Examination Statistics Prof. Dr. Andersson, Prof. Dr. Falkenberg Course of Study: Computer Sciences 13.2.2018

Name Matriculat	ion Number	: : _										
I hereby confirm that I am physically fit to take the examination.												
Signature student												
	Problems	1	2	3	4	5	Sum	Mark				
	Max. scores	13	9	10	8	9	49		1			
	Obt. scores											

Authorized examinations aids:

Scientific calculator, one english-german dictionary, one file folder

Further instructions:

- 1. Do not use your own paper. Blank paper is attached to this question paper. Extra sheets will be provided on demand.
- 2. Please notice, not only the solution but the deriviation of the solution has to be given.
- 3. Switch off all electronic devices und remove them from the table.

Good Luck!

Dr. Andersson, Dr. Falkenberg

1. The number of miles travelled by a group of engineering salesmen of a company and the corresponding value of orders taken in ten equal time periods is given in the table below.

km travelled	orders taken (Euro'000)
1370	23
1050	17
980	19
1770	22
1340	27
1560	23
2110	30
1540	23
1480	25
1670	19

- (a) Draw a boxplot for the orders taken.
- (b) Describe the relationship between the travelled miles and the value of orders taken by a linear regression.
 - i. Choose an appropriate predictor variable.
 - ii. Interpret the coefficients of the regression line.
 - iii. Which proportion of variation of the criterion variable could be explained by the predictor variable.
 - iv. Determine a predicted value of orders taken if $2500~\mathrm{km}$ are travelled.

- 2. A box contains 8 fair, standard coins (heads and tails) and 1 coin which has heads on both sides. A coin is selected randomly and flipped 4 times.
 - (a) Find the probability of getting all heads.
 - (b) If getting all heads and the coin is flipped again what is the probability that it will be head?
 - (c) Find the probability that the coin is fair resp. unfair if the number of heads is known.

- 3. A snack bar offers a hamburger for 3.50 Euro, a fried sausage for 3 Euro, a sandwich for 2 Euro and fish and chips for 4 Euro. A customer coming to the snack bar orders a hamburger with probability 0.2, a fried sausage with probability 0.35, a sandwich with probability 0.15 and fish and chips with probability 0.3.
 - (a) Find the expected value and the variance of the value of an order.
 - (b) Determine an approximate value for the probability that the sales revenue of 200 orders is bigger than 1000 Euro.
 - (c) Find an approximate value of the 90% quantile of the sales revenue of 200 orders.

Hint: Apply the central limit theorem in question b) and c).

- 4. We have done a survey about the political awareness of the students on our campus. One question was whether the students voted at the last election of the parliaments. The 95% confidence interval based on the data for the unknown proportion of the voters is [0.75; 0.83].
 - (a) Find the proportion of the voters in the sample and the sample size
 - (b) Compute a lower 99% confidence bound for the unknown proportion of the voters.

- 5. An institute published an article stating that approximately 9.5 percent of the adults in the population suffer from a certain disease. Suppose that in a survey of 100 people of a certain town, seven of them suffered from this disease. Conduct a hypothesis test to determine if the true proportion of people suffering from the disease in the town is lower than the percent in the general adult population.
 - (a) State the null hypothesis and the alternative.
 - (b) Find the rejection region of an appropriate test on $\alpha=0.05$ level and conduct the test.
 - (c) Compute the p-value.

Table of the Standard Normal Distribution N(0,1)

	?,?0	?,?1	?,?2	?,?3	?,?4	?,?5	?,?6	?,?7	?,?8	?,?9
0	0.500000	0.503989	0.507978	0.511966	0.515953	0.519939	0.523922	0.527903	0.531881	0.535856
0.1	0.539828	0.543795	0.547758	0.551717	0.555670	0.559618	0.563559	0.567495	0.571424	0.575345
0.2	0.579260	0.583166	0.587064	0.590954	0.594835	0.598706	0.602568	0.606420	0.610261	0.614092
0.3	0.617911	0.621720	0.625516	0.629300	0.633072	0.636831	0.640576	0.644309	0.648027	0.651732
0.4	0.655422	0.659097	0.662757	0.666402	0.670031	0.673645	0.677242	0.680822	0.684386	0.687933
0.5	0.691462	0.694974	0.698468	0.701944	0.705401	0.708840	0.712260	0.715661	0.719043	0.722405
0.6	0.725747	0.729069	0.732371	0.735653	0.738914	0.742154	0.745373	0.748571	0.751748	0.754903
0.7	0.758036	0.761148	0.764238	0.767305	0.770350	0.773373	0.776373	0.779350	0.782305	0.785236
0.8	0.788145	0.791030	0.793892	0.796731	0.799546	0.802337	0.805105	0.807850	0.810570	0.813267
0.9	0.815940	0.818589	0.821214	0.823814	0.826391	0.828944	0.831472	0.833977	0.836457	0.838913
1	0.841345	0.843752	0.846136	0.848495	0.850830	0.853141	0.855428	0.857690	0.859929	0.862143
1.1	0.864334	0.866500	0.868643	0.870762	0.872857	0.874928	0.876976	0.879000	0.881000	0.882977
1.2	0.884930	0.886861	0.888768	0.890651	0.892512	0.894350	0.896165	0.897958	0.899727	0.901475
1.3	0.903200	0.904902	0.906582	0.908241	0.909877	0.911492	0.913085	0.914657	0.916207	0.917736
1.4	0.919243	0.920730	0.922196	0.923641	0.925066	0.926471	0.927855	0.929219	0.930563	0.931888
1.5	0.933193	0.934478	0.935745	0.936992	0.938220	0.939429	0.940620	0.941792	0.942947	0.944083
1.6	0.945201	0.946301	0.947384	0.948449	0.949497	0.950529	0.951543	0.952540	0.953521	0.954486
1.7	0.955435	0.956367	0.957284	0.958185	0.959070	0.959941	0.960796	0.961636	0.962462	0.963273
1.8	0.964070	0.964852	0.965620	0.966375	0.967116	0.967843	0.968557	0.969258	0.969946	0.970621
1.9	0.971283	0.971933	0.972571	0.973197	0.973810	0.974412	0.975002	0.975581	0.976148	0.976705
2	0.977250	0.977784	0.978308	0.978822	0.979325	0.979818	0.980301	0.980774	0.981237	0.981691
2.1	0.982136	0.982571	0.982997	0.983414	0.983823	0.984222	0.984614	0.984997	0.985371	0.985738
2.2	0.986097	0.986447	0.986791	0.987126	0.987455	0.987776	0.988089	0.988396	0.988696	0.988989
2.3	0.989276	0.989556	0.989830	0.990097	0.990358	0.990613	0.990863	0.991106	0.991344	0.991576
2.4	0.991802	0.992024	0.992240	0.992451	0.992656	0.992857	0.993053	0.993244	0.993431	0.993613
2.5	0.993790	0.993963	0.994132	0.994297	0.994457	0.994614	0.994766	0.994915	0.995060	0.995201
2.6	0.995339	0.995473	0.995604	0.995731	0.995855	0.995975	0.996093	0.996207	0.996319	0.996427
2.7	0.996533	0.996636	0.996736	0.996833	0.996928	0.997020	0.997110	0.997197	0.997282	0.997365
2.8	0.997445	0.997523	0.997599	0.997673	0.997744	0.997814	0.997882	0.997948	0.998012	0.998074
2.9	0.998134	0.998193	0.998250	0.998305	0.998359	0.998411	0.998462	0.998511	0.998559	0.998605
3	0.998650	0.998694	0.998736	0.998777	0.998817	0.998856	0.998893	0.998930	0.998965	0.998999
3.1	0.999032	0.999065	0.999096	0.999126	0.999155	0.999184	0.999211	0.999238	0.999264	0.999289
3.2	0.999313	0.999336	0.999359	0.999381	0.999402	0.999423	0.999443	0.999462	0.999481	0.999499
3.3	0.999517	0.999534	0.999550	0.999566	0.999581	0.999596	0.999610	0.999624	0.999638	0.999651
3.4	0.999663	0.999675	0.999687	0.999698	0.999709	0.999720	0.999730	0.999740	0.999749	0.999758
3.5	0.999767	0.999776	0.999784	0.999792	0.999800	0.999807	0.999815	0.999822	0.999828	0.999835
3.6	0.999841	0.999847	0.999853	0.999858	0.999864	0.999869	0.999874	0.999879	0.999883	0.999888
3.7	0.999892	0.999896	0.999900	0.999904	0.999908	0.999912	0.999915	0.999918	0.999922	0.999925
3.8	0.999928	0.999931	0.999933	0.999936	0.999938	0.999941	0.999943	0.999946	0.999948	0.999950
3.9	0.999952	0.999954	0.999956	0.999958	0.999959	0.999961	0.999963	0.999964	0.999966	0.999967
4	0.999968	0.999970	0.999971	0.999972	0.999973	0.999974	0.999975	0.999976	0.999977	0.999978

Quantiles of the Standard Normal Distribution $N(0,1)\ u_p$

	р	X	p	X	р	X
1	0.800	0.8416212	0.950	1.6448536	0.990	2.3263479
2	0.820	0.9153651	0.955	1.6953977	0.991	2.3656181
3	0.840	0.9944579	0.960	1.7506861	0.992	2.4089155
4	0.860	1.0803193	0.965	1.8119107	0.993	2.4572634
5	0.880	1.1749868	0.970	1.8807936	0.994	2.5121443
6	0.900	1.2815516	0.975	1.9599640	0.995	2.5758293
7	0.920	1.4050716	0.980	2.0537489	0.996	2.6520698
8	0.940	1.5547736	0.985	2.1700904	0.997	2.7477814
9	0.960	1.7506861	0.990	2.3263479	0.998	2.8781617
10	0.980	2.0537489	0.995	2.5758293	0.999	3.0902323

Quantiles of the t_n -Distribution $t_{n,p}$

	p=0.6	p = 0.65	p=0.7	p = 0.75	p=0.8	p = 0.85	p=0.9	p = 0.95	p = 0.96	p = 0.97	p=0.975	p = 0.98	p=0.985	p = 0.99	p=0.995	p=0.999	p=0.9995
1	0.3249	0.5095	0.7265	1.0000	1.3764	1.9626	3.0777	6.3138	7.9158	10.5789	12.7062	15.8945	21.2049	31.8205	63.6567	318.3088	636.6192
2	0.2887	0.4447	0.6172	0.8165	1.0607	1.3862	1.8856	2.9200	3.3198	3.8964	4.3027	4.8487	5.6428	6.9646	9.9248	22.3271	31.5991
3	0.2767	0.4242	0.5844	0.7649	0.9785	1.2498	1.6377	2.3534	2.6054	2.9505	3.1824	3.4819	3.8960	4.5407	5.8409	10.2145	12.9240
4	0.2707	0.4142	0.5686	0.7407	0.9410	1.1896	1.5332	2.1318	2.3329	2.6008	2.7764	2.9985	3.2976	3.7469	4.6041	7.1732	8.6103
5	0.2672	0.4082	0.5594	0.7267	0.9195	1.1558	1.4759	2.0150	2.1910	2.4216	2.5706	2.7565	3.0029	3.3649	4.0321	5.8934	6.8688
6	0.2648	0.4043	0.5534	0.7176	0.9057	1.1342	1.4398	1.9432	2.1043	2.3133	2.4469	2.6122	2.8289	3.1427	3.7074	5.2076	5.9588
7	0.2632	0.4015	0.5491	0.7111	0.8960	1.1192	1.4149	1.8946	2.0460	2.2409	2.3646	2.5168	2.7146	2.9980	3.4995	4.7853	5.4079
8	0.2619	0.3995	0.5459	0.7064	0.8889	1.1081	1.3968	1.8595	2.0042	2.1892	2.3060	2.4490	2.6338	2.8965	3.3554	4.5008	5.0413
9	0.2610	0.3979	0.5435	0.7027	0.8834	1.0997	1.3830	1.8331	1.9727	2.1504	2.2622	2.3984	2.5738	2.8214	3.2498	4.2968	4.7809
10	0.2602	0.3966	0.5415	0.6998	0.8791	1.0931	1.3722	1.8125	1.9481	2.1202	2.2281	2.3593	2.5275	2.7638	3.1693	4.1437	4.5869
11	0.2596	0.3956	0.5399	0.6974	0.8755	1.0877	1.3634	1.7959	1.9284	2.0961	2.2010	2.3281	2.4907	2.7181	3.1058	4.0247	4.4370
12	0.2590	0.3947	0.5386	0.6955	0.8726	1.0832	1.3562	1.7823	1.9123	2.0764	2.1788	2.3027	2.4607	2.6810	3.0545	3.9296	4.3178
13	0.2586	0.3940	0.5375	0.6938	0.8702	1.0795	1.3502	1.7709	1.8989	2.0600	2.1604	2.2816	2.4358	2.6503	3.0123	3.8520	4.2208
14	0.2582	0.3933	0.5366	0.6924	0.8681	1.0763	1.3450	1.7613	1.8875	2.0462	2.1448	2.2638	2.4149	2.6245	2.9768	3.7874	4.1405
15	0.2579	0.3928	0.5357	0.6912	0.8662	1.0735	1.3406	1.7531	1.8777	2.0343	2.1314	2.2485	2.3970	2.6025	2.9467	3.7328	4.0728
16	0.2576	0.3923	0.5350	0.6901	0.8647	1.0711	1.3368	1.7459	1.8693	2.0240	2.1199	2.2354	2.3815	2.5835	2.9208	3.6862	4.0150
17	0.2573	0.3919	0.5344	0.6892	0.8633	1.0690	1.3334	1.7396	1.8619	2.0150	2.1098	2.2238	2.3681	2.5669	2.8982	3.6458	3.9651
18	0.2571	0.3915	0.5338	0.6884	0.8620	1.0672	1.3304	1.7341	1.8553	2.0071	2.1009	2.2137	2.3562	2.5524	2.8784	3.6105	3.9216
19	0.2569	0.3912	0.5333	0.6876	0.8610	1.0655	1.3277	1.7291	1.8495	2.0000	2.0930	2.2047	2.3456	2.5395	2.8609	3.5794	3.8834
20	0.2567	0.3909	0.5329	0.6870	0.8600	1.0640	1.3253	1.7247	1.8443	1.9937	2.0860	2.1967	2.3362	2.5280	2.8453	3.5518	3.8495
21	0.2566	0.3906	0.5325	0.6864	0.8591	1.0627	1.3232	1.7207	1.8397	1.9880	2.0796	2.1894	2.3278	2.5176	2.8314	3.5272	3.8193
22	0.2564	0.3904	0.5321	0.6858	0.8583	1.0614	1.3212	1.7171	1.8354	1.9829	2.0739	2.1829	2.3202	2.5083	2.8188	3.5050	3.7921
23	0.2563	0.3902	0.5317	0.6853	0.8575	1.0603	1.3195	1.7139	1.8316	1.9782	2.0687	2.1770	2.3132	2.4999	2.8073	3.4850	3.7676
24	0.2562	0.3900	0.5314	0.6848	0.8569	1.0593	1.3178	1.7109	1.8281	1.9740	2.0639	2.1715	2.3069	2.4922	2.7969	3.4668	3.7454
25	0.2561	0.3898	0.5312	0.6844	0.8562	1.0584	1.3163	1.7081	1.8248	1.9701	2.0595	2.1666	2.3011	2.4851	2.7874	3.4502	3.7251
26	0.2560	0.3896	0.5309	0.6840	0.8557	1.0575	1.3150	1.7056	1.8219	1.9665	2.0555	2.1620	2.2958	2.4786	2.7787	3.4350	3.7066
27	0.2559	0.3894	0.5306	0.6837	0.8551	1.0567	1.3137	1.7033	1.8191	1.9632	2.0518	2.1578	2.2909	2.4727	2.7707	3.4210	3.6896
28	0.2558	0.3893	0.5304	0.6834	0.8546	1.0560	1.3125	1.7011	1.8166	1.9601	2.0484	2.1539	2.2864	2.4671	2.7633	3.4082	3.6739
29	0.2557	0.3892	0.5302	0.6830	0.8542	1.0553	1.3114	1.6991	1.8142	1.9573	2.0452	2.1503	2.2822	2.4620	2.7564	3.3962	3.6594
30	0.2556	0.3890	0.5300	0.6828	0.8538	1.0547	1.3104	1.6973	1.8120	1.9546	2.0423	2.1470	2.2783	2.4573	2.7500	3.3852	3.6460
40	0.2550	0.3881	0.5286	0.6807	0.8507	1.0500	1.3031	1.6839	1.7963	1.9357	2.0211	2.1229	2.2503	2.4233	2.7045	3.3069	3.5510
50	0.2547	0.3875	0.5278	0.6794	0.8489	1.0473	1.2987	1.6759	1.7870	1.9244	2.0086	2.1087	2.2338	2.4033	2.6778	3.2614	3.4960
60	0.2545	0.3872	0.5272	0.6786	0.8477	1.0455	1.2958	1.6706	1.7808	1.9170	2.0003	2.0994	2.2229	2.3901	2.6603	3.2317	3.4602
70	0.2543	0.3869	0.5268	0.6780	0.8468	1.0442		1.6669	1.7765	1.9118	1.9944	2.0927	2.2152	2.3808	2.6479	3.2108	3.4350
80	0.2542	0.3867	0.5265	0.6776	0.8461	1.0432			1.7732	1.9078	1.9901	2.0878	2.2095	2.3739	2.6387	3.1953	3.4163
90	0.2541	0.3866	0.5263	0.6772	0.8456	1.0424		1.6620	1.7707	1.9048	1.9867	2.0839	2.2050	2.3685	2.6316	3.1833	3.4019
100	0.2540	0.3864	0.5261	0.6770	0.8452	1.0418	1.2901	1.6602	1.7687	1.9024	1.9840	2.0809	2.2015	2.3642	2.6259	3.1737	3.3905
200	0.2537	0.3859	0.5252	0.6757	0.8434	1.0391	1.2858	1.6525	1.7596	1.8915	1.9719	2.0672	2.1857	2.3451	2.6006	3.1315	3.3398
300	0.2536	0.3857	0.5250	0.6753	0.8428	1.0382	1.2844	1.6499	1.7566	1.8879	1.9679	2.0627	2.1805	2.3388	2.5923	3.1176	3.3233
400	0.2535	0.3856	0.5248	0.6751	0.8425	1.0378	1.2837	1.6487	1.7551	1.8861	1.9659	2.0605	2.1779	2.3357	2.5882	3.1107	3.3150
500	0.2535	0.3855	0.5247	0.6750	0.8423	1.0375	1.2832	1.6479	1.7543	1.8851	1.9647	2.0591	2.1763	2.3338	2.5857	3.1066	3.3101
∞	0.2533	0.3853	0.5244	0.6745	0.8416	1.0364	1.2816	1.6449	1.7507	1.8808	1.9600	2.0537	2.1701	2.3263	2.5758	3.0902	3.2905

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Quantiles of the χ_n^2 -Distribution $\chi_{n,p}$

	p=0.005	p=0.01	p=0.015	p=0.02	p=0.025	p=0.05	p=0.1	p = 0.5	p = 0.9	p=0.95	p=0.975	p=0.98	p=0.985	p=0.99	p=0.995
1	0.000	0.000	0.000	0.001	0.001	0.004	0.016	0.455	2.706	3.841	5.024	5.412	5.916	6.635	7.879
2	0.010	0.020	0.030	0.040	0.051	0.103	0.211	1.386	4.605	5.991	7.378	7.824	8.399	9.210	10.597
3	0.072	0.115	0.152	0.185	0.216	0.352	0.584	2.366	6.251	7.815	9.348	9.837	10.465	11.345	12.838
4	0.207	0.297	0.368	0.429	0.484	0.711	1.064	3.357	7.779	9.488	11.143	11.668	12.339	13.277	14.860
5	0.412	0.554	0.662	0.752	0.831	1.145	1.610	4.351	9.236	11.070	12.833	13.388	14.098	15.086	16.750
6	0.676	0.872	1.016	1.134	1.237	1.635	2.204	5.348	10.645		14.449	15.033	15.777	16.812	18.548
7	0.989	1.239	1.418	1.564	1.690	2.167	2.833	6.346	12.017		16.013	16.622	17.398	18.475	20.278
8	1.344	1.646	1.860	2.032	2.180	2.733	3.490	7.344	13.362		17.535	18.168	18.974	20.090	21.955
9	1.735	2.088	2.335	2.532	2.700	3.325	4.168	8.343		16.919	19.023	19.679	20.513	21.666	23.589
10	2.156	2.558	2.837	3.059	3.247	3.940	4.865		15.987		20.483	21.161	22.021	23.209	25.188
11	2.603	3.053	3.363	3.609	3.816	4.575	5.578				21.920		23.503	24.725	26.757
12	3.074	3.571	3.910	4.178	4.404	5.226	6.304				23.337	24.054	24.963	26.217	28.300
13	3.565	4.107	4.476	4.765	5.009	5.892	7.042				24.736	25.472	26.403	27.688	29.819
14	4.075	4.660	5.057	5.368	5.629	6.571	7.790		21.064		26.119	26.873	27.827	29.141	31.319
15	4.601	5.229	5.653	5.985	6.262	7.261	8.547	14.339	22.307	24.996	27.488	28.259	29.235	30.578	32.801
16	5.142	5.812	6.263	6.614	6.908	7.962	9.312		23.542		28.845	29.633	30.629	32.000	34.267
17	5.697	6.408	6.884	7.255	7.564	8.672	10.085			27.587	30.191	30.995	32.011	33.409	35.718
18	6.265	7.015	7.516	7.906	8.231	9.390	10.865		25.989	28.869	31.526	32.346	33.382	34.805	37.156
19	6.844	7.633	8.159	8.567	8.907	10.117	11.651		27.204	30.144	32.852	33.687	34.742	36.191	38.582
20	7.434	8.260	8.810	9.237	9.591	10.851	12.443		28.412		34.170	35.020	36.093	37.566	39.997
25	10.520		12.187	12.697	13.120	14.611	16.473		34.382	37.652	40.646	41.566	42.725	44.314	46.928
30	13.787		15.719	16.306	16.791	18.493	20.599		40.256	43.773	46.979	47.962	49.199	50.892	53.672
35	17.192		19.369	20.027	20.569	22.465	24.797		46.059	49.802	53.203	54.244	55.553	57.342	60.275
40	20.707	_	23.113	23.838	24.433	26.509	29.051	39.335	51.805	55.758	59.342	60.436	61.812	63.691	66.766
45	24.311		26.933		28.366	30.612	33.350		57.505	61.656	65.410		67.994	69.957	73.166
50	27.991		30.818	31.664	32.357	34.764	37.689	49.335	63.167	67.505	71.420	72.613	74.111	76.154	79.490
60	35.534		38.744		40.482	43.188	46.459		74.397	79.082	83.298	84.580	86.188		91.952
70	43.275	45.442	46.836		48.758	51.739	55.329	69.334			95.023			100.425	104.215
80	51.172		55.061		57.153	60.391	64.278			101.879		108.069			
90	59.196		63.394	64.635	65.647	69.126	73.291				118.136				
100	67.328		71.818	73.142	74.222	77.929	82.358				129.561				
110	75.550	78.458	80.318	81.723	82.867	86.792					140.917				
120	83.852		88.886	90.367							152.211				
130	92.222	000-	97.512								163.453				
140		104.034													
150											185.800				
160		121.346													
170		130.064													
180		138.820													
190		147.610													
200	152.241	156.432	159.096	161.100	162.728	168.279	174.835	199.334	$2\frac{2}{5}6.021$	233.994	241.058	243.187	245.845	249.445	255.264