

AOA ASSIGNMENT

OBJECTIVE:

- Implement three graph functions such as `shortest_path`, `connected_components` and `cycles` in JAVA and then test these functions using three simulated graphs (`n_cycles`, `complete_graph` and `Equivalence mod K`).
- To construct graph using Netflix-prize challenge data for different adjacency criteria and output the number of connected components and size of each component for the graph.

DESCRIPTION:

GRAPH OPERATIONS:

The following three graph functions are implemented as follows:

- *Connected components ()*: The depth first search methodology is used to return the connected components present in our graph for each vertex. If there are no vertices connected to the given vertex then also it is considered as a component. Our output is represented like `v1->v2->....`
`->vn` (incase of `n` connected components) or `v1` (if the vertex has no other connected vertices).
- *one cycle ()*: The depth first search methodology is used to return the first detected cycle present in the graph. If there are no cycles, then an empty list is returned.
- *shortest_path ()*: We have implemented the Dijkstra's algorithm to find the shortest path to every other node from source in the graph. We have taken source to be 0 for all simulated graphs.

GRAPH SIMULATORS:

In our project we have generated three simulated graphs using JAVA namely,

- `n_cycle`
- a complete graph on `n` vertices
- `Equivalence mod K`.

SIMULATED TEST:

The simulated graphs produced are tested for different number of nodes for all three functions. The testing is done by getting the number of nodes from the user. Then the user chooses any one of the simulated graphs and the system outputs the number of connected components, shortest path from vertex 0 to all other vertices (up to `n-1`), one cycle if present in the graph and the adjacency list of the graph.

NETFLIX DATA TEST:

For the Netflix data, we extract the data from the four .txt files. After storing the data we generate graphs based on different adjacency criteria.

Adjacency Criteria 1: We create an edge between the two customer ids if they have given a rating for at least one movie in common.

Adjacency Criteria 2: We create an edge between the two customer ids if they have given a rating for at least 5 movies in common.

DATA STRUCTURES USED FOR VARIOUS OPERATIONS:

- The data structure used to store the **Graph** for simulated test is ArrayList n nodes, where each index in the ArrayList contains a list edge objects associated with them. Each edge object contains source, destination and weight in it. Here we assume the weight to be a default 1 value.
- The data structure used in **connected components** is a Boolean array to mark the already visited nodes and a recursive DFS function is applied on unvisited nodes until they are also visited through traversal.
- The data structures used in **shortest_paths()** are Priority queue(minheap), list(size is total no of nodes) of integers to store the shortest distance, a Boolean array to keep track of nodes for which the shortest distance to node is already found and Integer array to store parent of each node.
- The data structures used in **one_cycle()** is a List to store one cycle present in the graph which makes use of the already defined DFS function to find the nodes in the cycle.
- The data structure used to store Netflix data is a Multimap where the customer ids are the key and the movies which were given rating by them are the corresponding values for that key.
- For both the adjacency criteria we use a HashSet. We find intersection between the two list of movies between two customers by storing them temporarily in HashSet for each loop iteration.

PEAK MEMORY USAGE AND CPU TIME FOR EXPERIMENT USING SIMULATED DATA:

- For the simulated graph, when n=10 the running time to execute all three functions is 205ms and the total memory usage is 500.50Kb.
- When n=100, the running time to execute all three functions is 3s and the total memory usage is 4030.77Kb.

Thus, the time complexity for performing three functions for simulated data is $O(n^2)$.

SAMPLE OUTPUT FROM TESTS OF SIMULATED DATA:

WHEN THE VALUE OF N IS 10,

OUTPUT:

Enter the number of Vertices you want

10

Enter the type of graph you want

1. N_Cycle Graph

2. Complete_Graph

3. Equivalence_Mod_K Graph

1

Following are the Shortest path from Vertex 0:

Path (0 -> 1): Minimum Cost = 1, Route = [0, 1]

Path (0 -> 2): Minimum Cost = 2, Route = [0, 1, 2]

Path (0 -> 3): Minimum Cost = 3, Route = [0, 1, 2, 3]

Path (0 -> 4): Minimum Cost = 4, Route = [0, 1, 2, 3, 4]

Path (0 -> 5): Minimum Cost = 5, Route = [0, 1, 2, 3, 4, 5]

Path (0 -> 6): Minimum Cost = 4, Route = [0, 9, 8, 7, 6]

Path (0 -> 7): Minimum Cost = 3, Route = [0, 9, 8, 7]

Path (0 -> 8): Minimum Cost = 2, Route = [0, 9, 8]

Path (0 -> 9): Minimum Cost = 1, Route = [0, 9]

Following are the Connected Graph Components:

0 1 2 3 4 5 6 7 8 9

Graph Display:

Adjacency list of vertex0

head -> 1 -> 9

Adjacency list of vertex1

head -> 0 -> 2

Adjacency list of vertex2

head -> 1 -> 3

Adjacency list of vertex3

head -> 2 -> 4

Adjacency list of vertex4

head -> 3 -> 5

Adjacency list of vertex5

head -> 4 -> 6

Adjacency list of vertex6

head -> 5 -> 7

Adjacency list of vertex7

head -> 6 -> 8

Adjacency list of vertex8

head -> 7 -> 9

Adjacency list of vertex9

head -> 0 -> 8

Following are one cycle details:

[0, 9, 8, 7, 6, 5, 4, 3, 2, 1]

Enter the type of graph you want

1. N_Cycle Graph

2. Complete_Graph

3. Equivalence_Mod_K Graph

2

Following are the Shortest path from Vertex 0:

Path (0 -> 1): Minimum Cost = 1, Route = [0, 1]

Path (0 -> 2): Minimum Cost = 1, Route = [0, 2]

Path (0 -> 3): Minimum Cost = 1, Route = [0, 3]

Path (0 -> 4): Minimum Cost = 1, Route = [0, 4]

Path (0 -> 5): Minimum Cost = 1, Route = [0, 5]

Path (0 -> 6): Minimum Cost = 1, Route = [0, 6]
Path (0 -> 7): Minimum Cost = 1, Route = [0, 7]
Path (0 -> 8): Minimum Cost = 1, Route = [0, 8]
Path (0 -> 9): Minimum Cost = 1, Route = [0, 9]
Following are the Connected Graph Components:

0 1 2 3 4 5 6 7 8 9

Graph Display:

Adjacency list of vertex0

head -> 1 -> 2 -> 3 -> 4 -> 5 -> 6 -> 7 -> 8 -> 9

Adjacency list of vertex1

head -> 0 -> 2 -> 3 -> 4 -> 5 -> 6 -> 7 -> 8 -> 9

Adjacency list of vertex2

head -> 0 -> 1 -> 3 -> 4 -> 5 -> 6 -> 7 -> 8 -> 9

Adjacency list of vertex3

head -> 0 -> 1 -> 2 -> 4 -> 5 -> 6 -> 7 -> 8 -> 9

Adjacency list of vertex4

head -> 0 -> 1 -> 2 -> 3 -> 5 -> 6 -> 7 -> 8 -> 9

Adjacency list of vertex5

head -> 0 -> 1 -> 2 -> 3 -> 4 -> 6 -> 7 -> 8 -> 9

Adjacency list of vertex6

head -> 0 -> 1 -> 2 -> 3 -> 4 -> 5 -> 7 -> 8 -> 9

Adjacency list of vertex7

head -> 0 -> 1 -> 2 -> 3 -> 4 -> 5 -> 6 -> 8 -> 9

Adjacency list of vertex8

head -> 0 -> 1 -> 2 -> 3 -> 4 -> 5 -> 6 -> 7 -> 9

Adjacency list of vertex9

head -> 0 -> 1 -> 2 -> 3 -> 4 -> 5 -> 6 -> 7 -> 8

Following are one cycle details:

[0, 2, 1]

Enter the type of graph you want

1. N_Cycle Graph
 2. Complete_Graph
 3. Equivalence_Mod_K Graph
- 3

Value of K:7

Following are the Shortest path from Vertex 0:

Path (0 -> 7): Minimum Cost = 1, Route = [0, 7]

Following are the Connected Graph Components:

0 7

1 8

2 9

3

4

5

6

Graph Display:

Adjacency list of vertex0

head -> 7

Adjacency list of vertex1

head -> 8

Adjacency list of vertex2

head -> 9

Adjacency list of vertex3

head

Adjacency list of vertex4

head

Adjacency list of vertex5

head

Adjacency list of vertex6

head

Adjacency list of vertex7

head -> 0

Adjacency list of vertex8

head -> 1

Adjacency list of vertex9

head -> 2

Following are one cycle details:

[]

SAMPLE OUTPUT FROM TESTS OF REAL DATA:

Adjacency Criteria 1 For the first 4 movies

Following are the Connected Graph Components:

0 1 2 3 4 5 6 9 11 12 13 15 16 17 18 19 20 22 23 24 26 27 28 29 30 31 32 34 37 38 39 40 41 42 43 56 57 58
59 60 61 62 63 66 67 68 72 73 74 75 78 80 81 83 84 85 86 87 88 89 91 92 95 97 98 99 100 102 103 104
105 107 110 111 112 113 114 116 118 119 120 121 122 123 126 127 130 131 132 133 134 136 137 138
139 144 146 148 152 154 155 156 157 158 160 162 163 164 166 167 168 169 170 171 172 173 174 175
176 177 179 181 182 183 184 185 189 190 191 192 193 194 195 196 197 199 201 202 203 206 207 209
210 211 212 213 214 215 216 217 218 219 220 221 222 223 224 225 226 229 230 231 232 233 234 235
236 237 238 240 243 244 245 246 247 250 252 254 255 256 257 258 259 260 261 263 264 266 267 268
269 271 272 273 274 276 277 278 280 281 282 283 284 286 287 288 289 290 292 294 295 296 297 298
299 301 302 303 304 306 307 308 309 310 311 312 314 315 316 317 318 320 321 322 324 325 326 327
328 330 331 332 333 336 337 338 339 340 341 343 344 345 346 348 349 351 352 353 356 357 358 359
360 361 363 364 365 366 367 368 369 370 371 373 374 375 376 378 379 380 384 385 386 387 390 391
392 393 394 395 396 398 399 400 402 403 404 405 406 407 408 409 410 411 412 414 415 416 417 418
419 420 422 423 426 427 428 429 431 432 433 434 435 438 439 442 443 444 445 446 448 449 450 451
452 453 454 456 457 459 460 461 462 463 464 465 466 467 469 471 472 473 475 476 477 478 479 480
481 482 483 489 490 491 492 493 494 495 496 497 498 499 501 504 505 509 510 511 513 514 515 517
518 519 520 521 523 525 526 527 530 531 532 536 537 538 539 540 541 542 544 545 546 547 548 549
550 551 552 553 554 555 7 8 14 21 25 35 36 44 45 46 48 50 51 55 64 65 69 77 94 96 117 124 10 47 70 79
109 115 125 129 141 145 149 178 186 228 249 262 285 329 354 389 506 563 564 570 582 617 627 639
649 682 684 695 720 742 33 49 52 53 54 71 76 82 90 93 101 106 108 150 159 180 239 241 251 253 305
313 362 424 436 468 470 487 524 534 557 560 587 591 610 615 621 660 685 702 739 773 782 789 792
794 817 828 861 887 892 897 128 135 140 142 143 147 151 153 161 165 187 188 198 200 204 205 208
227 242 248 265 270 275 279 291 293 300 319 323 334 335 342 347 350 355 372 377 381 382 383 388
397 401 413 421 425 430 437 440 441 447 455 458 474 484 485 486 488 500 502 503 507 508 512 516
522 528 529 533 535 543 561 567 569 573 575 583 588 597 607 613 624 626 632 635 654 657 661 662
665 679 706 709 713 716 728 729 735 741 743 747 748 749 750 755 756 757 759 763 764 768 776 786
787 788 790 805 839 842 850 855 857 859 867 874 875 880 883 885 888 894 895 916 920 936 954 959
970 975 976 981 982 983 987 988 990 995 999 1002 1010 556 558 559 562 565 566 568 571 572 574 576
577 578 579 580 581 584 585 586 589 590 592 593 594 595 596 598 599 600 601 602 603 604 605 606
608 609 611 612 614 616 618 619 620 622 623 625 628 629 630 631 633 634 636 637 638 640 641 642
643 644 645 646 647 648 650 651 652 653 655 656 658 659 663 664 666 667 668 669 670 671 672 673
674 675 676 677 678 680 681 683 686 687 688 689 690 691 692 693 694 696 697 698 699 700 701 703
704 705 707 708 710 711 712 714 715 717 718 719 721 722 723 724 725 726 727 730 731 732 733 734
736 737 738 740 744 745 746 751 753 754 758 760 761 762 765 766 767 769 770 771 772 774 775 777
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910 752 797 809 812 847 862 898 918 1056 1078 1093 1119 1147 1200 1217 1228 1229 1236 1248 1251
911 912 913 914 915 917 919 921 922 923 924 925 926 927 928 929 930 931 932 933 934 935 937 938
939 940 941 942 943 944 945 947 948 949 950 951 952 953 955 956 957 958 960 961 962 963 964 965
966 967 968 969 971 972 973 974 977 978 979 980 984 985 986 989 992 993 994 996 997 998 1000 1001
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2345 2346 2351 2352 1721 1785 1833 1864 1871 1914 1921 1931 1932 1958 1976 2007 2029 2102 2129
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2089 2090 2091 2093 2094 2095 2096 2099 2100 2101 2106 2107 2108 2109 2111 2112 2113 2115 2116
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2198 2201 2202 2203 2205 2206 2207 2208 2209 2215 2217 2219 2222 2223 2224 2225 2226 2227 2228
2230 2231 2232 2233 2234 2236 2237 2238 2239 2242 2243 2246 2248 2249 2250 2251 2252 2253 2255
2257 2258 2259 2260 2261 2263 2265 2267 2268 2269 2273 2275 2276 2277 2278 2279 2280 2281 2282
2283 2286 2287 2288 2289 2290 2291 2292 2293 2294 2295 2296 2297 2298 2299 2301 2302 2303 2304
2306 2307 2308 2309 2311 2312 2314 2316 2317 2319 2321 2322 2324 2325 2326 2327 2329 2330 2331
2332 2333 2335 2337 2339 2341 2342 2343 2347 2349 2350 2354 2355 2356 2357 2358 2360 2361 2362
2363 2364 2365 2367 2369 2371 2372 2373 2374 2375 2376 2377 2378 2379 2380 2381 2382 2383 2385
2386 2387 2388 2389 2390 2391 2392 2393 2394 2395 2396 2398 2399 2400 2401 2402 2403 2404 2405
2406 2407 2411 2413 2414 2415 2416 2417 2419 2420 2421 2422 2427 2428 2429 2430 2432 2433 2434
2435 2437 2438 2440 2441 2442 2443 2447 2448 2449 2451 2452 2453 2454 2457 2458 2460 2461 2463
2464 2465 2466 2467 2468 2469 2472 2473 2475 2478 2479 2480 2482 2483 2484 2485 2488 2490 2491
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2546 2547 2549 2551 2552 2554 2556 2558 2559 2560 2561 2562 2564 2565 2566 2567 2569 2570 2571
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2597 2598 2599 2600 2602 2603 2605 2608 2609 2610 2611 2612 2614 2615 2616 2618 2621 2622 2623
2624 2627 2628 2629 2630 2631 2632 2634 2636 2637 2638 2639 2641 2642 2643 2645 2646 2648 2650
2652 2653 2655 2657 2658 2659 2661 2662 2663 2665 2666 2670 2671 2672 2674 2675 2676 2359 2368
2397 2408 2412 2418 2423 2425 2426 2436 2445 2455 2459 2470 2474 2476 2486 2487 2489 2492 2494
2503 2507 2508 2522 2523 2529 2536 2542 2553 2555 2557 2568 2586 2592 2596 2601 2604 2606 2607
2613 2620 2625 2626 2633 2647 2649 2651 2660 2667 2669 2677 2679 2687 2691 2692 2704 2707 2708
2678 2680 2681 2682 2683 2684 2685 2686 2688 2690 2693 2694 2695 2696 2697 2698 2700 2701 2702
2703 2705 2709 2710 2712 2713 2714 2715 2716 2717 2718 2719 2721 2723 2724 2456 2462 2481 2537
2540 2550 2563 2575 2590 2619 2635 2644 2654 2664 2673 2689 2706 2722 2740 2786 2789 2798 2711
2745 2746 2748 2750 2759 2760 2764 2765 2778 2779 2725 2726 2727 2728 2729 2730 2731 2732 2733
2734 2735 2736 2737 2738 2739 2742 2743 2744 2747 2749 2751 2753 2754 2755 2756 2757 2758 2761

2762 2763 2766 2768 2769 2770 2771 2772 2773 2774 2775 2776 2777 2780 2781 2782 2783 2784 2785
2787 2788 2791 2793 2799 2800 2801 2802 2792 2794 2795 2796 2241 2284 2285 2320 2348 2353 2384
2410 2431 2446 2471 2477 2497 2502 2520 2544 2548 2595 2617 2640 2656 2668 2699 2720 2741 2752
2767 2790 2797

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Adjacency Criteria 2 For the first 4 movies

Following are the Connected Graph Components:

0 1 2 3 4 5 6 9 11 12 13 15 16 17 18 19 20 22 23 24 26 27 28 29 30 31 32 34 37 38 39 40 41 42 43 56 57 58
59 60 61 62 63 66 67 68 72 73 74 75 78 80 81 83 84 85 86 87 88 89 91 92 95 97 98 99 100 102 103 104
105 107 110 111 112 113 114 116 118 119 120 121 122 123 126 127 130 131 132 133 134 136 137 138
139 144 146 148 152 154 155 156 157 158 160 162 163 164 166 167 168 169 170 171 172 173 174 175
176 177 179 181 182 183 184 185 189 190 191 192 193 194 195 196 197 199 201 202 203 206 207 209
210 211 212 213 214 215 216 217 218 219 220 221 222 223 224 225 226 229 230 231 232 233 234 235
236 237 238 240 243 244 245 246 247 250 252 254 255 256 257 258 259 260 261 263 264 266 267 268
269 271 272 273 274 276 277 278 280 281 282 283 284 286 287 288 289 290 292 294 295 296 297 298
299 301 302 303 304 306 307 308 309 310 311 312 314 315 316 317 318 320 321 322 324 325 326 327
328 330 331 332 333 336 337 338 339 340 341 343 344 345 346 348 349 351 352 353 356 357 358 359
360 361 363 364 365 366 367 368 369 370 371 373 374 375 376 378 379 380 384 385 386 387 390 391
392 393 394 395 396 398 399 400 402 403 404 405 406 407 408 409 410 411 412 414 415 416 417 418
419 420 422 423 426 427 428 429 431 432 433 434 435 438 439 442 443 444 445 446 448 449 450 451
452 453 454 456 457 459 460 461 462 463 464 465 466 467 469 471 472 473 475 476 477 478 479 480
481 482 483 489 490 491 492 493 494 495 496 497 498 499 501 504 505 509 510 511 513 514 515 517
518 519 520 521 523 525 526 527 530 531 532 536 537 538 539 540 541 542 544 545 546 547 548 549
550 551 552 553 554 555 7 8 14 21 25 35 36 44 45 46 48 50 51 55 64 65 69 77 94 96 117 124 10 47 70 79
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