

1. The better approach to choose the range in the bisection can be looping through values from  $x=-R$  to  $x=R$  in small steps. After iterating in the interval  $[x, x+step]$  we'll check if  $f(x)*f(x+steps)<0$ . If yes, then we found the interval that contains a root. This is a better approach because it will take approximately 0.01 second in search but it will reduce the time and iteration for bisection.

Lets take an example,

$$f(x)=x^3-x-2$$

Instead of guessing the range, we automatically search for the root. We'll walk along the x-axis from  $x = -10$  to  $x = 10$ , in small steps (like 0.5). Between  $x = 1.5$  and  $x = 2.0$ , the value of  $f(x)$  changes sign (from negative to positive). That means there's a root in between.

Method	Search Time	Iterations	Total Time
Traditional	0.0s	14	0.07s
Better Method	0.01s	10	$0.01 + (10 \times 0.005) = 0.06s$

If checking between  $-10$  to  $10$  fails, and the root lies outside that range, then if we take bigger range like  $-100$  to  $100$  it'll also take less time and iteration from traditional method. So, we can say that it is a better approach.