

$$a) f(x) = 1.16x^4 - 2x^3 + 0.75x^2 - x + 3.6$$

$$f'(x) = 4.64x^3 - 6x^2 + 1.5x$$

$$\bar{x} = 1.75$$

$$\epsilon_a = 0.05 \leftarrow \Delta \tilde{x}$$

$$x \in [1.7, 1.8] \quad \Delta f(1.75) = |4.64(1.75)^3 - 6(1.75)^2 + 1.5(1.75)| \cdot 0.05$$

$$\Delta f(1.75) = 0.455875$$

$$\begin{aligned} f(1.75) &= 1.16(1.75)^4 - 2(1.75)^3 + 0.75(1.75)^2 - (1.75) + 3.6 \\ &= 4.3076 \end{aligned}$$

$$f(x) \in (4.30765625 - 0.455875, 4.30765625 + 0.455875)$$

$$f(x) \in [3.85178125, 4.76353125]$$

b)

$$f(x) = \sin(x) = \ln(2x)$$

$$f'(x) = \cos(x) \ln(2x) + \frac{\sin(x)}{x}$$

$$\bar{x} = \frac{2\pi}{3}$$

$$\epsilon_a = 0.005$$

$$x \in (2.08939, 2.09939)$$

$$\Delta f\left(\frac{2\pi}{3}\right) = \left| \cos\left(\frac{2\pi}{3}\right) \cdot \ln\left(2 \cdot \frac{2\pi}{3}\right) + \sin\left(\frac{2\pi}{3}\right) \cdot \frac{1}{\frac{2\pi}{3}} \right| \cdot 0.005$$

$$\Delta f\left(\frac{2\pi}{3}\right) = 0.03195$$

Scribe

$$f\left(\frac{2\pi}{3}\right) = \sin\left(\frac{2\pi}{3}\right) \cdot \ln\left(2 \cdot \frac{2\pi}{3}\right) = 0.022734$$

$$f(x) \in [0.022734 + 0.03795, 0.022734 - 0.03795]$$

$$f(x) \in [0.054684, 0.065897]$$