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     MODULE MOD RLLSLL
      CONTAINS
     SUBROUTINE RLLSLL(RPANBOUND, RMESH, VLL, RLL, SLL, TLLP, &
                    NCHEB, NPAN, LMSIZE, LMSIZE2, NRMAX, &
                    nvec,jlk_index,hlk,jlk,hlk2,jlk2,GMATPREFACTOR, &
                    cmoderll,cmodesll,cmodetest,vll2ddr)
/ **********************
! radial wave functions by the integral equation method of
 Gonzalez et al, Journal of Computational Physics 134, 134-149 (1997)
 *************************
 This routine solves the following two equations:
! RLL(r) = J(r) - PRE * J(r) * int 0^r( dr' r'^2 H2(r') * op(V(r')) * RLL(r') 
             + PRE * H(r) * int_0^r( dr' r'^2 J2(r') * op(V(r')) * RLL(r') )
! SLL(r) = H(r) - PRE * H(r) * int_0^r( dr' r'^2 H2(r') * op(V(r')) * RLL(r')
             + PRE * J(r) * int_0^r( dr' r'^2 H2(r') * op(V(r')) * SLL(r') )
! where the integral int 0^r() runs from 0 to r
! Potential matrix : VLL(LMSIZE*NVEC,LMSIZE*NVEC)
Green function prefacor PRE=GMATPREFACTOR (scalar value)
! Source terms : J, H (nvec*lmsize,lmsize) or (lmsize,nvec*lmsize)
              J2,H2 (lmsize,nvec*lmsize) or (nvec*lmsize,lmsize)
! The source term J is for LMSIZE=3 and NVEC=2 given by:
! J =
           jlk(jlk\_index(1))
                            jlk(jlk\_index(2))
                0
                0
                                             jlk(jlk\_index(3))
           jlk(jlk\_index(4))
                0
                            jlk(jlk\_index(5))
                0
                                             ilk(ilk index(6))
                                 0
 Operator op() can be chosen to be a unity or a transpose operation
     The unity operation is used to calculate the right solution
     The transpose operation is used to calculate the left solution
 ****************
 RMESH
           - radial mesh
! RPANBOUND - panel bounds RPANBOUND(0) left panel border of panel 1
                        RPANBOUND(1) right panel border of panel 1
! NCHEB
           - highes chebyshev polynomial
            number of points per panel = NCHEB + 1
! NPAN
           - number of panels
! LMSIZE
           - number of colums for the source matrix J etc...
I LMSTZE2
           - number of rows for the source matrix J etc...
! NRMAX
           - total number of radial points (NPAN*(NCHEB+1))
! NVEC
           - number of LMSIZE*LMSIZE blocks in J (LMSIZE2=NVEC*LMSIZE)
USE MOD TIMING
USE MOD BESHANK
USE MOD_CHEBINT
USE MOD_CONFIG, only: config_testflag
USE MOD_checknan
USE MOD_RLLSLLTOOLS
use mod_physic_params,only: cvlight
USE SourceTerms
USE MOD CHEBYSHEV
IMPLICIT NONE
     INTEGER NCHEB, NPAN, LMSIZE, LMSIZE2
     INTEGER NRMAX
     INTEGER IVEC, IVEC2, NVEC
      PARAMETER (NRMAX= (N+1)*MMAX)
     DOUBLE COMPLEX CI, CONE, CZERO
     PARAMETER (CI= (0.0D0,1.0D0),CONE=(1.0D0,0.0D0))
     PARAMETER (CZERO=(0.0D0,0.0D0))
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     .. Local Scalars ..
    DOUBLE COMPLEX GMATPREFACTOR
      DOUBLE COMPLEX AU, BU, AS, BS, F1U, F2U, F1S, F2S
     DOUBLE PRECISION PLLM
     INTEGER INFO, ICHEB3, ICHEB2, ICHEB, ICHEB1, IPAN, MN, NM, MN2, NPLM
     INTEGER L1, L2, LM1, LM2, LM3
     .. Local Arrays ..
     DOUBLE COMPLEX :: HLK(:,:), &
                    JLK(:,:)
                      NLK(:,:)
     DOUBLE COMPLEX :: HLK2(:,:), &
                    JLK2(:,:)
                      NLK2(:::)
      DOUBLE COMPLEX HLK(0:(LMAX+1)*NVEC-1,0:N),
                      JLK(0:(LMAX+1)*NVEC-1,0:N),
                      NLK(0:(LMAX+1)*NVEC-1,0:N)
       DOUBLE COMPLEX HLK2(0:(LMAX+1)*NVEC-1,0:N),
                      JLK2(0:(LMAX+1)*NVEC-1,0:N),
                      NLK2(0:(LMAX+1)*NVEC-1,0:N)
     character(len=1) :: cmoderll,cmodesll,cmodetest
    DOUBLE COMPLEX &
                    SLL(LMSIZE2,LMSIZE,NRMAX), &
                    RLL(LMSIZE2,LMSIZE,NRMAX), TLLP(LMSIZE,LMSIZE), &
                    SRLLP(LMSIZE,LMSIZE), &
                    VLL(LMSIZE*nvec,LMSIZE*nvec,NRMAX)
    DOUBLE COMPLEX,allocatable :: VLL2DDR(:,:)
     DOUBLE COMPLEX, allocatable :: ULL(:,:,:)
    DOUBLE COMPLEX, allocatable :: &
                      SRLLP(:,:),
                    WORK(:,:), &
                    WORK2(:,:), &
                    ALLP(:,:,:),BLLP(:,:,:), &
                    CLLP(:,:,:),DLLP(:,:,:), &
                    SLV(:,:,:,:),SRV(:,:,:,:), &
                    SLV1(:,:,:,:),SRV1(:,:,:,:), &
                    SLV2(:,:,:,:),SRV2(:,:,:,:), &
                    SLV3(:,:,:,:),SRV3(:,:,:,:), &
                    MRNVY(:,:,:), MRNVZ(:,:,:), &
                    MRJVY(:,:,:), MRJVZ(:,:,:), &
                    MIHVY(:,:,:),MIHVZ(:,:,:), &
                    MIJVY(:,:,:),MIJVZ(:,:,:), &
                    YILL(:,:,:),ZILL(:,:,:), &
                    YRLL(:,:,:), ZRLL(:,:,:), YRLLTMP(:,:,:), &
                    YILL1(:,:,:),ZILL1(:,:,:), &
                    YRLL1(:,:,:), ZRLL1(:,:,:), &
                    YILL2(:,:,:),ZILL2(:,:,:), &
                    YRLL2(:,:,:), ZRLL2(:,:,:), &
                      ULL(:,:,:),SLL(:,:,:),
                      RLL(:,:,:), !HLL(LMSIZE,LMSIZE,NRMAX),
                      VNL(:,:,:),
                    VHLR(:,:,:), &
                    VJLR(:,:,:), &
                    VHLI(:,:,:), &
                    VJLI(:,:,:)
                      VLL(:,:,:)
    DOUBLE COMPLEX, allocatable :: YIF(:,:,:), &
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                      YRF(:,:,:,:), &
                      ZIF(:,:,:,:), &
                     ZRF(:,:,:,:)
      DOUBLE COMPLEX ZSLC1SUM(0:NCHEB)
      DOUBLE PRECISION C1(0:NCHEB, 0:NCHEB), RPANBOUND(0:NPAN)
      DOUBLE PRECISION CSLC1(0:NCHEB,0:NCHEB), CSRC1(0:NCHEB,0:NCHEB), &
                       TAU(0:NCHEB,0:NPAN),CDDRC1(0:NCHEB,0:NCHEB),CDDRC1temp(0:
NCHEB), CDDRC1temp2, &
                       SLC1SUM(0:NCHEB),RMESH(NRMAX)
      INTEGER jlk index(:),IPIV(0:NCHEB,LMSIZE2)
      INTEGER, allocatable :: IPIV2(:)
      LOGICAL TEST
      INTEGER :: IERROR, USE SRATRICK
        INTEGER ISPINfullgmat
        DOUBLE PRECISION, parameter :: CVLIGHT = 274.0720442D0
      .. External Subroutines ..
      EXTERNAL ZGETRF, ZGETRS
      .. Intrinsic Functions ..
      INTRINSIC ABS, ATAN, COS, DIMAG, EXP, MAX, MIN, SIN, SQRT
      if ( .not. config_testflag('sph') .or. LMSIZE==1 ) then
        use_sratrick=0
      elseif ( config_testflag('sph') ) then
        use sratrick=1
      else
        stop '[rllsll] use_sratrick error '
      end if
         call timing_start('rllsll')
            call timing_start('prestuff2')
         IF (NSRA<=2) THEN
                       HLK(0:(LMAX+1)*NVEC-1,0:N),
        ALLOCATE(
                       JLK(0:(LMAX+1)*NVEC-1,0:N),
                         NLK(0:(LMAX+1)*NVEC-1,0:N),
                       HLK2(0:(LMAX+1)*NVEC-1,0:N),
                       JLK2(0:(LMAX+1)*NVEC-1,0:N)
                         NLK2(0:(LMAX+1)*NVEC-1,0:N)
        ELSEIF (NSRA==3) THEN
        ALLOCATE(
                       HLK (2*LMSIZE,0:N),
                       JLK (2*LMSIZE,0:N),
                         NLK (2*LMSIZE,0:N),
                       HLK2(2*LMSIZE,0:N),
                       JLK2(2*LMSIZE,0:N))
                         NLK2(2*LMSIZE,0:N) )
         ELSE.
         STOP '[RLLSLL] NSRA not known'
        END IF
! if ( config_testflag('writesourceterms')) then
    do lm1=1,ubound(jlk,1)
      write(3661,'(50000E)') jlk(lm1,:)
      write(3662,'(50000E)') hlk(lm1,:)
      write(3663,'(50000E)') jlk2(lm1,:)
     write(3664,'(50000E)') hlk2(lm1,:)
    end do
    write(*,*) jlk_index
! stop
! end if
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if ( config_testflag('checknanrllsll') ) then
  call checknan(vll,ierror)
  if (ierror==1) then
    write(*,*) 'vll nan'
    stop
  end if
  call checknan(hlk,ierror)
  if (ierror==1) then
    write(*,*) 'hlk nan'
    stop
  end if
  call checknan(jlk,ierror)
  if (ierror==1) then
    write(*,*) 'ilk nan'
    stop
  end if
  call checknan(hlk2,ierror)
  if (ierror==1) then
    write(*,*) 'hlk2 nan'
  end if
  call checknan(jlk2,ierror)
  if (ierror==1) then
    write(*,*) 'jlk2 nan'
    stop
  end if
end if
! write(*,*) jlk_index
      ALLOCATE ( ULL(LMSIZE2,LMSIZE,NRMAX)
    if ( use_sratrick==0 ) then
      ALLOCATE (SLV(0:NCHEB,LMSIZE2,0:NCHEB,LMSIZE2),SRV(0:NCHEB,LMSIZE2,0:NCHEB
,LMSIZE2) )
    elseif ( use sratrick==1 ) then
      ALLOCATE (WORK2((NCHEB+1)*LMSIZE,(NCHEB+1)*LMSIZE), IPIV2((NCHEB+1)*LMSIZE
))
      ALLOCATE (SLV1(0:NCHEB,LMSIZE,0:NCHEB,LMSIZE),SRV1(0:NCHEB,LMSIZE,0:NCHEB,
LMSIZE), &
                SLV2(0:NCHEB,LMSIZE,0:NCHEB,LMSIZE),SRV2(0:NCHEB,LMSIZE,0:NCHEB,
LMSIZE), &
                SLV3(0:NCHEB,LMSIZE,0:NCHEB,LMSIZE),SRV3(0:NCHEB,LMSIZE,0:NCHEB,
LMSIZE) )
     ALLOCATE (
                     YILL1(0:NCHEB,LMSIZE,LMSIZE),ZILL1(0:NCHEB,LMSIZE,LMSIZE),
&
                      YRLL1(0:NCHEB,LMSIZE,LMSIZE),ZRLL1(0:NCHEB,LMSIZE,LMSIZE),
                      YILL2(0:NCHEB,LMSIZE,LMSIZE),ZILL2(0:NCHEB,LMSIZE,LMSIZE),
æ
                      YRLL2(0:NCHEB,LMSIZE,LMSIZE),&RLL2(0:NCHEB,LMSIZE,LMSIZE),&
                      YRLLTMP(0:NCHEB,LMSIZE,LMSIZE) )
     stop '[rllsll] error with testflag sph'
   end if
      ALLOCATE(
                WORK(LMSIZE,LMSIZE),&
                ALLP(LMSIZE,LMSIZE,0:NPAN),BLLP(LMSIZE,LMSIZE,0:NPAN),&
                CLLP(LMSIZE,LMSIZE,0:NPAN),DLLP(LMSIZE,LMSIZE,0:NPAN),&
                MRNVY(LMSIZE,LMSIZE,NPAN),MRNVZ(LMSIZE,LMSIZE,NPAN),&
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                MRJVY(LMSIZE,LMSIZE,NPAN),MRJVZ(LMSIZE,LMSIZE,NPAN),&
                MIHVY(LMSIZE,LMSIZE,NPAN),MIHVZ(LMSIZE,LMSIZE,NPAN),&
                MIJVY(LMSIZE,LMSIZE,NPAN),MIJVZ(LMSIZE,LMSIZE,NPAN),&
                YILL(0:NCHEB,LMSIZE2,LMSIZE),&
                YRLL(0:NCHEB,LMSIZE2,LMSIZE),ZRLL(0:NCHEB,LMSIZE2,LMSIZE),&
                       ULL(LMSIZE,LMSIZE,NRMAX),SLL(LMSIZE,LMSIZE,NRMAX),
                       RLL(LMSIZE,LMSIZE,NRMAX), !HLL(LMSIZE,LMSIZE,NRMAX),
                VJLR(LMSIZE,LMSIZE2,0:NCHEB),VHLR(LMSIZE,LMSIZE2,0:NCHEB),&
                VJLI(LMSIZE,LMSIZE2,0:NCHEB),VHLI(LMSIZE,LMSIZE2,0:NCHEB))
      YRLL=(0.0D0,0.0D0)
      ZILL=(0.0D0,0.0D0)
      YRLL=(0.0D0,0.0D0)
      ZILL=(0.0D0,0.0D0)
      ALLOCATE( &
                     YIF (LMSIZE2, LMSIZE, 0:NCHEB, NPAN), &
                     YRF(LMSIZE2,LMSIZE,0:NCHEB,NPAN),&
                     ZIF(LMSIZE2,LMSIZE,0:NCHEB,NPAN),&
                     ZRF(LMSIZE2,LMSIZE,0:NCHEB,NPAN) )
       ERVD = ETN
        LM1 = 1
       DO L1 = 0, LMAX
          DO\ M = -L1, L1
           LOFLM(LM1) = L1
           LM1 = LM1 + 1
          END DO
        END DO
          write(*,*) nvec,LMSIZE2,LMSIZE
           stop
! Bauer added for Spinorbit Coupling
! LOFLM is an (LMAX+1)**2 array. LOFLM = (/ LOFLM, LOFLM /)
!!
         VLL=czero
       IF (NSRA<=2) THEN
          LM1 = 1
          DO IVEC=1,NVEC
           DO ISPINfullgmat=0,use_fullgmat
             DO L1 = 0.LMAX
               DO\ M = -L1, L1
                 LOFLM(LM1) = L1+(IVEC-1)*(LMAX+1)
    !
                   print *, lm1,loflm(lm1)
                 LM1 = LM1 + 1
               END DO
             END DO
           END DO!ISPINORBIT=0, use_fullgmat
          END DO !NVEC
       ELSE IF (NSRA==3) THEN
         DO LM1=1,LMSIZE*NVEC
           LOFLM(LM1) = LM1
          END DO !NVEC
       END TF
      DO IPAN = 1, NPAN
       DO ICHEB = 0, NCHEB
          MN = IPAN*NCHEB + IPAN - ICHEB
          TAU(ICHEB, IPAN) = RMESH(MN)
       END DO
      END DO
        IF (nsra==1) THEN
1 1
           EK = SQRT(ERYD)
          GMATPREFACTOR = SQRT(ERYD)
        ELSEIF (nsra==2) THEN
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           EK = SORT(ERYD+(ERYD/CVLIGHT)**2)
         GMATPREFACTOR = SQRT(ERYD+(ERYD/CVLIGHT)**2) *(1.0D0+ERYD/CVLIGHT**2)
       ELSEIF (nsra==3) THEN
           EK = SORT(ERYD+(ERYD/CVLIGHT)**2)
         GMATPREFACTOR = SQRT(ERYD+(ERYD/CVLIGHT)**2)
         stop'[rllsll] wrong value for nvec'
       END IF
     call getCLambdaCinv(Ncheb,CDDRC1)
       do icheb = 0, ncheb
         do icheb2 = 0, icheb-1
           write(*,*) 'sub',icheb,icheb2
                              = CDDRC1(icheb2,icheb)
           CDDRC1temp2
           CDDRC1(icheb2,icheb) = CDDRC1(icheb,icheb2)
           CDDRC1(icheb,icheb2) = CDDRC1temp2
         end do
       end do
! stop
       do icheb = 0, ncheb
         write(11,'(5000E)') CDDRC1(icheb,:)
       end do
       do\ icheb = 0, (ncheb-1)/2
         write(*,*) 'sub',icheb,ncheb-icheb
         CDDRC1temp
                         = CDDRC1(:,icheb)
         CDDRC1(:,icheb)
                             = CDDRC1(:,ncheb-icheb)
         CDDRC1(:,ncheb-icheb) = CDDRC1temp
       do icheb = 0, (ncheb-1)/2
         write(*,*) 'sub',icheb,ncheb-icheb
                             = CDDRC1(icheb,:)
         CDDRC1temp
         CDDRC1(icheb,:)
                             = CDDRC1(ncheb-icheb,:)
        CDDRC1(ncheb-icheb,:) = CDDRC1temp
       end do
! stop
       do icheb = 0, ncheb
        write(12,'(5000E)') CDDRC1(icheb.:)
       end do
       CDDRC1=0.0D0
       DO icheb=0.ncheb
         CDDRC1(icheb,icheb)=1.0D0
     CALL CHEBINT(CSLC1,CSRC1,SLC1SUM,C1,NCHEB)
       do icheb = 0, ncheb
        write(13,'(5000E)') CSLC1(icheb,:)
       end do
call timing_start('local')
! loop over subintervals
     DO IPAN = 1,NPAN
! initialization
     call timing_start('local1')
         DO LM2 = 1, LMSIZE
           DO LM1 = 1.LMSIZE2
             DO ICHEB = 0,NCHEB
               YRLL(ICHEB, LM1, LM2) = CZERO
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                ZRLL(ICHEB, LM1, LM2) = CZERO
                YILL(ICHEB, LM1, LM2) = CZERO
                ZILL(ICHEB, LM1, LM2) = CZERO
              END DO
            END DO
          END DO
          DO LM2 = 1, LMSIZE2
            DO LM1 = 1, LMSIZE2
              DO ICHEB = 0,NCHEB
                DO ICHEB1 = 0,NCHEB
                  SLV(ICHEB1, LM1, ICHEB, LM2) = 0.0D0
                  SRV(ICHEB1,LM1,ICHEB,LM2) = 0.0D0
              END DO
            END DO
          END DO
          DO LM1 = 1, LMSIZE2
            DO\ ICHEB\ =\ O\ ,NCHEB
              SLV(ICHEB, LM1, ICHEB, LM1) = 1.0D0
              SRV(ICHEB, LM1, ICHEB, LM1) = 1.0D0
            END DO
          END DO
          VNL=czero
        VHLR=czero
        VJLR=czero
        VHLI=czero
        VJLI=czero
        if (use_sratrick==0) then
          YRLL=czero
          ZRLL=czero
          YILL=czero
          ZILL=czero
        else
          YRLL1=czero
          ZRLL1=czero
          YILL1=czero
          ZILL1=czero
          YRLL2=czero
          ZRIJ2=czero
          YILL2=czero
          ZILL2=czero
          end if
! 1. prepare VJLR, VNL, VHLR, which appear in the integrands
! TAU(K.IPAN) is used instead of TAU(K,IPAN)**2, which directly gives
! RLL(r) and SLL(r) multiplied with r
! 2. prepare the source terms YR, ZR, YI, ZI
! because of the conventions used by
! Gonzalez et al, Journal of Computational Physics 134, 134-149 (1997)
! a factor sqrt(E) is included in the source terms
! this factor is removed by the definition of ZSLC1SUM given below
       DO ICHEB = 0, NCHEB
          MN = IPAN*NCHEB + IPAN - ICHEB
             write(76301,'(50000E)') JLK(:,MN) !(:,:,:,M)
             write(76301,'(50000E)') HLK(:,MN) !(:,:,:,M)
            IF (NSRA<=2) THEN
              CALL BESHANK(HLK(0,K),JLK(0,K),EK*TAU(K,IPAN),LMAX)
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              IF (NSRA==2) THEN
                CALL BESHANK_SMALLCOMP(HLK(0,K),JLK(0,K),
                                   EK*TAU(K, IPAN), TAU(K, IPAN), ERYD, LMAX)
               DO L1 = 0.NVEC*(LMAX+1)-1
                 HLK(L1,K) = -CI*HLK(L1,K)
               END DO
               DO L1 = 0, NVEC*(LMAX+1)-1
                 JLK2(L1,K) = JLK(L1,K)
                 HLK2(L1,K) = HLK(L1,K)
            ELSE IF (NSRA==3) THEN
                               PASCAL
                 ! Schleifen richtig? zusAmtzlich noch NLK, NLK2 definieren.
            call SourceTermSuperVector(LMAX,ERYD,TAU(K,IPAN),JLK(:,K),
                   HLK(:,K),JLK2(:,K),HLK2(:,K))
            END IF
            stop
            DO IVEC=1,NVEC
              DO\ LM2 = 1, LMSIZE2
                DO LM1 = 1, LMSIZE
                  L1 = jlk\_index(LM1+LMSIZE*(IVEC-1))
                  VJLR(LM1,LM2,ICHEB) = VJLR(LM1,LM2,ICHEB) + &
                       GMATPREFACTOR*TAU(ICHEB, IPAN)*JLK2(L1,MN)*VLL(LM1+LMSIZE*(
IVEC-1), LM2, MN)
                  VJLI(LM1,LM2,ICHEB) = VJLI(LM1,LM2,ICHEB) + &
                       GMATPREFACTOR*TAU(ICHEB, IPAN)*JLK2(L1,MN)*VLL(LM2,LM1+LMS
IZE*(IVEC-1),MN)
                  VHLR(LM1,LM2,ICHEB) = VHLR(LM1,LM2,ICHEB) + &
                       GMATPREFACTOR*TAU(ICHEB, IPAN)*HLK2(L1,MN)*VLL(LM1+LMSIZE*
(IVEC-1), LM2, MN)
                  VHLI(LM1,LM2,ICHEB) = VHLI(LM1,LM2,ICHEB) + &
                       GMATPREFACTOR*TAU(ICHEB, IPAN)*HLK2(L1,MN)*VLL(LM2,LM1+LMS
IZE*(IVEC-1),MN)
                END DO
              END DO
            END DO !NVEC
                 (cmoderll=='1') THEN
            DO IVEC2=1, NVEC
              DO LM2 = 1,LMSIZE
                DO IVEC=1, NVEC
                  DO LM1 = 1,LMSIZE
                    L1 = jlk_index( LM1+LMSIZE*(IVEC-1) )
                    VJLR(LM1,LM2+LMSIZE*(IVEC2-1),ICHEB) = VJLR(LM1,LM2+LMSIZE*(
IVEC2-1), ICHEB) + &
                         GMATPREFACTOR*TAU(ICHEB, IPAN)*JLK2(L1,MN)*VLL(LM1+LMSIZE
*(IVEC-1),LM2+LMSIZE*(IVEC2-1),MN)
                    VHLR(LM1,LM2+LMSIZE*(IVEC2-1),ICHEB) = VHLR(LM1,LM2+LMSIZE*(
IVEC2-1), ICHEB) + &
                         GMATPREFACTOR*TAU(ICHEB, IPAN)*HLK2(L1,MN)*VLL(LM1+LMSIZE
*(IVEC-1),LM2+LMSIZE*(IVEC2-1),MN)
                  END DO
                END DO
              END DO
            END DO !NVEC
          ELSEIF (cmoderll=='T') THEN
            DO IVEC2=1, NVEC
              DO LM2 = 1.LMSIZE
                DO IVEC=1, NVEC
                  DO LM1 = 1,LMSIZE
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                    L1 = jlk index( LM1+LMSIZE*(IVEC-1) )
                    VJLR(LM1,LM2+LMSIZE*(IVEC2-1),ICHEB) = VJLR(LM1,LM2+LMSIZE*(
IVEC2-1), ICHEB) + &
                        GMATPREFACTOR*TAU(ICHEB, IPAN)*JLK2(L1,MN)*VLL(LM2+LMSIZE
*(IVEC-1),LM1+LMSIZE*(IVEC2-1),MN)
                    VHLR(LM1,LM2+LMSIZE*(IVEC2-1),ICHEB) = VHLR(LM1,LM2+LMSIZE*(
IVEC2-1), ICHEB) + &
                        GMATPREFACTOR*TAU(ICHEB,IPAN)*HLK2(L1,MN)*VLL(LM2+LMSIZE
*(IVEC-1),LM1+LMSIZE*(IVEC2-1),MN)
                  END DO
                END DO
              END DO
            END DO !NVEC
          ELSEIF (cmoderll=='0') THEN
                    VJLR(:,:,ICHEB) = CZERO
                    VHLR(:,:,ICHEB) = CZERO
          ELSE
            STOP' [RLLSLL] MODE NOT KNOWN'
          END IF
                 (cmodesll=='1') THEN
          TF
            DO IVEC2=1, NVEC
              DO LM2 = 1,LMSIZE
                DO IVEC=1, NVEC
                  DO LM1 = 1,LMSIZE
                    L1 = jlk_index( LM1+LMSIZE*(IVEC-1) )
                    VJLI(LM1,LM2+LMSIZE*(IVEC2-1),ICHEB) = VJLI(LM1,LM2+LMSIZE*(
IVEC2-1), ICHEB) + &
                        GMATPREFACTOR*TAU(ICHEB, IPAN)*JLK2(L1,MN)*VLL(LM1+LMSIZE
*(IVEC-1),LM2+LMSIZE*(IVEC2-1),MN)
                    VHLI(LM1,LM2+LMSIZE*(IVEC2-1),ICHEB) = VHLI(LM1,LM2+LMSIZE*(
IVEC2-1),ICHEB) + &
                        GMATPREFACTOR*TAU(ICHEB,IPAN)*HLK2(L1,MN)*VLL(LM1+LMSIZE
*(IVEC-1),LM2+LMSIZE*(IVEC2-1),MN)
                  END DO
                END DO
              END DO
            END DO !NVEC
          ELSEIF (cmodesll=='T') THEN
            DO IVEC2=1.NVEC
              DO LM2 = 1,LMSIZE
                DO IVEC=1, NVEC
                  DO LM1 = 1,LMSIZE
                    L1 = jlk_index( LM1+LMSIZE*(IVEC-1) )
                    VJLI(LM1,LM2+LMSIZE*(IVEC2-1),ICHEB) = VJLI(LM1,LM2+LMSIZE*(
IVEC2-1), ICHEB) + &
                        GMATPREFACTOR*TAU(ICHEB, IPAN)*JLK2(L1,MN)*VLL(LM2+LMSIZE
*(IVEC-1),LM1+LMSIZE*(IVEC2-1),MN)
                    VHLI(LM1,LM2+LMSIZE*(IVEC2-1),ICHEB) = VHLI(LM1,LM2+LMSIZE*(
IVEC2-1), ICHEB) + &
                        GMATPREFACTOR*TAU(ICHEB, IPAN)*HLK2(L1,MN)*VLL(LM2+LMSIZE
*(IVEC-1),LM1+LMSIZE*(IVEC2-1),MN)
                  END DO
                END DO
              END DO
            END DO !NVEC
          ELSEIF (cmodes11=='0') THEN
                    VJLI(:,:,ICHEB) = CZERO
                    VHLI(:,:,ICHEB) = CZERO
          FLSE
            STOP' [RLLSLL] MODE NOT KNOWN'
          END IF
            DO IVEC=1,NVEC
              DO LM2 = 1, LMSIZE
                DO LM1 = 1.LMSIZE
                  L1 = LOFLM( LM1+LMSIZE*(IVEC-1) )
                  VJLR(LM1,LM2+LMSIZE*(IVEC-1),K) =
```

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                     EK*TAU(K, IPAN)*JLK(L1,K)*VLL(LM1,LM2,MN)
                  VNL(LM1,LM2+LMSIZE*(IVEC-1),K) =
                    -EK*TAU(K, IPAN)*NLK(L1,K)*VLL(LM1,LM2,MN)
                  VHLR(LM1,LM2+LMSIZE*(IVEC-1),K) =
                    -EK*TAU(K,IPAN)*HLK(L1,K)*VLL(LM1,LM2,MN)
                END DO
              END DO
            END DO !IVEC=1,NVEC
          if ( use sratrick==0 ) then
           DO IVEC=1, NVEC
              DO LM1 = 1,LMSIZE
                L1 = jlk index( LM1+LMSIZE*(IVEC-1) )
                YRLL(ICHEB,LM1+LMSIZE*(IVEC-1),LM1) = TAU(ICHEB,IPAN)*JLK(L1,MN
                ZRLL(ICHEB,LM1+LMSIZE*(IVEC-1),LM1) = TAU(ICHEB,IPAN)*HLK(L1,MN
                YILL(ICHEB, LM1+LMSIZE*(IVEC-1), LM1) = TAU(ICHEB, IPAN)*HLK(L1, MN
                ZILL(ICHEB,LM1+LMSIZE*(IVEC-1),LM1) = TAU(ICHEB,IPAN)*JLK(L1,MN
                  write(76401,'(50000E)') YRLL(ICHEB,LM1+LMSIZE*(IVEC-1),LM1), &
                                          ZRLL(ICHEB,LM1+LMSIZE*(IVEC-1),LM1), &
                                          YILL(ICHEB,LM1+LMSIZE*(IVEC-1),LM1), &
                                          ZILL(ICHEB,LM1+LMSIZE*(IVEC-1),LM1)
               if (cmodetest=='c') then
                  ZRLL(ICHEB,LM1+LMSIZE*(IVEC-1),LM1) = conjg(ZRLL(ICHEB,LM1+L
MSIZE*(IVEC-1),LM1) )
                  YILL(ICHEB,LM1+LMSIZE*(IVEC-1),LM1) = conjg( ZRLL(ICHEB,LM1+L
MSIZE*(IVEC-1),LM1) )
               end if
              END DO
            END DO !IVEC=1,NVEC
          elseif ( use_sratrick==1 ) then
            DO LM1 = 1,LMSIZE
              L1 = jlk_index( LM1+LMSIZE*(1-1) )
              L2 = ilk index( LM1+LMSIZE*(2-1) )
              YRLL1(ICHEB,LM1+LMSIZE*(1-1),LM1) = TAU(ICHEB,IPAN)*JLK(L1,MN)
              ZRLL1(ICHEB,LM1+LMSIZE*(1-1),LM1) = TAU(ICHEB,IPAN)*HLK(L1,MN)
              YILL1(ICHEB,LM1+LMSIZE*(1-1),LM1) = TAU(ICHEB,IPAN)*HLK(L1,MN)
              ZILL1(ICHEB,LM1+LMSIZE*(1-1),LM1) = TAU(ICHEB,IPAN)*JLK(L1,MN)
              YRLL2(ICHEB,LM1+LMSIZE*(1-1),LM1) = TAU(ICHEB,IPAN)*JLK(L2,MN)
              ZRLL2(ICHEB,LM1+LMSIZE*(1-1),LM1) = TAU(ICHEB,IPAN)*HLK(L2,MN)
              YILL2(ICHEB, LM1+LMSIZE*(1-1), LM1) = TAU(ICHEB, IPAN)*HLK(L2, MN)
              ZILL2(ICHEB,LM1+LMSIZE*(1-1),LM1) = TAU(ICHEB,IPAN)*JLK(L2,MN)
           END DO
          end if
        END DO
          write(76200,'(50000E)') TAU!(ICHEB,IPAN)
          write(76201,'(50000E)') YRLL !(:,:,:,M)
          write(76202,'(50000E)') ZRLL !(:,:,:,M)
          write(76203,'(50000E)') YILL !(:,:,:,M)
          write(76204,'(50000E)') ZILL !(:,:,:,M)
          stop
! determine the matrices in equations (4.5a) and (4.5b)
        if ( use_sratrick==0 ) then
```

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          DO ICHEB2 = 0, NCHEB
            DO ICHEB = 0, NCHEB
              MN = IPAN*NCHEB + IPAN - ICHEB
              DO LM2 = 1, LMSIZE2
                DO IVEC=1, NVEC
                  DO LM3 = 1,LMSIZE
                    LM1=LM3+(IVEC-1)*LMSIZE
                    L1 = jlk_index(LM1)
                    SLV(ICHEB, LM1, ICHEB2, LM2) = &
                   ( TAU(ICHEB, IPAN)*JLK(L1,MN)*CSLC1(ICHEB,ICHEB2)*VHLR(LM3,LM2,
ICHEB2) &
                    -TAU(ICHEB, IPAN)*HLK(L1,MN)*CSLC1(ICHEB,ICHEB2)*VJLR(LM3,LM2
,ICHEB2))&
                  *(RPANBOUND(IPAN)-RPANBOUND(IPAN-1))/ 2.D0
                    SRV(ICHEB,LM1,ICHEB2,LM2) = &
                   (-TAU(ICHEB, IPAN)*JLK(L1,MN)*CSRC1(ICHEB,ICHEB2)*VHLI(LM3,LM2,
ICHEB2) &
                    +TAU(ICHEB, IPAN)*HLK(L1,MN)*CSRC1(ICHEB,ICHEB2)*VJLI(LM3,LM2
,ICHEB2)) &
                      *(RPANBOUND(IPAN)-RPANBOUND(IPAN-1))/ 2.D0
                  END DO
                END DO
              END DO
            END DO
          END DO
       write(*,*) 'test'
! SLV=(0.0D0,0.0D0)
         if (allocated(VLL2DDR)) then
            DO LM1 = 1, LMSIZE
              L1 = jlk\_index(LM1)
              DO ICHEB2 = 0,NCHEB
                DO ICHEB = 0,NCHEB
                  DO ICHEB3 = 0,NCHEB
                    MN = IPAN*NCHEB + IPAN - ICHEB3
                    MN2 = IPAN*NCHEB + IPAN - ICHEB
                    DO IVEC=1,NVEC
                      DO LM3 = 1.LMSIZE
                        LM1=LM3+(IVEC-1)*LMSIZE
                      SLV(ICHEB,LM1,ICHEB2,LM1) = SLV(ICHEB,LM1,ICHEB2,LM1) + &
                    ( TAU(ICHEB, IPAN)*JLK(L1, MN2)*CSLC1(ICHEB, ICHEB3)*TAU(ICHEB3
,IPAN)*HLK2(L1,MN)*VLL2DDR(LM1,MN)*CDDRC1(ICHEB3,ICHEB2) &
                     -TAU(ICHEB, IPAN)*HLK(L1, MN2)*CSLC1(ICHEB, ICHEB3)*TAU(ICHEB3
,IPAN)*JLK2(L1,MN)*VLL2DDR(LM1,MN)*CDDRC1(ICHEB3,ICHEB2))&
                       *GMATPREFACTOR !&
1 1
                      *(RPANBOUND(IPAN)-RPANBOUND(IPAN-1))/ 2.D0
                      SRV(ICHEB,LM1,ICHEB2,LM1) = SRV(ICHEB,LM1,ICHEB2,LM1) + &
                    ( TAU(ICHEB, IPAN)*JLK(L1,MN2)*CSRC1(ICHEB, ICHEB3)*TAU(ICHEB3
,IPAN)*HLK2(L1,MN)*VLL2DDR(LM1,MN)*CDDRC1(ICHEB3,ICHEB2) &
                     -TAU(ICHEB, IPAN)*HLK(L1, MN2)*CSRC1(ICHEB, ICHEB3)*TAU(ICHEB3
,IPAN)*JLK2(L1,MN)*VLL2DDR(LM1,MN)*CDDRC1(ICHEB3,ICHEB2))&
                      *GMATPREFACTOR !&
!!
                       *(RPANBOUND(IPAN)-RPANBOUND(IPAN-1))/ 2.D0
                        SRV(TCHEB.LM1.TCHEB2.LM2) = &
                      (-TAU(ICHEB, IPAN)*JLK(L1, MN)*CSRC1(ICHEB, ICHEB2)*VHLI(LM3,
LM2, ICHEB2) &
1 1
                        +TAU(ICHEB, IPAN)*HLK(L1,MN)*CSRC1(ICHEB, ICHEB2)*VJLI(LM3
,LM2,ICHEB2)) &
!!
                          *(RPANBOUND(IPAN)-RPANBOUND(IPAN-1))/ 2.D0
1 1
                      END DO
!!
                    END DO
                  END DO
                END DO
              END DO
            END DO
```

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         end if !allocated
              DO LM1 = 1,LMSIZE
                DO ICHEB = 0,NCHEB
                  write(5523,'(50000E)') SLV(:,:,ICHEB,LM1)
                END DO
              END DO
        write(*,*) 'test'
! stop
          DO LM1 = 1,LMSIZE2
            DO ICHEB = 0, NCHEB
              SLV(ICHEB,LM1,ICHEB,LM1) = SLV(ICHEB,LM1,ICHEB,LM1) + 1.D0
              SRV(ICHEB,LM1,ICHEB,LM1) = SRV(ICHEB,LM1,ICHEB,LM1) + 1.D0
            END DO
          END DO
        ELSEIF ( use_sratrick==1 ) then
          DO ICHEB2 = 0,NCHEB
            DO ICHEB = 0,NCHEB
              MN = IPAN*NCHEB + IPAN - ICHEB
              DO LM2 = 1,LMSIZE
                DO IVEC=1,1
                  DO LM3 = 1, LMSIZE
                    LM1=LM3+(IVEC-1)*LMSIZE
                    L1 = jlk\_index(LM1)
                    SLV1(ICHEB,LM1,ICHEB2,LM2) = &
                  ( TAU(ICHEB, IPAN)*JLK(L1,MN)*CSLC1(ICHEB,ICHEB2)*VHLR(LM3,LM2,
ICHEB2) &
                   -TAU(ICHEB, IPAN)*HLK(L1, MN)*CSLC1(ICHEB, ICHEB2)*VJLR(LM3, LM2,
ICHEB2))&
                  *(RPANBOUND(IPAN)-RPANBOUND(IPAN-1))/ 2.D0
                    SRV1(ICHEB,LM1,ICHEB2,LM2) = &
                  (-TAU(ICHEB, IPAN)*JLK(L1,MN)*CSRC1(ICHEB,ICHEB2)*VHLI(LM3,LM2,
ICHEB2) &
                   +TAU(ICHEB, IPAN)*HLK(L1,MN)*CSRC1(ICHEB,ICHEB2)*VJLI(LM3,LM2,
ICHEB2)) &
                       *(RPANBOUND(IPAN)-RPANBOUND(IPAN-1))/ 2.D0
                  END DO
                END DO
              END DO
            END DO
          END DO
          DO ICHEB2 = 0, NCHEB
            DO ICHEB = 0, NCHEB
              MN = IPAN*NCHEB + IPAN - ICHEB
              DO LM2 = 1,LMSIZE
                DO IVEC=2,2
                  DO LM3 = 1,LMSIZE
                    LM1=LM3+(IVEC-1)*LMSIZE
                    L1 = jlk_index(LM1)
                    SLV2(ICHEB,LM3,ICHEB2,LM2) = &
                  ( TAU(ICHEB, IPAN)*JLK(L1, MN)*CSLC1(ICHEB, ICHEB2)*VHLR(LM3, LM2,
ICHEB2) &
                   -TAU(ICHEB, IPAN)*HLK(L1, MN)*CSLC1(ICHEB, ICHEB2)*VJLR(LM3, LM2,
ICHEB2))&
                  *(RPANBOUND(IPAN)-RPANBOUND(IPAN-1))/ 2.D0
                    SRV2(ICHEB,LM3,ICHEB2,LM2) = &
                  (-TAU(ICHEB, IPAN)*JLK(L1,MN)*CSRC1(ICHEB,ICHEB2)*VHLI(LM3,LM2
```

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ICHEB2) &
                   +TAU(ICHEB, IPAN)*HLK(L1, MN)*CSRC1(ICHEB, ICHEB2)*VJLI(LM3, LM2,
ICHEB2)) &
                       *(RPANBOUND(IPAN)-RPANBOUND(IPAN-1))/ 2.D0
                  END DO
                END DO
              END DO
            END DO
          END DO
          DO LM1 = 1,LMSIZE
            DO ICHEB = 0, NCHEB
              SLV1(ICHEB,LM1,ICHEB,LM1) = SLV1(ICHEB,LM1,ICHEB,LM1) + 1.D0
              SRV1(ICHEB,LM1,ICHEB,LM1) = SRV1(ICHEB,LM1,ICHEB,LM1) + 1.D0
                SLV2(ICHEB,LM1,ICHEB,LM1) = SLV2(ICHEB,LM1,ICHEB,LM1) + 1.D0
                SRV2(ICHEB,LM1,ICHEB,LM1) = SRV2(ICHEB,LM1,ICHEB,LM1) + 1.D0
          END DO
        ELSE
          stop '[rllsll] error in inversion '
        END IF
        call timing_pause('local1')
        call timing_start('local2')
 determine the local solutions
 solve the equations SLV*YRLL=S and SLV*ZRLL=C
                 and SRV*YILL=C and SRV*ZILL=S
          DO LM1 = 1, LMSIZE
          DO J = 0,N
                 write(452,'(5000F)') SLV(:,:,J,LM1)
          END DO
          END DO
          DO LM1 = 1,LMSIZE
          DO ICHEB = 0,NCHEB
                 write(452,'(5000F)') YRLL(ICHEB,:,:)
          END DO
          END DO
         if (lmsize/=1) then
          DO LM1 = 1.LMSIZE2
            DO ICHEB = 0.NCHEB
          write(3883,'(5000E)') slv(:,:,ICHEB,lm1)
          end do
          end do
          stop
         end if
         if (lmsize/=1) then
          DO LM1 = 1, LMSIZE
            DO ICHEB = 0,NCHEB
          write(3884,'(5000E)') slv1(:,:,ICHEB,lm1)
          end do
          end do
          DO LM1 = 1, LMSIZE
           DO ICHEB = 0,NCHEB
          write(3885,'(5000E)') slv2(:,:,ICHEB,lm1)
          end do
          end do
          stop
         end if
```

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           if ( .true. ) then
      if ( use_sratrick==0 ) then
        NPLM = (NCHEB+1)*LMSIZE2
          IF (cmoderll/='0') THEN
            CALL ZGETRF(NPLM, NPLM, SLV, NPLM, IPIV, INFO)
             IF (INFO/=0) STOP'RLLSLL: ZGETRF'
            CALL ZGETRS('N', NPLM, LMSIZE, SLV, NPLM, IPIV, YRLL, NPLM, INFO)
            CALL ZGETRS('N', NPLM, LMSIZE, SLV, NPLM, IPIV, ZRLL, NPLM, INFO)
            ELSE
               YRLL=CZERO
               ZRLL=CZERO
          END IF
          IF (cmodesl1/='0') THEN
            CALL ZGETRF(NPLM, NPLM, SRV, NPLM, IPIV, INFO)
            IF (INFO/=0) STOP'RLLSLL: ZGETRF'
            CALL ZGETRS('N', NPLM, LMSIZE, SRV, NPLM, IPIV, YILL, NPLM, INFO)
            CALL ZGETRS('N', NPLM, LMSIZE, SRV, NPLM, IPIV, ZILL, NPLM, INFO)
            ELSE
               YILL=CZERO
               ZILL=CZERO
          END IF
          elseif ( .false. ) then
      elseif ( use_sratrick==1 ) then
        NPLM = (NCHEB+1)*LMSIZE
               call rllslltools solvesra(NPLM,LMSIZE,SLV,YRLL,ZRLL)
        call timing start('local2.1')
         call inverse(NPLM,slv1,work2,ipiv2)
! call ZGETRF( NPLM, NPLM, slv1, NPLM, IPIV2, INFO )
!! if (info/=0) stop '[inverse] error INFO'
! call ZGETRI( NPLM, slv1, NPLM, IPIV2, WORK2, NPLM*NPLM, INFO )
         call inverse(NPLM, srv1, work2, ipiv2)
! call ZGETRF( NPLM, NPLM, srv1, NPLM, IPIV2, INFO )
!! if (info/=0) stop '[inverse] error INFO'
! call ZGETRI( NPLM, srv1, NPLM, IPIV2, WORK2, NPLM*NPLM, INFO )
        call timing_pause('local2.1')
        call timing_start('local2.2')
            CALL ZGEMM('N','N',NPLM,NPLM,NPLM,-CONE,slv2, &
                 NPLM, slv1, NPLM, CZERO, slv3, NPLM)
           CALL ZGEMM('N','N',NPLM,NPLM,NPLM,-CONE,srv2, &
                 NPLM, srv1, NPLM, CZERO, srv3, NPLM)
         CALL ZGEMM('N','N', NPLM, LMSIZE, NPLM, CONE, slv1, &
               NPLM, YRLL1, NPLM, CZERO, YRLLTMP, NPLM)
         YRLL1=YRLLTMP
         CALL ZGEMM('N','N', NPLM, LMSIZE, NPLM, -CONE, slv2, &
               NPLM, YRLL1, NPLM, CONE, YRLL2, NPLM)
         CALL ZGEMM('N','N',NPLM,LMSIZE,NPLM,CONE,slv1, &
              NPLM, ZRLL1, NPLM, CZERO, YRLLTMP, NPLM)
          ZRLL1=YRLLTMP
         CALL ZGEMM('N','N', NPLM, LMSIZE, NPLM, -CONE, slv2, &
               NPLM, ZRLL1, NPLM, CONE, ZRLL2, NPLM)
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         CALL ZGEMM('N','N',NPLM,LMSIZE,NPLM,CONE,srv1, &
              NPLM,YILL1,NPLM,CZERO,YRLLTMP,NPLM)
         YILL1=YRLLTMP
         CALL ZGEMM('N','N',NPLM,LMSIZE,NPLM,-CONE,srv2, &
              NPLM,YILL1,NPLM,CONE,YILL2,NPLM)
         CALL ZGEMM('N','N', NPLM, LMSIZE, NPLM, CONE, srv1, &
              NPLM,ZILL1,NPLM,CZERO,YRLLTMP,NPLM)
         ZILL1=YRLLTMP
         CALL ZGEMM('N','N',NPLM,LMSIZE,NPLM,-CONE,srv2, &
              NPLM, ZILL1, NPLM, CONE, ZILL2, NPLM)
        call timing pause('local2.2')
            call rllslltools(NPLM, NCHEB+1, LMSIZE, SLV, YRLL, ZRLL)
            call rllslltools(NPLM,NCHEB+1,LMSIZE,SRV,YILL,ZILL)
        ELSE.
          stop '[rllsll] error in inversion '
        END IF
if ( config_testflag('checknanrllsll') ) then
 call checknan(YRLL,ierror)
 if (ierror==1) then
    write(*,*) 'YRLL nan'
    stop
 end if
end if
         if (lmsize/=1) then
          DO ICHEB = 0,NCHEB
                 write(453,'(5000F)') YRLL1(ICHEB,:,:)
          END DO
            stop
! end if
      if ( use sratrick==0 ) then
       DO ICHEB = 0, NCHEB
          DO LM2 = 1.LMSIZE
            DO LM1 = 1.LMSIZE2
              YRF(LM1,LM2,ICHEB,IPAN) = YRLL(ICHEB,LM1,LM2)
              ZRF(LM1,LM2,ICHEB,IPAN) = ZRLL(ICHEB,LM1,LM2)
              YIF(LM1,LM2,ICHEB,IPAN) = YILL(ICHEB,LM1,LM2)
              ZIF(LM1,LM2,ICHEB,IPAN) = ZILL(ICHEB,LM1,LM2)
            END DO
          END DO
        END DO
      elseif ( use_sratrick==1 ) then
       DO ICHEB = 0.NCHEB
          DO LM2 = 1,LMSIZE
            DO LM1 = 1,LMSIZE
              YRF(LM1,LM2,ICHEB,IPAN) = YRLL1(ICHEB,LM1,LM2)
              ZRF(LM1,LM2,ICHEB,IPAN) = ZRLL1(ICHEB,LM1,LM2)
              YIF(LM1,LM2,ICHEB,IPAN) = YILL1(ICHEB,LM1,LM2)
              ZIF(LM1,LM2,ICHEB,IPAN) = ZILL1(ICHEB,LM1,LM2)
            END DO
          END DO
        END DO
        DO ICHEB = 0, NCHEB
          DO LM2 = 1,LMSIZE
```

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             DO LM1 = 1,LMSIZE
               YRF(LM1+LMSIZE,LM2,ICHEB,IPAN) = YRLL2(ICHEB,LM1,LM2)
               ZRF(LM1+LMSIZE,LM2,ICHEB,IPAN) = ZRLL2(ICHEB,LM1,LM2)
               YIF (LM1+LMSIZE, LM2, ICHEB, IPAN) = YILL2(ICHEB, LM1, LM2)
               ZIF(LM1+LMSIZE,LM2,ICHEB,IPAN) = ZILL2(ICHEB,LM1,LM2)
           END DO
         END DO
      end if
! if (lmsize/=1) then
          write(76101,'(99000E)') YRF(:,:,1,IPAN)
           write(76102,'(99000E)') ZRF(:,:,1,IPAN)
           write(76103,'(99000E)') YIF(:,:,1,IPAN)
           write(76104,'(99000E)') ZIF(:,:,1,IPAN)
! stop
! end if
! determine the left hand sides of equations (3.5), (3,6)
! (3.8), and (3.9) with the equations on page 143.
      call timing_pause('local2')
      call timing_start('local3')
      DO ICHEB = 0,NCHEB
         ZSLC1SUM(ICHEB) = SLC1SUM(ICHEB) * (RPANBOUND(IPAN)-RPANBOUND(IPAN-1))/
(2.D0)
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(0),VHLR(1,1,0), &
               LMSIZE, YRF(1,1,0,IPAN), LMSIZE2, CZERO, MRNVY(1,1,IPAN), LMSIZE)
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(0),VJLR(1,1,0), &
               LMSIZE, YRF(1,1,0,IPAN), LMSIZE2, CZERO, MRJVY(1,1,IPAN), LMSIZE)
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(0),VHLR(1,1,0), &
               LMSIZE, ZRF(1,1,0,IPAN), LMSIZE2, CZERO, MRNVZ(1,1,IPAN), LMSIZE)
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(0),VJLR(1,1,0), &
               LMSIZE, ZRF(1,1,0,IPAN), LMSIZE2, CZERO, MRJVZ(1,1,IPAN), LMSIZE)
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(0),VHLI(1,1,0), &
               LMSIZE, YIF(1,1,0,IPAN), LMSIZE2, CZERO, MIHVY(1,1,IPAN), LMSIZE)
          \textbf{CALL} \ \ \textbf{ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(0),VJLI(1,1,0), \& } \\
               LMSIZE, YIF(1,1,0,IPAN), LMSIZE2, CZERO, MIJVY(1,1,IPAN), LMSIZE)
         CALL ZGEMM('N','N', LMSIZE, LMSIZE, LMSIZE2, ZSLC1SUM(0), VHLI(1,1,0), &
               LMSIZE, ZIF(1,1,0,IPAN), LMSIZE2, CZERO, MIHVZ(1,1,IPAN), LMSIZE)
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE,ZSLC1SUM(0),VJLI(1,1,0), &
               LMSIZE, ZIF(1,1,0,IPAN), LMSIZE2, CZERO, MIJVZ(1,1,IPAN), LMSIZE)
         DO ICHEB = 1, NCHEB
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(ICHEB),VHLR(1,1,ICHE
B), &
               LMSIZE, YRF(1,1,1CHEB, IPAN), LMSIZE2, CONE, MRNVY(1,1,1PAN), LMSIZE)
          \textbf{CALL} \ \ \textbf{ZGEMM}(\ 'N'\ ,\ 'N'\ , \texttt{LMSIZE}\ , \texttt{LMSIZE}\ , \texttt{LMSIZE2}\ , \texttt{ZSLC1SUM}(\ \texttt{ICHEB}\ )\ , \texttt{VJLR}(\ 1\ ,\ 1\ ,\ \texttt{ICHE}\ )
B), &
               LMSIZE, YRF(1,1,ICHEB,IPAN),LMSIZE2,CONE,MRJVY(1,1,IPAN),LMSIZE)
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(ICHEB),VHLR(1,1,ICHE
B), &
               LMSIZE, ZRF(1,1,ICHEB,IPAN), LMSIZE2, CONE, MRNVZ(1,1,IPAN), LMSIZE)
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(ICHEB),VJLR(1,1,ICHE
B), &
               LMSIZE, ZRF(1,1,ICHEB, IPAN), LMSIZE2, CONE, MRJVZ(1,1,IPAN), LMSIZE)
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(ICHEB),VHLI(1,1,ICHE
B), &
               LMSIZE, YIF(1,1,1CHEB, IPAN), LMSIZE2, CONE, MIHVY(1,1,1PAN), LMSIZE)
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(ICHEB),VJLI(1,1,ICHE
B), &
               LMSIZE, YIF(1,1,ICHEB, IPAN), LMSIZE2, CONE, MIJVY(1,1,IPAN), LMSIZE)
         CALL ZGEMM('N','N', LMSIZE, LMSIZE, LMSIZE2, ZSLC1SUM(ICHEB), VHLI(1,1, ICHE
B), &
               LMSIZE, ZIF(1,1,ICHEB,IPAN),LMSIZE2,CONE,MIHVZ(1,1,IPAN),LMSIZE)
         CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE2,ZSLC1SUM(ICHEB),VJLI(1,1,ICHE
B), &
               LMSIZE, ZIF(1,1,ICHEB,IPAN), LMSIZE2, CONE, MIJVZ(1,1,IPAN), LMSIZE)
```

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        END DO
       call timing_pause('local3')
if ( config testflag('checknanrllsll') ) then
 call checknan(MRNVY,ierror)
 if (ierror==1) then
    write(*,*) 'MRNVY nan'
 end if
end if
if ( config_testflag('checknanrllsll') ) then
 call checknan(MRJVY,ierror)
 if (ierror==1) then
    write(*,*) 'MRJVY nan
   stop
 end if
end if
          write(76001,'(50000E)') MRNVY(:,:,IPAN)
          write(76002,'(50000E)') MRNVZ(:,:,IPAN)
          write(76003,'(50000E)') MIJVY(:,:,IPAN)
          write(76004,'(50000E)') MIJVZ(:,:,IPAN)
! end of loop over the subintervals
          call timing_stop('local')
          call timing start ('afterlocal')
! calculate A(M), B(M), C(M), D(M) for m from 1 to MMAX
! starting from A(0) = 1, B(0) = 0, C(MMAX) = 0 and D(MMAX) = 1
     DO LM2 = 1,LMSIZE
       DO LM1 = 1,LMSIZE
          BLLP(LM1,LM2,0) = 0.D0
          ALLP(LM1,LM2,0) = 0.D0
       END DO
      END DO
     DO LM1 = 1,LMSIZE
       ALLP(LM1,LM1,0) = 1.D0
     END DO
     DO IPAN = 1, NPAN
        CALL ZCOPY(LMSIZE*LMSIZE, ALLP(1,1,IPAN-1),1,ALLP(1,1,IPAN),1)
       CALL ZCOPY(LMSIZE*LMSIZE,BLLP(1,1,IPAN-1),1,BLLP(1,1,IPAN),1)
       CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE,-CONE,MRNVY(1,1,1PAN), &
                LMSIZE, ALLP(1,1,IPAN-1), LMSIZE, CONE, ALLP(1,1,IPAN), LMSIZE)
       CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE,-CONE,MRNVZ(1,1,IPAN), &
               LMSIZE, BLLP(1,1, IPAN-1), LMSIZE, CONE, ALLP(1,1, IPAN), LMSIZE)
       CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE, CONE,MRJVY(1,1,IPAN), &
                LMSIZE, ALLP(1,1,IPAN-1), LMSIZE, CONE, BLLP(1,1,IPAN), LMSIZE)
       CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE, CONE,MRJVZ(1,1,1PAN), &
               LMSIZE, BLLP(1,1,IPAN-1), LMSIZE, CONE, BLLP(1,1,IPAN), LMSIZE)
if ( config_testflag('checknanrllsll') ) then
 call checknan(MRNVY,ierror)
 if (ierror==1) then
    write(*,*) 'MRNVY nan'
    stop
 end if
end if
if ( config_testflag('checknanrllsll') ) then
 call checknan(MRNVZ,ierror)
 if (ierror==1) then
    write(*,*) 'MRNVY nan'
```

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  end if
end if
if ( config_testflag('checknanrllsll') ) then
  call checknan(ALLP, ierror)
  if (ierror==1) then
    write(*,*) 'ALLP nan'
    write(*,*) 'ALLP nan', ipan
    write(7878, '(50000E)') ALLP(:,:,IPAN)
    stop
  end if
end if
      END DO
      DO LM2 = 1,LMSIZE
        DO LM1 = 1,LMSIZE
          DLLP(LM1,LM2,NPAN) = 0.D0
          CLLP(LM1, LM2, NPAN) = 0.D0
        END DO
      END DO
      DO LM1 = 1,LMSIZE
        DLLP(LM1,LM1,NPAN) = 1.D0
      END DO
      DO IPAN = NPAN, 1, -1
        CALL ZCOPY(LMSIZE*LMSIZE,CLLP(1,1,IPAN),1,CLLP(1,1,IPAN-1),1)
        CALL ZCOPY(LMSIZE*LMSIZE,DLLP(1,1,IPAN),1,DLLP(1,1,IPAN-1),1)
         \textbf{CALL} \ \ \textbf{ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE, CONE,MIHVZ(1,1,IPAN), \& } \\
                  LMSIZE, CLLP(1,1,IPAN), LMSIZE, CONE, CLLP(1,1,IPAN-1), LMSIZE)
        CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE, CONE,MIHVY(1,1,IPAN), &
                  LMSIZE, DLLP(1,1,IPAN), LMSIZE, CONE, CLLP(1,1,IPAN-1), LMSIZE)
        CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE,-CONE,MIJVZ(1,1,IPAN), &
                  LMSIZE, CLLP(1,1,IPAN), LMSIZE, CONE, DLLP(1,1,IPAN-1), LMSIZE)
        CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE,-CONE,MIJVY(1,1,IPAN), &
                  LMSIZE, DLLP(1,1,IPAN), LMSIZE, CONE, DLLP(1,1,IPAN-1), LMSIZE)
      END DO
! determine the regular solution ULL and the irregular solution SLL
      DO IPAN = 1,NPAN
        DO ICHEB = 0.NCHEB
          MN = IPAN*NCHEB + IPAN - ICHEB
        CALL ZGEMM('N','N',LMSIZE2,LMSIZE,LMSIZE,CONE,YRF(1,1,ICHEB,IPAN), &
                  LMSIZE2, ALLP(1,1,1PAN-1), LMSIZE, CZERO, ULL(1,1,MN), LMSIZE2)
        CALL ZGEMM('N','N',LMSIZE2,LMSIZE,LMSIZE,CONE,ZRF(1,1,ICHEB,IPAN), &
                  LMSIZE2, BLLP(1,1,IPAN-1), LMSIZE, CONE, ULL(1,1,MN), LMSIZE2)
        CALL ZGEMM('N','N',LMSIZE2,LMSIZE,LMSIZE,CONE,ZIF(1,1,ICHEB,IPAN), &
                  LMSIZE2, CLLP(1,1,1PAN), LMSIZE, CZERO, SLL(1,1,MN), LMSIZE2)
        CALL ZGEMM('N','N',LMSIZE2,LMSIZE,LMSIZE,CONE,YIF(1,1,ICHEB,IPAN), &
                 LMSIZE2, DLLP(1,1,IPAN), LMSIZE, CONE, SLL(1,1,MN), LMSIZE2)
          write(6670,'(50000E)') CLLP(:,:,IPAN)
          write(6671,'(50000E)') DLLP(:,:,IPAN)
        END DO
      END DO
          call timing_stop('afterlocal')
            call timing_start('endstuff')
! replace regular wave function in the first subinterval by a
! linear function times r**(1+1)
! replace irregular wave function in the first subinterval by a
! linear function divided by r**1
        IF(config_testflag('wforigin')) THEN
        DO LM2 =1,LMSIZE
```

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        DO LM1 =1,LMSIZE
        PLLM = 0.5D0*(LOFLM(LM1)+LOFLM(LM2))
        PLLM = LOFLM(LM1)
        F1U = ULL(LM1, LM2, 2*N+2-N)/TAU(N, 2)**(PLLM+1.D0)
       F2U = ULL(LM1, LM2, 2*N+2-N/2)/TAU(N/2, 2)**(PLLM+1.D0)
        AU = (F1U*TAU(N/2,2)-F2U*TAU(N,2))/(TAU(N/2,2)-TAU(N,2))
        BU = (F1U-F2U)/(TAU(N,2)-TAU(N/2,2))
       F1S = SLL(LM1, LM2, 2*N+2-N)*TAU(N, 2)**PLLM
        F2S = SLL(LM1, LM2, 2*N+2-N/2)*TAU(N/2, 2)**PLLM
        AS = (F1S*TAU(N/2,2)-F2S*TAU(N,2))/(TAU(N/2,2)-TAU(N,2))
        BS = (F1S-F2S)/(TAU(N,2)-TAU(N/2,2))
       DO K = 0,N
          MN = N + 1 - K
          ULL(LM1,LM2,MN) = (AU+BU*TAU(K,1))*TAU(K,1)**(PLLM+1.D0)
          SLL(LM1,LM2,MN) = (AS+BS*TAU(K,1))/TAU(K,1)**PLLM
       END DO
       END DO
       END IF
! transform from Volterra solution to Fredholm solution
 calculate alpha and t matrices
        CALL ZAXPY(LMSIZE*LMSIZE,CI,BLLP(1,1,MMAX),1,ALLP(1,1,MMAX),1)
                                                                               ! C
alculate the transformation matrix alpha
                                                                            ! assu
ming A is calculated with a neuman function
                                                                            ! n=h+
ij (?)
!David
        DO NM = 1, NRMAX
       CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE,CONE,SLL(1,1,NM),
                    LMSIZE, ALLP(1,1,MMAX), LMSIZE, CZERO, HLL(1,1,NM), LMSIZE)
       END DO
! end David
      CALL ZGETRF(LMSIZE,LMSIZE,ALLP(1,1,NPAN),LMSIZE,IPIV,INFO)
invert alpha
      CALL ZGETRI(LMSIZE, ALLP(1,1,NPAN), LMSIZE, IPIV, WORK, LMSIZE*LMSIZE, INFO)
!invert alpha -> transformation matrix RLL=alpha^-1*RLL
      CALL ZGEMM('N','N',LMSIZE,LMSIZE,LMSIZE,CONE/GMATPREFACTOR,BLLP(1,1,NPAN
         ! calc t-matrix TLL = BLL*alpha^-1
                  LMSIZE, ALLP(1,1,NPAN), LMSIZE, CZERO, TLLP, LMSIZE)
       DO LM2 = 1.LMSIZE
       DO LM1 = 1, LMSIZE
        SRLLP(LM1,LM2) = 2.D0*EK*TLLP(LM1,LM2)
        END DO
       SRLLP(LM2,LM2) = SRLLP(LM2,LM2) + CI
       END DO
       CALL ZGETRF(LMSIZE.LMSIZE.SRLLP.LMSIZE.IPIV.INFO)
       CALL ZGETRI(LMSIZE, SRLLP, LMSIZE, IPIV, WORK, LMSIZE*LMSIZE, INFO)
      DO NM = 1, NRMAX
      CALL ZGEMM('N','N',LMSIZE2,LMSIZE,LMSIZE,CONE,ULL(1.1,NM), &
                  LMSIZE2, ALLP(1,1,NPAN), LMSIZE, CZERO, RLL(1,1,NM), LMSIZE2)
      END DO
      call timing_stop('endstuff')
      call timing_start('checknan')
       DO LM2 = 1, LMSIZE
          DO LM1 = 1, LMSIZE
           write(7381,'(50000E)') ULL(lm1,lm2,:)
          END DO
        END DO
            write(7382,'(50000E)') ALLP(:,:,NPAN)
```

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if ( config_testflag('checknanrllsll') ) then
  call checknan(ULL, ierror)
  if (ierror==1) then
    write(*,*) 'ULL nan'
    stop
  end if
end if
if ( config testflag('checknanrllsll') ) then
  call checknan(RLL,ierror)
  if (ierror==1) then
    write(*,*) 'RLL nan'
    stop
  end if
end if
      call timing_stop('checknan')
      call timing_stop('local1')
      call timing_stop('local2')
     if (use_sratrick==1) call timing_stop('local2.1')
     if (use_sratrick==1) call timing_stop('local2.2')
      call timing_stop('local3')
      call timing_stop('rllsll')
! stop
! write(554321,'(50000E)') ull(1,1,:)
      RETURN
      END SUBROUTINE
subroutine inverse(nmat, mat)
!interface
integer
                :: nmat
double complex :: mat(nmat,nmat)
double complex :: work(nmat,nmat)
!local
integer
                :: IPIV(nmat)
integer
               :: info
call ZGETRF( nmat, nmat, mat, nmat, IPIV, INFO )
if (info/=0) stop '[inverse] error INFO'
call ZGETRI( nmat, mat, nmat, IPIV, WORK, nmat*nmat, INFO )
if (info/=0) stop '[inverse] error INFO'
end subroutine inverse
      END MODULE MOD_RLLSLL
```