

# Project1

## Information Exposure Maximization

*Evaluator & Heuristic Search*

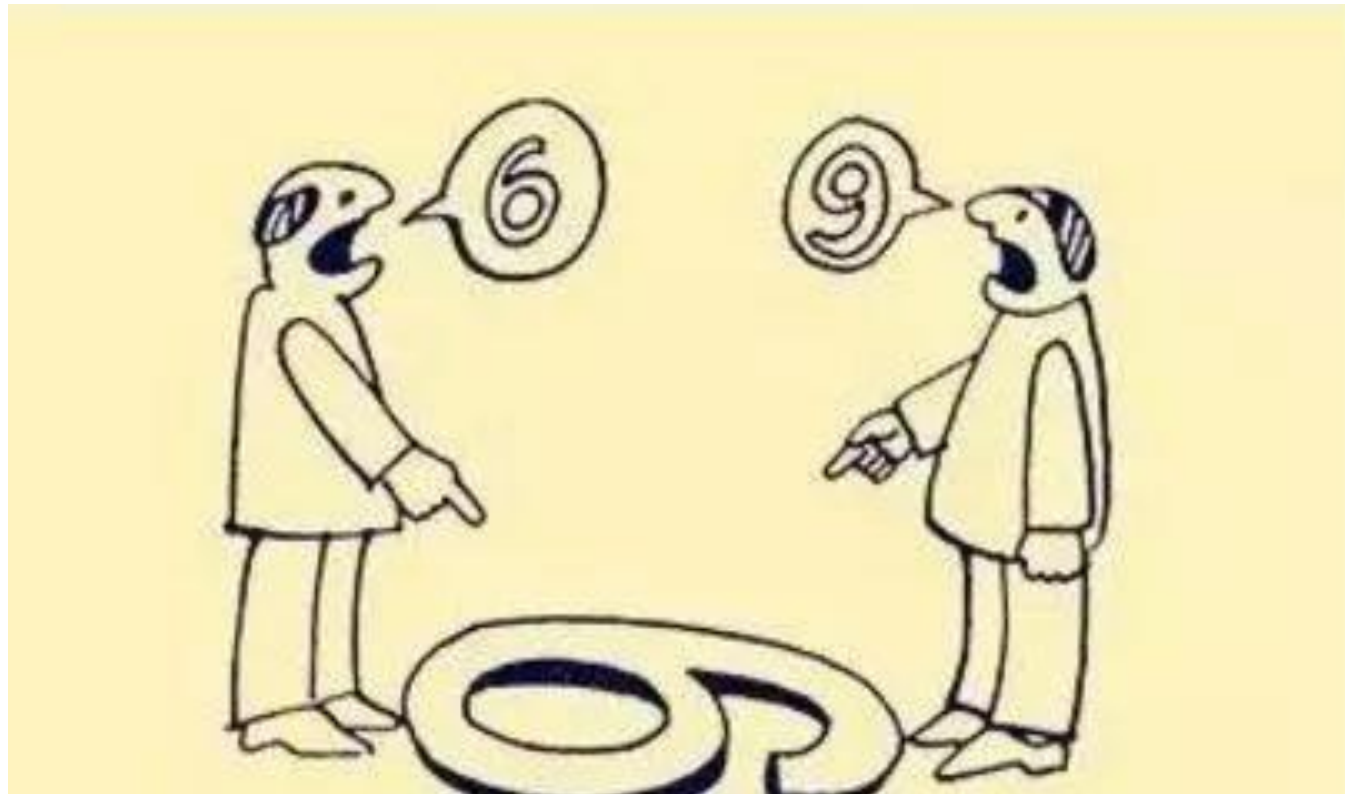
- A brief review of information exposure maximization
- An estimation method for balanced information exposure
- A heuristic algorithm for information exposure maximization
- Summary

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# Brief review of IEM

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- The Information Exposure Maximization (IEM) problem is proposed to solve the echo chamber effect on social media.



# Brief review of IEM

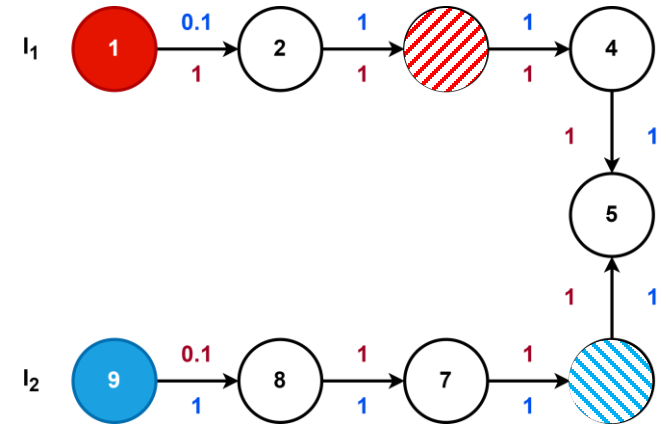
Given a social network  $G = (V, E)$ , two initial seed sets  $I_1$  and  $I_2$ , and a budget  $k$ .

The IEM is **to find two balanced seed sets  $S_1$  and  $S_2$** , where  $|S_1| + |S_2| \leq k$ , and **maximize the balanced information exposure**, i.e.,

$$\max \Phi(S_1, S_2) = \max \mathbb{E}[|V \setminus (r_1(I_1 \cup S_1) \triangle r_2(I_2 \cup S_2))|]$$

$$\text{s. t. } |S_1| + |S_2| \leq k$$

$$S_1, S_2 \subseteq V$$



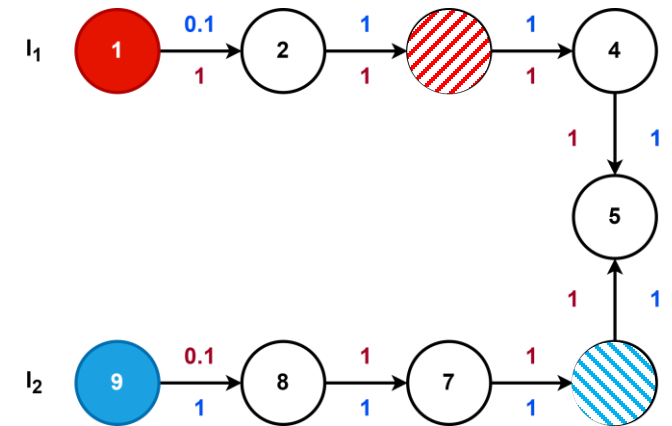
# Brief review of IEM

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$$\max \Phi(S_1, S_2) = \max \mathbb{E}[|V \setminus (r_1(I_1 \cup S_1) \Delta r_2(I_2 \cup S_2))|]$$

Both are **random variables** determined by the stochastic process of the diffusion model and their diffusion probabilities



- Finding an optimal solution of IEM is NP-hard.
- Computing the balanced information exposure for a given solution is NP-hard.

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## Monte Carlo simulation

- A computational algorithm that uses **repeated random sampling** to obtain the likelihood of a range of results of occurring

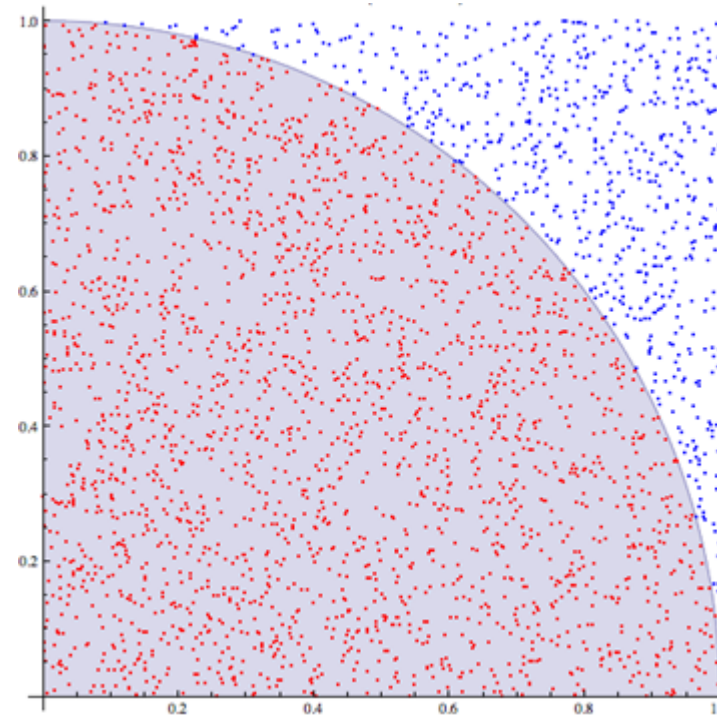


## Monte Carlo simulation

- A computational algorithm that uses **repeated random sampling** to obtain the likelihood of a range of results of occurring

Example2:Estimate  $\pi$

As shown in the figure, if  $n=3000$  points are randomly generated in the square region of  $1*1$ , 2375 points are obtained in the quarter circle with radius 1, then the value of  $\pi$  can be evaluated as?

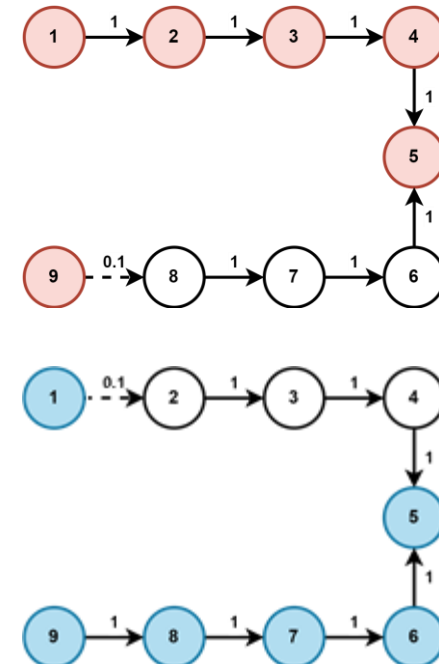
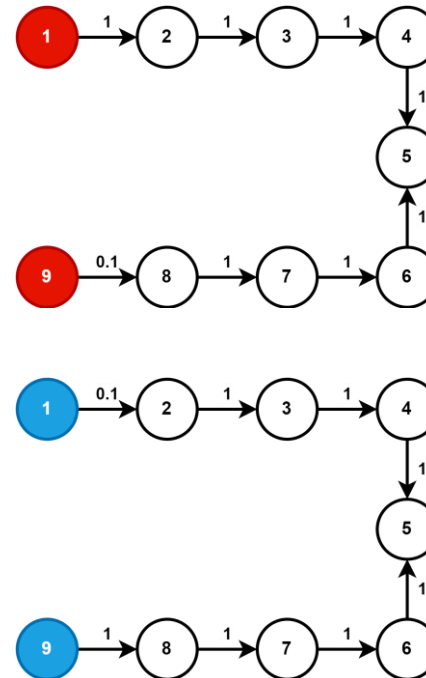


## Monte Carlo simulation

- A computational algorithm that uses **repeated random sampling** to obtain the likelihood of a range of results of occurring

Estimate balanced  
information exposure:

$$\begin{aligned}\Phi_{g \sim G}(S_1, S_2) \\ &= |V \setminus (r_1(I_1 \cup S_1) \triangle r_2(I_2 \cup S_2))|_g \\ &= |\{1, 2, 5, 8, 9\}| = 5\end{aligned}$$



## Monte Carlo simulation

- A computational algorithm that uses **repeated random sampling** to obtain the likelihood of a range of results of occurring

Estimate balanced  
information exposure:

$$\max \Phi(S_1, S_2) = \max \mathbb{E}[|V \setminus (r_1(I_1 \cup S_1) \triangle r_2(I_2 \cup S_2))|]$$



$$\hat{\Phi}(S_1, S_2) = \frac{\sum_{i=1}^N \Phi_{g_i}(S_1, S_2)}{N}$$

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## Greedy best-first search

- Main idea: expand the node with the largest  $h(v)$  value

$h(v)$  = increment to the balanced information exposure

### Algorithm: Greedy best-first search

$S_1 \leftarrow S_2 \leftarrow \emptyset;$

while  $|S_1| + |S_2| \leq k$  do

$v_1^* \leftarrow \arg \max_v (\Phi(S_1 \cup \{v\}, S_2) - \Phi(S_1, S_2));$

$v_2^* \leftarrow \arg \max_v (\Phi(S_1, S_2 \cup \{v\}) - \Phi(S_1, S_2));$

add the better option between  $\langle v_1^*, \emptyset \rangle$  and  $\langle \emptyset, v_2^* \rangle$  to  $\langle S_1, S_2 \rangle$  while respecting the budget.

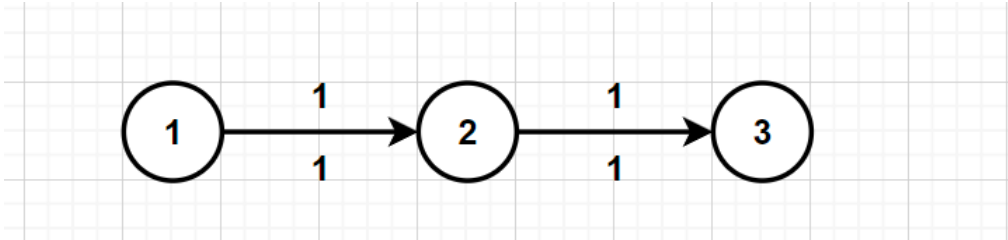
# Heuristic algorithm for IEM

## Greedy best-first search

Input:

$$I_1 = \{1\}, I_2 = \{3\}, k = 2$$

Network  $G = (V, E)$



Iteration 1:

$$I_1 = \{1\}, I_2 = \{3\}, S_1 = S_2 = \{\}$$

Step1: Find  $v_1^*$ :

$$v = 1, U_1 = \{1\}, U_2 = \{3\}, E_1 = \{1, 2, 3\}, E_2 = \{3\}, \Phi = 1$$

$$v = 2, U_1 = \{1, 2\}, U_2 = \{3\}, E_1 = \{1, 2, 3\}, E_2 = \{3\}, \Phi = 1$$

$$v = 3, U_1 = \{1, 3\}, U_2 = \{3\}, E_1 = \{1, 2, 3\}, E_2 = \{3\}, \Phi = 1$$

$$v_1^* = 1$$

Step2: Find  $v_2^*$ :

$$v = 1, U_1 = \{1\}, U_2 = \{1, 3\}, E_1 = \{1, 2, 3\}, E_2 = \{1, 2, 3\}, \Phi = 3$$

$$v = 2, U_1 = \{1\}, U_2 = \{2, 3\}, E_1 = \{1, 2, 3\}, E_2 = \{2, 3\}, \Phi = 2$$

$$v = 3, U_1 = \{1\}, U_2 = \{3\}, E_1 = \{1, 2, 3\}, E_2 = \{3\}, \Phi = 1$$

$$v_2^* = 1$$

Step3: add the better option between  $\langle v_1^*, \emptyset \rangle$  and  $\langle \emptyset, v_2^* \rangle$  to  $\langle S_1, S_2 \rangle$

$$\langle \{\}, \{\} \rangle \rightarrow \langle \{\}, \{1\} \rangle$$

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- Information exposure maximization is computationally complex
- **Monte Carlo simulations** for balanced information exposure estimation
- **Greedy best-first search** to find balanced seed sets
- **Improvements in solution quality or computing efficiency are encouraged**