

# Algorithmique Répartie

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  - Hypotheses
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Motivations :

Related work :

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- Global-Strong Multiplicity Detection

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- Global-Strong Multiplicity Detection
- Local-Strong and Global-Weak Multiplicity Detection

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**ASYNC** Asynchronous - The robots are activated/executed asynchronously

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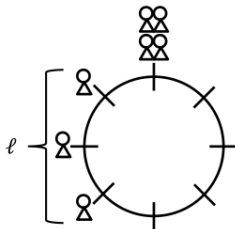
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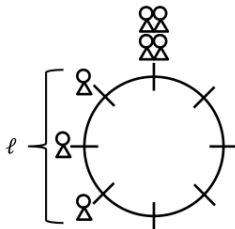
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**Set formation problem** : The goal of the set formation problem is to gather the robots in a specific predefined configuration.

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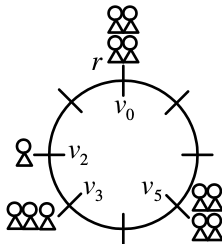
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- **Take care !** The scheduler is an enemy and will activate the robots in the worst way.

Let's consider the  $M(C)$  nodes :

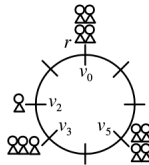
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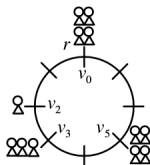
- Case 1 There is only one such node : the tower can be identified by the robots and they can get closer to the tower node.
- **The scheduler is an enemy !**
  - Less than  $M(C)$  nodes should move in the same direction !

Case 2 There are multiple such nodes :





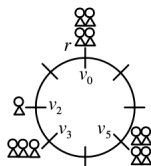
Case 2 There are multiple such nodes :



Take  $h_{min}$  the minimal distance between a M(C)-robot node and a neighboring robot node. Take  $V$  the set of nodes at distance  $h_{min}$  of a M(C)-node and  $R$  the robots on these nodes.

Cas 2.1  $|R| = 1$  - This robot gets to his closer M(C)-robot node.

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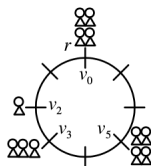


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Complexity :  $O(n \log k)$  rounds and  $O(kn)$  moves.

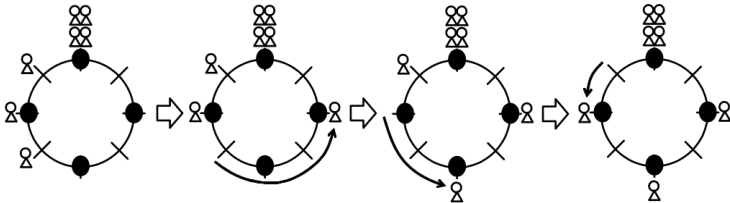


We can now apply the two previous algorithms to solve the **set formation problem**.

- Solve the orientation algorithm for  $I = |SET| - 1$ ,

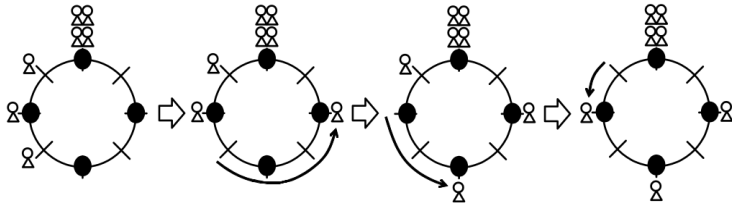
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## In order to go further we could :

- Find the problems we can solve with weaker hypotheses,
- Work with a weaker scheduler, like an oblivious one,
- Work with a more complex graph than a ring.