$$oldsymbol{H}_{exchange} \ = \ - \sum_{i,j,i
eq j}^{N} J\left(r_{ij}
ight) \ ec{s}_{i} \cdot ec{s}_{j}$$