Word Embedding

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Slides mostly made by my student, Yunjey Choi, Cheonbok Park

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1. Word Embedding

- 1-1. Word Embedding이란?
- 1-2. Word2Vec 모델 및 알고리듬
- 1-3. Word2Vec 적용분야



기존의 Word Representation 방법

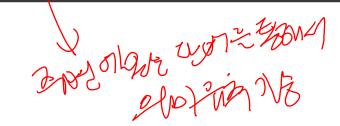
- 가장 쉬운 방법으로는 "one-hot" representation
- e.g., horse = [0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0]
- zebra = [0000000000001000]
- horse와 zebra 간의 유사도를 구하는 방법 중 하나를 생각해보면 horse ∩ zebra = 0 (nothing)
- 그러나, 우리는 horse와 zebra가 최소한 포유동물이라는 공통점을 가진다는 것을 알고 있음.
- 만약 단어의 개수가 증가한다면??

Word Embedding 이란?

- 한 단어를 **벡터 형태**로 표현
- 'cat'과 'kitty'는 비슷한 단어이므로 비슷한 단어 표현형을 가짐
- 'hamburger'는 'cat', 'kitty'와 비슷하지 않으므로 다른 표현형 = 거 리가 멀다

Word의 기존의 다른 Vector Representation 방법들

Distributional semantics: A word's meaning is given
 by the words that frequently appear close-by

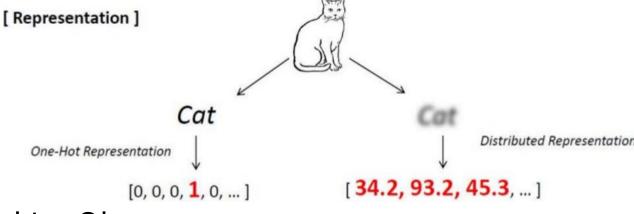


- "You shall know a word by the company it keeps" (J. R. Firth 1957: 11)
- One of the most successful ideas of modern statistical NLP!
- When a word w appears in a text, its context is the set of words that appear nearby (within a fixed-size window).
- Use the many contexts of w to build up a representation of w

```
...government debt problems turning into banking crises as happened in 2009...
...saying that Europe needs unified banking regulation to replace the hodgepodge...
...India has just given its banking system a shot in the arm...
```

Word2Vec

• Word의 distributed vector representation 학습기법



- 주변 단어로 해당 단어를 학습시키는 알 고리증
 - 주변에 있으면 단어의 의미가 더 비슷할 것이 라 가정
- 예시)
 - The cat purrs.
 - This cat hunts mice.

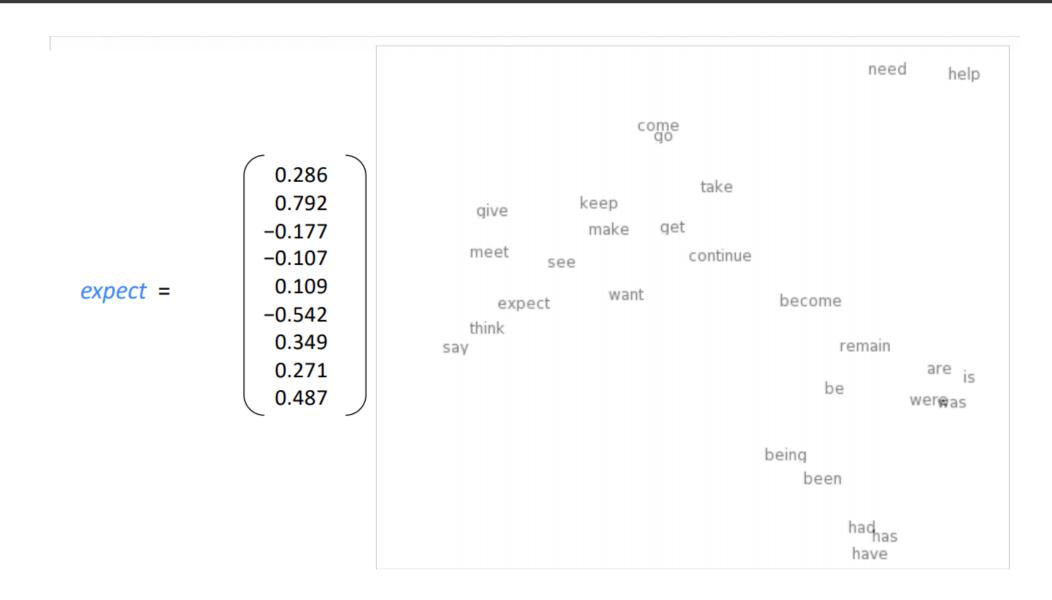


Distributed Representation : Word Vector

We will build a dense vector for each word, chosen so that it is similar to vectors of words that appear in similar contexts

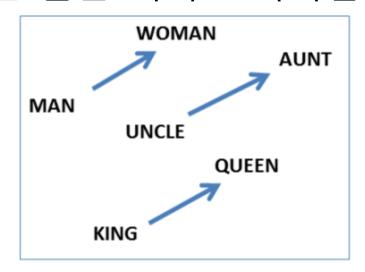
Note: word vectors are sometimes called word embeddings or word representations. They are a distributed representation.

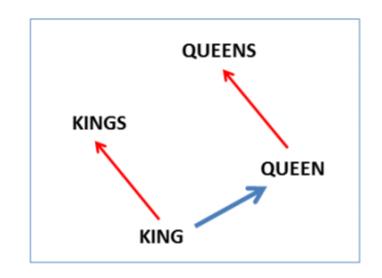
Word meaning as a neural word vector – visualization



Word2Vec의 특성

- 워드 벡터, 즉 공간에서의 벡터 포인트 간의 관계는 해당 단어들 간 의 관계를 나타냄.
- 같은 관계는 같은 벡터로 나타남.



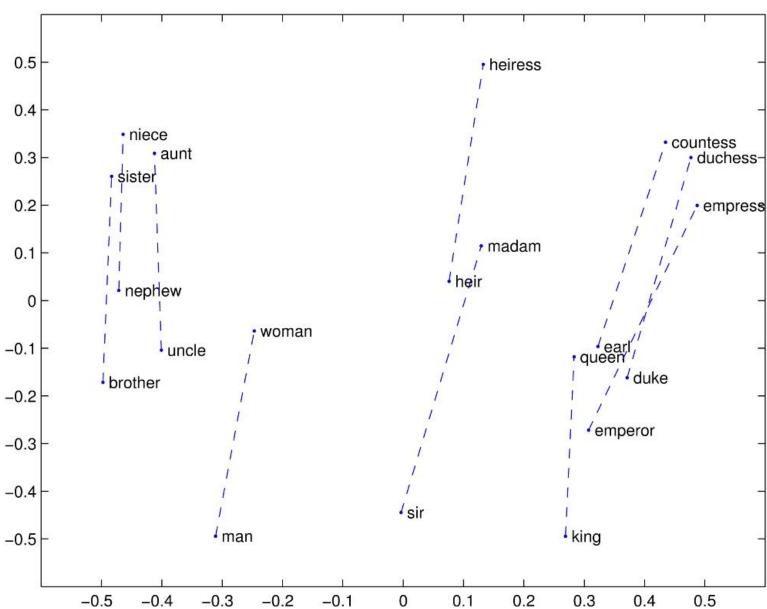


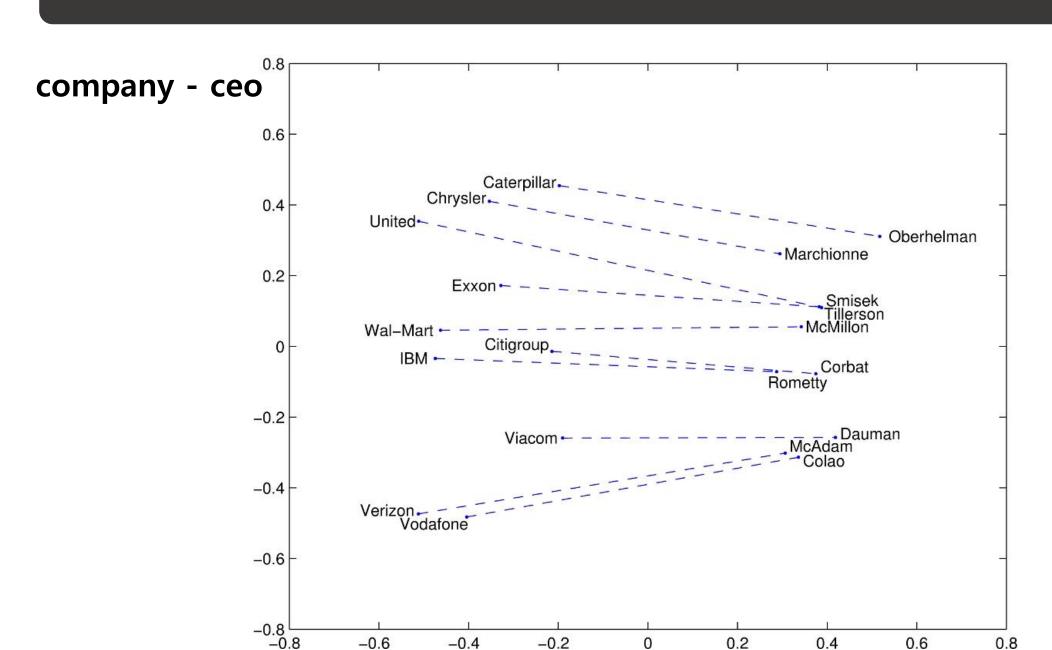
• e.g.,

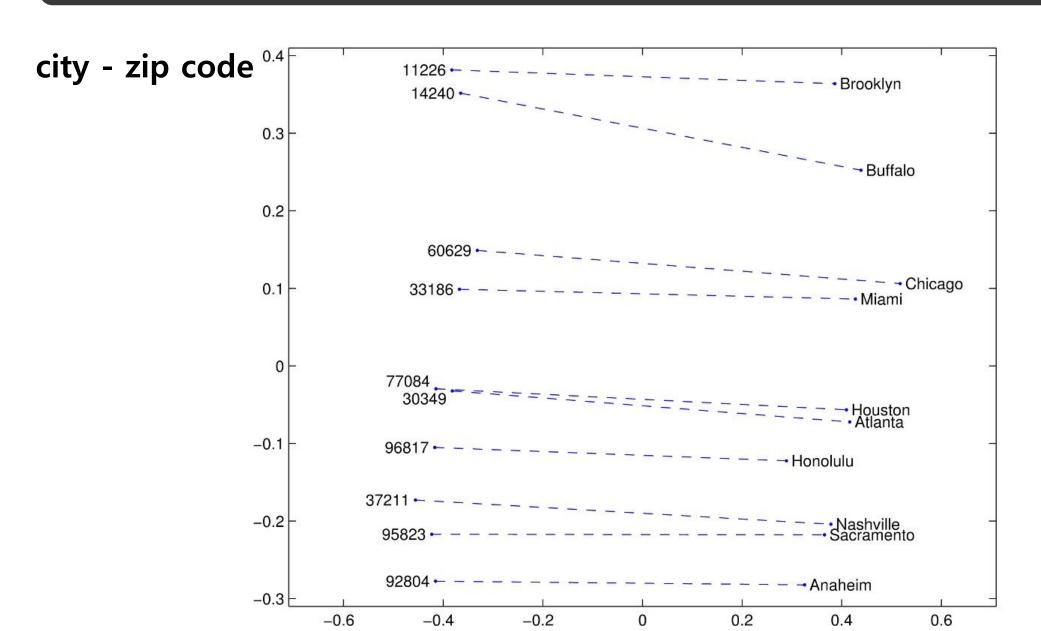
(Mikolov et al., NAACL HLT, 2013)

vec[queen] - vec[king] = vec[woman] - vec[man]

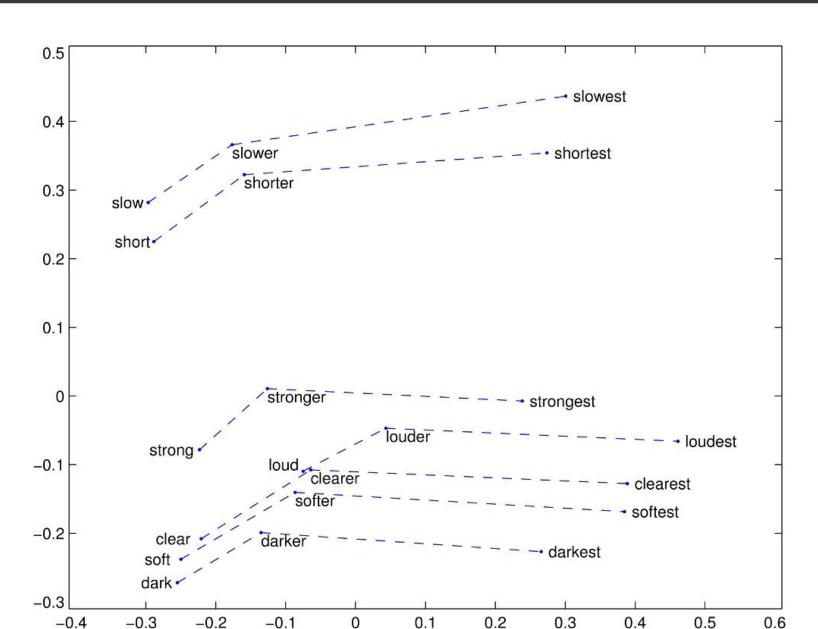






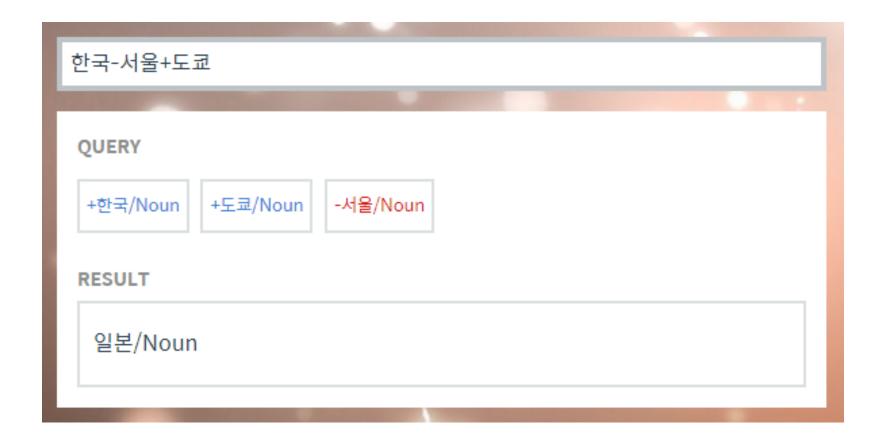


comparative - superlative



Word2Vec의 특성 – Analogy Reasoning

- 예제: 한글 word2vec
 - http://w.elnn.kr/search/



Word2Vec의 특성 – Analogy Reasoning

- 다른 예제들: http://wonjaekim.com/archives/50
- 여기서 wor2vec이 만들지 않은 예제는?
- 1) 컴퓨터-기계+인간 = 일반인
- 2) 인간 생각 = 악마
- 3) 사랑 + 이별 = 추억
- 4) 사랑 이별 = 미움
- 5) 나+운명 = 당신
- 6)이명박 돈 = 박근혜

Word2Vec의 특성 – Semantic Similarity

• 예제: https://github.com/dhammack/Word2VecExample

- Word intrusion detection
 - staple hammer saw drill
 - math shopping reading science
 - rain snow sleet sun
 - eight six seven five three owe nine
 - breakfast cereal dinner lunch
 - england spain france italy greece germany portugal australia

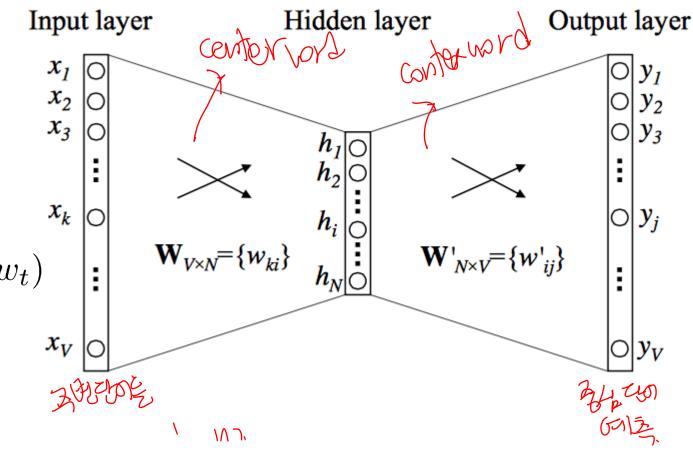
How Word2Vec Algorithm Works

- V: vocabulary size
- N: embedding dimension
- Objective criterion

$$J(\theta) = \frac{1}{T} \sum_{t=1}^{T} \sum_{-m \le j \le m, j \ne 0} \log p(w_{t+j}|w_t)$$

where

$$\log p(o|c) = \log \frac{\exp \left(u_o^T v_c\right)}{\sum_{w=1}^W \exp \left(u_w^T v_c\right)} \text{, which is a softmax function.}$$



Word2vec : overview

Word2vec (Mikolov et al. 2013) is a framework for learning word vectors

Idea:

- We have a large corpus of text
- Every word in a fixed vocabulary is represented by a vector
- Go through each position t in the text, which has a center word c and context ("outside") words o
- Use the similarity of the word vectors for c and o to calculate the probability of o given c (or vice versa)
- Keep adjusting the word vectors to maximize this probability

Word2vec: overview

• Example windows and process for computing $P(w_{t+j} \mid w_t)$

 $P(w_{t-2} \mid w_t)$ $P(w_{t+1} \mid w_t)$ $P(w_{t+2} \mid w_t)$ $P(w_{t+1} \mid$

Word2vec : objective function

For each position t = 1, ..., T, predict context words within a window of fixed size m, given center word w_i .

or each position
$$t=1,\ldots,T$$
, predict context words within a indow of fixed size m , given center word w_j .

Likelihood = $L(\theta) = \prod_{t=1}^{T} \prod_{-m \leq j \leq m} P(w_{t+j} | w_t; \theta)$
 θ is all variables to be optimized sometimes called $cost$ or $loss$ function

The objective function $J(\theta)$ is the (average) negative log likelihood:

$$J(\theta) = -\frac{1}{T} \log L(\theta) = -\frac{1}{T} \sum_{t=1}^{T} \sum_{-m \le j \le m} \log P(w_{t+j} \mid w_t; \theta)$$

Minimizing objective function \Leftrightarrow Maximizing predictive accuracy

Word2vec : overview with Vectors

We want to minimize the objective function:

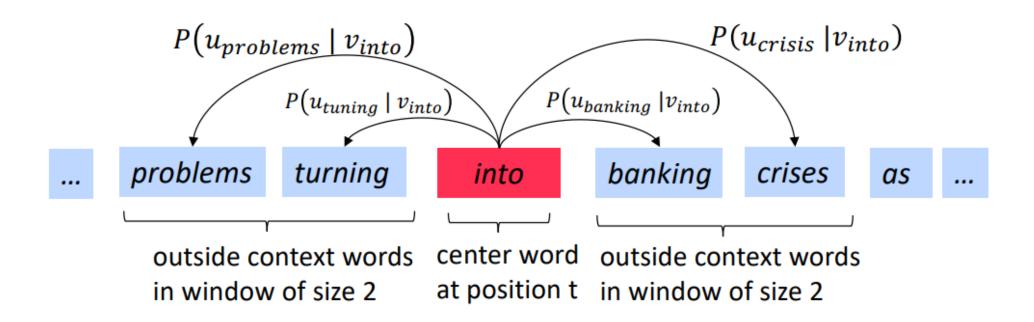
$$J(\theta) = -\frac{1}{T} \sum_{t=1}^{T} \sum_{\substack{-m \le j \le m \\ j \ne 0}} \log P(w_{t+j} \mid w_t; \theta)$$

- Question: How to calculate $P(w_{t+j} | w_t; \theta)$?
- Answer: We will use two vectors per word w:
 - v_w when w is a center word
 - u_w when w is a context word
- Then for a center word c and a context word o:

$$P(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w \in V} \exp(u_w^T v_c)}$$
 where embedding

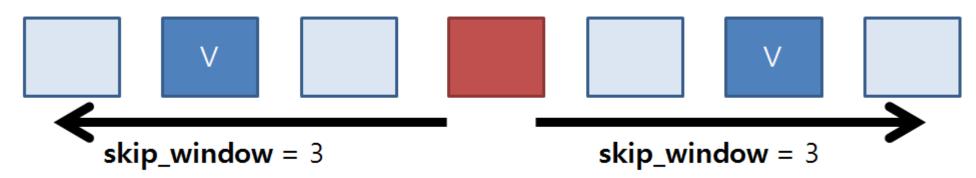
Word2vec: overview

- Example windows and process for computing $P(w_{t+j} \mid w_t)$
- $P(u_{problems} | v_{into})$ short for $P(problems | into ; u_{problems}, v_{into}, \theta)$



How Word2Vec Algorithm Works

• 먼저 window 크기를 정하고

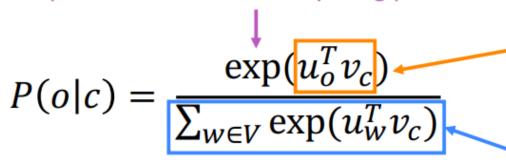


num_skips: #selected words in windows = 2

- Skipgram: 중심 단어로 window 내의 주변 단어 (context words)를 예측
 - Semantic task에 장점을 보이나, 학습이 느림.
- CBOW: 주변 단어들로 중심 단어를 예측
 - Syntactic task에 장점을 보이고, 학습이 상대적으로 빠름

Word2vec : overview

Exponentiation makes anything positive



Dot product compares similarity of o and c.

$$u^Tv=u.$$
 $v=\sum_{i=1}^nu_iv_i$
Larger dot product = larger probability

Normalize over entire vocabulary to give probability distribution

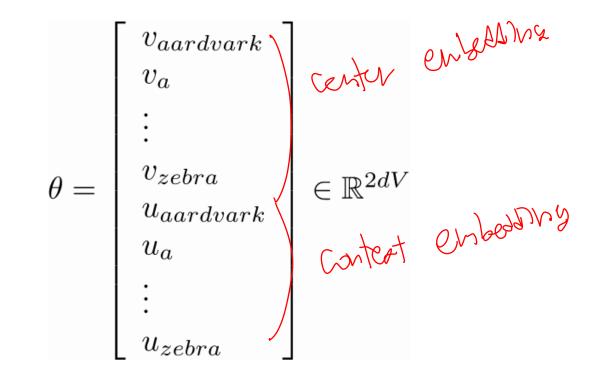
• This is an example of the softmax function $\mathbb{R}^n \to \mathbb{R}^n$

$$\operatorname{softmax}(x_i) = \frac{\exp(x_i)}{\sum_{j=1}^n \exp(x_j)} = p_i$$

- The softmax function maps arbitrary values x_i to a probability distribution p_i
 - "max" because amplifies probability of largest x_i
 - "soft" because still assigns some probability to smaller x_i
 - Frequently used in Deep Learning

To train the model: Compute all vector gradients

- Recall: θ represents all model parameters, in one long vector
- In our case with *d*-dimensional vectors and *V*-many words:



- Remember: every word has two vectors
- We optimize these parameters by walking down the gradient

Word2vec

Why two vectors? → Easier optimization. Average both at the end.

Two model variants:

- Skip-grams (SG)
 - Predict context ("outside") words (position independent) given center word
- Continuous Bag of Words (CBOW)

Predict center word from (bag of) context words

This lecture so far: **Skip-gram model**

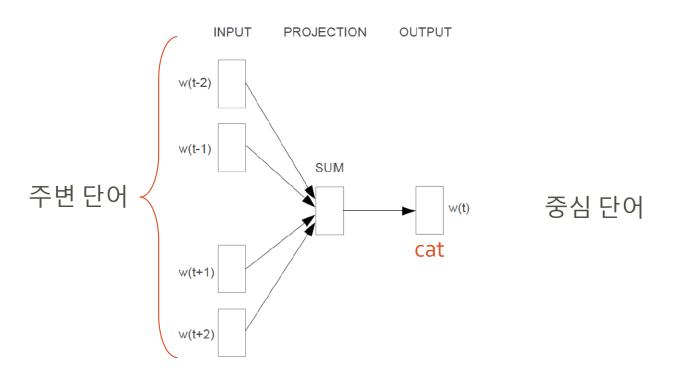
Additional efficiency in training:

Negative sampling

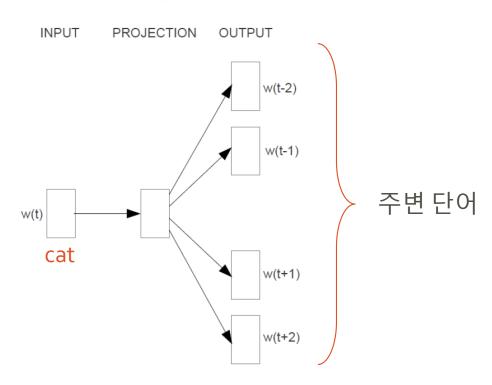
So far: Focus on naïve softmax (simpler training method)

Two Models of Word2Vec

Continuous Bag-Of-Words (CBOW)



Skip-gram

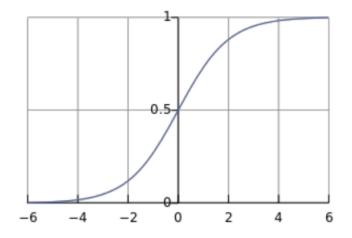


The skip-gram model with negative sampling

- From paper: "Distributed Representations of Words and Phrases and their Compositionality" (Mikolov et al. 2013)
- Overall objective function (they maximize): $J(\theta) = \frac{1}{T} \sum_{t=1}^{T} J_t(\theta)$

$$J_t(\theta) = \log \sigma \left(u_o^T v_o \right) + \sum_{i=1}^{\infty} \mathbb{E}_{j \sim P(w)} \left[\log \sigma \left(-u_j^T v_o \right) \right]$$

- The sigmoid function: $\sigma(x) = \frac{1}{1+e^{-x}}$ (we'll become good friends soon)
- So we maximize the probability of two words co-occurring in first log



The skip-gram model with negative sampling

Notation more similar to class and HW2:

$$J_{neg-sample}(\boldsymbol{o},\boldsymbol{v}_c,\boldsymbol{U}) = -\log(\sigma(\boldsymbol{u}_o^{\top}\boldsymbol{v}_c)) - \sum_{k=1}^K \log(\sigma(-\boldsymbol{u}_k^{\top}\boldsymbol{v}_c))$$

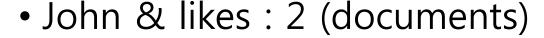
- We take k negative samples (using word probabilities)
- Maximize probability that real outside word appears,
 minimize prob. that random words appear around center word
- $P(w)=U(w)^{3/4}/Z$, the unigram distribution U(w) raised to the 3/4 power (We provide this function in the starter code).
- The power makes less frequent words be sampled more often

기존의 방법으로 Word 간 유사도 구하려면?

- 전 슬라이드의 방법을 사용하여 term-document matrix 구축
- e.g., Document 1 = "John likes movies. Mary likes too." Document 2 = "John also likes football."
- 두 간어가 얼마나 자주 같은 문서에서 등장했나로 유사도를 측정

Vocabulary	Doc 1	Doc 2		
John	1	1		
likes	2	1		
movies	1	0		
also	0	1		
football	0	1		
Mary	1	0		
too	1	0		

Co-occurrence similarity



• movies & also: 0 (documents)

Word의 기존의 다른 Vector Representation 방법들

- Matrix factorization 기반 기법들
 - Singular vector representation (혹은 latent semantic indexing)
 - Nonnegative matrix factorization
- Probabilistic topic modeling 기반 기법들
 - Probabilistic latent semantic indexing
 - Latent Dirichlet allocation

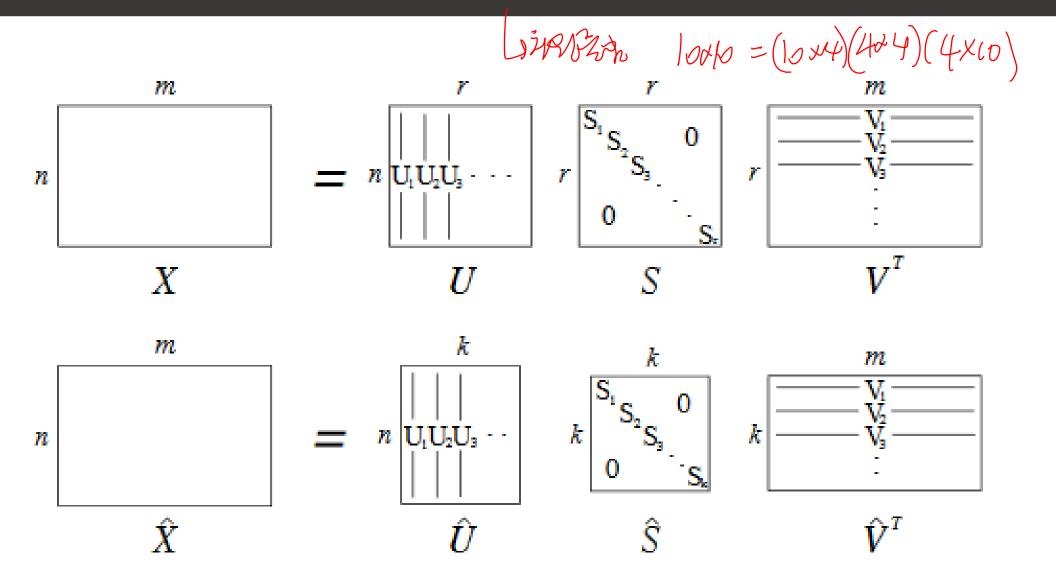
Singular Value Decomposition

```
Corpus = {"I like deep learning" Context = previous word and next word
"I like NLP"

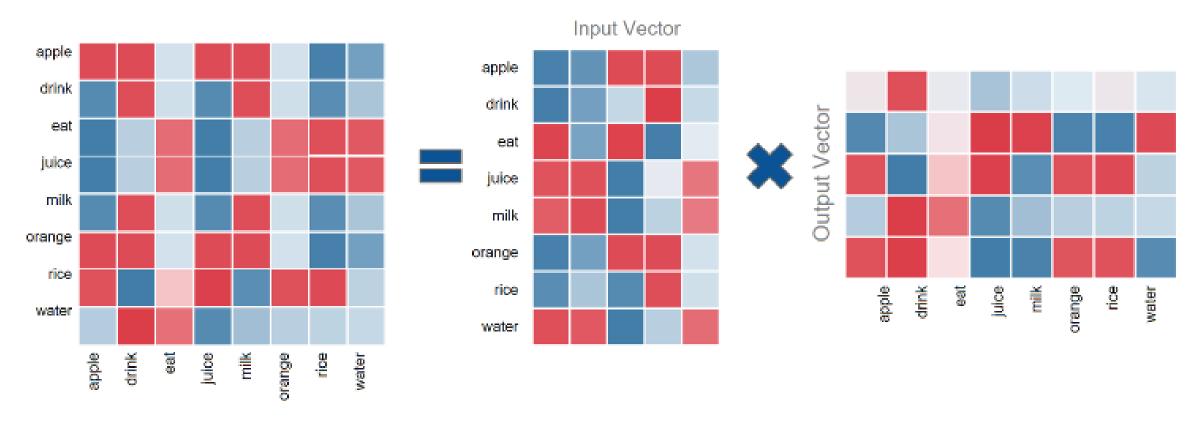
"I enjoy flying"}
```

counts	1	like	enjoy	deep	learning	NLP	flying	
1	0	2	1	0	0	0	0	0
like	2	0	0	1	0	1	0	0
enjoy	1	0	0	0	0	0	1	0
deep	0	1	0	0	1	0	0	0
learning	0	0	0	1	0	0	0	1
NLP	0	1	0	0	0	0	0	1
flying	0	0	1	0	0	0	0	1
	0	0	0	0	1	1	1	0

Dimension Reduction using Singular Value Decomposition



Singular Value Decomposition Example

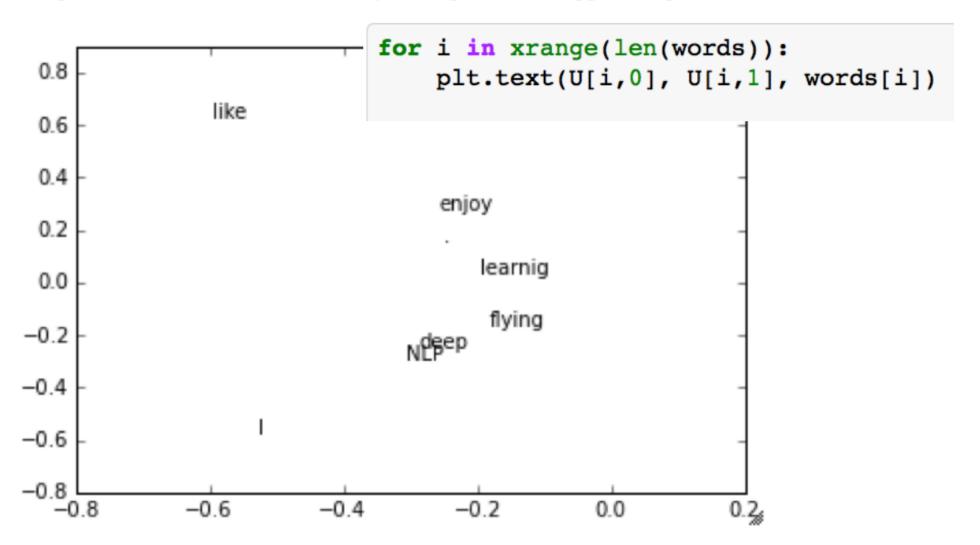


The problem with this method, is that we may end up with matrices having billions of rows and columns, which makes SVD computationally restrictive.

Singular Value Decomposition Example

Corpus: I like deep learning. I like NLP. I enjoy flying.

Printing first two columns of U corresponding to the 2 biggest singular values



Interesting semantic patterns emerge in the vectors



COALS model from An Improved Model of Semantic Similarity Based on Lexical Co-Occurrence Rohde et al. ms., 2005

Interesting semantic patterns emerge in the vectors



COALS model from An Improved Model of Semantic Similarity Based on Lexical Co-Occurrence Rohde et al. ms., 2005

Hacks to X (several used in Rohde et al. 2005)

Scaling the counts in the cells can help *a lot*

- Problem: function words (the, he, has) are too
 frequent syntax has too much impact. Some fixes:
 - min(X,t), with t ≈ 100
 - Ignore them all
- Ramped windows that count closer words more
- Use Pearson correlations instead of counts, then set negative values to 0
- Etc.

Count based vs. direct prediciton

- LSA, HAL (Lund & Burgess),
- COALS, Hellinger-PCA (Rohde et al, Lebret & Collobert)

- Fast training
- Efficient usage of statistics
- Primarily used to capture word similarity
- Disproportionate importance given to large counts

- Skip-gram/CBOW (Mikolov et al)
- NNLM, HLBL, RNN (Bengio et al; Collobert & Weston; Huang et al; Mnih & Hinton)
- Scales with corpus size
- Inefficient usage of statistics
- Generate improved performance on other tasks
- Can capture complex patterns beyond word similarity

Encoding meaning in vector differences

Crucial insight: Ratios of co-occurrence probabilities can encode meaning components

	x = solid	x = gas	x = water	x = random
P(x ice)	large	small	large	small
P(x steam)	small	large	large	small
$\frac{P(x \text{ice})}{P(x \text{steam})}$	large	small	~1	~1

Encoding meaning in vector differences

Crucial insight: Ratios of co-occurrence probabilities can encode meaning components

	x = solid	x = gas	x = water	x = fashion
P(x ice)	1.9 x 10 ⁻⁴	6.6 x 10 ⁻⁵	3.0 x 10 ⁻³	1.7 x 10 ⁻⁵
P(x steam)	2.2 x 10 ⁻⁵	7.8 x 10 ⁻⁴	2.2 x 10 ⁻³	1.8 x 10 ⁻⁵
$\frac{P(x \text{ice})}{P(x \text{steam})}$	8.9	8.5 x 10 ⁻²	1.36	0.96

Encoding meaning in vector differences

Q: How can we capture ratios of co-occurrence probabilities as linear meaning components in a word vector space?

A: Log-bilinear model: $w_i \cdot w_j = \log P(i|j)$

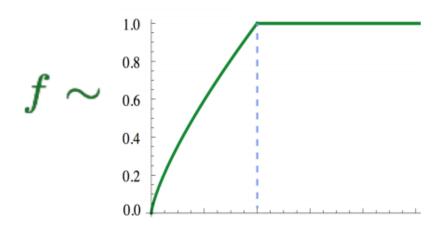
with vector differences $w_x \cdot (w_a - w_b) = \log \frac{P(x|a)}{P(x|b)}$

Combining the best of both worlds GloVe

$$w_i \cdot w_j = \log P(i|j)$$

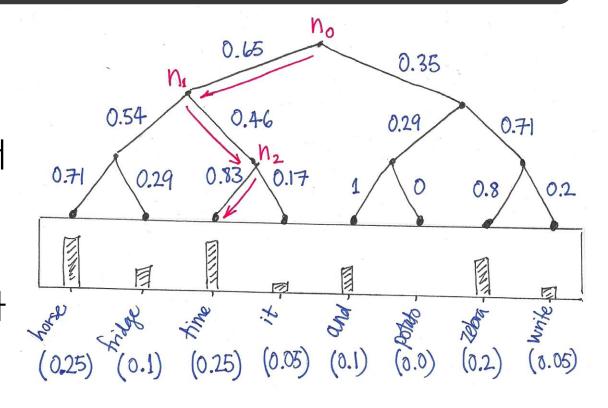
$$J = \sum_{i,j=1}^{V} f\left(X_{ij}\right) \left(w_i^T \tilde{w}_j + b_i + \tilde{b}_j - \log X_{ij}\right)^2$$

- Fast training
- Scalable to huge corpora
- Good performance even with small corpus and small vectors



Efficient Solution 1: Hierarchical Softmax

- 각 단어들을 leaves로 가지는 binary tree 를 생성함.
- 해당하는 단어의 확률을 계산할 때 root 에서부터 해당 leaf로 가는 path에 따라서 확률을 곱해나가는 식으로 해당 단어가 나올 최종적인 확률을 계산함.
- 즉, 각각의 internal node를 왼쪽, 오른쪽 노드들로 분기하는 Bernoulli 확률 변수라 생각하여, 각 단어의 확률을 계산함



$$P(\text{time}|\mathcal{C}) = P_{n_0}(\text{left}|\mathcal{C})P_{n_1}(\text{right}|\mathcal{C})P_{n_2}(\text{left}|\mathcal{C})$$

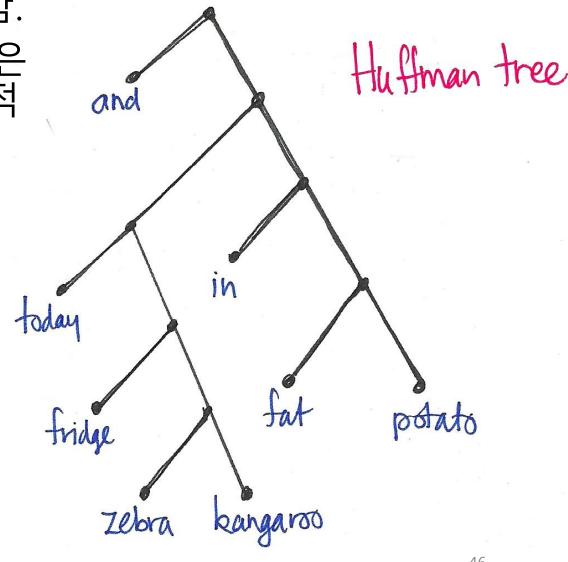
• 이를 통해 1/번의 계산을 log 1/번의 계산으로 줄일 수 있음.

Efficient Solution 1: Hierarchical Softmax

• Binary tree는 Huffman tree를 사용함.

• 즉, 자주 등장하는 단어들은 보다 짧은 path로 도달할 수 있기 때문에 전체적 인 계산량이 더 낮아지는 효과를 냄.

word	count	
fat	3	
fridge	2	
zebra	1	,
potato	3	\longrightarrow
and	14	
in	7	
today	4	
kangaroo	2	



Word2Vec의 적용 분야

자연어 처리 거의 모든 분야에서 성능 향상을 가져왔음.

- Word similarity
- Machine translation
- Part-of-speech tagging and named entity recognition
- Sentiment analysis
- Clustering
- Semantic lexicon building

Word2Vec의 적용 분야 – Machine Translation

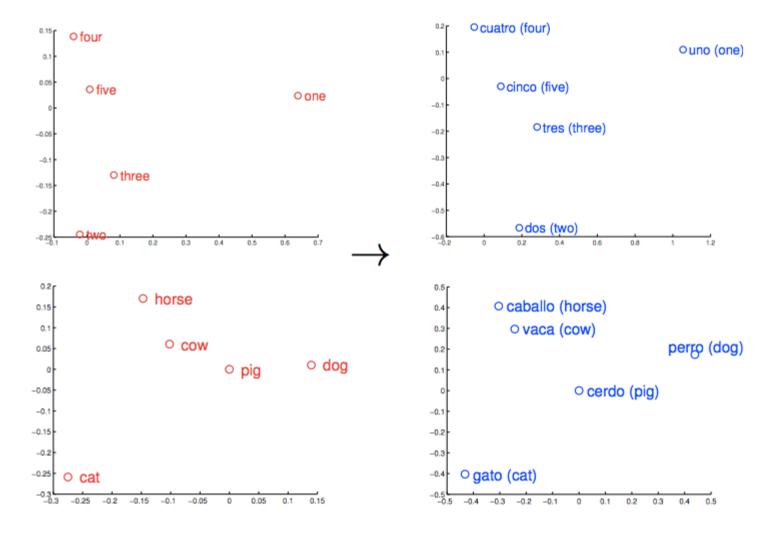
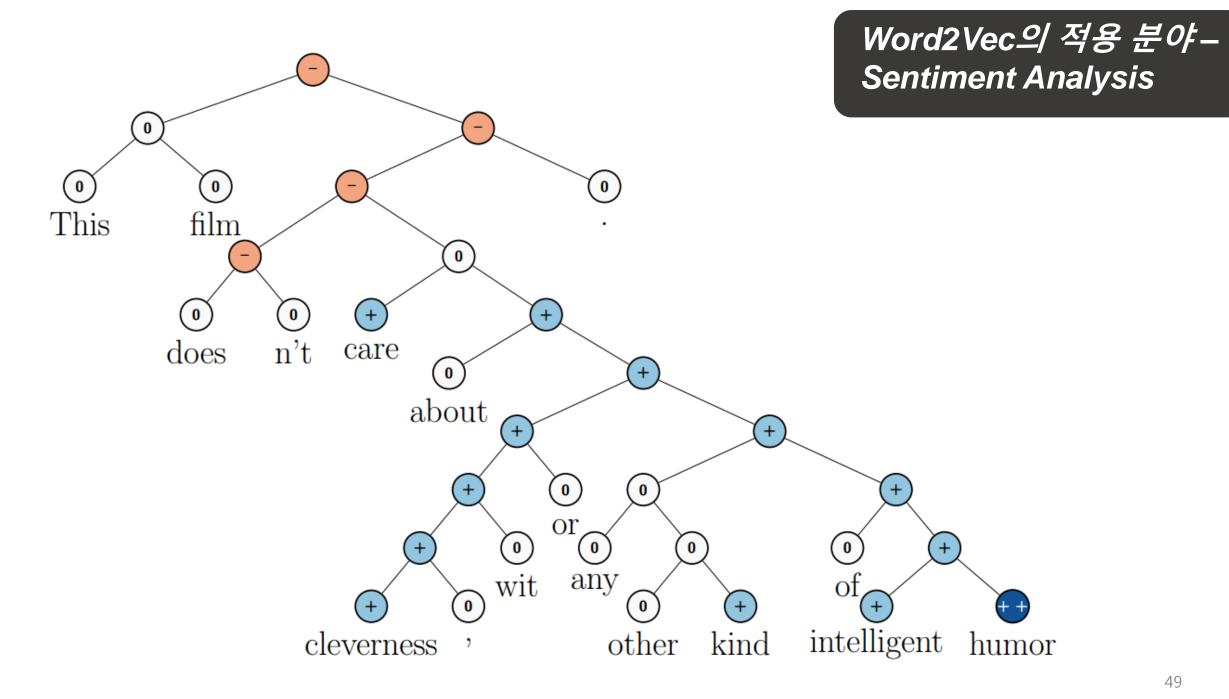


Figure 1: Distributed word vector representations of numbers and animals in English (left) and Spanish (right). The five vectors in each language were projected down to two dimensions using PCA, and then manually rotated to accentuate their similarity. It can be seen that these concepts have similar geometric arrangements in both spaces, suggesting that it is possible to learn an accurate linear mapping from one space to another. This is the key idea behind our method of translation.



Word2Vec의 적 용 분야 – Image Captioning























Describes without errors

Describes with minor errors

Somewhat related to the image

Unrelated to the image

Figure 5. A selection of evaluation results, grouped by human rating.

References

코드

- Python: https://radimrehurek.com/gensim/models/word2vec.html
- C++: https://code.google.com/archive/p/word2vec/
- FastText: https://github.com/facebookresearch/fastText

Useful resources

- https://shuuki4.wordpress.com/2016/01/27/word2vec-%EA%B4%80%EB%A0%A8-%EC%9D%B4%EB%A1%A0-%EC%A0%95%EB%A6%AC/
- https://code.facebook.com/posts/1438652669495149/fair-open-sources-fasttext/
- http://cs224d.stanford.edu/
- https://ronxin.github.io/wevi/
- https://www.lucypark.kr/slides/2015-pyconkr/
- http://cs224n.stanford.edu/