## **Quantitative Economics**

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University of Warsaw

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Office Hours: by appointment

Course Description This course is a comprehensive introduction to quantitative methods used in modern economics. There are two main parts of the course. In the first part we discuss elementary topics in numerical analysis with applications to statistics, econometrics and economics. In the second part we will focus on recursive methods for solving sequential decision problems. The emphasis will be mostly on tools, techniques and theories used by macroeconomists. We will analyze consumption-savings problems, income dynamics and wealth inequality in partial and general equilibrium. To confront our models with the data we will solve them on a computer and compare their predictions with empirical regularities. Time permitting, we will also cover a range of other tools and techniques used in modern macroeconomics, primarily in models of business cycles.

We will make extensive use of mathematics, numerical methods and computer programming. There is a heavy theoretical component: this course provides basic background in dynamic programming techniques (Bellman equation) frequently used in modern economics. We will also study economic theory related to consumption, savings, wealth and income distributions. There is also a heavy computational component: we will study numerical methods and learn to apply them in various settings.

We will use Julia, a modern, open source, high productivity language primarily used in technical and scientific computing. No prior knowledge of Julia is needed as a brief introduction to this language and example code will be provided.

Students who do not find such a quantitative, computational approach to economics appealing, are strongly advised against taking this course.

## **Outline:**

- 1. Programming in Julia.
- 2. Efficient and reproducible workflow: version control, debugging, benchmarking, modules, and packages.

- 3. Elementary concepts in scientific computing.
- 4. Linear and nonlinear (systems of) equations.
- 5. Optimization.
- 6. Function approximation and interpolation.
- 7. Numerical integration and Markov processes.
- 8. Introduction to dynamic programming.
- 9. Discrete Markov decision processes.
- 10. Continuous state models.
- 11. Heterogeneous agent models in macroeconomics.
- 12. Perturbation methods.
- 13. (Stochastic) difference equations and linear rational expectations models.
- 14. Projection methods.

## Requirements

- Problem sets (x4) 50%
- Final project 40%
- Class participation 10%

There will be four problem sets. They will usually ask you to derive some theoretical results and/or implement some extensions of material covered in class on a computer and study their properties. If you wish, you may work on the assignments in groups of up to five students. You can (and you are encouraged to do so) discuss your solutions with other students, even those outside of your group. You must credit the people with whom you have worked on the problem set. You will have two weeks for each problem set. You need to submit your code in Julia as well as a write-up.

There will be also a final project, similar in style to problem sets, but longer and more difficult. Its details will be announced in the last week of classes. You will have three weeks to solve it. You are allowed to work on it in a group of up to five students.

Class attendance and participation will also be rewarded. Sometimes we will assign mandatory readings and you will be cold-called to give a short (5 minutes) summary of them at the beginning of class.

**Materials** There does not exist a single textbook for this course. We will mostly rely on materials posted here. We will also post journal articles. Textbooks which you might find useful to get better understanding of theoretical aspects of the course are:

- Stokey, Lucas and Prescott (1989) Recursive Methods in Economic Dynamics
- Ljungqvist and Sargent (2018) Recursive Macroeconomic Theory
- Sargent and Stachurski (2023) Dynamic Programming Volume I: Foundations
- Jappelli and Pistaferri (2017) The Economics of Consumption

This great book provides a gentle introduction to Julia:

• Kamiński (2023) Julia for Data Analysis

Extra resources related to computation in economics:

- QuantEcon: https://quantecon.org/. The most relevant lectures in the Julia module (https://julia.quantecon.org/intro.html) are Lectures 31-38 and 51.
- Heer and Maussner (2009) Dynamic General Equilibrium Modeling
- Miranda and Fackler (2002) Applied Computational Economics and Finance
- Judd (1998) Numerical Methods in Economics

You can find more details about numerical analysis here:

• Kincaid and Cheney (2009) Numerical Mathematics and Computing