# **Hashing**

- Associative Indexing
- Hashing
- Hash Table ADT
- Hash Functions
- Problems with Hashing

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## Associative Indexing

Regular array indexing is positional ([0], [1], [2], ...):

- can access items by their position in an array
- but generally don't know position for an item with key K
- we need to search for the item in the collection using K
- search can be linear (O(n)) or binary (O(log<sub>2</sub>n))

An alternative approach to indexing:

- use the key value as an index ... no searching needed
- access data for item with key K as array [K]

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## ... Associative Indexing

#### Difference between positional and associative indexing:

Positional (normal) indexing

	[0]	[1]	[2]	[3]	[4]	
courses[]	data about COMP1511	data about COMP1521	data about COMP1531	data about COMP2511	data about COMP2521	

courses [4] gives access to COMP2521 data

Associative indexing

["COMP2521"] ["COMP1511"] ["COMP1521"] ["COMP1531"] ["COMP2511"] data about data about data about data about data about courses[] COMP1511 COMP1521 COMP1531 COMP2511 COMP2521

courses ["COMP2521"] gives access to COMP2521 data

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## Hashing

Hashing allows us to get close to associative indexing

Ideally, we would like ...

```
courses["COMP3311"] = "Database Systems";
printf("%s\n", courses["COMP3311"]);
```

but C doesn't have non-integer index values.

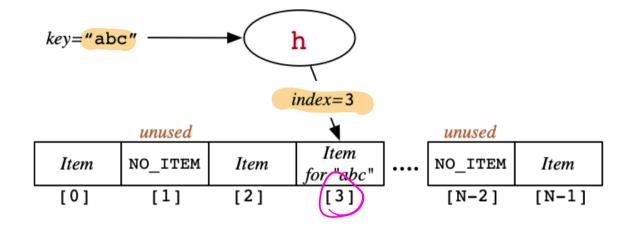
Something almost as good:

Hash function **h** converts key to integer and uses that as the index.

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# ... Hashing

What the h (hash) function does



Converts a key value (of any type) into an integer index.

Sounds good ... in practice, not so simple ...

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### ... Hashing

Reminder: what we'd like ...

```
courses[h("COMP3311")] = "Database Systems";
printf("%s\n", courses[h("COMP3311")]);
```

In practice, we do something like ...

```
key = "COMP3311";
item = {"COMP3311", "Database Systems", ...};
courses = HashInsert(courses, key, item);
printf("%s\n", HashGet(courses, "COMP3311"));
```

## ... Hashing

To use arbitrary values as keys, we need ...

- set of **Key** values *dom*(**Key**), each key identifies one **Item**
- an array (of size N) to store Items
- a hash function h() of type  $dom(Key) \rightarrow [0..N-1]$ 
  - requirement: if (x = y) then h(x) = h(y)
  - $\circ$  requirement: h(x) always returns same value for given x

A problem: array is size N, but  $dom(Key) \gg N$ 

So, we also need a collision resolution method

index

• collision =  $(x \neq y \text{ but } h(x) = h(y))$ 

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. Many keys -> bre onder

#### Hash Table ADT

Generalised ADT for a collection of **Items** 

Interface:

```
typedef struct CollectionRep *Collection;

Collection newCollection();  // make new empty collection
Item *search(Collection, Key); // find item with key
void insert(Collection, Item); // add item into collection
void delete(Collection, Key); // drop item with key
```

Implementation:

```
typedef struct CollectionRep {
    ... some data structure to hold multiple Items ...
} CollectionRep;
```

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#### ... Hash Table ADT

For hash tables, make one change to "standard" Collection interface:

```
typedef struct HashTabRep *HashTable;
// make new empty table of size N
HashTable newHashTable(int);
// add item into collection
void HashInsert(HashTable, Item);
// find item with key
Item *HashGet(HashTable, Key);
// drop item with key
void HashDelete(HashTable, Key);
// free memory of a HashTable
void dropHashTable(HashTable);
```

i.e. we specify max # elements that can be stored in the collection

#### ... Hash Table ADT

Example hash table implementation:

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#### ... Hash Table ADT

Hash table implementation (cont)

```
void HashInsert(HashTable(ht) Item it) {
   int h = hash(key(it), ht->N);
   // assume table slot empty!?
   ht->items[h] = copy(it);
   ht->nitems++;
}
Item *HashGet(HashTable ht, Key k) {
   int h = hash(k, ht->N);
   Item *itp = ht->items[h];
   if (itp != NULL) && equal(key(*itp),k))
      return itp;
   else
      return NULL;
}
```

key() and copy() come from Item type; equal() from Key type

#### ❖ ... Hash Table ADT

Hash table implementation (cont)

```
void HashDelete(HashTable ht, Key k) {
  int h = hash(k, ht->N);
  Item *itp = ht->items[h];
  if (itp != NULL && equal(key(*itp),k)) {
    free(itp);
    ht->items[h] = NULL;
    ht->nitems--;
  }
}
void dropHashTable(HashTable ht) {
  for (int i = 0; i < ht->N; i++) {
    if (ht->items[i] != NULL) free(ht->items[i]);
  }
  free(ht);
}
```

#### << ^ >>

#### Hash Functions

#### Characteristics of hash functions:

- converts Key value to index value [0..N-1]
- deterministic (key value k always maps to same value)
- use mod function to map hash value to index value
- spread key values uniformly over address range
   (assumes that keys themselves are uniformly distributed) \(\mathcal{\times}\)
- as much as possible,  $h(k) \neq h(j)$  if  $j \neq k$
- cost of computing hash function must be cheap

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#### ... Hash Functions

Basic mechanism of hash functions:

```
int hash(Key key, int N)
{
  int val = convert key to 32-bit int;
  return val % N;
}
```

If keys are ints, conversion is easy (identity function)

How to convert keys which are strings? (e.g. "COMP1927" or "John")

Definitely prefer that  $hash("cat",N) \neq hash("dog",N)$ 

Prefer that hash("cat",N) ≠ hash("act",N) ≠ hash("tac",N)

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## ... Hash Functions

Universal hashing uses entire key, with position info:

```
int hash(char *key, int N)
{
  int h = 0, a = 31415, b = 21783;
  char *c;
  for (c = key; *c != '\0'; c++) {
    a = a*b % (N-1);
    h = (a * h + *c) % N;
  }
  return h;
}
```

Has some similarities with RNG. Aim: "spread" hash values over [0..N-1]

#### ... Hash Functions

A real hash function (from PostgreSQL DBMS):

```
hash any(unsigned char *k, register int keylen, int N)
   register uint32 a, b, c, len;
   // set up internal state
   len = keylen;
   a = b = 0x9e3779b9;
   c = 3923095;
   // handle most of the key, in 12-char chunks
  while (len \geq= 12) {
      a += (k[0] + (k[1] << 8) + (k[2] << 16) + (k[3] << 24));
      b += (k[4] + (k[5] << 8) + (k[6] << 16) + (k[7] << 24));
      c += (k[8] + (k[9] << 8) + (k[10] << 16) + (k[11] << 24));
     mix(a, b, c);
      k += 12; len -= 12;
   }
   // collect any data from remaining bytes into a,b,c
  mix(a, b, c);
  return c % N;
```

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#### ... Hash Functions

Where mix is defined as:

```
#define mix(a,b,c) \

a -= b; a -= c; a ^= (c>>13); \
b -= c; b -= a; b ^= (a<<8); \
c -= a; c -= b; c ^= (b>>13); \
a -= b; a -= c; a ^= (c>>12); \
b -= c; b -= a; b ^= (a<<16); \
c -= a; c -= b; c ^= (b>>5); \
a -= b; a -= c; a ^= (c>>3); \
b -= c; b -= a; b ^= (a<<10); \
c -= a; c -= b; c ^= (b>>15); \
}
```

i.e. scrambles all of the bits from the bytes of the key value

#### <<

## Problems with Hashing

In ideal scenarios, search cost in hash table is O(1).

Problems with hashing:

- hash function relies on size of array (⇒can't expand)
  - changing size of array effectively changes the hash function
  - if change array size, then need to re-insert all Items
- items are stored in (effectively) random order
- if size(KeySpace) » size(IndexSpace), collisions inevitable
  - collision: k≠j && hash(k,N) = hash(j,N)
- if nitems > nslots, collisions inevitable

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