model description

Justin Pomeranz

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Introduction

This model extends that of Zhou et al. 2013 which incorporates continuous predation and seasonal reproduction (typical life history of many aquatic organisms) of a 2-species predator-prey model.

We extend this model to include intraguild predation, in which a basal species B is consumed by two predators C, and P, where P (also called intraguild predator) can also consume C (also called intraguild prey).

Model overview

Assume there are habitat patches, x, located across a landscape. Within each patch, three species may exist. A basal species B, a consumer species C, and a predator species P. In the absence of predation, the basal species population abundance is assumed to grow exponentially to to some population level, K, (logistic growth) based on some characteristic of the habitat patch (i.e. environmental condition, patch size).

The consumer species (also know as the intraguild prey) receives all of its energy from the basal species. The consumer species population varies in direct proportion to the density of B, following a type II functional response (Holling's disk equation). The consumer species is also predated upon by the predator species, P.

The predator species consumes both B and C, and responds to each following a type II functional response.

Dispersal

The model starts with some initial nonzero population abundances for all three species in each patch. First, dispersal from all patches is accounted for. The number of emmigrants, E, for each species from each patch is estimated, Then, the number of emmigrants from patch i is divided into immigrants, I, for each patch j. The likelihood of an individual dispersal from patch i to j declines exponentially with increasing distance from patch i to j.

The probability that an individual disperses can be set with p_dispersal. A single value can be used for all trophic levels, or can be set for each individually.

NOTE

The above formulation uses a single value of dispersal probability $p_{dispersal}$. Might be worth looking at a distribution of probabilities, such as $p_{dispersal} \sim \mathsf{Beta}(\alpha, \beta)$ to add stochasticity to this function.

Predation

After dispersal, continuous predation occurs. The number of prey i eaten by consumer j, W_{ij} , in a season is calculated as:

$$W_{ij} = \frac{\alpha_{ij} N_i N_j}{\beta_{ij} N_j + N_i}$$

where N_i is the population abundance of resource i, N_j is the population abundance of consumer i, and α_{ij} and β_{ij} are coefficients describing the functional response as the ratio of resources to consumers increases. β_{ij} describes how fast the predation curve reaches the asymptote of the type II functional response, and $\frac{\alpha}{\beta}$ determines the location of the asymptote.

The total number of Basal species individual eaten is the sum of the individuals eaten by C and P:

$$W_B = W_{BC} + W_{CP}$$

##Survival

After accounting for predation, the remaining individuals are reduced by the base survival probability:

$$B' = S_0(B - W_B)$$

$$C' = S_0(C - W_{CP})$$

$$P' = S_0P$$

##Reproduction

Finally, those individuals remaining (X_i) reproduce according to the following:

$$B_{t+1} = \frac{r_{max}}{1 + bB'} B'$$

$$C_{t+1} = \frac{e_{bc}\alpha_{bc}B}{\beta_{bc}C + B}C'$$

$$P_{t+1} = \left(\frac{e_{bp}\alpha_{bp}B}{\beta_{bp}P + B} + \frac{e_{cp}\alpha_{cp}C}{\beta_{cp}P + C}\right)P'$$

where r_{max} is the maximum per-capita reproduction rate of the basal species and $b = \frac{r_{max}-1}{K}$ determines the asymptotic relationship of population growth, where K is carrying capacity. In the absence of predation, population growth of the basal species follows a logistic growth relationship. Note the use of X_i in determining the predation effects (terms inside of the parentheses) and X_i' to estimate reproduction in the next generation. This can be viewed as a time lag, which incorporates continuous predation through the season, and synchronous reproduction only for the surviving individuals.

For the consumer species (C and P) the product of $e_{ij}\alpha_{ij}$ is the maximum reproductive rate of consumer j on resource i. The carying capacity of consumer j on resource i is $\frac{N_i(e_{ij}\alpha_{ij}-1)}{\beta_{ij}}$ when N_i is constant

NOTE

The above formulation requires individual parameters for e_{ij} , α_{ij} and β_{ij} for all pairwise combinations (i.e. 3 * $(e + \alpha + \beta) = 9$ parameters).

An alternative formulation assumes one value of e, α and β for both consumers (species C and P) and uses a preference term δ to control the strength of IGP (δ = preference of P for B over C).

I have conducted some brief testing of this using $igp_sim2()$ function, and it seems to work. This may be a simpler model which can display complex dynamics by only adjusting the δ parameter, as opposed to complex arrangements of adjusting the 3 x 3 parameter matrix mentioned above.

However, I'm not sure if only adjusting δ can produce full range of dynamics, and it may be nice to be able to adjust the search rates for individual consumer-resource pairs.

Time t+1

To ensure that the number of individuals in time t+1 is an integer and to include stochasticity in our model, the population abundance for t+1 is drawn from a Poisson distribution:

$$X_i \sim \text{Poisson}(\lambda_i)$$

where λ is a vector of values for each species:

$$\lambda_i = B_{t+1}, C_{t+1}, P_{t+1}$$

Disturbance

We also include a disturbance probability $p_{disturb}$, which determines the probability of a disturbance occurring in patch X at time t. If a disturbance occurs, the abundance of each species is reduced by the value set with $mag_{disturb} = 0.25$ a disturbance in a patch reduces the abundance of all species by 25%.

Disturbance correlation. The correlation value can be set such that if one patch undergoes a disturbance as described above, then patches located nearby (euclidean distance, same branch, etc.) are also more likely to undergo that disturbance. This can be viewed as a flood disturbance through a river branch, or a large storm even across a 2-dimensional landscape. *NOTE*: correlation is not yet implemented.

Resource extinction

An explicit assumption of our model is that the presence of a consumer is dependent on the presence of at least one of its' resources. Therefore, if the population abundance of B is equal to 0 at the beginning of a timestep, we force the abundances of C and P to also equal zero. Note that C and P can become locally extinct and the simulation will continue as normal, and any secondary extinctions are the direct result of trophic dynamics.

FCL: Food Chain Length

There are 5 possible outcomes, and their corresponding food chain lengths

- all species are extinct FCL = 0
- B only FCL = 1
- B + C FCL = 2
- B + P FCL = 2.5
- B + C + P FCL = 3

Environment

The carrying capacity, K, is a function which is determined by ecosystem area (i.e., number of patches upstream) or some environmental condition. If determined by environmental condition, patches can either be randomly assigned a value, or can be spatially auto-correlated, such that nearby patches are more likely to have similar environmental values. *NOTE*: this is a work in progress.

Simulation function igp_sim()

The main function is igp_sim(), which simulates trophic dynamics between three species in patches. By default, the species are classified as basal B, consumer C, and predator P.

A distance matrix describing how patches are oriented spatially can be included with the dist_mat argument, or otherwise patches are assumed to be randomly distributed in a 10x10 square.

Carrying capacity of the basal species can be determined by the k argument. If one value is supplied, it is assumed that carrying capacity is the same for all patches. You can set k for each patch individuals with a a vector of length = n_patch in the k argument. In the **future**, a function will be implemented to calculate carrying capacity based on number of patches upstream, or randomly across all patches (possibly other implementations). r_max controls the maximum reproduction rate for the basal species, B.

The initial population abundances can be st with the n_0 argument. The default is to start B, C and P at (0.8*k, 0.5*k) respectively. If one value is supplied, all three species start at the same value, or a vector of length 3 can be used to set the starting abundances for each individually.

The probability that and individual will disperse from a patch is set with the p_dispersal argument, and can take values from 0 to 1. If one value is supplied it as applied to all three species, otherwise a vector of length 3 can be used to set probabilities for species B, C and P (in that order). The theta argument determines how quickly dispersal ability declines with increasing distance (higher values of theta means individuals will disperse shorter distances). Currently, only one value of theta is applied to all three species.

Trophic dynamics are determined with the arguments eij, alphaij and betaij, where ij describes the relationship between resource i and consumer j. eij refers to the conversion efficiency, and alphaij and betaij are parameters controlling the type II functional response.

The s0 argument controls the base survival probability. Currently it sets the same survival probability for all species.

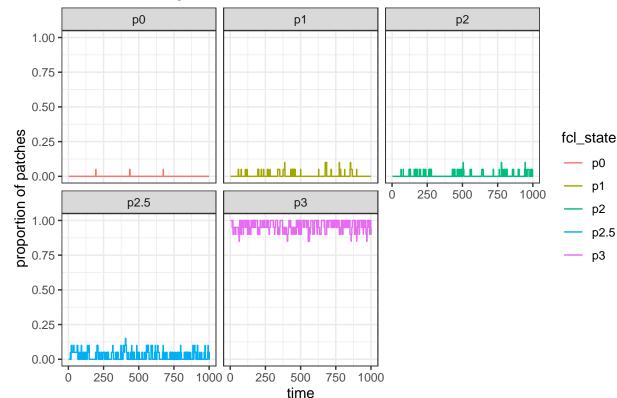
The p_disturb argument sets the probability that any given patch experiences a disturbance in a given time step. This value should be set very low (i.e., 1e-4) due to the high number of rolls in a given simulation n_patch * t. The mag_disturb argument controls the strength of disturbance, and reduces the population of all species to that value. i.e. mag_disturb = 0.25 reduces the population to 25%.

t controls the number of timesteps to run the simulation for.

The plot_{descriptor} arguments control which plots will be displayed.

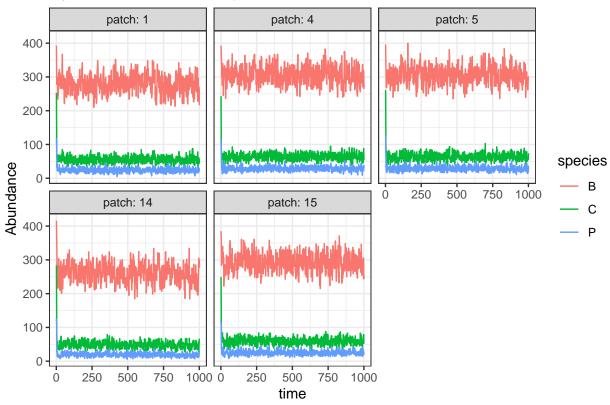
Proportion of patches with food chain length S at each time step:

- ## [1] "No distance matrix supplied, assuming 10x10 square landscape"
- ## [1] "only one value of k supplied, assuming it is the same in all patches"



Dynamics of 5 random patches

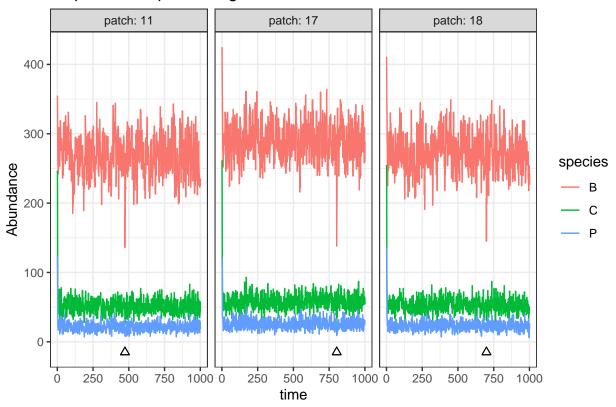
- ## [1] "No distance matrix supplied, assuming 10x10 square landscape"
- ## [1] "only one value of k supplied, assuming it is the same in all patches"



dynamics of all patches which experienced a distrubance: (if no disturbances occur, currently throws an error. Maybe remove this from main function and add it as a separate function to run on the output of $gp_sim()$?)

- ## [1] "No distance matrix supplied, assuming 10x10 square landscape"
- ## [1] "only one value of k supplied, assuming it is the same in all patches"

All patches experiencing disturbances

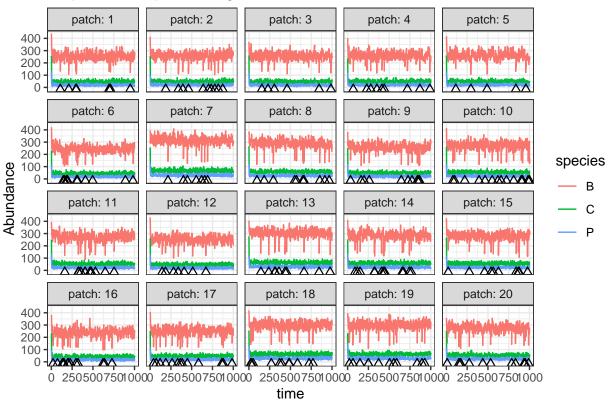


When a disturbance occurs at time step = t, it is displayed with a triangle below the x axis. Increasing the frequency of disturbance makes this clear:

```
## [1] "No distance matrix supplied, assuming 10x10 square landscape"
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^{## [1] &}quot;only one value of k supplied, assuming it is the same in all patches"

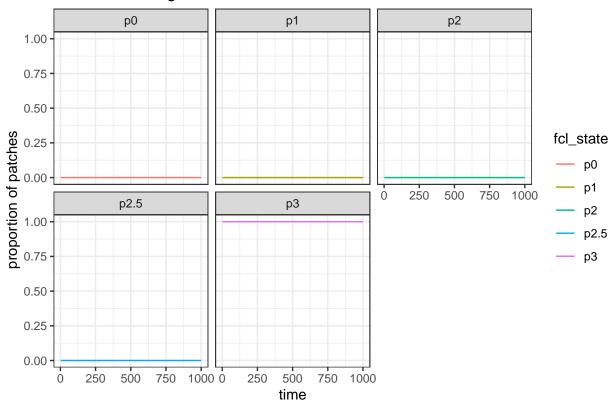




Customize settings

The arguments controlling the trophic dynamics are currently set to maximize stability and coexistence of all three species (parameter values based on the results of Zhou et al. 2013). This can be seen if we turn off dispersal and reduce disturbance probability

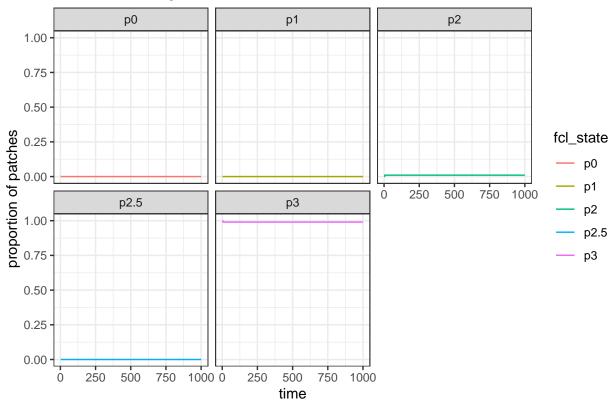
```
## [1] "No distance matrix supplied, assuming 10x10 square landscape"
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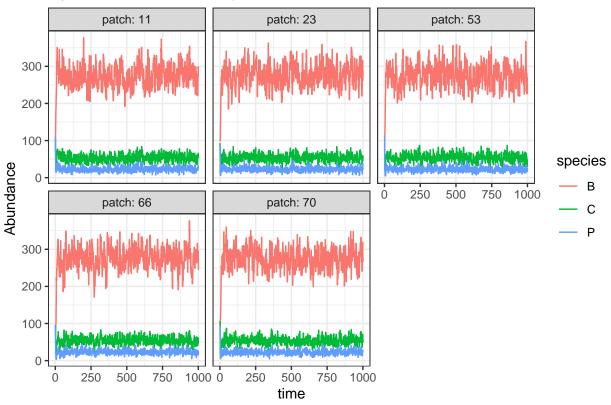


As we can see, the proportion of patches with FCL_state = 3 (all species present) is 100%.

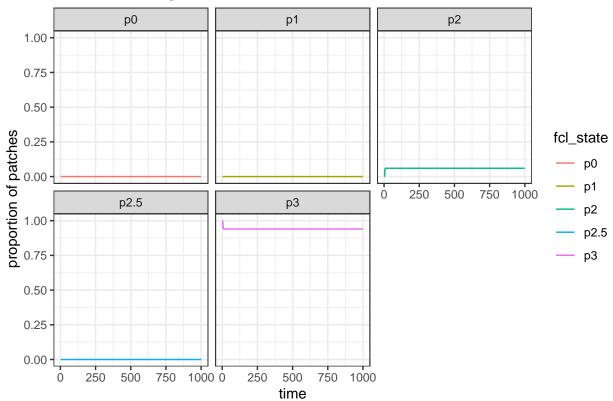
This is relatively insensitive to the starting abundances. (Staring abundances above =400, 250, and 125, respectively.)

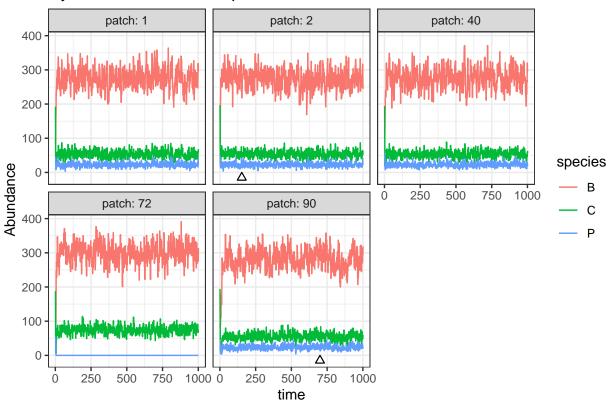
- ## [1] "No distance matrix supplied, assuming 10x10 square landscape"
- ## [1] "only one value of k supplied, assuming it is the same in all patches"





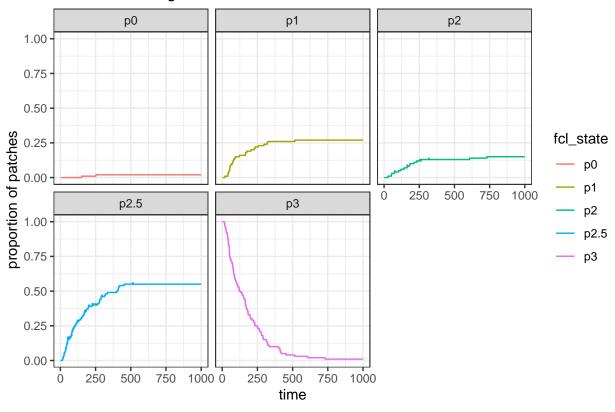
- ## [1] "No distance matrix supplied, assuming 10x10 square landscape"
- ## [1] "only one value of k supplied, assuming it is the same in all patches"





Keeping dispersal and disturbance low, we can modify the strength of the trophic dynamics. A key point that increases stability, is ensuring that C out competes P for their shared resource (weak IGP). We can increase probability of extinction if we make P a stronger competitor

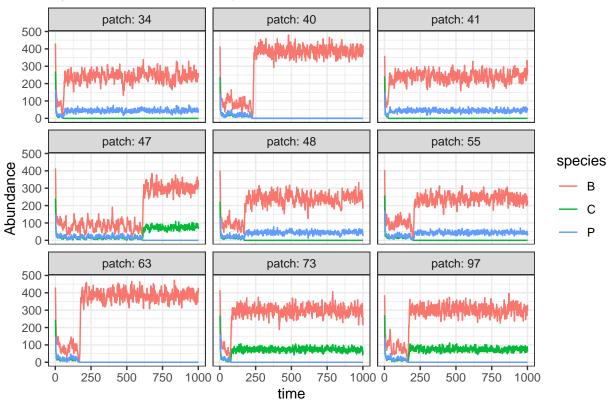
- ## [1] "No distance matrix supplied, assuming 10x10 square landscape"
- ## [1] "only one value of k supplied, assuming it is the same in all patches"



FCL_state = 2.5 -> has species B and P, and C is removed.

Plot of patch dynamics for 9 random patches:

```
set.seed(122)
d$sp_dynamics %>%
filter(patch %in% sample(1:100, 9)) %>%
ggplot(
   aes(y = value,
        x = time,
        color = species))+
geom_line() +
facet_wrap(.~patch, labeller = label_both) +
labs(y = "Abundance",
        title = "Dynamics for 9 random patches") +
theme_bw() +
NULL
```

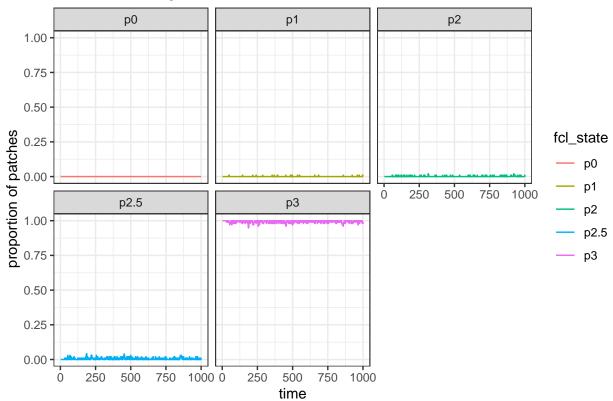


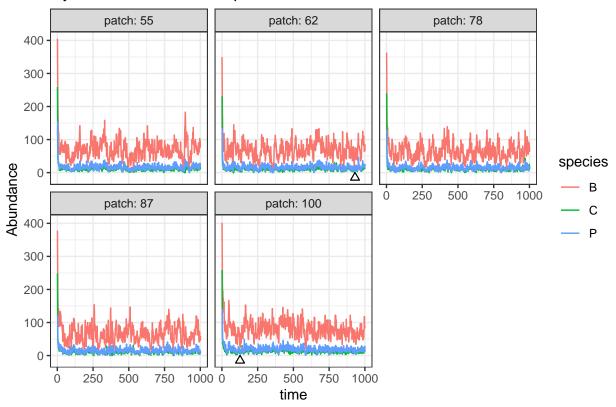
Here we can see that the green species (C) often goes extinct, and the blue species (P) also sometimes goes extinct.

Turning on dispersal

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## [1] "No distance matrix supplied, assuming 10x10 square landscape"
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^{## [1] &}quot;only one value of k supplied, assuming it is the same in all patches"





Dispersal is able to "rescue" most of the patches and returns the mean condition to FCL = 3 (all species present)

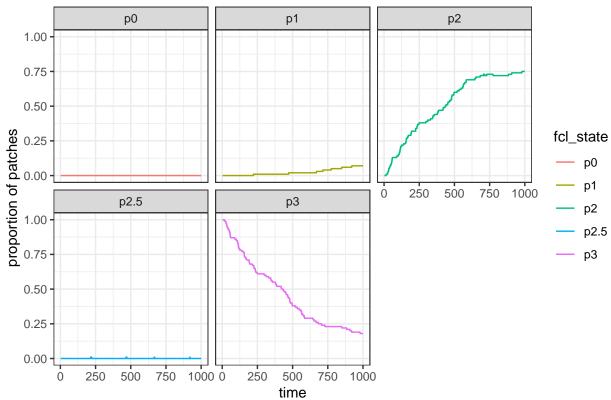
Disturbance

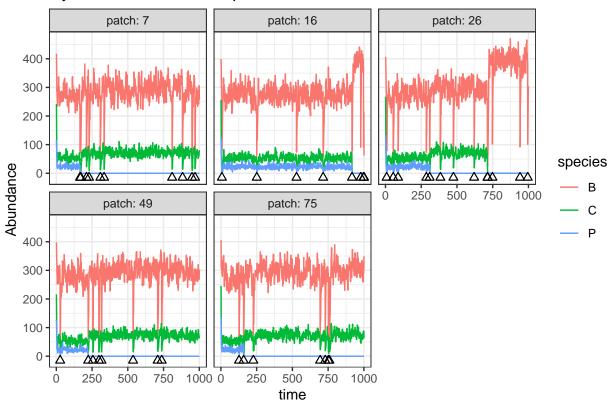
Increasing the frequency and magnitude of disturbance with no dispersal casues many patch extinctions:

```
## [1] "No distance matrix supplied, assuming 10x10 square landscape"
```

^{## [1] &}quot;only one value of k supplied, assuming it is the same in all patches"

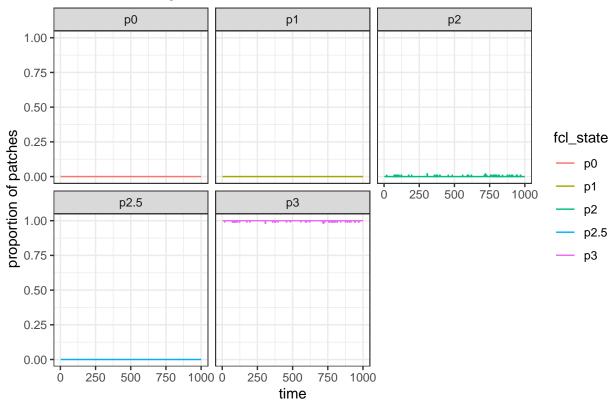


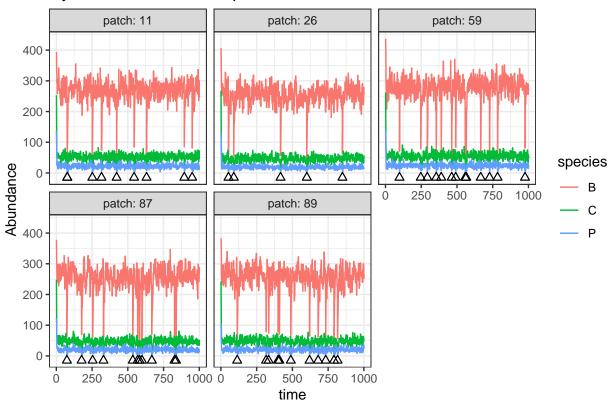




Disturbance + Dispersal

- ## [1] "No distance matrix supplied, assuming 10x10 square landscape"
- ## [1] "only one value of k supplied, assuming it is the same in all patches"





With parameters supporting coexistence and dispersal on, we can see that disturbance generally does not eradicate species (but see how abundance of red generally drops significantly in response to disturbance event (triangle)).

Trophic dynamics, Disturbance, dispersal

Increase alpha (higher reproduction) and decrease beta (higher K) creates chaotic dynamics

```
## [1] "No distance matrix supplied, assuming 10x10 square landscape"
```

^{## [1] &}quot;only one value of k supplied, assuming it is the same in all patches"

