

Matemáticas Computacionales Evaluación 1.

1) Sean los conjuntos

$$A = \{3, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30\}$$

$$B = \{2, 5, 7, 9, 15, 22, 33\}$$

$$C = \{3, 5, 7, 11, 13, 17, 19, 23, 29\}$$

$$(A \cap C) \cup (A \oplus B) = \{3, 8, 10, 11, 12, 13, 14, 16, 17, 18, 19, 20, 21, 23, 24, 25, 26, 27, 28, 29, 30, 2, 5, 33\}$$

$$A \cap C = \{3, 11, 13, 17, 19, 23, 29\} \quad A \oplus B = \{8, 10, 11, 12, 13, 14, 16, 17, 18, 19, 20, 21, 23, 24, 25, 26, 27, 28, 29, 30, 2, 5, 33\}$$

$$((A \cup C) \oplus B) \cap (A - C) = \{8, 10, 12, 14, 16, 18, 20, 21, 24, 25, 26, 27, 28, 30\}$$

$$(A \cup C) \oplus B = \{3, 8, 10, 11, 12, 13, 14, 16, 17, 18, 19, 20, 21, 23, 24, 25, 26, 27, 28, 29, 30, 2, 33\}$$

$$(A - C) = \{8, 9, 10, 12, 14, 15, 16, 18, 20, 21, 22, 24, 25, 26, 27, 28, 30\}$$

$$((A \oplus B) - (A \cap C)) \cap (A \cup B \cup C) = \{2, 5, 8, 9, 10, 12, 14, 15, 16, 18, 20, 21, 23, 24, 25, 26, 27, 28, 30\}$$

$$(A \oplus B) - (A \cap C) = \{2, 5, 8, 9, 10, 12, 14, 15, 16, 18, 20, 21, 22, 24, 25, 26, 27, 28, 30\}$$

$$(A \cup B \cup C) = \{3, 3, 5, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 33\}$$

2)

a) De cuantas formas se puede conformar el comité si se quiere que ninguno este en el.

$$C(6, 4) = \frac{6!}{(6-4)! 4!} = 15$$

b) Si se quiere que mora este en el comité

$$C(7, 4) = \frac{7!}{(7-4)! 4!} = 35$$

c) Que ambos esten en el

$$C(8, 4) = \frac{8!}{(8-4)! 4!} = 70$$

d) De cuantas formas si se quiere 900 manzanas

$$\frac{2.6}{1.3} = 4$$

3) Conversión de forma manual de base 10 a la base indicada

a) 35 a base 2. = 100011.

$$\begin{array}{r} 35 \overline{) 2} \\ \underline{17} \end{array}$$

$$\begin{array}{r} 17 \overline{) 2} \\ \underline{8} \end{array}$$

$$\begin{array}{r} 8 \overline{) 2} \\ \underline{4} \end{array}$$

$$\begin{array}{r} 4 \overline{) 2} \\ \underline{2} \end{array}$$

$$\begin{array}{r} 2 \overline{) 2} \\ \underline{2} \end{array}$$

b) 138 a

4. $x = 1,3$ $h = 0,002$

$$f(x) = 0,3x^4 - 0,4x^3 + 0,9x^2 - 3x + 3.$$

$$f'(x) = 1,2x^3 - 1,2x^2 + 1,8x - 3$$

$$f''(x) = 3,6x^2 - 2,4x + 1,8$$

	x	$f(x)$
x_1	1,3	0,59903
x_{1+1}	1,302	0,5989363373
x_{1-1}	1,298	0,5991427187
x_{1+2}	1,304	0,5988617863
x_{1-2}	1,296	0,5992744318

► Primera diferencia finita dividida hacia adelante.

$$1/2 f'(1,3) = -0,051$$

$$f'(1,3) \approx \frac{0,5989363373 - 0,59903}{0,002} = -0,04683135$$

► Primera diferencia finita dividida hacia atrás.

$$f'(1,3) \approx \frac{0,59903 - 0,5991427187}{0,002} = -0,05635935$$

► Primera diferencia finita centrada

$$f'(1,3) \approx \frac{0,5989363373 - 0,5991427187}{2(0,002)} = 0,05159535$$

► Segunda diferencia finita dividida hacia adelante.

$$f''(1,3) \approx \frac{0,5988617863 - 2(0,5989363373) + 0,59903}{(0,002)^2} = 4,77792$$

► Segunda diferencia finita dividida hacia atrás.

$$f''(1,3) \approx \frac{0,59903 - 2(0,5991427187) + 0,5992744318}{(0,002)^2} = 4,7501$$

► Segunda diferencia finita dividida centrada

$$f''(1,3) \approx \frac{0,5989363373 - 2(0,59903) + 0,5991427187}{(0,002)^2} = 4,764$$