## Lenguajes de Programación Tarea 3

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## Problema I

```
Fibonacci
\Gamma \mid fib: (number \leftarrow number) \Gamma \mid n:number
\Gamma \vdash [fib \leftarrow number] \quad \Gamma \vdash \{fib n\}:number
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        [A]
\Gamma \vdash \{\text{rec } \{\text{fib: number }\}\}
                                                                                                              {fun (n:number):number
                                                                                                                                                                   \{if (<= n 1)\}
                                                                                                                                                                      (+ (fib (- n 1)) (fib (- n 2)))}}}}{fib n}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  \Gamma \hspace{0.2em}\rule{0.5em}{0.8em}\hspace{0.2em}\rule{0.5em}{0.8em}\hspace{0.2em} n : \hspace{0.2em} n \hspace{0.2em}\rule{0.5em}{0.8em}\hspace{0.2em}\rule{0.5em}{0.8em}\hspace{0.2em}\hspace{0.2em}\rule{0.5em}{0.8em}\hspace{0.2em}\rule{0.5em}{0.8em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\rule{0.5em}{0.8em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace{0.2em}\hspace
                                                                                                                                                                                     \Gamma \vdash 1:number \Gamma \vdash n:number \Gamma \vdash 1:number
                                                      \Gamma \mid n:number
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          \Gamma \vdash 2:number
                                                       \Gamma \vdash (\leq n \ 1):bool
                                                                                                                                                                                                                                                                                                                                                                               \Gamma \vdash (fib (-n 1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        \Gamma \vdash (fib (-n 2))
                                                      \Gamma \vdash (\leq n \ 1):bool \Gamma \vdash 1:number \Gamma \vdash (+ (fib \ (-n \ 1)) \ (fib \ (-n \ 2)))
                                                     \Gamma, [fib \leftarrow number] \vdash (if (\leq n 1)
                                                                                                                                                                                                     (+ (fib (- n 1)) (fib (- n 2))))
[A]=\overline{\Gamma}, [fib \leftarrow number] \vdash (fun (n:number):number: number \rightarrow number
                                                                                                                                                                                                                                  \{if (<= n 1)\}
                                                                                                                                                                                                                                          (+ (fib (- n 1)) (fib (- n 2)))})
```

**Empty List** 

$$\frac{\Gamma \mid \text{empty}?:(\text{list} \rightarrow \text{bool}) \qquad \Gamma \mid \text{l:list}}{\Gamma \mid \text{empty}? \mid 1}$$

## Problema II

Problema III

Problema IV

Problema V

Problema VI