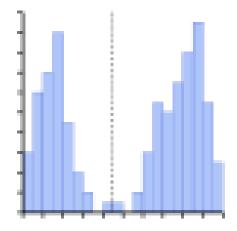
Otsu Method

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Otsu thresholding

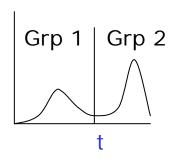
- → Converting a grayscale image to monochrome
- ◆ Otsu's method, named after its inventor *Nobuyuki Otsu*, is one of many binarization algorithms



Assumption: the histogram is bimodal



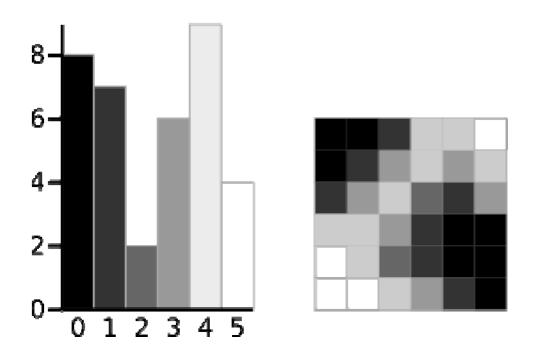
- → This method *involves iterating* through all the possible thr eshold values and calculating a measure of spread for the pixel levels each side of the threshold, i.e. *the pixels that either fall in foreground or background*
- → The aim is to find the threshold value where the sum of foreground and background spreads is at its minimum



Assumption: the histogram is bimodal



- ◆ Simple 6x6 image shown below and the histogram for the image is shown next
- → To simplify the explanation, only 6 grayscale levels are used

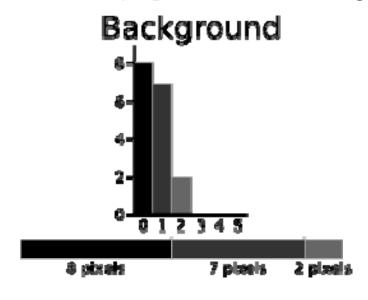






Cont. (For Background)

→ The calculations are bellow for finding the foreground & background variances (the measure of spread) for a single threshold

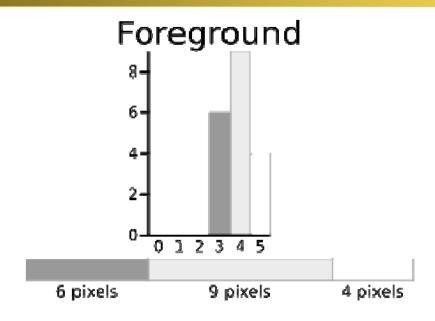


Weight
$$W_b = \frac{8+7+2}{36} = 0.4722$$

Mean $\mu_b = \frac{(0\times8) + (1\times7) + (2\times2)}{17} = 0.6471$
Variance $\sigma_b^2 = \frac{((0-0.6471)^2 \times 8) + ((1-0.6471)^2 \times 7) + ((2-0.6471)^2 \times 2)}{17}$
 $= \frac{(0.4187 \times 8) + (0.1246 \times 7) + (1.8304 \times 2)}{17}$
 $= 0.4637$

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Cont. (For Foreground)



Weight
$$W_f = \frac{6+9+4}{36} = 0.5278$$

Mean $\mu_f = \frac{(3\times 6) + (4\times 9) + (5\times 4)}{19} = 3.8947$
Variance $\sigma_f^2 = \frac{((3-3.8947)^2 \times 6) + ((4-3.8947)^2 \times 9) + ((5-3.8947)^2 \times 4)}{19}$
 $= \frac{(4.8033 \times 6) + (0.0997 \times 9) + (4.8864 \times 4)}{19}$
 $= 0.5152$

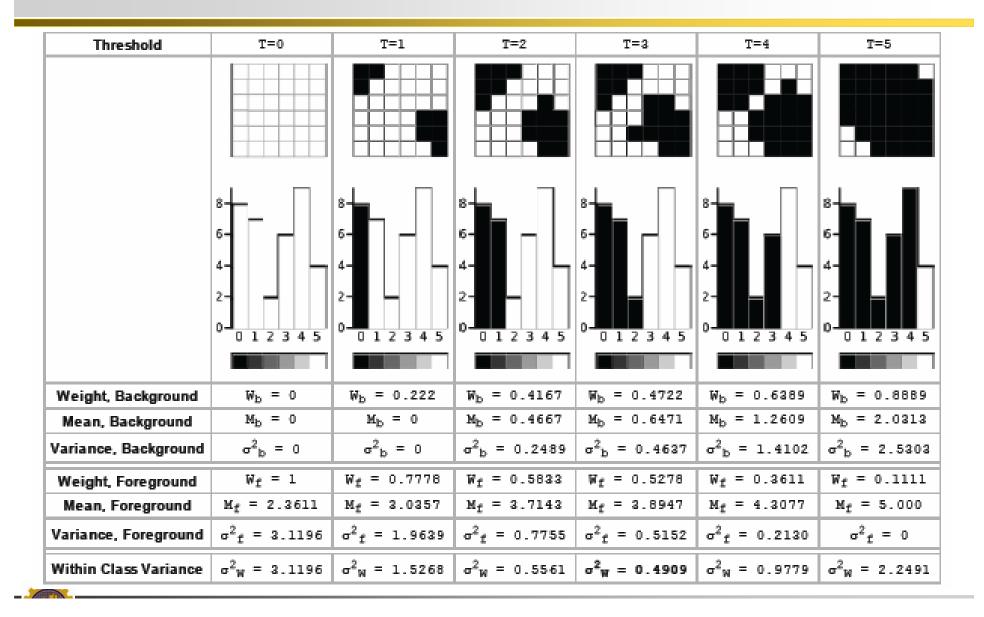


→ The next step is to calculate the *Within-Class Variance* 'i.e. this is simply the sum of the two variances multiplied by their associated weights

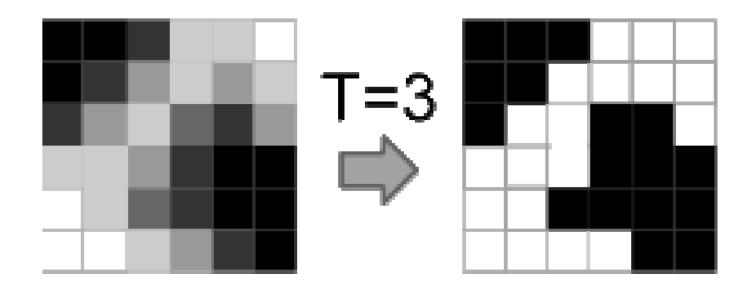
Within Class Variance
$$\sigma_W^2 = W_b \, \sigma_b^2 + W_f \, \sigma_f^2 = 0.4722 * 0.4637 + 0.5278 * 0.5152$$

= 0.4909





Conclusion



Result of Otsu method



Between class variance

Within Class Variance
$$\sigma_W^2 = W_b \, \sigma_b^2 + W_f \, \sigma_f^2$$
 (as seen above)
Between Class Variance $\sigma_B^2 = \sigma^2 - \sigma_W^2$
 $= W_b (\mu_b - \mu)^2 + W_f (\mu_f - \mu)^2$ (where $\mu = W_b \, \mu_b + W_f \, \mu_f$)
 $= W_b \, W_f \, (\mu_b - \mu_f)^2$

Threshold	T=0	T=1	T=2	T=3	T=4	T=5
Within Class Variance	$\sigma^2_{W} = 3.1196$	$\sigma^2_{W} = 1.5268$	$\sigma^2_{W} = 0.5561$	$\sigma_{W}^{2} = 0.4909$	$\sigma^2_{W} = 0.9779$	$\sigma_{W}^{2} = 2.2491$
Between Class Variance	$\sigma^2_B = 0$	$\sigma_B^2 = 1.5928$	$\sigma_B^2 = 2.5635$	$\sigma_B^2 = 2.6287$	$\sigma_B^2 = 2.1417$	$\sigma_B^2 = 0.8705$



