

Assignment - 06 [AIIES]

* Title :

Implement a local search algorithm for
eg : n-queens, chess, TSP

* Aim :

Implement hill climbing algorithm for TSP

* Objective :

Write a program in C/C++/Python to solve the hill climbing algorithm for TSP.

* Theory :

1.) Local Search Algorithm

Local search algorithms are optimization techniques used to find solutions by exploring the solution space incrementally. These algorithms start with an initial solution and iteratively make small changes to it.

Key Characteristics :

- Focuses on a single current solution.
- Moves to a neighbouring solution if it improves the current one.
- Finds a good solution in a reasonable time.

2) Hill Climbing Algorithm

Hill climbing is a specific type of local search algorithm that continuously moves towards higher (or lower) values in the search space.

It is an iterative algorithm that starts with an arbitrary solution and makes incremental changes to improve it.

Key Characteristics :-

- Greedy Approach
- Simple and easy to implement

Types of Hill Climbing :-

- Single hill climbing
- Steepest hill climbing
- Stochastic hill climbing

* Input :-

$n \times n$ matrix of distance of TSP.

* Output :-

An optimal distance between 2 cities

* Algorithm :-

Hill Climbing Algorithm

* Platform :
linux

* FAQ's :

Q.1. Explain hill climbing with example.

→ Hill climbing is a specific type of local search algorithm that continuously moves towards higher (or lower) values in the search space.

It is a heuristic search technique used for mathematical operation optimization problems.
Steps of hill climbing algorithm :

- (i) Initialisation
- (ii) Evaluation
- (iii) Generate neighbour
- (iv) Select best neighbour
- (v) Move to next best neighbour
- (vi) Check for termination

Example : $f(x) = -x^2 + 4x$

(i) Initialize $x=0$

(ii) Evaluate :

$$f(x=0) = 0$$

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(iii) Generate neighbours

$$f(x=-1) = 3$$

$$f(x=1) = 5$$

(iv) Thus best neighbour ($x=-1$)

(v) Move to $x=1$

(vi) Repeat steps (iii) - (v)

(vii) Here, the algorithm terminates at $x=2$ with max function value $f(2)=4$

Q.2 Explain limitations of hill climbing and solutions to it.

→ Limitations :

- Hill climbing can get stuck in local optima.
- Hill climbing can get stuck on plateaus, flat areas of the search space where neighbouring points have same value
- Hill climbing does not consider the possibility of backtracking.
- The quality of final solⁿ depends heavily on starting point.

Solutions to overcome limitations :

- Run the algorithm multiple times from different random starting points.
- Simulated Annealing

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- Genetic Algorithms : These use principles of natural selection and genetics to search for optimal solutions.
- Beam Search and Tabu Search.

Q.3. Solve n queens problem using local search algorithm.

→ The n queens problem is a classic combinatorial problem where the goal is to place N queens on an $N \times N$ chessboard such that no two queens attack each other.

Steps to solve N -queens problem :

(i) Initialisation : Start with a random placement of n queens on an $N \times N$ Chessboard.

(ii) Iterate :

For a given no. of conflicts :

- Select a queen in this conflict
- Move the selected queen to a position that minimizes the conflict

(iii.) Termination :

If no conflicts are present, the solution is found.

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* Algorithm :

```
def hill-climbing (problem):  
    current_solution = problem.initial_solution()
```

```
    while True:
```

```
        neighbours = problem.generate_neighbours(current_solution)
```

```
        next_solution = None
```

```
        for neighbour in neighbours:
```

```
            if problem.evaluate(neighbour) >
```

```
                problem.evaluate(current_solution):
```

```
                next_solution = neighbour
```

```
            break:
```

```
        if next_solution is None:
```

```
            return current_solution
```

```
        current_solution = next_solution
```

* Conclusion :

We learned hill climbing algorithm, local search algorithm and TSP.

20/7/21

```
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+ Code + Markdown | ▶ Run All | Clear All Outputs | Outline ...
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import random

def compute_tour_length(tour:list[int], adj_matrix:list[list[int]]):
    total_distance = 0
    num_cities = len(tour)
    for i in range(num_cities):
        j = (i + 1) % num_cities # Next city in the tour
        total_distance += adj_matrix[tour[i]][tour[j]]
    return total_distance

def generate_random_route(num_cities:int):
    start = int(input("Start City? num/-1:"))
    random_ro = list(range(num_cities))
    random.shuffle(random_ro)
    if start != -1:
        random_ro.remove(start)
        random_ro.insert(0, start)
    print("Initial route", random_ro)
    return random_ro

def local_search_tsp(adj_matrix:list[list[int]]):
    g = int(0)
    num_cities = len(adj_matrix)
    current_tour = generate_random_route(num_cities) # Initial tour, can start with any permutation

    best_tour = current_tour.copy()
    best_tour_length = compute_tour_length(best_tour, adj_matrix)

    improvement = True
    while improvement:
        g += 1
        improvement = False
        for i in range(1, num_cities - 1):
            for j in range(i + 1, num_cities):
                neighbor_tour = current_tour.copy()
                neighbor_tour[i], neighbor_tour[j] = neighbor_tour[j], neighbor_tour[i]
```



```

neighbor_tour = current_tour.copy()
neighbor_tour[i], neighbor_tour[j] = neighbor_tour[j], neighbor_tour[i]
neighbor_tour_length = compute_tour_length(neighbor_tour, adj_matrix)

if neighbor_tour_length < best_tour_length:
    current_tour = neighbor_tour.copy()
    best_tour = current_tour.copy()
    best_tour_length = neighbor_tour_length
    print("Selected improved neighbour",current_tour)
    improvement = True
    break

if improvement:
    break

return best_tour, best_tour_length,g

adjacency_matrix = [
    [0, 400, 500, 300],
    [400, 0, 300, 500],
    [500, 300, 0, 400],
    [300, 500, 400, 0]
]

best_tour, best_tour_length ,total_steps= local_search_tsp(adjacency_matrix)
print("Best Tour:", best_tour)
print("Tour Length:", best_tour_length)
print("Total Steps:", total_steps)

```



```
... Initial route [2, 1, 3, 0]
Selected improved neighbour [2, 1, 0, 3]
Best Tour: [2, 1, 0, 3]
Tour Length: 1400
Total Steps: 2
```

