

$$H_{\text{exchange}} = - \sum_{i,j,i \neq j}^N J(r_{ij}) \vec{s}_i \cdot \vec{s}_j$$