- two categorical variables
- Are they related?

Test for Homogeneity

- one categorical variable
- Does it act the same for different populations?

- took a random sample of 300 students from some university
- for each student, recorded their status as an undergraduate student or a graduate student
- also recorded whether the majority of their classes are given in-person, remotely, or in a hybrid manner

Question: Is student status independent of class delivery type?

	in-person	hybrid	
ugrads	121	47	31
grads	33	57	

	in-person	remote	hybrid	
ugrads	121	47	31	199
grads	33	57	11	101
	154	104	42	300

	in-person	remote	hybrid	
ugrads	121	47	31	199
grads	33	57	11	101
	154	104	42	300

 estimated probability person in sample is an undergraduate is

199300

	in-person	remote	hybrid	
ugrads	121	47	31	199
grads	33	57		101
	154	104	42	300

 estimated probability person in sample is taking a majority of inperson courses is

300

	in-person	remote	hybrid	
ugrads	121	47	31	199
grads	33	57	111	101
	154	104	42	300

 If delivery type and student type are independent, the probability we fall in this square should be 199 154

	in-person	remote	hybrid	
ugrads	121	47	31	199
grads	33	57	111	101
	154	104	42	300

 The expected number of people, out of the total of 300 sampled, who fall in that square should be

$$\frac{199}{300} \cdot \frac{154}{300} \cdot 300 = \frac{(199)(154)}{300} \approx 102.15$$

 Under the assumption of independence, the expected counts are

	in-person	remote	hybrid	
ugrads	(199)(154) 300	(199)(104) 300	(199)(42) 300	199
grads	(101)(154) 300	(101)(104) 300	(101)(42) 300	101
	154	104	42	300

H₀: Student status and class delivery type are independent

H₁: Student status and class delivery type are not independent

Test Statistic:

$$W := \sum_{i} \frac{(O_{i} - E_{i})^{2}}{E_{i}} \sim \chi^{2}(?)$$

Degrees of freedom parameter is

(number of rows -1)(number of cols -1)

Reject H_0 , in favor of H_1 if W is "large".

For our example, the test statistic is

W \approx 32.193

The critical value ($\alpha = 0$. 10) is

$$\chi_{0.10,2}^2 = 4.60517$$

Reject H₀!

There is sufficient evidence in the data to conclude that student status and class delivery type are dependent at level 0.10.

- took a random sample of 199 undergraduate students
- took an independent random sample of 101 graduate students
- For each sample, recorded whether the majority of their classes are given in-person, remotely, or in a hybrid manner.

Question: Is the distribution of inperson, to remote, to hybrid the same for both groups?

	in-person	remote	hybrid	
ugrads	121	47	31	199
grads	33	57		101
	154	104	42	300

H₀: The distribution of class type is the same for undergraduate and graduate students.

H₁: Not H₀.

	in-person	remote	hybrid	
ugrads	121	47	31	199
grads	33	57	11	101
	154	104	42	300

Overall "in-person" probability is estimated to be 154

300

	in-person	remote	hybrid	
ugrads	121	47	31	199
grads	33	57	11	101
	154	104	42	300

• Since there are 199 undergrads, the expected number in the in-person group under H_0 is $\frac{154}{200} \cdot 199$

Expected number under the assumption of independence:

$$\frac{199 \cdot 154}{300 \cdot 300} \cdot \frac{300}{300}$$

Expected number under the assumption of homogeneity: