
  mtk::Tools::EndUnitTestNo(8);
  mtk::Tools::Assert(assertion);
}

int main () {

  std::cout << "Testing MTK 1D Laplacian" << std::endl;

  TestDefaultConstructorFactoryMethodDefault();
  TestDefaultConstructorFactoryMethodFourthOrder();
  TestDefaultConstructorFactoryMethodSixthOrder();
  TestDefaultConstructorFactoryMethodEightOrderDefThreshold();
  TestDefaultConstructorFactoryMethodTenthOrderDefThreshold();
  TestDefaultConstructorFactoryMethodTwelfthOrderDefThreshold();
```

```
  TestReturnAsDenseMatrix();
}

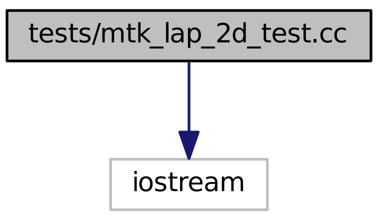
#else
#include <iostream>
int main () {
  std::cout << "This code HAS to be compiled to support C++11." << std::endl;
  std::cout << "Exiting..." << std::endl;
}
#endif
```

17.107 tests/mtk_lap_2d_test.cc File Reference

Test file for the mtk::Lap2D class.

`#include <iostream>`

Include dependency graph for mtk_lap_2d_test.cc:



Functions

- int main ()

17.107.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_lap_2d_test.cc.

17.107.2 Function Documentation

17.107.2.1 int main ( )

Definition at line 139 of file mtk_lap_2d_test.cc.

17.108 mtk_lap_2d_test.cc

```
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ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT
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SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#if __cplusplus == 201103L

#include <cmath>
#include <ctime>

#include <iostream>

#include "mtk.h"

void TestDefaultConstructorFactory() {

  mtk::Tools::BeginUnitTestNo(1);

  mtk::Lap2D ll;

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
  mtk::Real cc = 0.0;
  mtk::Real dd = 1.0;

  int nn = 5;
  int mm = 5;

  mtk::UniStgGrid2D llg(aa, bb, nn, cc, dd, mm);

  bool assertion = ll.ConstructLap2D(llg);

  if (!assertion) {
    std::cerr << "Mimetic lap (2nd order) could not be built." << std::endl;
  }

```

```
  mtk::Tools::EndUnitTestNo(1);
  mtk::Tools::Assert(assertion);
}

void TestReturnAsDenseMatrixWriteToFile() {

  mtk::Tools::BeginUnitTestNo(2);

  mtk::Lap2D ll;

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
  mtk::Real cc = 0.0;
  mtk::Real dd = 1.0;

  int nn = 5;
  int mm = 5;

  mtk::UniStgGrid2D llg(aa, bb, nn, cc, dd, mm);

  bool assertion = ll.ConstructLap2D(llg);

  if (!assertion) {
    std::cerr << "Mimetic lap (2nd order) could not be built." << std::endl;
  }

  mtk::DenseMatrix llm(ll.ReturnAsDenseMatrix());

  assertion = assertion && (llm.num_rows() != 0);

  std::cout << llm << std::endl;

  assertion = assertion && llm.WriteToFile("mtk_lap_2d_test_02.dat");

  if(!assertion) {
    std::cerr << "Error writing to file." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(2);
  mtk::Tools::Assert(assertion);
}

int main () {

  std::cout << "Testing mtk::Lap2D class." << std::endl;

  TestDefaultConstructorFactory();
  TestReturnAsDenseMatrixWriteToFile();
}

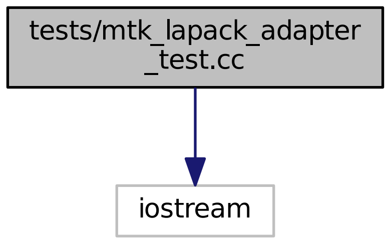
#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

17.109 tests/mtk_lapack_adapter_test.cc File Reference

Test file for the mtk::LAPACKAdapter class.

```
#include <iostream>
```

Include dependency graph for mtk_lapack_adapter_test.cc:



Functions

- int main ()

17.109.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Todo Test the mtk::LAPACKAdapter class.

Definition in file mtk_lapack_adapter_test.cc.

17.109.2 Function Documentation

17.109.2.1 int main ( )

Definition at line 81 of file mtk_lapack_adapter_test.cc.

17.110 mtk_lapack_adapter_test.cc

```
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00010 /*
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00017 1. Modifications to source code should be reported to: esanchez@mail.sdsu.edu
00018 and a copy of the modified files should be reported once modifications are
00019 completed, unless these modifications are made through the project's GitHub
00020 page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
00021 should be developed and included in any deliverable.
```

```
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downloads from the project's GitHub page: http://www.csrc.sdsu.edu/mtk

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ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT
(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#if __cplusplus == 201103L

#include <iostream>
#include <ctime>

#include "mtk.h"

void Test1() {

  mtk::Tools::BeginUnitTestNo(1);

  mtk::Tools::EndUnitTestNo(1);
}

int main () {

  std::cout << "Testing mtk::LAPACKAdapter class." << std::endl;

  Test1();
}

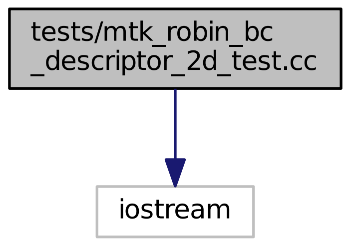
#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

17.111 tests/mtk_robin_bc_descriptor_2d_test.cc File Reference

Test file for the mtk::RobinBCDescriptor2D class.

```
#include <iostream>
```

Include dependency graph for mtk_robin_bc_descriptor_2d_test.cc:



Functions

- int main ()

17.111.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_robin_bc_descriptor_2d_test.cc.

17.111.2 Function Documentation

17.111.2.1 int main ( )

Definition at line 197 of file mtk_robin_bc_descriptor_2d_test.cc.

17.112 mtk_robin_bc_descriptor_2d_test.cc

```

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page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
should be developed and included in any deliverable.

2. Redistributions of source code must be done through direct
downloads from the project's GitHub page: http://www.csrc.sdsu.edu/mtk

```

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ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT
(INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
*/

#if __cplusplus == 201103L

#include <cmath>
#include <ctime>

#include <iostream>

#include "mtk.h"

void TestDefaultConstructorGetters() {

  mtk::Tools::BeginUnitTestNo(1);

  mtk::RobinBCDescriptor2D bcd;

  bool assertion{true};

  assertion = assertion && bcd.highest_order_diff_west() == -1;
  assertion = assertion && bcd.highest_order_diff_east() == -1;
  assertion = assertion && bcd.highest_order_diff_south() == -1;
  assertion = assertion && bcd.highest_order_diff_north() == -1;

  mtk::Tools::EndUnitTestNo(1);
  mtk::Tools::Assert(assertion);
}

mtk::Real cc(const mtk::Real &xx, const mtk::Real &yy) {

  return mtk::kOne;
}

void TestPushBackImposeOnLaplacianMatrix() {

  mtk::Tools::BeginUnitTestNo(2);

  mtk::RobinBCDescriptor2D bcd;

  bool assertion{true};

  bcd.PushBackWestCoeff(cc);
  bcd.PushBackEastCoeff(cc);
  bcd.PushBackSouthCoeff(cc);
  bcd.PushBackNorthCoeff(cc);

  assertion = assertion && bcd.highest_order_diff_west() == 0;
  assertion = assertion && bcd.highest_order_diff_east() == 0;
  assertion = assertion && bcd.highest_order_diff_south() == 0;
  assertion = assertion && bcd.highest_order_diff_north() == 0;

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
```

```
  mtk::Real cc = 0.0;
  mtk::Real dd = 1.0;

  int nn = 5;
  int mm = 5;

  mtk::UniStgGrid2D llg(aa, bb, nn, cc, dd, mm);

  mtk::Lap2D ll;

  assertion = ll.ConstructLap2D(llg);

  if (!assertion) {
    std::cerr << "Mimetic lap (2nd order) could not be built." << std::endl;
  }

  mtk::DenseMatrix llm(ll.ReturnAsDenseMatrix());

  assertion = assertion && (llm.num_rows() != 0);

  bcd.ImposeOnLaplacianMatrix(ll, llg, llm);

  assertion = assertion && llm.WriteToFile("mtk_bc_descriptor_2d_test_02.dat");

  mtk::Tools::EndUnitTestNo(2);
  mtk::Tools::Assert(assertion);
}

mtk::Real ScalarField(const mtk::Real &xx, const mtk::Real &yy) {

  mtk::Real aux{-(1.0/2.0)*xx*xx - (1.0/2.0)*yy*yy};

  return xx*yy*exp(aux);
}

mtk::Real HomogeneousDiricheletBC(const mtk::Real &xx,
                                  const mtk::Real &tt) {

  return mtk::kZero;
}

void TestImposeOnGrid() {

  mtk::Tools::BeginUnitTestNo(3);

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
  mtk::Real cc = 0.0;
  mtk::Real dd = 1.0;

  int nn = 5;
  int mm = 5;

  mtk::UniStgGrid2D gg(aa, bb, nn, cc, dd, mm);

  gg.BindScalarField(ScalarField);

  mtk::RobinBCDescriptor2D desc;

  desc.set_west_condition(HomogeneousDiricheletBC);
  desc.set_east_condition(HomogeneousDiricheletBC);
  desc.set_south_condition(HomogeneousDiricheletBC);
  desc.set_north_condition(HomogeneousDiricheletBC);

  desc.ImposeOnGrid(gg);

  bool assertion{gg.WriteToFile("mtk_bc_descriptor_2d_test_03.dat",
                                "x",
                                "y",
                                "u(x,y)")};

  if(!assertion) {
    std::cerr << "Error writing to file." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(3);
  mtk::Tools::Assert(assertion);
}

int main () {

```

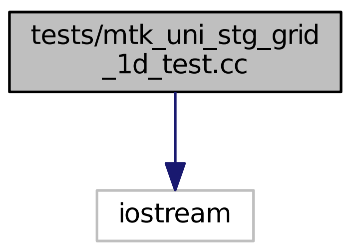
```
  std::cout << "Testing mtk::RobinBCDescriptor2D class." << std::endl;

  TestDefaultConstructorGetters();
  TestPushBackImposeOnLaplacianMatrix();
  TestImposeOnGrid();
}

#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

17.113 tests/mtk_uni_stg_grid_1d_test.cc File Reference

Test file for the mtk::UniStgGrid1D class.

`#include <iostream>`

Include dependency graph for mtk_uni_stg_grid_1d_test.cc:



Functions

- int main ()

17.113.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_uni_stg_grid_1d_test.cc.

17.113.2 Function Documentation

17.113.2.1 int main ( )

Definition at line 172 of file mtk_uni_stg_grid_1d_test.cc.

17.114 mtk_uni_stg_grid_1d_test.cc

```
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00008 /*
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00016 and a copy of the modified files should be reported once modifications are
00017 completed, unless these modifications are made through the project's GitHub
00018 page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
00019 should be developed and included in any deliverable.
00020
00021 2. Redistributions of source code must be done through direct
00022 downloads from the project's GitHub page: http://www.csrc.sdsu.edu/mtk
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00049 ANY THEORY OF LIABILITY, WHETHER IN CONTRACT, STRICT LIABILITY, OR TORT
00050 (INCLUDING NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
00051 SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
00052 */
00053
00054 #if __cplusplus == 201103L
00055
00056 #include <iostream>
00057 #include <ctime>
00058
00059 #include "mtk.h"
00060
00061 void TestDefaultConstructor() {
00062
00063   mtk::Tools::BeginUnitTestNo(1);
00064
00065   mtk::UniStgGrid1D gg;
00066
00067   mtk::Tools::EndUnitTestNo(1);
00068   mtk::Tools::Assert(gg.delta_x() == mtk::kZero);
00069 }
00070
00071 mtk::Real ScalarField(const mtk::Real &xx) {
00072
00073   return 2.0*xx;
00074 }
00075
00076 void TestConstructWithWestBndyEastBndyNumCellsOStreamOperatorBindScalarField() {
```

```

  mtk::Tools::BeginUnitTestNo(2);

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;

  int nn = 5;

  mtk::UniStgGrid1D gg(aa, bb, nn);

  gg.BindScalarField(ScalarField);

  std::cout << gg << std::endl;

  mtk::Tools::EndUnitTestNo(2);
  mtk::Tools::Assert(gg.delta_x() == 0.2 && gg.
num_cells_x() == 5);
}

void TestBindScalarFieldWriteToFile() {

  mtk::Tools::BeginUnitTestNo(3);

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;

  int nn = 5;

  mtk::UniStgGrid1D gg(aa, bb, nn);

  bool assertion{true};

  gg.BindScalarField(ScalarField);

  assertion =
    assertion &&
    gg.discrete_field()[0] == 0.0 &&
    gg.discrete_field()[gg.num_cells_x() + 2 - 1] == 2.0;

  if(!gg.WriteToFile("mtk_uni_stg_grid_1d_test_03.dat", "x", "u(x)")) {
    std::cerr << "Error writing to file." << std::endl;
    assertion = false;
  }

  mtk::Tools::EndUnitTestNo(3);
  mtk::Tools::Assert(assertion);
}

mtk::Real VectorFieldPComponent(mtk::Real xx) {

  return xx*xx;
}

void TestBindVectorField() {

  mtk::Tools::BeginUnitTestNo(4);

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;

  int nn = 20;

  mtk::UniStgGrid1D gg(aa, bb, nn, mtk::VECTOR);

  bool assertion{true};

  gg.BindVectorField(VectorFieldPComponent);

  assertion =
    assertion &&
    gg.discrete_field()[0] == 0.0 &&
    gg.discrete_field()[gg.num_cells_x() + 1 - 1] == 1.0;

  if(!gg.WriteToFile("mtk_uni_stg_grid_1d_test_04.dat", "x", "v(x)")) {
    std::cerr << "Error writing to file." << std::endl;
    assertion = false;
  }

  mtk::Tools::EndUnitTestNo(4);
  mtk::Tools::Assert(assertion);
}
```

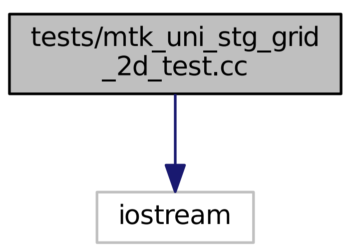
```

int main () {

  std::cout << "Testing mtk::UniStgGrid1D class." << std::endl;

  TestDefaultConstructor();
  TestConstructWithWestBndyEastBndyNumCellsOStreamOperatorBindScalarField();
  TestBindScalarFieldWriteToFile();
  TestBindVectorField();
}

#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

17.115 tests/mtk_uni_stg_grid_2d_test.cc File Reference

Test file for the mtk::UniStgGrid2D class.

`#include <iostream>`

Include dependency graph for mtk_uni_stg_grid_2d_test.cc:



Functions

- int main ()

17.115.1 Detailed Description

Author

: Eduardo J. Sanchez (ejspeiro) - esanchez at mail dot sdsu dot edu

Definition in file mtk_uni_stg_grid_2d_test.cc.

17.115.2 Function Documentation

17.115.2.1 int main ( )

Definition at line 202 of file mtk_uni_stg_grid_2d_test.cc.

17.116 mtk_uni_stg_grid_2d_test.cc

```
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00008 /*
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00016 and a copy of the modified files should be reported once modifications are
00017 completed, unless these modifications are made through the project's GitHub
00018 page: http://www.csrc.sdsu.edu/mtk. Documentation related to said modifications
00019 should be developed and included in any deliverable.
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00052 */
00053
00054 #if __cplusplus == 201103L
00055
00056 #include <cmath>
00057 #include <ctime>
00058
00059 #include <iostream>
00060
00061 #include "mtk.h"
00062
00063 void TestDefaultConstructor() {
00064
00065   mtk::Tools::BeginUnitTestNo(1);
00066
00067   mtk::UniStgGrid2D gg;
00068
00069   mtk::Tools::EndUnitTestNo(1);
00070   mtk::Tools::Assert(gg.delta_x() == mtk::kZero && gg.delta_y() == mtk::kZero);
00071 }
00072
00073 void
00074 TestConstructWithWestEastNumCellsXSouthNorthBndysNumCellsYOStreamOperator() {
00075
```

```
  mtk::Tools::BeginUnitTestNo(2);

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
  mtk::Real cc = 0.0;
  mtk::Real dd = 1.0;

  int nn = 5;
  int mm = 7;

  mtk::UniStgGrid2D gg(aa, bb, nn, cc, dd, mm);

  std::cout << gg << std::endl;

  mtk::Tools::EndUnitTestNo(2);
  mtk::Tools::Assert(gg.delta_x() == 0.2 &&
                     abs(gg.delta_y() - 0.142857) < mtk::kDefaultTolerance);
}

void TestGetters() {

  mtk::Tools::BeginUnitTestNo(3);

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
  mtk::Real cc = 0.0;
  mtk::Real dd = 1.0;

  int nn = 5;
  int mm = 7;

  mtk::UniStgGrid2D gg(aa, bb, nn, cc, dd, mm);

  bool assertion{true};

  assertion = assertion && (gg.west_bndy() == aa);
  assertion = assertion && (gg.east_bndy() == bb);
  assertion = assertion && (gg.num_cells_x() == nn);
  assertion = assertion && (gg.south_bndy() == cc);
  assertion = assertion && (gg.north_bndy() == dd);
  assertion = assertion && (gg.num_cells_y() == mm);

  mtk::Tools::EndUnitTestNo(3);
  mtk::Tools::Assert(assertion);
}

mtk::Real ScalarField(const mtk::Real &xx, const mtk::Real &yy) {

  mtk::Real aux{-(1.0/2.0)*xx*xx - (1.0/2.0)*yy*yy};

  return xx*yy*exp(aux);
}

void TestBindScalarFieldWriteToFile() {

  mtk::Tools::BeginUnitTestNo(4);

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
  mtk::Real cc = 0.0;
  mtk::Real dd = 1.0;

  int nn = 5;
  int mm = 5;

  mtk::UniStgGrid2D gg(aa, bb, nn, cc, dd, mm);

  gg.BindScalarField(ScalarField);

  if(!gg.WriteToFile("mtk_uni_stg_grid_2d_test_04.dat", "x", "y", "u(x,y)")) {
    std::cerr << "Error writing to file." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(4);
}

mtk::Real VectorFieldPComponent(const mtk::Real &xx, const mtk::Real &yy) {

  return xx + 0.01;
```

```
}

mtk::Real VectorFieldQComponent(const mtk::Real &xx, const mtk::Real &yy) {

  return yy + 0.01;
}

void TestBindVectorField() {

  mtk::Tools::BeginUnitTestNo(5);

  mtk::Real aa = 0.0;
  mtk::Real bb = 1.0;
  mtk::Real cc = 0.0;
  mtk::Real dd = 1.0;

  int nn = 5;
  int mm = 5;

  mtk::UniStgGrid2D gg(aa, bb, nn, cc, dd, mm, mtk::VECTOR);

  gg.BindVectorField(VectorFieldPComponent, VectorFieldQComponent);

  std::cout << gg << std::endl;

  if(!gg.WriteToFile("mtk_uni_stg_grid_2d_test_05.dat", "x", "y", "v(x,y)")) {
    std::cerr << "Error writing to file." << std::endl;
  }

  mtk::Tools::EndUnitTestNo(5);
}

int main () {

  std::cout << "Testing mtk::UniStgGrid2D class." << std::endl;

  TestDefaultConstructor();
  TestConstructWithWestEastNumCellsXSouthNorthBndysNumCellsYOStreamOperator();
  TestGetters();
  TestBindScalarFieldWriteToFile();
  TestBindVectorField();
}

#else
#include <iostream>
using std::cout;
using std::endl;
int main () {
  cout << "This code HAS to be compiled with support for C++11." << endl;
  cout << "Exiting..." << endl;
}
#endif
```

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