

# TOC Class Test

Subject: Theory of Computation [CS 2204]

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Q1) a) False, ~~Can~~ A context-free language over some  $\Sigma$  can't be a subset of some Regular Language over the same alphabet  $\Sigma$ .

→ We know that every Regular Language is not context free, but vice versa is true

↳ Eg: A PDA can accept language produced by ~~FA~~ <sup>RG</sup>, but A language produced by ~~PDA~~ <sup>CFG</sup> can't be accepted by FA.



b) Given a Non-Deterministic Finite Automata

$$M = (K, \Sigma, \Delta, \delta, F), \Delta \subseteq K \times \Sigma^* \times K$$

we create following ~~PFA~~ Push-down Automata.

$$M' = (K', \Sigma', \Gamma', \Delta', \delta', F')$$

$$\Delta' \subseteq K \times \Sigma^* \times \Gamma^* \times K \times \Gamma^*$$

$$\text{with } K' = K$$

$$\Sigma' = \Sigma$$

$$\Gamma' = \{\epsilon\}$$

$$\Delta' = \{(p, \alpha, \epsilon, q, \epsilon) \mid (p, \alpha, q) \in \Delta\}$$

$$\delta' = \delta$$

$$F' = F$$

i.e. we follow same procedure as NDFA  $M$  follows,  
but at each step we push and pop nothing (empty string)

→ As this construction just straightforwardly copies the given NDFA  $M$ , we can say that

$$L(M') = L(M)$$

∴ The given statement is True



c) The given statement is true

→ given  $\Sigma_1$  and  $\Sigma_2$  two alphabets,  $\Sigma_1 \cap \Sigma_2 = \emptyset$

There can't be common strings between  $L_1$ ,  
a language over  $\Sigma_1$  and  $L_2$ , language over  $\Sigma_2$

proof by contradiction

→ Let's assume that there ~~are some~~ <sup>is a</sup> common strings

~~Let~~  $w$  ~~is~~ between  $L_1$  and  $L_2$

→ This means  $w$  has ~~some~~ the symbols common to  
alphabet  $L_1$  and  $L_2$

→ that mean

$$L_1 \cap L_2 \neq \emptyset$$

→ which contradicts the given statement that  $L_1 \cap L_2 = \emptyset$

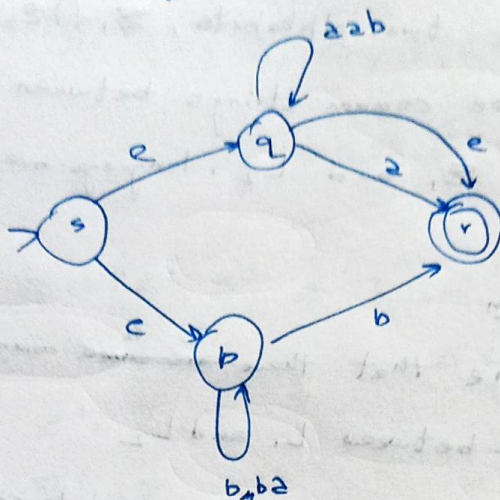
→ This means what we presumed was actually wrong.

→ Therefore if  $\Sigma_1 \cap \Sigma_2 = \emptyset$ , we can't have common  
strings between  $L_1 \subseteq \Sigma_1^*$  and  $L_2 \subseteq \Sigma_2^*$

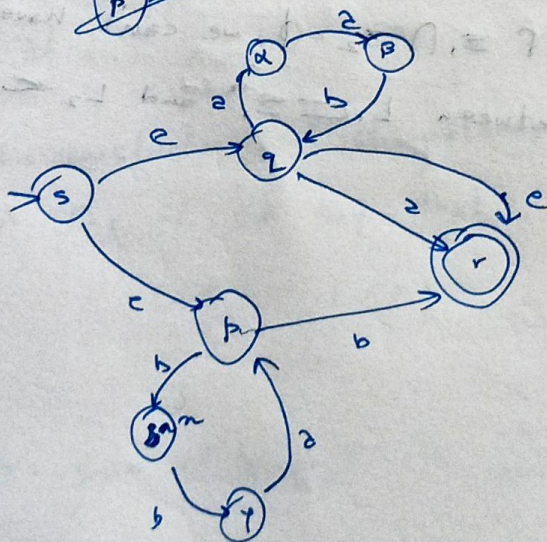
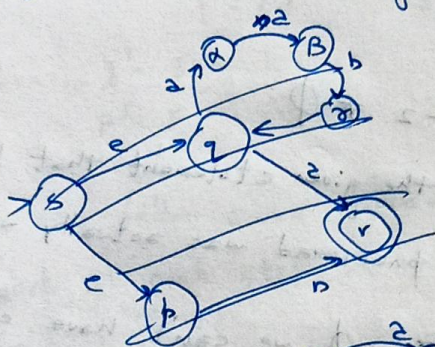




2) given Following NDEA

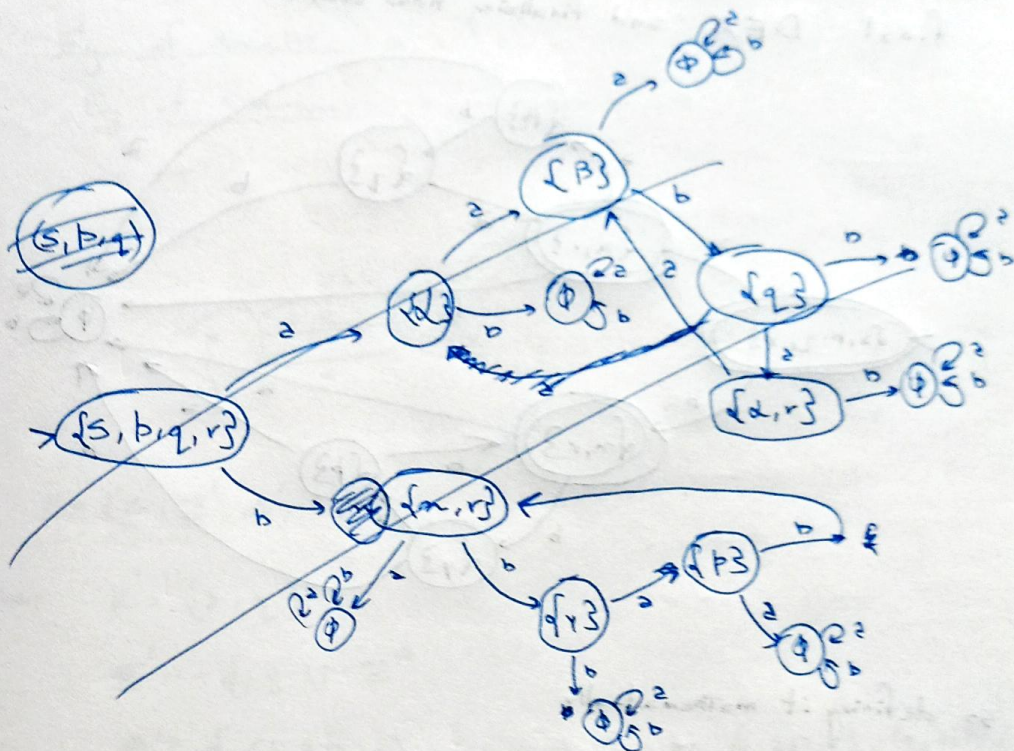


→ first we convert strings to single symbol transitions

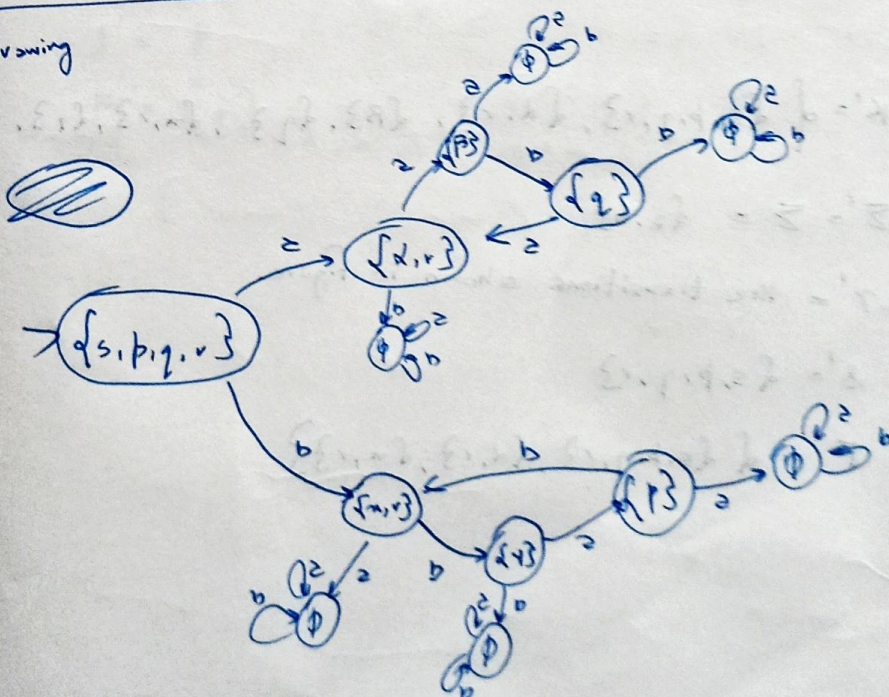




→ then we merge the empty closures

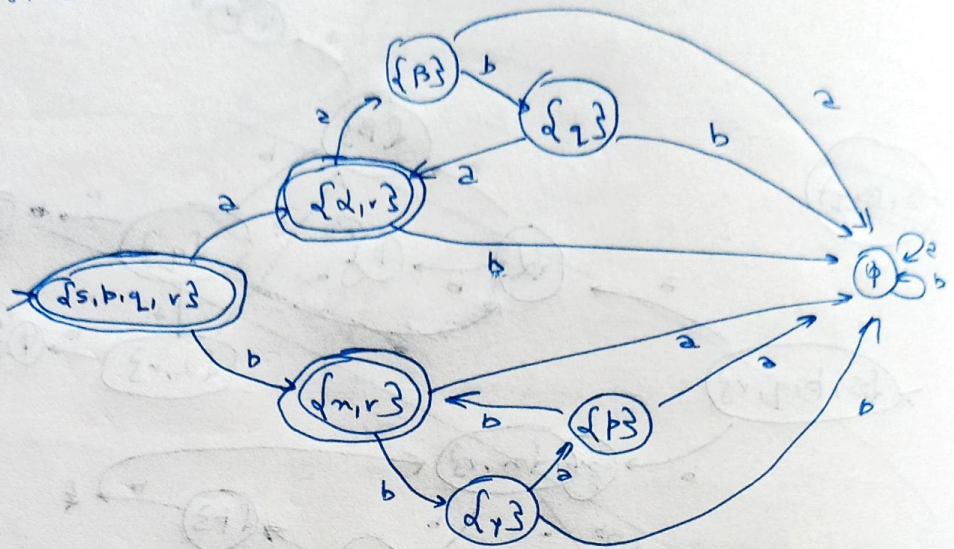


redrawing





→ now we merge the  $\phi$  state together to create final DFA and finalizing final states



so defining it mathematically,

$$M' = (K', \Sigma', \gamma', \delta', F')$$

$$K' = \{ \{s, p, q, r\}, \{d, r\}, \{B\}, \{q\}, \{n, r\}, \{r\}, \{\phi\} \}$$

$$\Sigma' = \Sigma = \{a, b\}$$

$\gamma'$  = the transitions shown in figure

$$\delta' = \{s, p, q, r\}$$

$$F' = \{ \{s, p, q, r\}, \{d, r\}, \{n, r\} \}$$

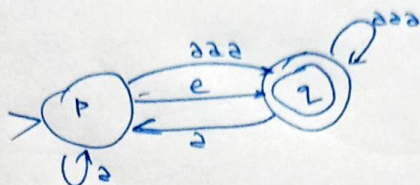


Q3) a)  $\{w \in \{a,b\}^* \mid \text{The no. of a's is divisible by 3}\}$

[FA]

Eg of accept:  $a^0, a^3, a^6, \dots$

Eg of Non-accept:  $a, a^2, \dots, a^4, a^5, \dots$



$$M = (K', \Sigma', \Delta', s', F')$$

where  $K' = \{p, q\}$

$$\Sigma' = \{e\} \cup \Sigma$$

$$\Delta' = \{(p, aaa, q), (p, e, q), (q, a, p), (q, aaa, q), (q, a, p)\}$$

$$s' = p$$

$$F' = \{q\}$$

Q3) b)  $L = \{a^m b^n c^l \mid l, m, n \geq 0 \text{ and } m + l + n\}$  [CFG]

### Rules

1)  $S \rightarrow ABC$

2)  $A \rightarrow aA$

3)  $A \rightarrow \epsilon$

4)  $B \rightarrow bB$

5)  $B \rightarrow \epsilon$

6)  $C \rightarrow cC$

7)  $C \rightarrow \epsilon$

$G = \{V, \Sigma, R, S\}$

with  $V = \{a, b, c, S, A, B, C\}$

$\Sigma = \{a, b, c\}$

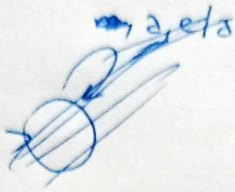
$R = \{S \rightarrow ABC, A \rightarrow aA, A \rightarrow \epsilon, B \rightarrow bB, B \rightarrow \epsilon, C \rightarrow cC, C \rightarrow \epsilon\}$

$S = S$



$$c) L = \{ a^m b^n \mid m, n \geq 0 \text{ and } m \geq n \}$$

[PDA]



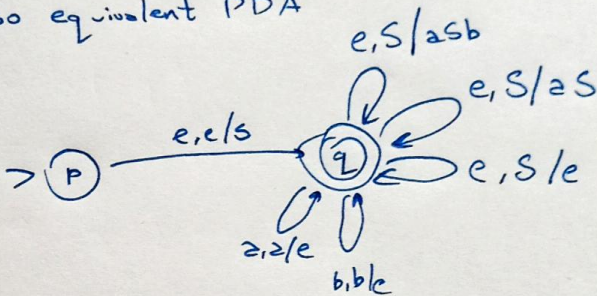
trying to make ~~CFG~~ CFG

$$S \rightarrow aSb$$

$$S \rightarrow aS$$

$$S \rightarrow \epsilon$$

so equivalent PDA



$$M = (K, \Sigma, \Gamma, \Delta, \delta, F)$$

$$K = \{p, q\}$$

$$\Sigma = \{a, b\}$$

$$\Gamma = \{S, a, b\}$$

$$\Delta = \{ (p, \epsilon, \epsilon, q, S), (q, \epsilon, S, q, aSb), (q, \epsilon, S, q, aS), (q, \epsilon, S, q, e), (q, b, b, q, e), (q, a, a, q, e) \}$$

$$S = \{p\}$$

$$F = \{q\}$$